Analyzing Quantum Many-Body Systems with ITensor and PastaQ

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► PhD from Caltech with John Preskill and Steve White (UCI) in 2018.



mtfishman.github.io











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- ► Develop PastaQ with Giacomo Torlai (AWS).



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- ► We are hiring postdocs, full-time scientists, part-time and full-time software developers, interns, etc.





SIMONS FOUNDATION

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ITENSOR









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- Find out more at: julialang.org.



What is PastaQ?



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 - ► Tensor network-based quantum state and process tomography.



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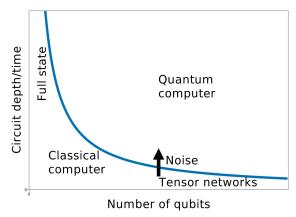


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 - ▶ Noisy circuit evolution with customizable noise models.
 - Approximate circuit evolution and optimization with MPS/MPO, etc.
- ► Find out more: github.com/GTorlai/PastaQ.jl

▶ In my opinion, tensor networks are the best general purpose tool we have right now for studying quantum many-body systems (while we wait for a general purpose quantum computer).



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 - ► ITensor and PastaQ handle this seamlessly.
 - ► This is not the focus of ITensor and PastaQ at the moment, specialized libraries like Yao.jl may be faster.
- ➤ Tensor networks are a common, general language for reasoning about quantum many-body systems (for example, quantum circuits).

What are tensor networks?



Matrix M_{ij} Order-2 tensor



Tensor T_{ijk} Order-3 tensor



What are tensor networks?



What are tensor networks?



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- 2. Launch Julia:
 - 1 \$ julia

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- 2. Launch Julia:

```
1 $ julia
```

3. Type the following commands:

```
julia > using Pkg
julia > Pkg.add("ITensors")
julia > Pkg.add("ITensors")
julia > Pkg.add("PastaQ")
julia > Pkg.add("PastaQ")
julia > Pkg.add("PastaQ")
```

Now you can use ITensors and PastaQ:

```
julia> using ITensors
julia> i = Index(2);
julia> A = ITensor(i);
```

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```

```
1  julia> using PastaQ
2
3  julia> gates = [("X", 1), ("CX", (1, 3))];
4
5  julia> ψ = runcircuit(gates);
```

```
1  using ITensors
2
3  i = Index(2)
4
5
```

Load ITensor

2-dimensional labeled Hilbert space (dim=2|id=510)

```
1     using ITensors
2
3     i = Index(2)
4
5
```



```
1     using ITensors
2
3     i = Index(2)
4
5
```

1
$$Zp = ITensor(i)$$

2 $Zp[i=>1] = 1$

$$4 \quad Zp = ITensor([1, 0], i)$$

i

$$|Z+\rangle = \begin{bmatrix} 1\\0 \end{bmatrix}$$

Construct from a Vector

```
using ITensors
   i = Index(2)
5
   Zp = ITensor(i)
   Zp[i=>1] = 1
   Zp = ITensor([1, 0], i)
```

i

3
$$Xp = ITensor([1, 1]/\sqrt{2}, i)$$

$$4 \quad Xm = \overline{ITensor}([1, -1]/\sqrt{2}, i)$$

$$\begin{split} |Z+\rangle &= \begin{bmatrix} 1 \\ 0 \end{bmatrix}, \qquad |Z-\rangle = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \\ |X+\rangle &= \begin{bmatrix} 1 \\ 1 \end{bmatrix} / \sqrt{2}, \ |X-\rangle = \begin{bmatrix} 1 \\ -1 \end{bmatrix} / \sqrt{2} \end{split}$$

```
1 Zp = ITensor([1, 0], i)

2 Zm = ITensor([0, 1], i)

3 Xp = ITensor([1, 1]/\sqrt{2}, i)

4 Xm = ITensor([1, -1]/\sqrt{2}, i)
```

1
$$Zp = ITensor([1, 0], i)$$

2 $Zm = ITensor([0, 1], i)$
3 $Xp = ITensor([1, 1]/\sqrt{2}, i)$
4 $Xm = ITensor([1, -1]/\sqrt{2}, i)$

$$Xp = (Zp + Zm)/\sqrt{2}$$

$$\frac{dag(Zp) * Xp}{inner(Zp, Xp)}$$

$$|X+\rangle = (|Z+\rangle + |Z-\rangle)/\sqrt{2}$$

$$\langle Z+|X+\rangle \approx 1/\sqrt{2}$$

$$\langle Z+|X+\rangle \approx 1/\sqrt{2}$$

```
1 Zp = ITensor([1, 0], i)

2 Zm = ITensor([0, 1], i)

3 Xp = ITensor([1, 1]/\sqrt{2}, i)

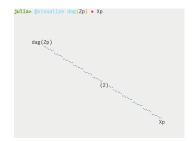
4 Xm = ITensor([1, -1]/\sqrt{2}, i)
```

$$\frac{1}{X+} = \frac{1}{Z+} + \frac{1}{Z-}$$

$$\sqrt{2}$$

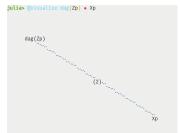
$$\overline{Z} + \overline{X} + = 1/\sqrt{2}$$

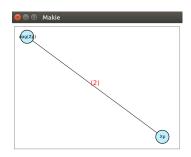
- 1 using ITensorUnicodePlots
- 2
 - @visualize dag(Zp) * Xp



- 1 using ITensorUnicodePlots
- $\overline{3}$ @visualize dag(Zp) * Xp

- 1 using ITensorGLMakie
- 2
 - @visualize dag(Zp) * Xp





Tutorial: One-site states

```
1 i = Index(2, "S=1/2")
2
3
4
5
6
7
8
```

```
(dim=2|id=25|"S=1/2")
```

"S=1/2" defines an operator basis

Additionally: "Qubit", "Qudit", "Electron", ...

Tutorial: One-site states

```
(dim=2|id=25|"S=1/2")

"S=1/2" defines an operator basis

Additionally:
"Qubit", "Qudit",
"Electron", . . .
```

```
1 Zp = state("Z+", i)

2 Zm = state("Z-", i)

3 Xp = state("X+", i)

4 Xm = state("X-", i)
```

```
1 ITensor([1 0], i)
2 ITensor([0 1], i)
3 ITensor([1 1]/√2, i)
4 ITensor([1 -1]/√2, i)
```

Tutorial: Custom one-site states

```
import ITensors: state

function state(
::StateName"iX-",
::SiteType"S=1/2"

return [im -im]/√2
end
```

Overload ITensors.jl behavior

Define a state with the name "iX-"

Tutorial: Custom one-site states

```
import ITensors: state

function state(
::StateName"iX-",
::SiteType"S=1/2"

)
return [im -im]/√2
end
```

```
1 iXm = state("iX-", i)
2
3
4 inner(Zm, iXm)
```

Overload ITensors.jl behavior

Define a state with the name "iX-"

$$|iX-\rangle = i|X-\rangle$$

$$\langle Z - | iX - \rangle = -i/\sqrt{2}$$

Tutorial: Custom one-site states

```
import ITensors: state

function state(
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return [im -im]/√2
end
```

```
1 iXm = state("iX-", i)
2
3
4 inner(Zm, iXm)
```

Overload ITensors.jl behavior

Define a state with the name "iX-"

$$iX+ = (iX+)*i$$

```
1 i = Index(2) (dim=2|id=837)

2 j = Index(2) (dim=2|id=839)

3 (dim=2|id=899)

4 i \neq j
```

```
 \begin{array}{ll} 1 & i = Index(2) \\ 2 & j = Index(2) \\ 3 & \\ 4 & i \neq j \end{array}
```

```
1 i = Index(2)

2 j = Index(2)

3 i \neq j
```

```
1  i = Index(2)
2
3  prime(i) == i'
4
5  i ≠ i'
6  noprime(i') == i
```

```
 \begin{array}{ll} 1 & i = Index(2) \\ 2 & j = Index(2) \\ 3 & \\ 4 & i \neq j \end{array}
```

```
1  i = Index(2)
2
3  prime(i) == i'
4
5  i ≠ i'
6  noprime(i') == i
```

$$\frac{\mathbf{i}}{\mathbf{i}}$$

$$\mathbf{rime}\left(\underline{\mathbf{i}}\right) = \underline{\mathbf{i}}'$$

$$\underline{\mathbf{i}} \quad \mathbf{1} \quad \underline{\mathbf{i}}'$$

- $1 \quad Z = ITensor(i', i)$
- Z[i'=>1, i=>1] = 1
- Z[i'=>2, i=>2] = -1

$$Z = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$

- $1 \quad Z = ITensor(i', i)$
- 2 Z[i'=>1, i=>1] = 1
- Z[i'=>2, i=>2] = -1



```
1 Z = ITensor(i', i)
2 Z[i'=>1, i=>1] = 1
3 Z[i'=>2, i=>2] = -1
```

```
1 z = [
2 10
3 0-1
4 ]
5 Z = ITensor(z, i', dag(i))
6
7
8 Z = op("Z", i)
```



Matrix representation Z

Convert to ITensor

Use predefined definition

```
 \begin{array}{lll} 1 & Z = op(\mbox{"}\mbox{Z"}, i) & Z \\ 2 & X = op(\mbox{"}\mbox{X"}, i) & X \\ 3 & & Zp = state(\mbox{"}\mbox{Z+"}, i) & |Z+\rangle \\ 5 & Zm = state(\mbox{"}\mbox{Z-"}, i) & |Z-\rangle \\ \end{array}
```

```
1 Z = op("Z", i)

2 X = op("X", i)

3 Zp = state("Z+", i)

5 Zm = state("Z-", i)
```

```
1 Z = op("Z", i)

2 X = op("X", i)

3 

4 Zp = state("Z+", i)

5 Zm = state("Z-", i)
```

$$\begin{array}{ll} 1 & X*Zp == Zm' \\ & \\ 3 & \\ 4 & noprime(X*Zp) == Zm \end{array}$$

```
1 Z = op("Z", i)

2 X = op("X", i)

3 

4 Zp = state("Z+", i)

5 Zm = state("Z-", i)
```

$$i'$$
 X i $Z+$ $=$ i' $Z-$

- $1 \quad dag(Zm)' * X * Zp$
- 2
- 3 inner(Zm', X, Zp)

$$\langle Z - |X|Z + \rangle \approx 1$$

- $1 \quad \frac{\mathrm{dag}(\mathrm{Zm})}{}, * \mathrm{X} * \mathrm{Zp}$
- 2
- 3 inner(Zm', X, Zp)

$$Z - X = Z + = 1$$

```
1 dag(Zm)' * X * Zp
2
3 inner(Zm', X, Zp)
```

$$Z-\frac{i'}{X}$$
 $Z+=1$

```
1    apply(X, Zp) ==
2    noprime(X * Zp)
3
4
5
6    inner(Zm, apply(X, Zp))
```

$$X|Z+\rangle$$

$$\langle Z - |X|Z + \rangle \approx 1$$

```
1 dag(Zm)' * X * Zp
2
3 inner(Zm', X, Zp)
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```
1    apply(X, Zp) ==
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6    inner(Zm, apply(X, Zp))
```

$$Z - \frac{i'}{X} X \frac{i}{Z} Z + = 1$$

apply
$$\left(\frac{1}{X}, \frac{1}{X}, \frac{1}{X}, \frac{1}{X}\right)$$

$$= \operatorname{noprime}\left(\frac{1}{X}, \frac{1}{X}, \frac{1}{X}\right)$$

$$= \frac{1}{X}$$

```
import ITensors: op
    function op(
     ::OpName"iX",
    ::SiteType"S=1/2"
6
     return [
      0 \text{ im}
    im 0
10
```

Overload ITensors.jl behavior

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import ITensors: op
    function op(
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```

$$\frac{i'}{iX} = \left(\frac{i'}{X}\right) * i$$

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```

$$\frac{\mathbf{i'} \quad \mathbf{iX} \quad \mathbf{i}}{\mathbf{iX} \quad \mathbf{i}} = \left(\frac{\mathbf{i'} \quad \mathbf{X} \quad \mathbf{i}}{\mathbf{X}} \right) * \mathbf{i}$$

```
1 op("iX", i)
```

```
import ITensors: op
   function op(
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6
     return [
      0 im
    im 0
10
```

$$\frac{\mathbf{i}^{\prime}}{\mathbf{i}\mathbf{X}} = \left(\frac{\mathbf{i}^{\prime}}{\mathbf{X}}\right) * \mathbf{i}$$

```
1 op("iX", i)
```

```
1 X * im
```

```
1 i1 = Index(2, "S=1/2")

2 i2 = Index(2, "S=1/2")

3 (dim=2|id=505|"S=1/2")

(dim=2|id=576|"S=1/2")

(dim=2|id=576|"S=1/2")

(dim=2|id=576|"S=1/2")

7 ZpZm = ITensor(i1, i2)

7 ZpZm[i1=>1, i2=>2] = 1 |Z+\rangle_1|Z-\rangle_2 = |Z+Z-\rangle
```

```
1 i1 = Index(2, "S=1/2")

2 i2 = Index(2, "S=1/2")

3 

4 i1 \neq i2

5 

6 ZpZm = ITensor(i1, i2)

7 ZpZm[i1=>1, i2=>2] = 1
```

$$\begin{array}{ccc} \underline{\mathbf{i}_1} & \underline{\mathbf{i}_2} & \mathbf{Z} + \\ \underline{\mathbf{i}_2} & \mathbf{Z} - \end{array}$$

```
    i1 = Index(2, "S=1/2")
    i2 = Index(2, "S=1/2")
    i1 ≠ i2
    ZpZm = ITensor(i1, i2)
    ZpZm[i1=>1, i2=>2] = 1
```

$$\begin{aligned} |Z+\rangle_1 \\ |Z+\rangle_2 \\ |Z-\rangle_1 \\ |Z-\rangle_2 \\ |Z+Z-\rangle &= |Z+\rangle_1 |Z-\rangle_2 \end{aligned}$$

```
1 i1 = Index(2, "S=1/2")

2 i2 = Index(2, "S=1/2")

3

4 i1 ≠ i2

5

6 ZpZm = ITensor(i1, i2)

7 ZpZm[i1=>1, i2=>2] = 1
```

```
1 Zp1 = state("Z+", i1)

2 Zp2 = state("Z+", i2)

3 

4 Zm1 = state("Z-", i1)

5 Zm2 = state("Z-", i2)

6 

7 ZpZm = Zp1 * Zm2
```

$$\begin{array}{ccc} \underline{\mathbf{i}_1} & \underline{\mathbf{i}_2} & \mathbf{Z} + \\ \underline{\mathbf{i}_2} & \mathbf{Z} - \end{array}$$



1
$$\psi = \text{ITensor}(i1, i2)$$

2 $\psi[i1=>1, i2=>2] = 1/\sqrt{2}$
3 $\psi[i1=>2, i2=>1] = 1/\sqrt{2}$
4
5 $\psi = (\text{Zp1} * \text{Zm2} + \text{Zm1} * \text{Zp2})/\sqrt{2}$

$$(|Z+\rangle|Z-\rangle + |Z-\rangle|Z+\rangle)/\sqrt{2}$$

From single-site states

```
1 \psi = \text{ITensor}(i1, i2)

2 \psi[i1=>1, i2=>2] = 1/\sqrt{2}

3 \psi[i1=>2, i2=>1] = 1/\sqrt{2}

4 \psi = (\text{Zp1} * \text{Zm2} + \text{Zm1} * \text{Zp2})/\sqrt{2}
```

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \Psi = \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \sqrt{2}$$

```
1 \psi = \text{ITensor}(i1, i2)

2 \psi[i1=>1, i2=>2] = 1/\sqrt{2}

3 \psi[i1=>2, i2=>1] = 1/\sqrt{2}

4 \psi = (\text{Zp1} * \text{Zm2} + \text{Zm1} * \text{Zp2})/\sqrt{2}
```

```
1 inner(ZpZm, \psi)
2
3
4 U, S, V = svd(ZmZp, i1)
5 s = diag(S)
6
7 U, S, V = svd(\psi, i1)
8 s = diag(S)
```

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \Psi = \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \sqrt{2}$$

$$\approx 1$$
 $\approx 1/\sqrt{2}$

$$\approx [1, 0]$$

$$\approx [1/\sqrt{2}, 1/\sqrt{2}]$$

```
1 \psi = \text{ITensor}(i1, i2)

2 \psi[i1=>1, i2=>2] = 1/\sqrt{2}

3 \psi[i1=>2, i2=>1] = 1/\sqrt{2}

4 \psi = (\text{Zp1} * \text{Zm2} + \text{Zm1} * \text{Zp2})/\sqrt{2}
```

```
inner(ZpZm, \psi)

U, S, V = svd(ZmZp, i1)

s = diag(S)

U, S, V = svd(\psi, i1)

s = diag(S)
```

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \Psi = \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \sqrt{2}$$

$$svd\left(\frac{i_{1}}{Z+Z-\frac{i_{2}}{2}}\right)$$

$$=\frac{i_{1}}{U}\frac{U}{S}\frac{v}{V}\frac{v}{i_{2}}$$

$$\frac{v}{S}\frac{v}{V}=\begin{bmatrix}1\\0\end{bmatrix}$$

```
1 \psi = \text{ITensor}(i1, i2)

2 \psi[i1=>1, i2=>2] = 1/\sqrt{2}

3 \psi[i1=>2, i2=>1] = 1/\sqrt{2}

4 \psi = (\text{Zp1} * \text{Zm2} + \text{Zm1} * \text{Zp2})/\sqrt{2}
```

```
1 inner(ZpZm, \psi)
2
3
4 U, S, V = svd(ZmZp, i1)
5 s = diag(S)
6
7 U, S, V = svd(\psi, i1)
8 s = diag(S)
```

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \Psi = \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \sqrt{2}$$

$$svd\left(\frac{i_{1}}{Z+Z-\frac{i_{2}}{2}}\right)$$

$$=\frac{i_{1}}{U}\frac{U}{S}\frac{v}{V}\frac{v}{v}$$

$$=\frac{1}{0}$$

```
1 H = ITensor(i1', i2', i1, i2)
2 H[i1'=>2, i2'=>1,
```

$$i1 = >2, i2 = >1] = -1$$

4 # ...

Make a Hamiltonian: Transverse field Ising (n = 2)

$$H = -\sum_{j=1}^{n-1} Z_j Z_{j+1} + h \sum_{j=1}^{n} X_j$$

```
\begin{array}{ll} 1 & H = ITensor(i1',\,i2',\,i1,\,i2) \\ 2 & H[i1'=>2,\,i2'=>1, \\ 3 & i1=>2,\,i2=>1] = -1 \\ 4 & \# \ ... \end{array}
```

```
1 Id1 = op("Id", i1)
2 Z1 = op("Z", i1)
3 X1 = op("X", i1)
4 # ...
5
6 ZZ = Z1 * Z2
7 XI = X1 * Id2
8 IX = Id1 * X2
9
10 h = 0.5
11 H = -ZZ + h * (XI + IX)
```

Make a Hamiltonian: Transverse field Ising (n = 2)

$$H = -\sum_{j}^{n-1} Z_{j}Z_{j+1} + h\sum_{j}^{n} X_{j}$$

Alternative:

Build from single-site operators. (Less error-prone.)

```
\begin{array}{ll} 1 & H = ITensor(i1',\,i2',\,i1,\,i2) \\ 2 & H[i1'=>2,\,i2'=>1, \\ 3 & i1=>2,\,i2=>1] = -1 \\ 4 & \# \ ... \end{array}
```

```
1 Id1 = op("Id", i1)
2 Z1 = op("Z", i1)
3 X1 = op("X", i1)
4 # ...
5
6 ZZ = Z1 * Z2
7 XI = X1 * Id2
8 IX = Id1 * X2
9
10 h = 0.5
11 H = -ZZ + h * (XI + IX)
```

Make a Hamiltonian: Transverse field Ising (n = 2)

$$H = -\sum_{j}^{n-1} Z_j Z_{j+1} + h \sum_{j}^{n} X_j$$

$$1 \quad ZpZp = Zp1 * Zp2$$

2

3 inner(ZpZp', H, ZpZp)

$$\langle \mathbf{H} \rangle = \langle \mathbf{Z} {+} \mathbf{Z} {+} | \mathbf{H} | \mathbf{Z} {+} \mathbf{Z} {+} \rangle$$

$$\begin{array}{ll} 1 & \mathrm{ZpZp} = \mathrm{Zp1} * \mathrm{Zp2} \\ 2 & \end{array}$$

$$\begin{bmatrix}
 Z + \frac{i_1}{i_2}, & \frac{i_1}{I_2} & \frac{Z}{Z} + \\
 Z + \frac{i_2}{i_2}, & \frac{i_1}{I_2} & \frac{Z}{Z} + \\
 \hline$$

$$1 \quad ZpZp = Zp1 * Zp2$$

2

3 inner(ZpZp', H, ZpZp)

1 D,
$$U = eigen(H)$$

$$\frac{Z + \frac{i_1}{i_2}}{Z + \frac{i_2}{i_2}} + \frac{\frac{i_1}{i_2}}{Z + \frac{i_2}{i_2}} = -1$$

$$\approx [-\sqrt{2}, -1, 1, \sqrt{2}]$$

$$\begin{array}{ll}
1 & ZpZp = Zp1 * Zp2 \\
2
\end{array}$$

inner(ZpZp', H, ZpZp)

diag(D)

$$\frac{\mathbf{i}_{1}'}{\mathbf{i}_{2}'} \mathbf{H} \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{U} \mathbf{U}$$

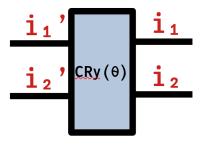
$$= \frac{\mathbf{i}_{1}'}{\mathbf{i}_{2}'} \mathbf{U} \mathbf{U}' \mathbf{D} \mathbf{U}$$

$$\frac{\mathbf{u}'}{\mathbf{D}} \mathbf{U} = \begin{bmatrix} -\sqrt{2} & -1 & 1 \\ 1 & \sqrt{2} & 1 \end{bmatrix}$$

```
import ITensors: op
2
    function op(
     ::OpName"CRy",
     ::SiteType"S=1/2":
6
     c = \cos(\theta/2)
     s = \sin(\theta/2)
   return
10
11
   1 \ 0 \ 0
12 0 1 0 0
  00c-s
13
14 	 0.0 s c
15
16
    end
```

```
Controlled-Ry (CRy) rotation gate CRy(\theta)
```

```
import ITensors: op
    function op(
     ::OpName"CRy".
     ::SiteType"S=1/2";
     c = \cos(\theta/2)
     s = \sin(\theta/2)
    return
10
11
    1000
12
   0\ 1\ 0\ 0
13
   0~0~\mathrm{c} -s
14 	 0.0 s c
15
16
    end
```



1 CH = op("CRy", i1, i2;
$$\theta = \pi/2$$
)

Controlled-Hadamard gate $CH = CRy(\theta = \pi/2)$

1 CH = op("CRy", i1, i2;
$$\theta = \pi/2$$
)

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}}$$
, $\frac{\mathbf{i}_{1}}{\mathbf{cRy}(m/2)}$ $\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}}$ = $\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}}$, CH $\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}}$

1 CH = op("CRy", i1, i2;
$$\theta = \pi/2$$
)

$$\frac{\mathbf{i}_1'}{\mathbf{i}_2'} \operatorname{cRy}(\pi/2) \frac{\mathbf{i}_1}{\mathbf{i}_2} = \frac{\mathbf{i}_1'}{\mathbf{i}_2'} \operatorname{CH} \frac{\mathbf{i}_1}{\mathbf{i}_2}$$

- $1 \quad \underset{}{\mathbf{apply}}(\mathrm{CH},\,\mathrm{Zp}\,\ast\,\mathrm{Zm}) ==$
- 2 Zp1 * Xm2

$$\mathrm{CH}|\mathrm{Z}{+}\mathrm{Z}{\text{-}}\rangle = |\mathrm{Z}{+}\mathrm{X}{\text{-}}\rangle$$

1 CH = op("CRy", i1, i2;
$$\theta = \pi/2$$
)

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}}, \frac{\mathbf{i}_{1}}{\mathbf{cry}(\mathbf{x}/2)} = \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}}, \mathbf{CH} = \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}}$$

$$\begin{array}{ll} \text{1} & \text{apply}(\text{CH, Zp} * \text{Zm}) == \\ \text{2} & \text{Zp1} * \text{Xm2} \end{array}$$

$$\begin{array}{c} \underbrace{i_1}' CH \underbrace{z_+} Z + \underbrace{z_+} Z + \underbrace{z_+} X + \underbrace{z_$$

```
1 function E(\psi)

2 \psi H \psi = inner(\psi', H, \psi)

3 \psi \psi = inner(\psi, \psi)

4 return \psi H \psi / \psi \psi

5 end
```

$$\mathrm{E}(\psi) = \langle \psi | \mathrm{H} | \psi \rangle / \langle \psi | \psi \rangle$$

```
1 function E(\psi)

2 \psi H \psi = inner(\psi', H, \psi)

3 \psi \psi = inner(\psi, \psi)

4 return \psi H \psi / \psi \psi

5 end
```



```
function E(\psi)
\psi H \psi = inner(\psi', H, \psi)
\psi \psi = inner(\psi, \psi)
return \psi H \psi / \psi \psi
\theta = \mathbf{n}
```

```
function minimize(f, \partial f, x;

nsteps, \gamma)

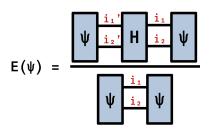
for n in 1:nsteps

x = x - \gamma * \partial f(x)

end

return x

end
```



Gradient descent.

f(x): function to minimize. $\partial f(x)$: gradient of f. γ : step size.

```
1 function E(\psi)

2 \psi H \psi = inner(\psi', H, \psi)

3 \psi \psi = inner(\psi, \psi)

4 return \psi H \psi / \psi \psi

5 end
```

```
1 function minimize(f, \partial f, x;

2 nsteps, \gamma)

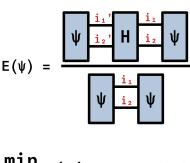
3 for n in 1:nsteps

4 x = x - \gamma * \partial f(x)

5 end

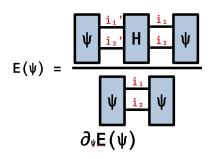
6 return x

7 end
```



$$_{\psi}^{\mathsf{min}}\mathsf{E}(\psi) \qquad \partial_{\psi}\!\mathsf{E}(\psi)$$

```
1 \psi_0 = (\mathrm{Zp1} * \mathrm{Zm2} + \mathrm{Zm1} * \mathrm{Zp2})/\sqrt{2}
3 4 \mathrm{E}(\psi_0) == -1
5 6 using Zygote # autodiff
7 8 \partial \mathrm{E}(\psi) = \mathrm{gradient}(\mathrm{E}, \psi)[1]
9 \mathrm{norm}(\partial \mathrm{E}(\psi_0)) == 2
```



```
1 \psi_0 = ({\rm Zp1} * {\rm Zm2} + {\rm Zm1} * {\rm Zp2})/\sqrt{2}

3 E(\psi_0) == -1

6 using Zygote # autodiff

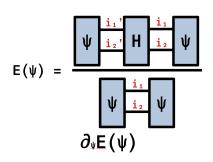
7 \partial E(\psi) = {\rm gradient}(E, \psi)[1]

9 {\rm norm}(\partial E(\psi_0)) == 2
```

```
1 \psi = \underset{\text{minimize}(E, \partial E, \psi_0;}{\text{msteps}=10, \gamma=0.1}

3 4 E(\psi_0), \underset{\text{norm}(\partial E(\psi_0))}{\text{morm}(\partial E(\psi))}

5 E(\psi), \underset{\text{norm}(\partial E(\psi))}{\text{morm}(\partial E(\psi))}
```



$$\begin{aligned} \min_{\psi} E(\psi) &= \\ \min_{\psi} \langle \psi | H | \psi \rangle / \langle \psi | \psi \rangle \end{aligned}$$

$$(-1, 2)$$

$$(-1.4142131, 0.0010865277)$$

$$\approx (-\sqrt{2}, 0)$$

4 ロ ト 4 倒 ト 4 豆 ト 4 豆 ト 9 0 0

```
# Circuit as a vector of gates:
     U(\theta, i1, i2) = [
      op("Ry", i1; \theta = \theta[1]),
       op("Ry", i2; \theta = \theta[2]),
     op("CX", i1, i2),
       op("Ry", i1; \theta = \theta[3]),
      op("Ry", i2; \theta = \theta[4]),
 8
 9
10
11
```

$$\frac{\mathbf{i}_{1}''}{\mathbf{i}_{2}''} | \mathbf{u}(\theta_{1}) | \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} = \frac{\mathbf{i}_{1}''}{\mathbf{i}_{2}'}, \mathbf{CX} | \frac{\mathbf{i}_{1}''}{\mathbf{i}_{2}'} | \mathbf{g}_{y(\theta_{1})} | \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}}$$

$$\frac{\mathbf{i}_{1}'}{\mathbf{i}_{2}'} | \mathbf{u}(\theta_{1}) | \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \rightarrow \frac{\mathbf{i}_{1}'}{\mathbf{i}_{2}'} | \mathbf{U}(\theta) | \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}}$$

```
# PastaQ notation:
u(\theta, j1, j2) = [
  ("Ry", j1, (; \theta = \theta[1])),
  ("Ry", j2, (; \theta = \theta[2])),
  ("CNOT", j1, j2),
  ("Ry", j1, (; \theta = \theta[3])),
  ("Ry", j2, (; \theta = \theta[4])),
U(\theta, i1, i2) =
  buildcircuit(u(\theta, 1, 2), [i1, i2])
```

$$\frac{\mathbf{i}_{1}''}{\mathbf{i}_{2}'}, \mathbf{u}(\theta_{1}) \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} = \frac{\mathbf{i}_{1}''}{\mathbf{i}_{2}}, \mathbf{CX} \frac{\mathbf{i}_{1}'}{\mathbf{i}_{2}}, \mathbf{R}_{y}(\theta_{1}) \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}}$$

$$\frac{\mathbf{i}_{1}''}{\mathbf{i}_{2}}, \mathbf{u}(\theta_{1}) \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \Rightarrow \frac{\mathbf{i}_{1}''}{\mathbf{i}_{2}}, \mathbf{u}(\theta) \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}}$$

```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 3 4 function \mathrm{E}(\theta)

5 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta), \psi_0)

6 return \mathrm{inner}(\psi_\theta, \mathrm{H}, \psi_\theta)

7 end
```

```
References state:

|0\rangle = |Z+Z+\rangle

\min_{\theta} E(\theta)

= \min_{\theta} \langle 0|U(\theta)^{\dagger} H U(\theta)|0\rangle

= \min_{\theta} \langle \theta|H|\theta\rangle
```

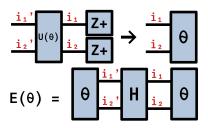
```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 3 4 function \mathrm{E}(\theta)

5 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta), \psi_0)

6 return \mathrm{inner}(\psi_\theta, \mathrm{H}, \psi_\theta)

7 end
```



```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 3 4 function \mathrm{E}(\theta)

5 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta), \psi_0)

6 return \mathrm{inner}(\psi_\theta, \mathrm{H}, \psi_\theta)

7 end
```

```
1 \theta_0 = [0, 0, 0, 0]

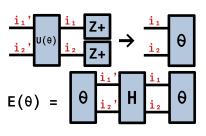
2 \partial E(\theta) = \text{gradient}(E, \theta)[1]

3 \theta = \text{minimize}(E, \partial E, \theta_0;

4 \text{nsteps=}40, \gamma = 0.5)

5 E(\theta_0) == -1

7 E(\theta) == -1.4142077 \approx -\sqrt{2}
```



$$\frac{\min}{\Theta} E(\Theta) \qquad \partial_{\theta} E(\Theta)$$

Tutorial: Two-site fidelity optimization

```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 \psi = (\mathrm{ZpZp} + \mathrm{ZmZm}) / \sqrt{2}

3 4 5 6 function F(\theta)

7 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta, \mathrm{i1}, \mathrm{i2}), \psi_0)

8 return -abs(inner(\psi, \psi_\theta))^2

9 end
```

Reference state:
$$\begin{aligned} |0\rangle &= |Z+Z+\rangle \\ \text{Target state:} \\ |\psi\rangle &= (|Z+Z+\rangle + |Z-Z-\rangle)/\sqrt{2} \\ \min_{\theta} &F(\theta) = \\ \min_{\theta} &-|\langle \psi | U(\theta) | 0 \rangle|^2 \end{aligned}$$

Tutorial: Two-site fidelity optimization

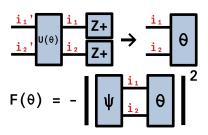
```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 \psi = (\mathrm{ZpZp} + \mathrm{ZmZm}) / \sqrt{2}

3 4 5 6 function F(\theta)

7 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta, \mathrm{i1}, \mathrm{i2}), \psi_0)

8 return -abs(inner(\psi, \psi_\theta))^2 end
```



Tutorial: Two-site fidelity optimization

```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 \psi = (\mathrm{ZpZp} + \mathrm{ZmZm}) / \sqrt{2}

3 4 5 6 function F(\theta)

7 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta, \mathrm{i1}, \mathrm{i2}), \psi_0)

8 return -abs(inner(\psi, \psi_\theta))^2 end
```

```
1 \theta_0 = [0, 0, 0, 0]

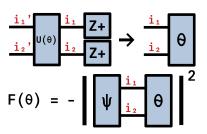
2 \partial F(\theta) = \text{gradient}(F, \theta)[1]

3 \theta = \text{minimize}(F, \partial F, \theta_0; \theta)

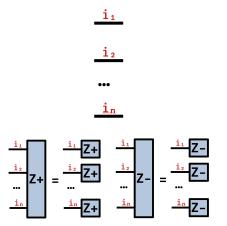
4 \text{nsteps}=50, \gamma=0.1

5 F(\theta_0) == -0.5

7 F(\theta) == -0.9938992 \approx -1
```



```
 \begin{array}{lll} 1 & n=30 \\ 2 & i=[Index(2,\,"S=1/2") \\ 3 & \quad for \ j \ in \ 1:n] \\ 4 \\ 5 & Zp=MPS(i,\,"Z+") \\ 6 & Zm=MPS(i,\,"Z-") \\ 7 \\ 8 & maxlinkdim(Zp) \end{array} \qquad \begin{array}{ll} n\text{-site state} \\ |Z+Z+\ldots Z+\rangle \\ |Z-Z-\ldots Z-\rangle \\ 1 \ (product \ state) \end{array}
```



1
$$\psi = (\mathrm{Zp} + \mathrm{Zm})/\sqrt{2}$$

2 3 4 $\mathrm{maxlinkdim}(\psi)$

$$\begin{array}{l}(|Z+Z+\ldots Z+\rangle+\\|Z-Z-\ldots Z-\rangle)/\sqrt{2}\end{array}$$

2 (entangled state)

1
$$\psi = (\mathrm{Zp} + \mathrm{Zm})/\sqrt{2}$$
2
3
4 $\mathrm{maxlinkdim}(\psi)$

1
$$\psi = (\mathrm{Zp} + \mathrm{Zm})/\sqrt{2}$$
2
3
4 $\mathrm{maxlinkdim}(\psi)$

- $1 \quad inner(Zp, Zp)$
- $2 \quad inner(Zm, Zp)$
- $3 \quad \text{norm}(\psi)$
- 4 $\operatorname{inner}(\operatorname{Zp}, \psi)$

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \quad \psi = \frac{\mathbf{i}_{1}}{\mathbf{i}_{1}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{1}} \mathbf{Z} - \frac{\mathbf{i}_{1}}{\mathbf{i}_{1}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} - \frac{\mathbf{i}_{1}}{\mathbf{i}_{1}} \mathbf{\psi}_{1} \leftarrow 2$$

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{1}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} - \frac{\mathbf{i}_{1}}{\mathbf{i}_{1}} \mathbf{\psi}_{1} \leftarrow 2$$

$$\frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \mathbf{\psi}_{1} \leftarrow 2$$

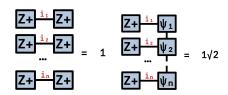
$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{\psi}_{1} \leftarrow 2$$

$$\begin{split} \langle Z + | Z + \rangle &\approx 1 \\ \langle Z - | Z + \rangle &\approx 0 \\ ||\psi\rangle| &\approx 1 \\ \langle Z + |\psi\rangle &\approx 1/\sqrt{2} \end{split}$$

1
$$\psi = (\mathrm{Zp} + \mathrm{Zm})/\sqrt{2}$$
2
3
4 $\mathrm{maxlinkdim}(\psi)$

 $\operatorname{inner}(\operatorname{Zp}, \operatorname{Zp})$ $\operatorname{inner}(\operatorname{Zm}, \operatorname{Zp})$ $\operatorname{norm}(\psi)$ $\operatorname{inner}(\operatorname{Zp}, \psi)$

$$\begin{array}{c} \underbrace{\begin{array}{c} \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{1}}_{1} \underbrace{\begin{array}{c} \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2}}_{2} + \underbrace{\begin{array}{c} \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2}}_{1} \underbrace{\begin{array}{c} \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2}}_{2} \\ \underbrace{\begin{array}{c} \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2}}_{1} \underbrace{\begin{array}{c} \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2}}_{2} \\ \underbrace{\begin{array}{c} \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2} \\ \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2} \\ \underbrace{\begin{array}{c} \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2} \\ \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2} \\ \underbrace{\begin{array}{c} \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2} \\ \underbrace{\begin{array}{c} \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2} \\ \underbrace{\begin{array}{c} \underbrace{i} \\ i \end{array}}_{2} \\$$



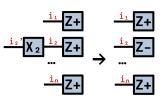
$$j = n/2$$

$$X_{j}$$

$$X_{j}|Z + Z + \dots Z + \rangle = |Z + Z + \dots Z - \dots Z + \rangle$$

$$|Z + Z + \dots Z - \dots Z + \rangle$$

```
1 \max_{j}(X_{j}Z_{p})
2 \max_{j}(Z_{p}, X_{j}Z_{p})
3 \max_{j}(X_{j}Z_{p}, x_{j}Z_{p})
```



```
\begin{array}{l} 1 \; (\text{product state}) \\ \approx 0 \\ \approx 1 \end{array}
```

```
1  function ising(n; h)
2  H = OpSum()
3  for j in 1:(n - 1)
4  H -= "Z", j, "Z", j + 1
5  end
6  for j in 1:n
7  H += h, "X", j
8  end
9  return H
10  end
```

```
n sites H = -\sum_{j}^{n-1} Z_{j} Z_{j+1} + h \sum_{j}^{n} X_{j}
```

```
1  function ising(n; h)
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9  return H
10  end
```

```
1 h = 0.5

2 H = MPO(ising(n; h=h), i)

3 maxlinkdim(H)

4 Zp = MPS(i, "Z+")

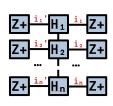
5 inner(Zp', H, Zp)
```

$$\langle Z+Z+...Z+|H|Z+Z+...Z+\rangle$$

 \approx -(n - 1) = -29

```
1 function ising(n; h)
2 H = OpSum()
3 for j in 1:(n - 1)
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```

```
 \begin{array}{ll} 1 & h = 0.5 \\ 2 & H = MPO(ising(n; h = h), i) \\ 3 & maxlinkdim(H) \\ 4 & Zp = MPS(i, "Z+") \\ 5 & inner(Zp', H, Zp) \\ 6 \\ \end{array}
```



```
1 \psi_0 = \text{MPS}(i, \text{"Z+"}) |0\rangle = |\text{Z+Z+...Z+}\rangle
2 3 \psi = \underset{\text{minimize}(E, \partial E, \psi_0; \\ \text{nsteps}=50, \gamma=0.1, \\ \text{maxdim}=10, \text{cutoff}=1e-5)} Minimize over \psi: \langle \psi | H | \psi \rangle / \langle \psi | \psi \rangle
6 7 E_{dmrg}, \psi_{dmrg} = \underset{\text{dmrg}(H, \psi_0; \\ \text{nsweeps}=10, \\ \text{maxdim}=10, \text{cutoff}=1e-5)} DMRG solves: H | \psi \rangle \approx | \psi \rangle
```

```
1 \psi_0 = \text{MPS}(i, "Z+")

2 \psi = \text{minimize}(E, \partial E, \psi_0;

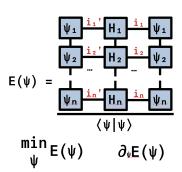
4 \text{nsteps}=50, \gamma=0.1,

5 \text{maxdim}=10, \text{cutoff}=1\text{e-}5)

6 E_{dmrg}, \psi_{dmrg} = \text{dmrg}(H, \psi_0;

8 \text{nsweeps}=10,

9 \text{maxdim}=10, \text{cutoff}=1\text{e-}5)
```



```
1 \psi_0 = \text{MPS}(i, "Z+")

2 \psi = \text{minimize}(E, \partial E, \psi_0;

4 \text{nsteps} = 50, \gamma = 0.1,

5 \text{maxdim} = 10, \text{cutoff} = 1\text{e-}5)

6 E_{dmrg}, \psi_{dmrg} = \text{dmrg}(H, \psi_0;

8 \text{nsweeps} = 10,

9 \text{maxdim} = 10, \text{cutoff} = 1\text{e-}5)
```

```
E(\psi) = \frac{\psi_{1} \frac{i_{1}' H_{1} \frac{i_{1}}{\psi_{1}}}{\psi_{2} \frac{i_{2}' H_{2} \frac{i_{2}}{\psi_{2}}}{\dots \frac{i_{n}' H_{n} \frac{i_{n}}{\psi_{n}}}}}{\langle \psi | \psi \rangle}
\min_{\psi} E(\psi) \qquad \partial_{\psi} E(\psi)
```

```
1 \max \lim \dim(\psi_0)

2 \max \lim \dim(\psi)

3 \max \lim \dim(\psi_{dmrg})

4 E(\psi_0), \operatorname{norm}(\partial(\psi_0))

5 E(\psi), \operatorname{norm}(\partial E(\psi))

6 E(\psi_{dmrg}), \operatorname{norm}(\partial E(\psi_{dmrg}))
```

```
= 1 (product state)

= 3 (entangled state)

= 2 (entangled state)

\approx (-29, 5.4772256)

\approx (-31.0317917, 0.06673780)

\approx (-31.0356110, 0.02413237)
```

```
1 Ry_layer(\theta, i) = [op("Ry", i[j]; \theta=\theta[j]) for j in 1:n]
2 CX_layer(i) = [op("CX", i[j], i[j+1]) for j in 1:2:(n-1)]
```

Tutorial: n-site circuit optimization

```
1 Ry_layer(\theta, i) = [op("Ry", i[j]; \theta = \theta[j]) for j in 1:n]
2 CX_layer(i) = [op("CX", i[j], i[j+1]) for j in 1:2:(n-1)]
```

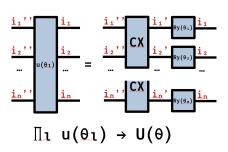
```
\begin{array}{lll} & \textbf{function} \ U(\theta, \ i; \ nlayers) \\ 2 & n = length(i) \\ 3 & U_{\theta} = Ry\_layer(\theta[1:n], \ i) \\ 4 & \textbf{for} \ l \ in \ 1: (nlayers - 1) \\ 5 & \theta_{l} = \theta[(1:n) \ .+ \ l * \ n] \\ 6 & U_{\theta} = [U_{\theta}; \ CX\_layer(i)] \\ 7 & U_{\theta} = [U_{\theta}; \ Ry\_layer(\theta_{l}, \ i)] \\ 8 & \textbf{end} \\ 9 & \textbf{return} \ U_{\theta} \\ 10 & \textbf{end} \end{array}
```

```
U(\theta) = Ry_1(\theta_1) \dots Ry_n(\theta_n)
* CX_{1,2} \dots CX_{n-1,n}
* Ry_1(\theta_{n+1}) \dots Ry_n(\theta_{2n})
* ...
```

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```
1 Ry_layer(\theta, i) = [op("Ry", i[j]; \theta=\theta[j]) for j in 1:n]
2 CX_layer(i) = [op("CX", i[j], i[j+1]) for j in 1:2:(n-1)]
```

```
\begin{array}{ll} \textbf{function} \ U(\theta, \, i; \, nlayers) \\ \textbf{2} & \textbf{n} = \textbf{length}(i) \\ \textbf{3} & \textbf{U}_{\theta} = \textbf{Ry\_layer}(\theta[1:n], \, i) \\ \textbf{4} & \textbf{for} \ l \ in \ 1: (nlayers - 1) \\ \textbf{5} & \theta_l = \theta[(1:n) \ .+ \ l * \ n] \\ \textbf{6} & \textbf{U}_{\theta} = [\textbf{U}_{\theta}; \ \textbf{CX\_layer}(i)] \\ \textbf{7} & \textbf{U}_{\theta} = [\textbf{U}_{\theta}; \ \textbf{Ry\_layer}(\theta_l, \, i)] \\ \textbf{8} & \textbf{end} \\ \textbf{9} & \textbf{return} \ \textbf{U}_{\theta} \\ \textbf{10} & \textbf{end} \\ \end{array}
```



```
1 \psi_0 = \text{MPS}(i, "Z+")

2 \text{nlayers} = 6

3 \text{function E}(\theta)

4 \psi_\theta = \text{apply}(\text{U}(\theta, i; \text{nlayers}), \psi_0)

5 \text{return inner}(\psi_\theta', \text{H}, \psi_\theta)

6 \text{end}

7 \theta_0 = \text{zeros}(\text{nlayers} * \text{n})

9 \theta = \text{minimize}(\text{E}, \partial \text{E}, \theta_0; \text{nsteps} = 20, <math>\gamma = 0.1)
```

$$|0\rangle = |Z+Z+...Z+\rangle$$

Minimize over θ : $|\theta\rangle = U(\theta)|0\rangle$ $E(\theta) = \langle \theta|H|\theta\rangle$

```
1 \psi_0 = \text{MPS}(i, "Z+")

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3 \text{function E}(\theta)

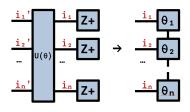
4 \psi_\theta = \text{apply}(U(\theta, i; \text{nlayers}), \psi_0)

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```
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```

```
1 \max \lim (\psi_0)

2 \max \lim (\psi_\theta)

3 E(\theta_0), \operatorname{norm}(\partial E(\theta_0))

4 E(\theta), \operatorname{norm}(\partial E(\theta))
```

```
1 (product state)
2 (entangled state)
(-29, 5.773335)
(-31.017062, 0.000759)
```

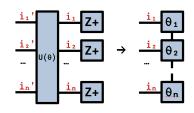
```
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       nlavers = 6
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         \psi_{\theta} = \text{apply}(U(\theta, i; \text{nlayers}), \psi_0)
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       end
       \theta_0 = \text{zeros}(\text{nlayers} * \text{n})
      \theta = \text{minimize}(E, \partial E, \theta_0);
              nsteps=20, \gamma=0.1)
10
       \operatorname{maxlinkdim}(\psi_0)
```

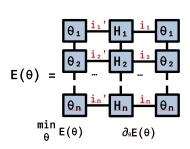
```
1 \operatorname{maxlinkdim}(\psi_0)

2 \operatorname{maxlinkdim}(\psi_{\theta})

3 \operatorname{E}(\theta_0), \operatorname{norm}(\partial \operatorname{E}(\theta_0))

4 \operatorname{E}(\theta), \operatorname{norm}(\partial \operatorname{E}(\theta))
```





```
1 \psi_0 = \text{MPS}(i, "Z+")

2 \text{nlayers} = 6

3 \text{function F}(\theta)

4 \psi_\theta = \text{apply}(U(\theta, i; \text{nlayers}), \psi_0)

5 \text{return -abs}(\text{inner}(\psi', \psi_\theta))^2

6 \text{end}

7 \theta_0 = \text{zeros}(\text{nlayers} * n)

9 \theta = \text{minimize}(F, \partial F, \theta_0; \text{nsteps} = 20, \gamma = 0.1)
```

```
# |0\rangle = |Z+Z+...Z+\rangle

# Minimize over \theta:

# F(\theta) = -|\langle \psi | U(\theta) | 0 \rangle|^2

# = -|\langle \psi | \theta \rangle|^2
```

```
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```

$$F(\theta) = - \begin{bmatrix} \psi_1 & \vdots & \vdots & \vdots & \vdots \\ \psi_2 & \vdots & \vdots & \vdots & \vdots \\ \psi_n & \vdots & \vdots & \vdots & \vdots \\ \psi_n & \vdots & \vdots & \vdots & \vdots \\ \psi_n & \vdots & \vdots & \vdots & \vdots \\ \psi_n & \vdots & \vdots & \vdots & \vdots \\ \theta_2 & \vdots & \vdots & \vdots & \vdots \\ \psi_n & \vdots & \vdots & \vdots & \vdots \\ \theta_2 & \vdots & \vdots & \vdots \\ \psi_n & \vdots & \vdots & \vdots \\ \theta_2 &$$

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```

```
1 \max \lim (\psi_0)

2 \max \lim (\psi_\theta)

3 F(\theta_0), \operatorname{norm}(\partial F(\theta_0))

4 F(\theta), \operatorname{norm}(\partial F(\theta))
```

```
# 1 (product state)
# 2 (entangled state)
# (-0.556066, 0.895717)
# (-0.995230, 0.048939)
```

► Noisy state and process simulation (PastaQ). AD/optimization support in progress.

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- ► Conserved quantities with multithreaded block sparse tensors (ITensor/PastaQ).
- ▶ More that I am probably forgetting... Ask Giacomo and me for more details.



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- ► Improved gradient optimization: higher order derivatives, preconditioners, isometrically constrained gradient optimization, etc.

► Free fermions/matchgates and conversion to tensor networks.

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- ▶ I'm interested in building general tools and algorithms, and I'm looking for people with problems to solve. Also, we need help, code to contributions are welcome!

