

1.

Greedyalgorithm()

For all jobs from  $j_1$  to  $j_N$

Dollars[ji] =  $d_i \cdot T_i$

Sort(dollars)

For every value in dollars[ji]

If  $t_i < T_i$  #calculated time limit < given time limit

Total = total + dollars[ji]

The time complexity for the for loop that calculates the earnings for each job is  $O(n)$

Time complexity for sorting the values from greatest to least is  $O(n \log n)$

The second for loop will also require a time of  $O(n)$

Total time complexity will be  $O(n \log n) + O(n)$ , or  $O(n^2)$

2.

Example 1

Matrix A: 40 x 20

Matrix B: 20 x 30

Matrix C: 30 x 10

Matrix D: 10 x 30

Proof by contradiction

a) Cheapest Multiplication =  $A((BC)D) = 36,000$

Most efficient =  $(A(BC))D = 26,000$

b) Most expensive multiplication =  $((AB)C)D = 48,000$

Most efficient =  $(A(BC))D = 26,000$

Example 2

Matrix A: 10 x 30

Matrix B: 30 x 70

Matrix C: 70 x 50

Matrix D: 50 x 20

Proof by contradiction

c) Multiplication between  $M_i$  and  $M_i + 1$  such that the number of columns in  $M_i$  is minimized =

$A(B(CD)) = 118,000$

Most efficient =  $((AB)C)D = 66,000$

3.

```
Knapsack()  
    //Check if k or n is zero  
    If n==0 || k==0  
        Return 0  
    //Check the weight to see if it is larger than the total weight  
    If (W[n] > k)  
        Max value = Knapsack(k,n-1)  
    If (W[n] <= k)  
        //take both cases and see which one gives the maximum value  
        First_case = Knapsack(k-W[n], n-1)  
        Second_case = Knapsack(k,n-1)  
        Return max(first_case, second_case)
```

4.

```
LCS()  
    Array[m+1][n+1]  
    Int counter  
    Vector vect  
    For every value in i to m  
        For every value in j to n  
            If i or j = 0  
                Set array[i][j] = 0  
            Else if firststring[i-1] == secondstring[j-1]  
                Increment counter by 1  
                Array[i][j] = array[i-1][j-1] + 1  
                Add the found letter to vect  
            Else  
                Set array[i][j] = maximum of (array[i-1][j], array[i][j-1])  
    Return counter or vect depending on if you want the # of characters in the lcs or the lcs  
    string itself
```