

# Analyzing Quantum Many-Body Systems with ITensor and PastaQ

Matthew Fishman

Center for Computational Quantum Physics (CCQ)

Flatiron Institute, NY

[mtfishman.github.io](https://mtfishman.github.io)

[github.com/mtfishman/ITensorTutorials.jl](https://github.com/mtfishman/ITensorTutorials.jl)

June 18, 2022

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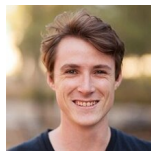
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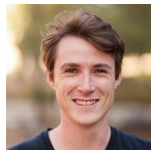
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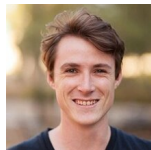
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- ▶ We are hiring postdocs, full-time scientists, part-time and full-time software developers, interns, etc.

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SIMONS FOUNDATION

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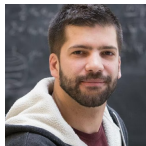


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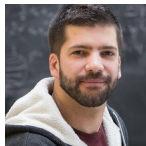


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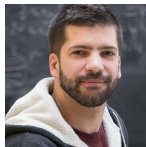




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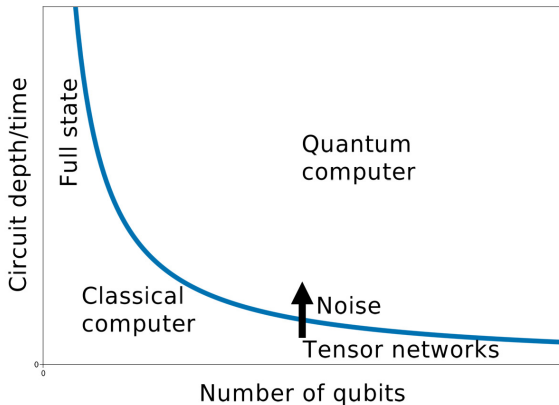


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- ▶ Find out more: [github.com/GTorlai/PastaQ.jl](https://github.com/GTorlai/PastaQ.jl)



## *When should I use tensor networks?*

- In my opinion, tensor networks are the best general purpose tool we have right now for simulating and analyzing quantum computers.



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  - ▶ ITensor and PastaQ handle this seamlessly.
  - ▶ This is not the focus of ITensor and PastaQ at the moment, specialized libraries like [Yao.jl](#) may be faster.
- ▶ Tensor networks are a common, general language for reasoning about quantum many-body systems (for example, quantum circuits).

# *What are tensor networks?*

Vector  $V_i$   
Order-1 tensor



Matrix  $M_{ij}$   
Order-2 tensor

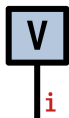


Tensor  $T_{ijk}$   
Order-3 tensor



# What are tensor networks?

Vector  $V_i$   
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$$\langle V|V \rangle = V_i V_i$$



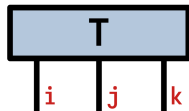
Matrix  $M_{ij}$   
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$$MM = M_{kj} M_{ji}$$



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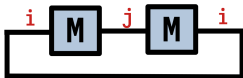
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$$\text{tr}(MM) = M_{ij} M_{ji}$$



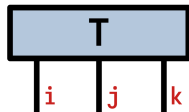
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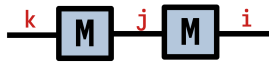
$$M|V \rangle = M_{ji} V_i$$



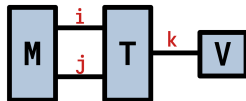
Tensor  $T_{ijk}$   
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$$MM = M_{kj} M_{ji}$$



$$M_{ij} T_{ijk} V_k$$



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2. Launch Julia:

```
1 $ julia
```

3. Type the following commands:

```
1 julia> using Pkg
2
3 julia> Pkg.add("ITensors")
4 [...]
5
6 julia> Pkg.add("PastaQ")
7 [...]
```

## *How do I install ITensor/PastaQ?*

Now you can use ITensors and PastaQ:

```
1 julia> using ITensors
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3 julia> i = Index(2);
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5 julia> A = ITensor(i);
```



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```
1 julia> using PastaQ
2
3 julia> gates = [("X", 1), ("CX", (1, 3))];
4
5 julia>  $\psi$  = runcircuit(gates);
```

## *Tutorial: One-site state basics*

```
1 using ITensors
2
3 i = Index(2)
4
5
```

Load ITensor

2-dimensional labeled  
Hilbert space  
(dim=2|id=510)

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## *Tutorial: One-site state basics*

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3 i = Index(2)
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```
1 Zp = ITensor(i)
2 Zp[i==1] = 1
3
4 Zp = ITensor([1, 0], i)
```

i

$$|Z+\rangle = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

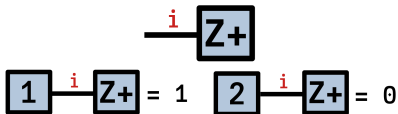
Construct from a Vector

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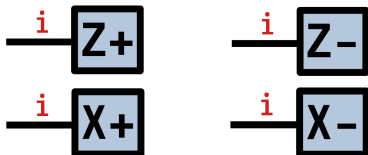
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```
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2 Zm = ITensor([0, 1], i)
3 Xp = ITensor([1, 1]/√2, i)
4 Xm = ITensor([1, -1]/√2, i)
```

$$\begin{aligned} |Z+\rangle &= \begin{bmatrix} 1 \\ 0 \end{bmatrix}, & |Z-\rangle &= \begin{bmatrix} 0 \\ 1 \end{bmatrix} \\ |X+\rangle &= \begin{bmatrix} 1 \\ 1 \end{bmatrix} / \sqrt{2}, & |X-\rangle &= \begin{bmatrix} 1 \\ -1 \end{bmatrix} / \sqrt{2} \end{aligned}$$

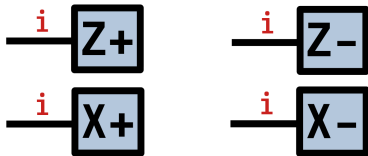
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```



```
1 Xp = (Zp + Zm)/√2
2
3
4
5 dag(Zp) * Xp
6 inner(Zp, Xp)
```

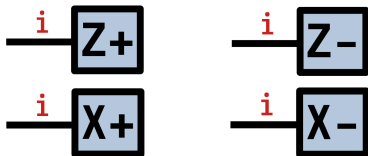
$$|X+\rangle = (|Z+\rangle + |Z-\rangle)/\sqrt{2}$$

$$\langle Z+ | X+ \rangle \approx 1/\sqrt{2}$$



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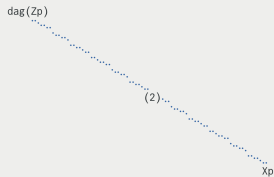
$$X_+ = \frac{Z_+ + Z_-}{\sqrt{2}}$$

$$Z_+ X_+ = 1/\sqrt{2}$$

## *Tutorial: One-site state basics*

```
1 using ITensorUnicodePlots
2
3 @visualize dag(Zp) * Xp
```

```
julia> @visualize dag(Zp) * Xp
```



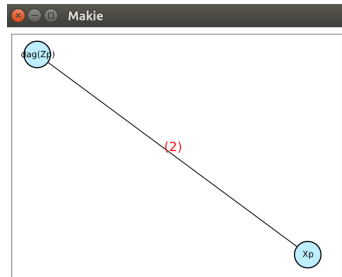
# Tutorial: One-site state basics

```
1 using ITensorUnicodePlots
2
3 @visualize dag(Zp) * Xp
```

```
julia> @visualize dag(Zp) * Xp
```



```
1 using ITensorGLMakie
2
3 @visualize dag(Zp) * Xp
```



## *Tutorial: One-site states*

```
1 i = Index(2, "S=1/2")
```

(dim=2|id=25|"S=1/2")

"S=1/2" defines an operator basis

Additionally:  
"Qubit", "Qudit",  
"Electron", ...

## Tutorial: One-site states

```
1 i = Index(2, "S=1/2")
```

(dim=2|id=25|"S=1/2")

"S=1/2" defines an operator basis

Additionally:

"Qubit", "Qudit",  
"Electron", ...

```
1 Zp = state("Z+", i)
2 Zm = state("Z-", i)
3 Xp = state("X+", i)
4 Xm = state("X-", i)
```

```
1 ITensor([1 0], i)
2 ITensor([0 1], i)
3 ITensor([1 1]/√2, i)
4 ITensor([1 -1]/√2, i)
```

## *Tutorial: Custom one-site states*

```
1 import ITensors: state
2
3
4 function state(
5     ::StateName "iX-",
6     ::SiteType "S=1/2"
7 )
8     return [im -im]/√2
9 end
```

Overload ITensors.jl  
behavior

Define a state with the  
name “iX-”

## Tutorial: Custom one-site states

```
1 import ITensors: state
2
3
4 function state(
5     ::StateName"iX-",
6     ::SiteType"S=1/2"
7 )
8     return [im -im]/√2
9 end
```

```
1 iXm = state("iX-", i)
2
3
4 inner(Zm, iXm)
```

Overload ITensors.jl  
behavior

Define a state with the  
name “iX-”

$$|iX-\rangle = i|X-\rangle$$

$$\langle Z- | iX- \rangle = -i/\sqrt{2}$$

## Tutorial: Custom one-site states

```
1 import ITensors: state
2
3
4 function state(
5     ::StateName"iX-",
6     ::SiteType"S=1/2"
7 )
8     return [im -im]/√2
9 end
```

```
1 iXm = state("iX-", i)
2
3
4 inner(Zm, iXm)
```

Overload ITensors.jl  
behavior

Define a state with the  
name “iX-”

$$\text{---} \overset{i}{\boxed{iX+}} = \left( \text{---} \overset{i}{\boxed{X+}} \right) * i$$



## *Tutorial: Priming*

```
1 i = Index(2)
2 j = Index(2)
3
4 i ≠ j
```

(dim=2|id=837)

(dim=2|id=899)

## *Tutorial: Priming*

```
1 i = Index(2)
2 j = Index(2)
3
4 i ≠ j
```

i ≠ j

## Tutorial: Priming

```
1 i = Index(2)
2 j = Index(2)
3
4 i ≠ j
```

```
1 i = Index(2)
2
3 prime(i) == i'
4
5 i ≠ i'
6 noprime(i') == i
```

$$\underline{i} \neq \underline{j}$$

(dim=2|id=837)

(dim=2|id=837)'

## Tutorial: Priming

```
1 i = Index(2)
2 j = Index(2)
3
4 i ≠ j
```

```
1 i = Index(2)
2
3 prime(i) == i'
4
5 i ≠ i'
6 noprime(i') == i
```

$$\underline{i} \neq \underline{j}$$

$$\text{prime}\left(\underline{i}\right) = \underline{i'}$$
$$\underline{i} \neq \underline{i'}$$

## *Tutorial: One-site operators*

```
1 i = Index(2, "S=1/2")
2 Z = ITensor(i', i)
3 Z[i'=>1, i=>1] = 1
4 Z[i'=>2, i=>2] = -1
```

$$Z = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$

## Tutorial: One-site operators

```
1 i = Index(2, "S=1/2")
2 Z = ITensor(i', i)
3 Z[i'=>1, i=>1] = 1
4 Z[i'=>2, i=>2] = -1
```



## Tutorial: One-site operators

```
1 i = Index(2, "S=1/2")
2 Z = ITensor(i', i)
3 Z[i'=>1, i=>1] = 1
4 Z[i'=>2, i=>2] = -1
```

```
1 z = [1 0; 0 -1]
2
3
4
5 Z = ITensor(z, i', i)
6
7
8 Z = op("Z", i)
```



Matrix representation  $Z$

Convert to ITensor

Use predefined definition

## *Tutorial: One-site operators*

```
1 Z = op("Z", i)
2 X = op("X", i)
3
4 Zp = state("Z+", i)
5 Zm = state("Z-", i)
```

Z

X

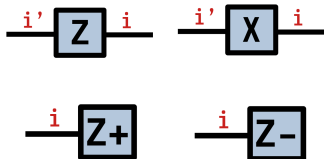
$|Z+\rangle$

$|Z-\rangle$



## Tutorial: One-site operators

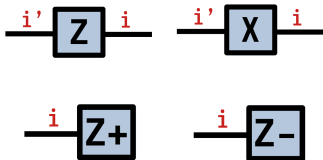
```
1 Z = op("Z", i)
2 X = op("X", i)
3
4 Zp = state("Z+", i)
5 Zm = state("Z-", i)
```



## Tutorial: One-site operators

```
1 Z = op("Z", i)
2 X = op("X", i)
3
4 Zp = state("Z+", i)
5 Zm = state("Z-", i)
```

```
1 X * Zp == Zm'
2 noprime(X * Zp) == Zm
```

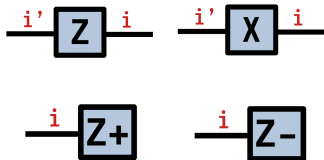


$$X|Z+\rangle = |Z-\rangle$$

## Tutorial: One-site operators

```
1 Z = op("Z", i)
2 X = op("X", i)
3
4 Zp = state("Z+", i)
5 Zm = state("Z-", i)
```

```
1 X * Zp == Zm'
2 noprime(X * Zp) == Zm
```



## *Tutorial: One-site operators*

```
1 dag(Zm)' * X * Zp  
2 inner(Zm', X, Zp)
```

$$\langle Z - |X|Z+ \rangle \approx 1$$

## *Tutorial: One-site operators*

```
1 dag(Zm)' * X * Zp  
2 inner(Zm', X, Zp)
```

$$\boxed{Z-} \overset{i'}{\text{---}} \boxed{X} \overset{i}{\text{---}} \boxed{Z+} = 1$$

## Tutorial: One-site operators

```
1 dag(Zm)' * X * Zp
2 inner(Zm', X, Zp)
```

$$\boxed{Z-} \overset{i'}{\text{---}} \boxed{X} \overset{i}{\text{---}} \boxed{Z+} = 1$$

```
1 apply(X, Zp) ==
2   noprime(X * Zp)
3
4
5
6 inner(Zm, apply(X, Zp))
```

$$X|Z+\rangle$$

$$\langle Z- | X | Z+ \rangle \approx 1$$

## Tutorial: One-site operators

```
1 dag(Zm)' * X * Zp
2 inner(Zm', X, Zp)
```

$$\boxed{Z-} \overset{i'}{\text{---}} \boxed{X} \overset{i}{\text{---}} \boxed{Z+} = 1$$

```
1 apply(X, Zp) ==
2   noprime(X * Zp)
3
4
5
6 inner(Zm, apply(X, Zp))
```

$$\begin{aligned} & \text{apply}\left(\overset{i'}{\text{---}} \boxed{X} \overset{i}{\text{---}}, \overset{i}{\text{---}} \boxed{Z+}\right) \\ &= \text{noprime}\left(\overset{i'}{\text{---}} \boxed{X} \overset{i}{\text{---}} \boxed{Z+}\right) \\ &= \overset{i}{\text{---}} \boxed{Z-} \end{aligned}$$

## *Tutorial: Custom one-site operators*

Overload ITensors.jl  
behavior

```
1  import ITensors: op
2
3  function op(
4      ::OpName"iX",
5      ::SiteType"S=1/2"
6  )
7      return [
8          0 im
9          im 0
10     ]
11  end
```



## Tutorial: Custom one-site operators

```
1  import ITensors: op
2
3  function op(
4      ::OpName"iX",
5      ::SiteType"S=1/2"
6  )
7      return [
8          0 im
9          im 0
10     ]
11  end
```

$$\text{---} \overset{i'}{\boxed{iX}} \text{---}^i = \left( \text{---} \overset{i'}{\boxed{X}} \text{---}^i \right) * i$$

## Tutorial: Custom one-site operators

```
1 import ITensors: op
2
3 function op(
4     ::OpName"iX",
5     ::SiteType"S=1/2"
6 )
7     return [
8         0 im
9         im 0
10    ]
11 end
```

```
1 op("iX", i)
```

$$\text{---} \overset{i'}{\boxed{iX}} \text{---}^i = \left( \text{---} \overset{i'}{\boxed{X}} \text{---}^i \right) * i$$

## Tutorial: Custom one-site operators

```
1 import ITensors: op
2
3 function op(
4     ::OpName"iX",
5     ::SiteType"S=1/2"
6 )
7     return [
8         0 im
9         im 0
10    ]
11 end
```

```
1 op("iX", i)
```

$$\text{---} \overset{i'}{\boxed{iX}} \text{---}^i = \left( \text{---} \overset{i'}{\boxed{X}} \text{---}^i \right) * i$$

```
1 X * im
```

## *Tutorial: Two-site states*

```
1 i1 = Index(2, "S=1/2")
2 i2 = Index(2, "S=1/2")
3
4 i1 ≠ i2
5
6 ZpZm = ITensor(i1, i2)
7 ZpZm[i1=>1, i2=>2] = 1
```

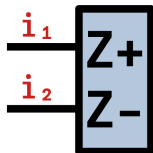
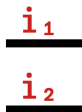
(dim=2|id=505|“S=1/2”)

(dim=2|id=576|“S=1/2”)

$$|Z+\rangle_1 |Z-\rangle_2 = |Z+Z-\rangle$$

## Tutorial: Two-site states

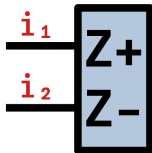
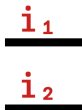
```
1 i1 = Index(2, "S=1/2")
2 i2 = Index(2, "S=1/2")
3
4 i1 ≠ i2
5
6 ZpZm = ITensor(i1, i2)
7 ZpZm[i1=>1, i2=>2] = 1
```



## Tutorial: Two-site states

```
1 i1 = Index(2, "S=1/2")
2 i2 = Index(2, "S=1/2")
3
4 i1 != i2
5
6 ZpZm = ITensor(i1, i2)
7 ZpZm[i1=>1, i2=>2] = 1
```

```
1 Zp1 = state("Z+", i1)
2 Zp2 = state("Z+", i2)
3
4 Zm1 = state("Z-", i1)
5 Zm2 = state("Z-", i2)
6
7 ZpZm = Zp1 * Zm2
```



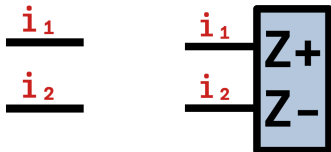
$$|Z+\rangle_1$$
$$|Z+\rangle_2$$

$$|Z-\rangle_1$$
$$|Z-\rangle_2$$

$$|Z+Z-\rangle = |Z+\rangle_1 |Z-\rangle_2$$

## Tutorial: Two-site states

```
1 i1 = Index(2, "S=1/2")
2 i2 = Index(2, "S=1/2")
3
4 i1 != i2
5
6 ZpZm = ITensor(i1, i2)
7 ZpZm[i1=>1, i2=>2] = 1
```



```
1 Zp1 = state("Z+", i1)
2 Zp2 = state("Z+", i2)
3
4 Zm1 = state("Z-", i1)
5 Zm2 = state("Z-", i2)
6
7 ZpZm = Zp1 * Zm2
```



## *Tutorial: Two-site states*

```
1   $\psi$  = ITensor(i1, i2)
2   $\psi[i1=>1, i2=>2]$  =  $1/\sqrt{2}$ 
3   $\psi[i1=>2, i2=>1]$  =  $1/\sqrt{2}$ 
4
5   $\psi$  = (Zp1 * Zm2 +
6         Zm1 * Zp2)/ $\sqrt{2}$ 
```

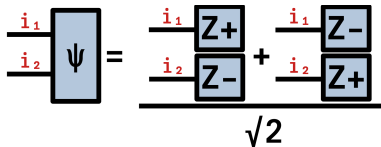
$$(|Z+\rangle|Z-\rangle + |Z-\rangle|Z+\rangle)/\sqrt{2}$$

From single-site states



## Tutorial: Two-site states

```
1   $\psi = \text{ITensor}(i1, i2)$   
2   $\psi[i1 \Rightarrow 1, i2 \Rightarrow 2] = 1/\sqrt{2}$   
3   $\psi[i1 \Rightarrow 2, i2 \Rightarrow 1] = 1/\sqrt{2}$   
4  
5   $\psi = (Z_{p1} * Z_{m2} +$   
6       $Z_{m1} * Z_{p2})/\sqrt{2}$ 
```



## Tutorial: Two-site states

```
1   $\psi = \text{ITensor}(i1, i2)$ 
2   $\psi[i1 \Rightarrow 1, i2 \Rightarrow 2] = 1/\sqrt{2}$ 
3   $\psi[i1 \Rightarrow 2, i2 \Rightarrow 1] = 1/\sqrt{2}$ 
4
5   $\psi = (\text{Zp1} * \text{Zm2} +$ 
6          $\text{Zm1} * \text{Zp2})/\sqrt{2}$ 
```

```
1   $\text{inner}(\text{ZpZm}, \psi) == 1/\sqrt{2}$ 
2
3
4   $\text{U}, \text{S}, \text{V} = \text{svd}(\text{ZmZp}, i1)$ 
5   $\text{diag}(\text{S}) == [1, 0]$ 
6
7   $\text{U}, \text{S}, \text{V} = \text{svd}(\psi, i1)$ 
8   $\text{diag}(\text{S}) == [1/\sqrt{2}, 1/\sqrt{2}]$ 
```

The diagram shows a blue box labeled  $\Psi$  with two input legs labeled  $i_1$  and  $i_2$ . This is equal to the sum of two terms, each divided by  $\sqrt{2}$ . The first term consists of two stacked blue boxes: the top one is labeled  $Z+$  and the bottom one is labeled  $Z-$ , with input legs  $i_1$  and  $i_2$  respectively. The second term consists of two stacked blue boxes: the top one is labeled  $Z-$  and the bottom one is labeled  $Z+$ , with input legs  $i_1$  and  $i_2$  respectively.

The diagram shows the singular value decomposition of the two-site state. The first line shows  $\text{svd}$  applied to a blue box labeled  $Z+Z-$  with input legs  $i_1$  and  $i_2$ . The second line shows the result as a product of three tensors: a blue box  $U$  with input leg  $i_1$  and output leg  $u$ ; a blue box  $S$  with input leg  $u$  and output leg  $v$ ; and a blue box  $V$  with input leg  $v$  and output leg  $i_2$ . The third line shows the singular value matrix  $S$  as a blue box with input leg  $u$  and output leg  $v$ , containing the values  $\begin{bmatrix} 1 & 0 \end{bmatrix}$ .

## Tutorial: Two-site states

```

1   $\psi = \text{ITensor}(i1, i2)$ 
2   $\psi[i1 \Rightarrow 1, i2 \Rightarrow 2] = 1/\sqrt{2}$ 
3   $\psi[i1 \Rightarrow 2, i2 \Rightarrow 1] = 1/\sqrt{2}$ 
4
5   $\psi = (\text{Zp1} * \text{Zm2} +$ 
6       $\text{Zm1} * \text{Zp2})/\sqrt{2}$ 

```

```

1   $\text{inner}(\text{ZpZm}, \psi) == 1/\sqrt{2}$ 
2
3
4   $U, S, V = \text{svd}(\text{ZmZp}, i1)$ 
5   $\text{diag}(S) == [1, 0]$ 
6
7   $U, S, V = \text{svd}(\psi, i1)$ 
8   $\text{diag}(S) == [1/\sqrt{2}, 1/\sqrt{2}]$ 

```

$$\psi = \frac{\begin{matrix} i_1 \\ i_2 \end{matrix} \begin{matrix} \boxed{Z+} \\ \boxed{Z-} \end{matrix} + \begin{matrix} i_1 \\ i_2 \end{matrix} \begin{matrix} \boxed{Z-} \\ \boxed{Z+} \end{matrix}}{\sqrt{2}}$$

$$\text{svd}\left(\begin{matrix} i_1 \\ i_2 \end{matrix} \boxed{Z+Z-}\right) = \begin{matrix} i_1 \\ u \end{matrix} \boxed{U} \begin{matrix} u \\ v \end{matrix} \boxed{S} \begin{matrix} v \\ i_2 \end{matrix} \boxed{V}$$

$$\begin{matrix} u \\ \end{matrix} \boxed{S} \begin{matrix} v \\ \end{matrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$\text{svd}\left(\begin{matrix} i_1 \\ i_2 \end{matrix} \boxed{\psi}\right) = \begin{matrix} i_1 \\ u \end{matrix} \boxed{U} \begin{matrix} u \\ v \end{matrix} \boxed{S} \begin{matrix} v \\ i_2 \end{matrix} \boxed{V}$$

$$\begin{matrix} u \\ \end{matrix} \boxed{S} \begin{matrix} v \\ \end{matrix} = \begin{bmatrix} 1/\sqrt{2} \\ 1/\sqrt{2} \end{bmatrix}$$

## *Tutorial: Two-site operators*

```
1 H = ITensor(i1', i2', i1,  
              i2)  
2 H[i1'=>2, i2'=>1,  
3   i1=>2, i2=>1] = -1  
4 # ...
```

Make a Hamiltonian:

Transverse field Ising ( $n = 2$ )

$$H = -\sum_j^{n-1} Z_j Z_{j+1} + h \sum_j^n X_j$$

## Tutorial: Two-site operators

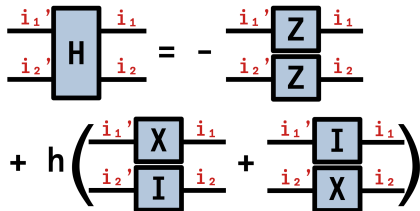
```
1 H = ITensor(i1', i2', i1,  
2       i2)  
3   H[i1'=>2, i2'=>1,  
4     i1=>2, i2=>1] = -1  
4 # ...
```

```
1 Id1 = op("Id", i1)  
2 Z1 = op("Z", i1)  
3 X1 = op("X", i1)  
4 # ...  
5  
6 ZZ = Z1 * Z2  
7 XI = X1 * Id2  
8 IX = Id1 * X2  
9  
10 h = 0.5  
11 H = -ZZ + h * (XI + IX)
```

Make a Hamiltonian:

Transverse field Ising ( $n = 2$ )

$$H = -\sum_j^{n-1} Z_j Z_{j+1} + h \sum_j^n X_j$$



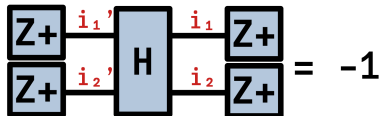
## *Tutorial: Two-site operators*

```
1 inner(Zp' * Zp', H, Zp * Zp)
```

$$\langle Z+Z+ | H | Z+Z+ \rangle$$

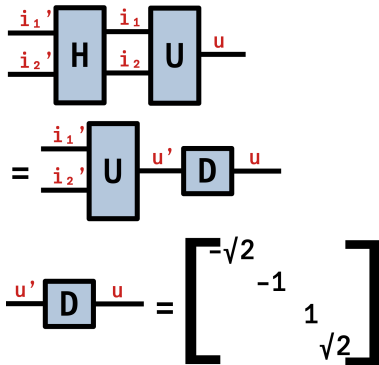
## Tutorial: Two-site operators

```
1 inner(Zp' * Zp', H, Zp * Zp)
```



## Tutorial: Two-site operators

```
1 D, U = eigen(H)
2 diag(D) == [-√2, -1, 1, √2]
```





## *Tutorial: Custom two-site operators*

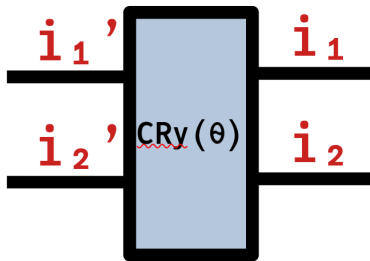
```
1  import ITensors: op
2
3  function op(
4      ::OpName"CRy",
5      ::SiteType"S=1/2";
6       $\theta$ 
7  )
8      c = cos( $\theta/2$ )
9      s = sin( $\theta/2$ )
10     return [
11         1 0 0 0
12         0 1 0 0
13         0 0 c -s
14         0 0 s  c
15     ]
16 end
```

Controlled-Ry (CRy)  
rotation gate

$\text{CRy}(\theta)$

## Tutorial: Custom two-site operators

```
1 import ITensors: op
2
3 function op(
4     ::OpName"CRy",
5     ::SiteType"S=1/2";
6     θ
7 )
8     c = cos(θ/2)
9     s = sin(θ/2)
10    return [
11        1 0 0 0
12        0 1 0 0
13        0 0 c -s
14        0 0 s  c
15    ]
16 end
```



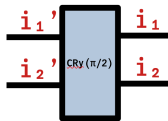
## *Tutorial: Custom two-site operators*

```
1 CRy = op("CRy", i1, i2;  $\theta=\pi/2$ )
```

Controlled-rotation gate  
 $\text{CRy}(\pi/2)$

## *Tutorial: Custom two-site operators*

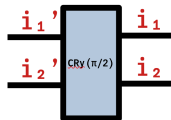
```
1 CRy = op("CRy", i1, i2;  $\theta=\pi/2$ )
```



## Tutorial: Custom two-site operators

```
1 CRy = op("CRy", i1, i2;  $\theta=\pi/2$ )
```

```
1 apply(CRy, Zm1 * Zp2) ==  
2 Zm1 * Xp2
```

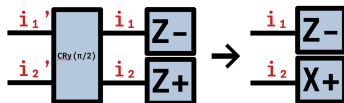
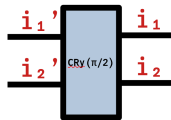


$$\text{CRy}(\pi/2)|Z-Z+\rangle = |Z-X+\rangle$$

## Tutorial: Custom two-site operators

```
1 CRy = op("CRy", i1, i2;  $\theta=\pi/2$ )
```

```
1 apply(CRy, Zm1 * Zp2) ==  
2      Zm1 * Xp2
```



## *Tutorial: Two-site state optimization*

```
1 function E( $\psi$ )  
2    $\psi H \psi = \text{inner}(\psi', H, \psi)$   
3    $\psi \psi = \text{inner}(\psi, \psi)$   
4   return  $\psi H \psi / \psi \psi$   
5 end
```

$$E(\psi) = \langle \psi | H | \psi \rangle / \langle \psi | \psi \rangle$$

## Tutorial: Two-site state optimization

```
1 function E( $\psi$ )  
2    $\psi H \psi = \text{inner}(\psi', H, \psi)$   
3    $\psi \psi = \text{inner}(\psi, \psi)$   
4   return  $\psi H \psi / \psi \psi$   
5 end
```

$$E(\psi) = \frac{\begin{array}{c} \boxed{\psi} \begin{array}{c} i_1' \\ i_2' \end{array} \boxed{H} \begin{array}{c} i_1 \\ i_2 \end{array} \boxed{\psi} \end{array}}{\begin{array}{c} \boxed{\psi} \begin{array}{c} i_1 \\ i_2 \end{array} \boxed{\psi} \end{array}}$$



## Tutorial: Two-site state optimization

```
1 function E( $\psi$ )
2    $\psi H \psi$  = inner( $\psi'$ , H,  $\psi$ )
3    $\psi \psi$  = inner( $\psi$ ,  $\psi$ )
4   return  $\psi H \psi$  /  $\psi \psi$ 
5 end
```

```
1 function minimize(f,  $\partial f$ , x;
2   nsteps,  $\gamma$ )
3   for n in 1:nsteps
4      $x = x - \gamma * \partial f(x)$ 
5   end
6   return x
7 end
```

$$E(\psi) = \frac{\begin{array}{|c|} \hline \Psi \\ \hline \end{array} \begin{array}{|c|} \hline i_1' \\ \hline i_2' \end{array} \begin{array}{|c|} \hline H \\ \hline \end{array} \begin{array}{|c|} \hline i_1 \\ \hline i_2 \end{array} \begin{array}{|c|} \hline \Psi \\ \hline \end{array}}{\begin{array}{|c|} \hline \Psi \\ \hline \end{array} \begin{array}{|c|} \hline i_1 \\ \hline i_2 \end{array} \begin{array}{|c|} \hline \Psi \\ \hline \end{array}}$$

Gradient descent.

$f(x)$ : function to minimize.

$\partial f(x)$ : gradient of  $f$ .

$\gamma$ : step size.

# Tutorial: Two-site state optimization

```
1 function E( $\psi$ )
2    $\psi H \psi$  = inner( $\psi'$ , H,  $\psi$ )
3    $\psi \psi$  = inner( $\psi$ ,  $\psi$ )
4   return  $\psi H \psi$  /  $\psi \psi$ 
5 end
```

```
1 function minimize(f,  $\partial f$ , x;
2   nsteps,  $\gamma$ )
3   for n in 1:nsteps
4     x = x -  $\gamma$  *  $\partial f(x)$ 
5   end
6   return x
7 end
```

$$E(\psi) = \frac{\begin{array}{|c|} \hline \psi \\ \hline \end{array} \begin{array}{|c|} \hline i_1' \\ \hline \end{array} \begin{array}{|c|} \hline H \\ \hline \end{array} \begin{array}{|c|} \hline i_1 \\ \hline \end{array} \begin{array}{|c|} \hline \psi \\ \hline \end{array}}{\begin{array}{|c|} \hline \psi \\ \hline \end{array} \begin{array}{|c|} \hline i_2' \\ \hline \end{array} \begin{array}{|c|} \hline H \\ \hline \end{array} \begin{array}{|c|} \hline i_2 \\ \hline \end{array} \begin{array}{|c|} \hline \psi \\ \hline \end{array}}$$

$$\min_{\psi} E(\psi) \quad \partial_{\psi} E(\psi)$$

## Tutorial: Two-site state optimization

```
1   $\psi_0 = (Zp1 * Zm2 +$   
2       $Zm1 * Zp2)/\sqrt{2}$   
3  
4   $E(\psi_0) == -1$   
5  
6  using Zygote # autodiff  
7  
8   $\partial E(\psi) = \text{gradient}(E, \psi)[1]$   
9   $\text{norm}(\partial E(\psi_0)) == 2$ 
```

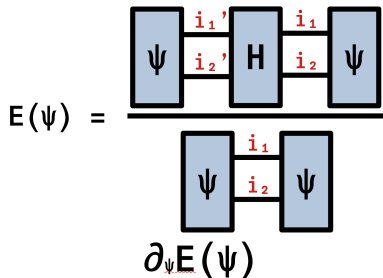
$$E(\psi) = \frac{\begin{array}{|c|} \hline \psi \\ \hline \end{array} \begin{array}{|c|} \hline i_1' \\ \hline \end{array} \begin{array}{|c|} \hline i_2' \\ \hline \end{array} \begin{array}{|c|} \hline H \\ \hline \end{array} \begin{array}{|c|} \hline i_1 \\ \hline \end{array} \begin{array}{|c|} \hline i_2 \\ \hline \end{array} \begin{array}{|c|} \hline \psi \\ \hline \end{array}}{\begin{array}{|c|} \hline \psi \\ \hline \end{array} \begin{array}{|c|} \hline i_1 \\ \hline \end{array} \begin{array}{|c|} \hline i_2 \\ \hline \end{array} \begin{array}{|c|} \hline \psi \\ \hline \end{array}}$$

$\partial_{\psi} E(\psi)$

## Tutorial: Two-site state optimization

```
1   $\psi_0 = (\text{Zp1} * \text{Zm2} +$   
2       $\text{Zm1} * \text{Zp2})/\sqrt{2}$   
3  
4   $E(\psi_0) == -1$   
5  
6  using Zygote # autodiff  
7  
8   $\partial E(\psi) = \text{gradient}(E, \psi)[1]$   
9   $\text{norm}(\partial E(\psi_0)) == 2$ 
```

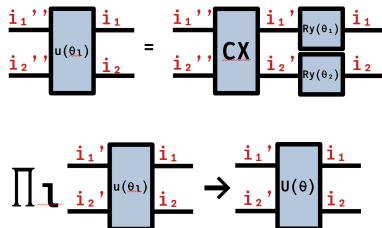
```
1   $\psi = \text{minimize}(E, \partial E, \psi_0;$   
2       $\text{nsteps}=10, \gamma=0.1)$   
3  
4   $E(\psi_0) == -1$   
5   $E(\psi) == -1.4142131 \approx -\sqrt{2}$   
6
```



$$\min_{\psi} E(\psi) = \min_{\psi} \langle \psi | H | \psi \rangle / \langle \psi | \psi \rangle$$

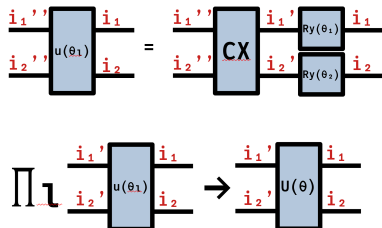
## Tutorial: Two-site circuit optimization

```
1 # Circuit as a vector of
  gates:
2 U( $\theta$ , i1, i2) = [
3   op("Ry", i1;  $\theta=\theta[1]$ ),
4   op("Ry", i2;  $\theta=\theta[2]$ ),
5   op("CX", i1, i2),
6   op("Ry", i1;  $\theta=\theta[3]$ ),
7   op("Ry", i2;  $\theta=\theta[4]$ ),
8 ]
9
10
11
```



# Tutorial: Two-site circuit optimization

```
1 # PastaQ notation:
2 u(θ) = [
3     ("Ry", 1, (; θ=θ[1])),
4     ("Ry", 2, (; θ=θ[2])),
5     ("CNOT", 1, 2),
6     ("Ry", 1, (; θ=θ[3])),
7     ("Ry", 2, (; θ=θ[4])),
8 ]
9
10 U(θ, i1, i2) =
11     buildcircuit(u(θ), [i1, i2
12                     ])
```



## *Tutorial: Two-site circuit optimization*

```
1   $\psi_0$  = Zp1 * Zp2
2
3
4  function E( $\theta$ )
5       $\psi_\theta$  = apply(U( $\theta$ , i1, i2),  $\psi_0$ 
6                  )
7      return inner( $\psi_\theta$ ', H,  $\psi_\theta$ )
8  end
```

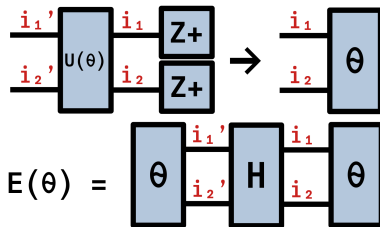
References state:

$$|0\rangle = |Z+Z+\rangle$$

$$\begin{aligned} \min_{\theta} E(\theta) &= \min_{\theta} \langle 0 | U(\theta)^\dagger H U(\theta) | 0 \rangle \\ &= \min_{\theta} \langle \theta | H | \theta \rangle \end{aligned}$$

## Tutorial: Two-site circuit optimization

```
1  $\psi_0$  = Zp1 * Zp2
2
3
4 function E( $\theta$ )
5      $\psi_\theta$  = apply(U( $\theta$ , i1, i2),  $\psi_0$ )
6     return inner( $\psi_\theta'$ , H,  $\psi_\theta$ )
7 end
```

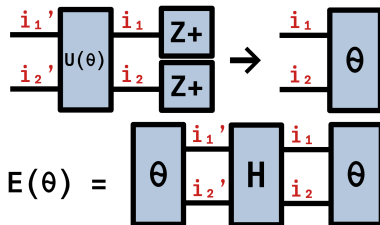




## Tutorial: Two-site circuit optimization

```
1  $\psi_0 = Z_{p1} * Z_{p2}$ 
2
3
4 function E( $\theta$ )
5      $\psi_\theta = \text{apply}(U(\theta, i_1, i_2), \psi_0)$ 
6     return inner( $\psi_\theta^\dagger$ , H,  $\psi_\theta$ )
7 end
```

```
1  $\theta_0 = [0, 0, 0, 0]$ 
2  $\partial E(\theta) = \text{gradient}(E, \theta)[1]$ 
3  $\theta = \text{minimize}(E, \partial E, \theta_0;$ 
4     nsteps=40,  $\gamma=0.5$ )
5
6  $E(\theta_0) == -1$ 
7  $E(\theta) == -1.4142077 \approx -\sqrt{2}$ 
```



$$\min_{\theta} E(\theta) \quad \partial_{\theta} E(\theta)$$

## *Tutorial: Two-site fidelity optimization*

```
1   $\psi_0 = Zp1 * Zp2$ 
2   $\psi = (ZpZp + ZmZm) / \sqrt{2}$ 
3
4
5
6  function F( $\theta$ )
7       $\psi_\theta = \text{apply}(\text{U}(\theta, i1, i2), \psi_0$ 
8           $)$ 
9      return  $-\text{abs}(\text{inner}(\psi, \psi_\theta))$ 
10          $^2$ 
11 end
```

Reference state:

$$|0\rangle = |Z+Z+\rangle$$

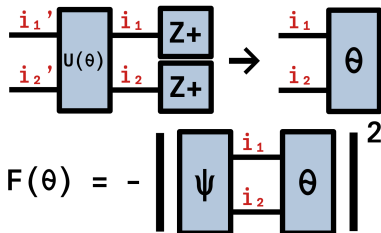
Target state:

$$|\psi\rangle = (|Z+Z+\rangle + |Z-Z-\rangle)/\sqrt{2}$$

$$\min_{\theta} F(\theta) = \min_{\theta} -|\langle\psi|\text{U}(\theta)|0\rangle|^2$$

## Tutorial: Two-site fidelity optimization

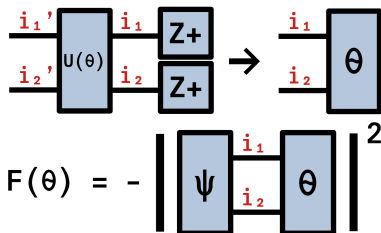
```
1  $\psi_0 = Zp1 * Zp2$ 
2  $\psi = (ZpZp + ZmZm) / \sqrt{2}$ 
3
4
5
6 function F( $\theta$ )
7      $\psi_\theta = \text{apply}(U(\theta, i1, i2), \psi_0)$ 
8     return  $-\text{abs}(\text{inner}(\psi, \psi_\theta))^2$ 
9 end
```



## Tutorial: Two-site fidelity optimization

```
1  $\psi_0 = Zp1 * Zp2$ 
2  $\psi = (ZpZp + ZmZm) / \sqrt{2}$ 
3
4
5
6 function F( $\theta$ )
7      $\psi_\theta = \text{apply}(U(\theta, i1, i2), \psi_0)$ 
8     return -abs(inner( $\psi, \psi_\theta$ ))
9     ^2
10 end
```

```
1  $\theta_0 = [0, 0, 0, 0]$ 
2  $\partial F(\theta) = \text{gradient}(F, \theta)[1]$ 
3  $\theta = \text{minimize}(F, \partial F, \theta_0;$ 
4     nsteps=50,  $\gamma=0.1$ )
5
6  $F(\theta_0) == -0.5$ 
7  $F(\theta) == -0.9938992 \approx -1$ 
```



$$\min_{\theta} F(\theta) \quad \partial_{\theta} F(\theta)$$

## *Tutorial: n-site states with MPS*

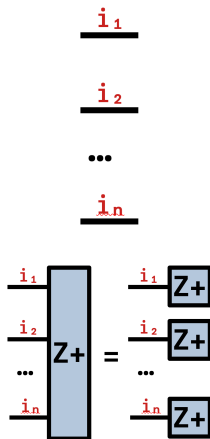
```
1  n = 30
2  i = [Index(2, "S=1/2")
3      for j
4        in 1:n]
5
6  Zp = MPS(i, "Z+")
7
8  maxlinkdim(Zp) == 1 #
   product state
```

$n$ -site state

$|Z + Z + \dots Z+\rangle$

## Tutorial: $n$ -site states with MPS

```
1  n = 30
2  i = [Index(2, "S=1/2")
3       for j
4         in 1:n]
5
6  Zp = MPS(i, "Z+")
7
8  maxlinkdim(Zp) == 1 #
   product state
```



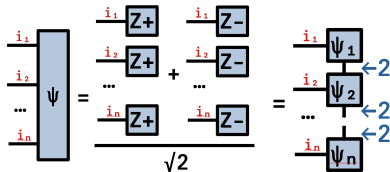
## *Tutorial: n-site states with MPS*

```
1   $\psi = (Zp + Zm)/\sqrt{2}$ 
2
3
4  maxlinkdim( $\psi$ ) == 2 #
    entangled state
```

$$\frac{(|Z + Z + \dots Z + \rangle + |Z - Z - \dots Z - \rangle)}{\sqrt{2}}$$

# Tutorial: $n$ -site states with MPS

```
1  $\psi = (Z_p + Z_m)/\sqrt{2}$ 
2
3
4 maxlinkdim( $\psi$ ) == 2 #
   entangled state
```



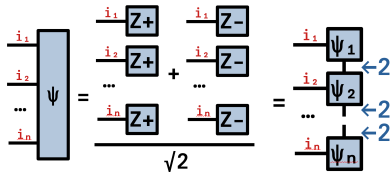


# Tutorial: $n$ -site states with MPS

```

1   $\psi = (Z_p + Z_m)/\sqrt{2}$ 
2
3
4  maxlinkdim( $\psi$ ) == 2 #
    entangled state

```



```

1  inner( $Z_p, Z_p$ ) == 1
2
3
4  inner( $Z_p, \psi$ ) == 1/\sqrt{2}

```

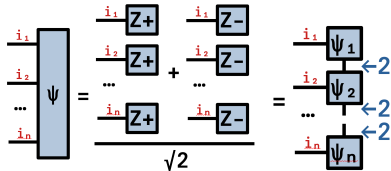
$$\langle Z_+ | Z_+ \rangle = 1$$

$$\langle Z_+ | \psi \rangle = 1/\sqrt{2}$$

# Tutorial: $n$ -site states with MPS

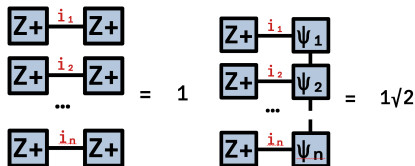
```

1   $\psi = (Z_p + Z_m)/\sqrt{2}$ 
2
3
4  maxlinkdim( $\psi$ ) == 2 #
    entangled state
  
```



```

1  inner(Zp, Zp) == 1
2
3
4  inner(Zp,  $\psi$ ) == 1/\sqrt{2}
  
```



## Tutorial: $n$ -site states with MPS

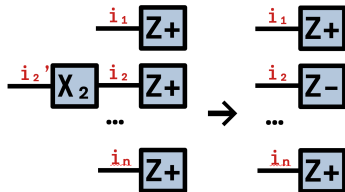
```
1  j = n ÷ 2
2  Xj = op("X", i[j])
3
4  XjZp = apply(Xj, Zp)
5
6
7  state = [k == j ? "Z-" : "Z+"
8           for k
9           in 1:n]
9  XjZp = MPS(i, state)
```

$$X_j |Z + Z + \dots Z + \rangle = \\ |Z + Z + \dots Z - \dots Z + \rangle$$

$$|Z + Z + \dots Z - \dots Z + \rangle$$

## Tutorial: $n$ -site states with MPS

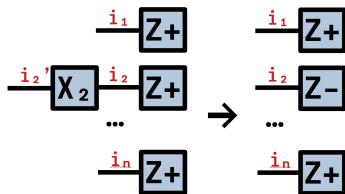
```
1  j = n ÷ 2
2  Xj = op("X", i[j])
3
4  XjZp = apply(Xj, Zp)
5
6
7  state = [k == j ? "Z-" : "Z+"
8           for k
9           in 1:n]
10 XjZp = MPS(i, state)
```



## Tutorial: $n$ -site states with MPS

```
1  j = n ÷ 2
2   $x_j = \text{op}(\text{"X"}, i[j])$ 
3
4   $x_j Z_p = \text{apply}(x_j, Z_p)$ 
5
6
7  state = [k == j ? "Z-" : "Z+"
8           for k
9           in 1:n]
10  $x_j Z_p = \text{MPS}(i, \text{state})$ 
```

```
1  maxlinkdim( $x_j Z_p$ ) == 1
2  inner( $Z_p, x_j Z_p$ ) == 0
```



## *Tutorial: n-site operators with MPO*

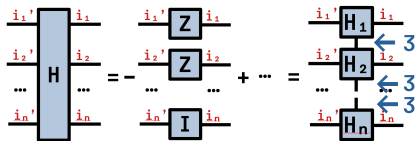
```
1 function ising(n; h)
2   H = OpSum()
3   for j in 1:(n - 1)
4     H -= "Z", j, "Z", j + 1
5   end
6   for j in 1:n
7     H += h, "X", j
8   end
9   return H
10 end
11
12 h = 0.5
13 H = MPO(ising(n; h=h), i)
14 maxlinkdim(H) == 3
```

$n$  sites

$$H = -\sum_j^{n-1} Z_j Z_{j+1} + h \sum_j^n X_j$$

## Tutorial: $n$ -site operators with MPO

```
1 function ising(n; h)
2   H = OpSum()
3   for j in 1:(n - 1)
4     H -= "Z", j, "Z", j + 1
5   end
6   for j in 1:n
7     H += h, "X", j
8   end
9   return H
10 end
11
12 h = 0.5
13 H = MPO(ising(n; h=h), i)
14 maxlinkdim(H) == 3
```



# Tutorial: $n$ -site operators with MPO

```

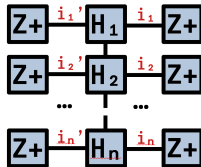
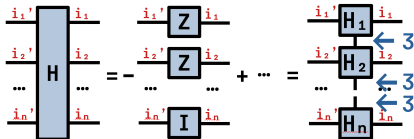
1  function ising(n; h)
2      H = OpSum()
3      for j in 1:(n - 1)
4          H -= "Z", j, "Z", j + 1
5      end
6      for j in 1:n
7          H += h, "X", j
8      end
9      return H
10 end
11
12 h = 0.5
13 H = MPO(ising(n; h=h), i)
14 maxlinkdim(H) == 3

```

```

1  Zp = MPS(i, "Z+")
2  inner(Zp', H, Zp) == -(n-1)
3

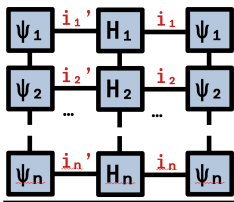
```





# Tutorial: $n$ -site state optimization

```
1 function E( $\psi$ )  
2    $\psi H \psi = \text{inner}(\psi', H, \psi)$   
3    $\psi \psi = \text{inner}(\psi, \psi)$   
4   return  $\psi H \psi / \psi \psi$   
5 end
```

$$E(\psi) = \frac{\langle \psi | H | \psi \rangle}{\langle \psi | \psi \rangle}$$


$\min_{\psi} E(\psi) \quad \partial_{\psi} E(\psi)$

# Tutorial: $n$ -site state optimization

```
1 function E( $\psi$ )
2    $\psi H \psi$  = inner( $\psi'$ , H,  $\psi$ )
3    $\psi \psi$  = inner( $\psi$ ,  $\psi$ )
4   return  $\psi H \psi$  /  $\psi \psi$ 
5 end
```

```
1  $\psi_0$  = MPS(i, "Z+")
2
3  $\psi$  = minimize(E,  $\partial E$ ,  $\psi_0$ ;
4           nsteps=50,  $\gamma$ =0.1,
5           maxdim=10, cutoff=1e-
6           5)
7
8  $E_{dmrg}$ ,  $\psi_{dmrg}$  = dmrg(H,  $\psi_0$ ;
9           nsweeps=10,
10          maxdim=10, cutoff=1e-
11          5)
```

$$E(\psi) = \frac{\langle \psi | \psi \rangle}{\langle \psi | \psi \rangle}$$

$\min_{\psi} E(\psi) \quad \partial_{\psi} E(\psi)$

# Tutorial: $n$ -site state optimization

```

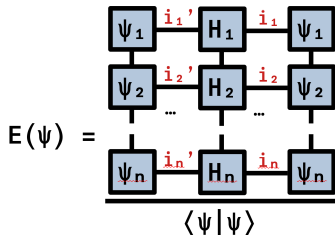
1 function E( $\psi$ )
2    $\psi H \psi = \text{inner}(\psi', H, \psi)$ 
3    $\psi \psi = \text{inner}(\psi, \psi)$ 
4   return  $\psi H \psi / \psi \psi$ 
5 end

```

```

1  $\psi_0 = \text{MPS}(i, \text{"Z+"})$ 
2
3  $\psi = \text{minimize}(E, \partial E, \psi_0;$ 
4    $\text{nsteps}=50, \gamma=0.1,$ 
5    $\text{maxdim}=10, \text{cutoff}=1e-$ 
6    $5)$ 
7  $E_{\text{dmrg}}, \psi_{\text{dmrg}} = \text{dmrg}(H, \psi_0;$ 
8    $\text{nsweeps}=10,$ 
9    $\text{maxdim}=10, \text{cutoff}=1e-$ 
10   $5)$ 

```



$$\min_{\psi} E(\psi) \quad \partial_{\psi} E(\psi)$$

```

1 maxlinkdim( $\psi_0$ ) == 1
2 maxlinkdim( $\psi$ ) == 3
3 maxlinkdim( $\psi_{\text{dmrg}}$ ) == 3
4  $E(\psi_0) == -29$ 
5  $E(\psi) == -31.0317917$ 
6  $E(\psi_{\text{dmrg}}) == -31.0356110$ 

```

## *Tutorial: n-site circuit optimization*

```
1 Ry_layer( $\theta$ , i) = [op("Ry", i[j];  $\theta=\theta[j]$ ) for j in 1:n]
2 CX_layer(i) = [op("CX", i[j], i[j+1]) for j in 1:2:(n-1)]
```

## Tutorial: $n$ -site circuit optimization

```
1 Ry_layer( $\theta$ , i) = [op("Ry", i[j];  $\theta=\theta[j]$ ) for j in 1:n]
2 CX_layer(i) = [op("CX", i[j], i[j+1]) for j in 1:2:(n-1)]
```

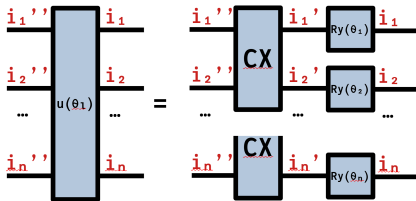
```
1 function U( $\theta$ , i; nlayers)
2     n = length(i)
3     for l in 1:(nlayers - 1)
4          $\theta_l$  =  $\theta[(1:n) .+ l * n]$ 
5          $U_\theta$  = [ $U_\theta$ ; Ry_layer( $\theta_l$ , i)
6             ]
7          $U_\theta$  = [ $U_\theta$ ; CX_layer(i)]
8     end
9     return  $U_\theta$ 
end
```

$$U(\theta) = \text{Ry}_1(\theta_1) \dots \text{Ry}_n(\theta_n) \\ * \text{CX}_{1,2} \dots \text{CX}_{n-1,n} \\ * \text{Ry}_1(\theta_{n+1}) \dots \text{Ry}_n(\theta_{2n}) \\ *$$

## Tutorial: $n$ -site circuit optimization

```
1 Ry_layer( $\theta$ , i) = [op("Ry", i[j];  $\theta=\theta[j]$ ) for j in 1:n]
2 CX_layer(i) = [op("CX", i[j], i[j+1]) for j in 1:2:(n-1)]
```

```
1 function U( $\theta$ , i; nlayers)
2     n = length(i)
3     for l in 1:(nlayers - 1)
4          $\theta_l$  =  $\theta[(1:n) .+ l * n]$ 
5          $U_\theta$  = [ $U_\theta$ ; Ry_layer( $\theta_l$ , i)
6             ]
7          $U_\theta$  = [ $U_\theta$ ; CX_layer(i)]
8     end
9     return  $U_\theta$ 
end
```



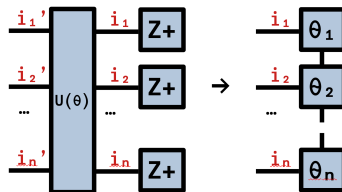
$$\prod_1 U(\theta_1) \rightarrow U(\theta)$$

# Tutorial: $n$ -site states with MPS

```

1   $\psi_0 = \text{MPS}(i, \text{"Z+"})$ 
2  nlayers = 6
3  function  $E(\theta)$ 
4       $\psi_\theta = \text{apply}(U(\theta, i; \text{nlayers}),$ 
5           $\psi_0)$ 
6      return inner( $\psi_\theta$ ,  $H$ ,  $\psi_\theta$ )
7  end
8   $\theta_0 = \text{zeros}(\text{nlayers} * n)$ 
9   $\theta = \text{minimize}(E, \partial E, \theta_0;$ 
10     nsteps=20,  $\gamma=0.1)$ 

```



$$E(\theta) =$$

$$\min_{\theta} E(\theta) \quad \partial_{\dot{\theta}} E(\theta)$$

# Tutorial: $n$ -site states with MPS

```

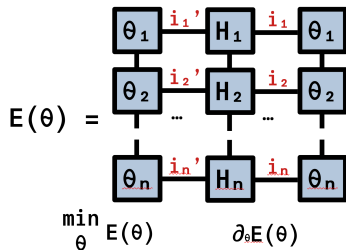
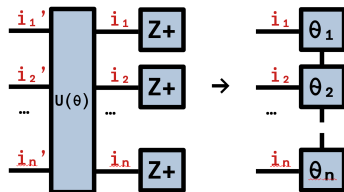
1   $\psi_0$  = MPS(i, "Z+")
2  nlayers = 6
3  function E( $\theta$ )
4       $\psi_\theta$  = apply(U( $\theta$ , i; nlayers),
                     $\psi_0$ )
5      return inner( $\psi_\theta$ ', H,  $\psi_\theta$ )
6  end
7
8   $\theta_0$  = zeros(nlayers * n)
9   $\theta$  = minimize(E,  $\partial E$ ,  $\theta_0$ ;
10               nsteps=20,  $\gamma=0.1$ )

```

```

1  maxlinkdim( $\psi_0$ ) = 1
2  maxlinkdim( $\psi_\theta$ ) = 3
3  E( $\theta_0$ ) == -29
4  E( $\theta$ ) == -31.017062

```



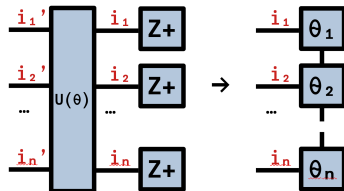


# Tutorial: $n$ -site states with MPS

```

1   $\psi_0 = \text{MPS}(i, "Z+")$ 
2  nlayers = 6
3  function F( $\theta$ )
4       $\psi_\theta = \text{apply}(U(\theta, i; \text{nlayers}),$ 
5                      $\psi_0)$ 
6      return  $-\text{abs}(\text{inner}(\psi', \psi_\theta))^2$ 
7  end
8   $\theta_0 = \text{zeros}(\text{nlayers} * n)$ 
9   $\theta = \text{minimize}(F, \partial F, \theta_0;$ 
10                nsteps=20,  $\gamma=0.1)$ 

```



$$F(\theta) = - \left| \begin{array}{ccc} \psi_1 & i_1 & \theta_1 \\ \psi_2 & i_2 & \theta_2 \\ \vdots & \vdots & \vdots \\ \psi_n & i_n & \theta_n \end{array} \right|^2$$

$$\min_{\theta} F(\theta) \quad \partial_{\theta} F(\theta)$$

# Tutorial: $n$ -site states with MPS

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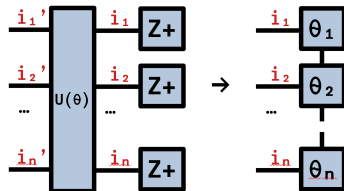
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2  nlayers = 6
3  function F( $\theta$ )
4       $\psi_\theta$  = apply(U( $\theta$ , i; nlayers),
                     $\psi_0$ )
5      return -abs(inner( $\psi'$ ,  $\psi_\theta$ ))^2
6  end
7
8   $\theta_0$  = zeros(nlayers * n)
9   $\theta$  = minimize(F,  $\partial F$ ,  $\theta_0$ ;
10               nsteps=20,  $\gamma=0.1$ )

```

```

1  maxlinkdim( $\psi_0$ ) == 1
2  maxlinkdim( $\psi_\theta$ ) == 2
3  F( $\theta_0$ ) == -0.556066
4  F( $\theta$ ) == -0.995230

```



$$F(\theta) = - \left| \begin{array}{ccc} \psi_1 & i_1 & \theta_1 \\ \psi_2 & i_2 & \theta_2 \\ \vdots & \vdots & \vdots \\ \psi_n & i_n & \theta_n \end{array} \right|^2$$

$$\min_{\theta} F(\theta) \quad \partial_{\theta} F(\theta)$$

## *Other features not mentioned*

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- ▶ More that I am probably forgetting... Ask Giacomo and me for more details.

## *Future directions/in progress*

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- ▶ I'm interested in building general tools and algorithms, and I'm looking for people with problems to solve. Also, we need help, code to contributions are welcome!