Analyzing Quantum Many-Body Systems with ITensor and PastaQ

Matthew Fishman
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https://mtfishman.github.io/

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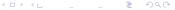
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- ► We are hiring postdocs, full-time scientists, part-time and full-time software developers, interns, etc.





SIMONS FOUNDATION

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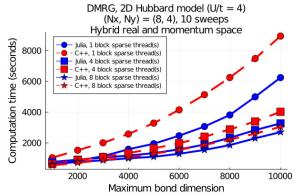


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- Great numerical libraries, code ended up faster.





What is PastaQ?



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Quantum computing extension to ITensor in Julia.

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 - Extensive and extendable gate definitions.
 - ▶ Built-in and easily extendable circuit definitions.
 - Approximate circuit evolution and optimization with MPS/MPO, etc.
- Find out more: github.com/GTorlai/PastaQ.jl $_{\tiny \square}$



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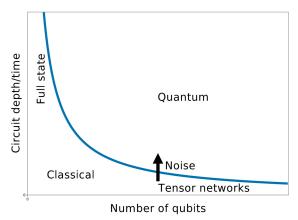
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 - ► ITensor and PastaQ handle this seamlessly.
 - ► This is not the focus of ITensor and PastaQ at the moment, specialized libraries like Yao.jl may be faster.
- ➤ Tensor networks are a common, general language for reasoning about quantum many-body systems (for example, quantum circuits).

▶ In my opinion, tensor networks are the best general purpose tool we have right now for studying quantum many-body systems (while we wait for a general purpose quantum computer).



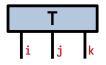
What are tensor networks?



Matrix M_{ij} Order-2 tensor



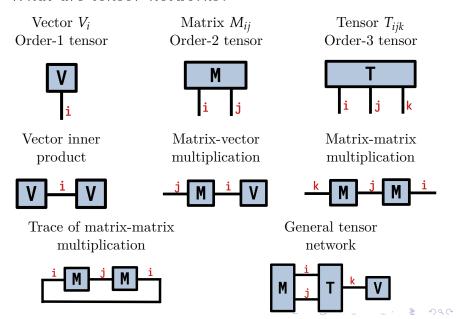
Tensor T_{ijk} Order-3 tensor



What are tensor networks?

Vector V_i Matrix M_{ij} Tensor T_{ijk} Order-1 tensor Order-2 tensor Order-3 tensor Vector inner Matrix-vector Matrix-matrix multiplication multiplication product

What are tensor networks?



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- 2. Launch Julia:
 - 1 \$ julia

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- 2. Launch Julia:

```
1 $ julia
```

3. Type the following commands:

```
julia> using Pkg
julia> Pkg.add("ITensors")
julia> Pkg.add("ITensors")
julia> Pkg.add("PastaQ")
julia> Pkg.add("PastaQ")
```

Now you can use ITensors and PastaQ:

```
julia> using ITensors
    julia > i = Index(2);
 4
    julia > A = ITensor(i);
 6
    julia > using PastaQ
 8
    julia > gates = [("X", 1), ("CX", (1, 3))];
 9
10
    julia >  psi = runcircuit(gates);
11
```

```
1  using ITensors
2
3  i = Index(2)
4
5
```

Load ITensor

2-dimensional labeled Hilbert space (dim=2|id=510)

```
1     using ITensors
2
3     i = Index(2)
4
5
```



```
1     using ITensors
2
3     i = Index(2)
4
5
```

$$\begin{array}{ccc}
1 & \text{Zp} & = & \text{ITensor}(i) \\
2 & & & & & & & & & & & & & & & & & & \\
\end{array}$$

$$2 \text{ Zp}[i=>1] = 1$$

4
$$Zp = ITensor([1, 0], i)$$

i

$$|Z+\rangle = \begin{bmatrix} 1\\0 \end{bmatrix}$$

Construct from a Vector

```
using ITensors
   i = Index(2)
5
   Zp = ITensor(i)
   Zp[i=>1] = 1
   Zp = ITensor([1, 0], i)
```

i

1
$$Zp = ITensor([1, 0], i)$$

2 $Zm = ITensor([0, 1], i)$
3 $Xp = ITensor([1, 1]//2, i)$

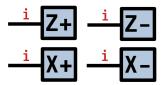
3
$$Xp = ITensor([1, 1]/\sqrt{2}, i)$$

4
$$\operatorname{Xm} = \operatorname{ITensor}([1, 1]/\sqrt{2}, 1)$$

$$|Z+\rangle = \begin{bmatrix} 1\\0 \end{bmatrix}, |Z-\rangle = \begin{bmatrix} 0\\1 \end{bmatrix}$$
$$|X+\rangle = \begin{bmatrix} 1\\1 \end{bmatrix} / \sqrt{2}, |X-\rangle = \begin{bmatrix} 1\\-1 \end{bmatrix} / \sqrt{2}$$

```
Zp = ITensor([1, 0], i)
Zm = ITensor([0, 1], i)
```

- $Xp = ITensor([1, 1]/\sqrt{2}, i)$
- $Xm = ITensor([1, -1]/\sqrt{2}, i)$



```
1 Zp = ITensor([1, 0], i)
    Zm = ITensor([0, 1], i)
   Xp = ITensor([1, 1]/\sqrt{2}, i)
    Xm = ITensor([1, -1]/\sqrt{2}, i)
1 (Zp + Zm)/\sqrt{2}
2 \quad dag(Zp) * Xp
3 \left( \frac{\operatorname{dag}(\mathrm{Zp}) * \mathrm{Xp}}{} \right) 
4 inner(Zp, Xp)
   norm(Xp)
```

```
\approx ITensor(1/\sqrt{2})
\approx 1/\sqrt{2}
\approx 1/\sqrt{2}
```

 $\approx Xp$

 ≈ 1

```
1 Zp = ITensor([1, 0], i)

2 Zm = ITensor([0, 1], i)

3 Xp = ITensor([1, 1]/\sqrt{2}, i)

4 Xm = ITensor([1, -1]/\sqrt{2}, i)

1 (Zp + Zm)/\sqrt{2}

2 dag(Zp) * Xp

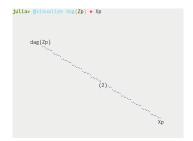
3 (dag(Zp) * Xp)

4 inner(Zp, Xp)

5 norm(Xp)
```

$$\frac{\mathbf{i}}{\mathbf{Z}} = \frac{\mathbf{i}}{\mathbf{X}} + \frac{\mathbf{i}}{\mathbf{Z}} = \frac{\mathbf{i}}{\mathbf{Z}} + \frac{\mathbf{i}}{\mathbf{Z}} = \frac{\mathbf{i}}{\sqrt{2}}$$

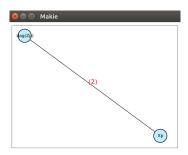
$$\mathbf{Z} + \frac{\mathbf{i}}{\mathbf{X}} + \mathbf{Z} = \frac{1}{\sqrt{2}}$$



- 1 **using**ITensorUnicodePlots
- $\overline{3}$ @visualize dag(Zp) * Xp

- 1 using ITensorGLMakie
- 2
- 3 @visualize dag(Zp) * Xp





Tutorial: One-site states

"S=1/2" defines an operator basis

Additionally: "Qubit", "Qudit", "Electron", ...

Tutorial: One-site states

```
1     i = Index(2, "S=1/2")
2
3
4
5
6
```

```
1 Zp = state("Z+", i)

2 Zm = state("Z-", i)

3 Xp = state("X+", i)

4 Xm = state("X-", i)
```

```
"S=1/2" defines an operator basis
```

```
Additionally: "Qubit", "Qudit", "Electron", . . .
```

```
1 ITensor([1 0], i)
2 ITensor([0 1], i)
3 (Zp + Zm)/\sqrt{2}
4 (Zp - Zm)/\sqrt{2}
```

Tutorial: Custom one-site states

```
import ITensors: state

function state(
::StateName"iX-",
::SiteType"S=1/2"

return [im -im]/√2
end
```

Overload ITensors.jl behavior

Define a state with the name "iX-"

Tutorial: Custom one-site states

```
import ITensors: state

function state(
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return [im -im]/√2
end
```

```
1 iXm = state("iX-", i)
2
3 inner(Zp, iXm)
4 inner(Zm, iXm)
```

Overload ITensors.jl behavior

Define a state with the name "iX-"

 \approx im * Xm

 $\approx \text{im}/\sqrt{2}$ $\approx -\text{im}/\sqrt{2}$

Tutorial: Custom one-site states

```
import ITensors: state

function state(
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return [im -im]/√2
end
```

Overload ITensors.jl behavior

Define a state with the name "iX-"

$$iX+ = (iX+)*i$$

Tutorial: Priming

```
1 i = Index(2) (dim=2|id=837)

2 j = Index(2) (dim=2|id=837)

3 (dim=2|id=899)

4 i == j false
```

Tutorial: Priming

```
1 i = Index(2)
2 j = Index(2)
3
4 i == j
```

Tutorial: Priming

```
1 i = Index(2)
2 j = Index(2)
3
4 i == j
```

```
1 i = Index(2)
2
3 prime(i)
4 i'
5 i ≠ i'
6 noprime(i') == i
```

Tutorial: Priming

```
1 i = Index(2)
2 j = Index(2)
3
4 i == j
```

```
1  i = Index(2)
2
3  prime(i)
4  i'
5  i ≠ i'
6  noprime(i') == i
```

$$\frac{\underline{i}}{\text{prime}\left(\underline{i}\right) = \underline{i'}}$$

$$\frac{\underline{i}}{\underline{j'}} \neq \underline{i'}$$

- $1 \quad Z = ITensor(i', i)$
- Z[i'=>1, i=>1] = 1
- Z[i'=>2, i=>2] = -1

$$Z = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$

- $1 \quad Z = ITensor(i', i)$
- 2 Z[i'=>1, i=>1] = 1
- Z[i'=>2, i=>2] = -1



```
1 Z = ITensor(i', i)
2 Z[i'=>1, i=>1] = 1
3 Z[i'=>2, i=>2] = -1
```



Matrix representation Z

Convert to ITensor

Use predefined definition

```
 \begin{array}{lll} 1 & Z = op(\mbox{"}\mbox{Z"}, i) & Z \\ 2 & X = op(\mbox{"}\mbox{X"}, i) & X \\ 3 & & Zp = state(\mbox{"}\mbox{Z+"}, i) & |Z+\rangle \\ 5 & Zm = state(\mbox{"}\mbox{Z-"}, i) & |Z-\rangle \\ \end{array}
```

```
1 Z = op("Z", i)

2 X = op("X", i)

3 Zp = state("Z+", i)

5 Zm = state("Z-", i)
```

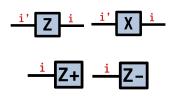
```
1  Z = op("Z", i)

2  X = op("X", i)

3  

4  Zp = state("Z+", i)

5  Zm = state("Z-", i)
```



$$X|Z+\rangle = |Z-\rangle$$
 false true true

$$\begin{array}{ll} 1 & XZp = X*Zp \\ 2 & XZp == Zm \\ 3 & XZp == Zm' \\ 4 & \text{noprime}(XZp) == Zm \end{array}$$

$$i'$$
 X i $Z+ = i' $Z-$$

```
1 XZp = X * Zp

2 dag(Zm) * XZp

4 |Z-\rangle\langle Z+|X|

5 dag(Zm') * XZp

6 dag(Zp') * XZp

7 \langle Z-|X|Z+\rangle \approx 1

8 dag(Zm)' * X * Zp

9 inner(Zm', X, Zp)

\langle Z-|X|Z+\rangle \approx 1

\langle Z-|X|Z+\rangle \approx 1
```

```
1  XZp = X * Zp
2  dag(Zm) * XZp
4  5  dag(Zm') * XZp
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7  8  dag(Zm)' * X * Zp
9  inner(Zm', X, Zp)
```

$$\frac{i'}{X} = \frac{i'}{Z}$$

$$\frac{i'}{X} = \frac{i'}{X}$$

$$\frac{i$$

```
1  XZp = X * Zp
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7  8  dag(Zm)' * X * Zp
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```

$$\frac{i'}{X} \frac{Z+}{Z+} = \frac{i'}{Z-} \frac{Z-}{Z-} \frac{i'}{Z-} \frac{i'}{Z-} \frac{Z-}{Z-} \frac{i'}{Z-} \frac{i$$

```
import ITensors: op
    function op(
     ::OpName"iX",
    ::SiteType"S=1/2"
6
     return [
      0 \text{ im}
    im 0
10
```

Overload ITensors.jl behavior

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import ITensors: op
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$$\frac{i'}{X} = \left(\frac{i'}{X}\right) * i$$

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$$\frac{\mathbf{i}^{\prime} \mathbf{i} \mathbf{X} \mathbf{i}}{\mathbf{i}} = \left(\frac{\mathbf{i}^{\prime} \mathbf{X} \mathbf{i}}{\mathbf{X}} \right) * \mathbf{i}$$

```
1 op("iX", i)
```

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10
```

$$\frac{\mathbf{i'} \mathbf{i} \mathbf{X} \cdot \mathbf{i}}{\mathbf{i}} = \left(\frac{\mathbf{i'} \mathbf{X} \cdot \mathbf{i}}{\mathbf{X}}\right) * \mathbf{i}$$

```
1 op("iX", i)
```

```
1 X * im
```

```
\begin{array}{lll} & \text{i1} = \text{Index}(2, \text{"S=1/2"}) \\ 2 & \text{i2} = \text{Index}(2, \text{"S=1/2"}) \\ 3 & & & & & & & & \\ 4 & \text{i1} == \text{i2} & & & & & \\ 5 & & & & & & & \\ 6 & \text{ZpZm} = \text{ITensor}(\text{i1, i2}) \\ 7 & \text{ZpZm}[\text{i1}=>1, \text{i2}=>2] = 1 & & & & & \\ |\text{Z}+\rangle_1|\text{Z-}\rangle_2 \end{array}
```

$$(\dim = 2|id = 505| \text{``S} = 1/2\text{''})$$

 $(\dim = 2|id = 576| \text{``S} = 1/2\text{''})$
false
 $|Z+\rangle_1|Z-\rangle_2 = |Z+Z-\rangle$

```
1 i1 = Index(2, "S=1/2")

2 i2 = Index(2, "S=1/2")

3

4 i1 == i2

5

6 ZpZm = ITensor(i1, i2)

7 ZpZm[i1=>1, i2=>2] = 1
```

$$\begin{array}{ccc} \underline{\mathbf{i}_1} & \underline{\mathbf{i}_2} & \mathbf{Z} + \\ \underline{\mathbf{i}_2} & \mathbf{Z} - \end{array}$$

```
1 Zp1 = state("Z+", i1)

2 Zp2 = state("Z+", i2)

3

4 Zm1 = state("Z-", i1)

5 Zm2 = state("Z-", i2)

6

7 ZpZm = Zp1 * Zm2

8 ZmZp = Zm1 * Zp2
```

$$\begin{aligned} |Z+\rangle_1 \\ |Z+\rangle_2 \\ |Z-\rangle_1 \\ |Z-\rangle_2 \\ |Z+Z-\rangle &= |Z+\rangle_1 |Z-\rangle_2 \\ |Z-Z+\rangle &= |Z-\rangle_1 |Z+\rangle_2 \end{aligned}$$

```
i1 = Index(2, "S=1/2")
  i2 = Index(2, "S=1/2")
3
  i1 == i2
5
   ZpZm = ITensor(i1, i2)
   ZpZm[i1=>1, i2=>2] = 1
```

$$\begin{array}{ccc} \underline{\mathbf{i}_1} & \underline{\mathbf{i}_2} & \mathbf{Z} + \\ \underline{\mathbf{i}_2} & \mathbf{Z} - \end{array}$$

$$\frac{i_{2}}{Z} = \frac{i_{1}}{Z} = \frac{i_{1}}{i_{2}} = \frac{i_{1}}{Z} = \frac{i_{1}}{i_{2}} = \frac{i_{1}}{Z} = \frac{i_{1}}{i_{2}} = \frac{i_{2}}{Z} = \frac{i_{1}}{Z} = \frac$$

1
$$\psi = \text{ITensor}(i1, i2)$$

2 $\psi[i1=>1, i2=>2] = 1/\sqrt{2}$
3 $\psi[i1=>2, i2=>1] = 1/\sqrt{2}$
4
5 $\psi = (\text{Zp1} * \text{Zm2} + \text{Zm1} * \text{Zp2})/\sqrt{2}$

$$(|Z+\rangle|Z-\rangle + |Z-\rangle|Z+\rangle)/\sqrt{2}$$

From single-site states

```
1 \psi = \text{ITensor}(i1, i2)

2 \psi[i1=>1, i2=>2] = 1/\sqrt{2}

3 \psi[i1=>2, i2=>1] = 1/\sqrt{2}

4 \psi = (\text{Zp1} * \text{Zm2} + \text{Zm1} * \text{Zp2})/\sqrt{2}
```

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \Psi = \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \sqrt{2}$$

```
1 \psi = \text{ITensor}(i1, i2)

2 \psi[i1=>1, i2=>2] = 1/\sqrt{2}

3 \psi[i1=>2, i2=>1] = 1/\sqrt{2}

4 \psi = (\text{Zp1} * \text{Zm2} + \text{Zm1} * \text{Zp2})/\sqrt{2}
```

```
\begin{array}{ll} 1 & \operatorname{inner}(\psi, \, \psi) \\ 2 & \operatorname{inner}(\operatorname{ZpZm}, \, \psi) \\ 3 & \\ 4 & \operatorname{U}, \operatorname{S}, \operatorname{V} = \operatorname{svd}(\operatorname{ZmZp}, \operatorname{i}1) \\ 5 & \operatorname{s} = \operatorname{diag}(\operatorname{S}) \\ 6 & \\ 7 & \operatorname{U}, \operatorname{S}, \operatorname{V} = \operatorname{svd}(\psi, \operatorname{i}1) \\ 8 & \operatorname{s} = \operatorname{diag}(\operatorname{S}) \\ \end{array}
```

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \Psi = \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \sqrt{2}$$

$$\approx 1$$
 $\approx 1/\sqrt{2}$

$$\approx [1, 0]$$

$$\approx [1/\sqrt{2}, 1/\sqrt{2}]$$

```
1 \psi = \text{ITensor}(i1, i2)

2 \psi[i1=>1, i2=>2] = 1/\sqrt{2}

3 \psi[i1=>2, i2=>1] = 1/\sqrt{2}

4 \psi = (\text{Zp1} * \text{Zm2} + \text{Zm1} * \text{Zp2})/\sqrt{2}
```

```
inner(\psi, \psi)
inner(ZpZm, \psi)

U, S, V = Svd(ZmZp, i1)

s = Svd(SmZp, i1)

U, S, V = Svd(FmZp, i1)

U, S, V = Svd(FmZp, i1)

s = Svd(FmZp, i1)
```

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \Psi = \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \sqrt{2}$$

$$svd\left(\frac{i_1}{Z+Z-\frac{i_2}{2}}\right)$$

$$=\frac{i_1}{U}\frac{U}{S}\frac{V}{V}\frac{i_2}{2}$$

$$\frac{U}{S}\frac{V}{V}=\begin{bmatrix}1\\0\end{bmatrix}$$

```
1 \psi = \text{ITensor}(i1, i2)

2 \psi[i1=>1, i2=>2] = 1/\sqrt{2}

3 \psi[i1=>2, i2=>1] = 1/\sqrt{2}

4 \psi = (\text{Zp1} * \text{Zm2} + \text{Zm1} * \text{Zp2})/\sqrt{2}
```

```
1 inner(\psi, \psi)

2 inner(ZpZm, \psi)

3

4 U, S, V = svd(ZmZp, i1)

5 s = diag(S)

6

7 U, S, V = svd(\psi, i1)

8 s = diag(S)
```

$$\frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \Psi = \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{Z} + \sqrt{2}$$

$$svd\left(\frac{i_{1}}{Z+Z-\frac{i_{2}}{2}}\right)$$

$$=\frac{i_{1}}{U}\frac{U}{S}\frac{v}{V}\frac{v}{i_{2}}$$

$$\frac{u}{S}\frac{v}{V}=\begin{bmatrix}1\\0\end{bmatrix}$$

$$svd\left(\frac{1}{1}, \frac{1}{\sqrt{1}}\right)$$

$$=\frac{1}{1}, \frac{1}{\sqrt{1}}$$

$$=\frac{1}{1}, \frac{1}{\sqrt{1}}$$

$$=\frac{1}{1}, \frac{1}{\sqrt{1}}$$

```
1 H = ITensor(i1', i2', i1, i2)
2 H[i1'=>2, i2'=>1,
```

$$[i1=>2, i2=>1]=-1$$

$$[11 = >2, 12 = >1] = -1$$

4 # ...

Make a Hamiltonian: Transverse field Ising (n = 2)

$$H = -\sum_{j=1}^{n-1} Z_j Z_{j+1} + h \sum_{j=1}^{n} X_j$$

```
\begin{array}{ll} 1 & H = ITensor(i1',\,i2',\,i1,\,i2) \\ 2 & H[i1'=>2,\,i2'=>1, \\ 3 & i1=>2,\,i2=>1] = -1 \\ 4 & \# \ ... \end{array}
```

```
1 Id1 = op("Id", i1)
2 Z1 = op("Z", i1)
3 X1 = op("X", i1)
4 # ...
5
6 ZZ = Z1 * Z2
7 XI = X1 * Id2
8 IX = Id1 * X2
9
10 h = 0.5
11 H = -ZZ + h * (XI + IX)
```

Make a Hamiltonian: Transverse field Ising (n = 2)

$$H = -\sum_{j}^{n-1} Z_{j}Z_{j+1} + h\sum_{j}^{n} X_{j}$$

Alternative:

Build from single-site operators. (Less error-prone.)

```
\begin{array}{ll} 1 & H = ITensor(i1',\,i2',\,i1,\,i2) \\ 2 & H[i1'=>2,\,i2'=>1, \\ 3 & i1=>2,\,i2=>1] = -1 \\ 4 & \# \ ... \end{array}
```

```
1 Id1 = op("Id", i1)
2 Z1 = op("Z", i1)
3 X1 = op("X", i1)
4 # ...
5
6 ZZ = Z1 * Z2
7 XI = X1 * Id2
8 IX = Id1 * X2
9
10 h = 0.5
11 H = -ZZ + h * (XI + IX)
```

Make a Hamiltonian: Transverse field Ising (n = 2)

$$H = -\sum_{j}^{n-1} Z_j Z_{j+1} + h \sum_{j}^{n} X_j$$

```
1 ZpZp = Zp1 * Zp2

2 3 4 5 (dag(ZpZp)' * H * ZpZp)[] 6 inner(ZpZp', H, ZpZp) 7 inner(ZpZp, apply(H, ZpZp))
```

Expectation value:
$$\langle H \rangle = \langle Z+Z+|H|Z+Z+ \rangle$$

$$\approx -1$$

```
1 ZpZp = Zp1 * Zp2

2 3 4 5 (dag(ZpZp)' * H * ZpZp)[] 6 inner(ZpZp', H, ZpZp) 7 inner(ZpZp, apply(H, ZpZp))
```

$$\begin{bmatrix}
 Z + \frac{i_1}{i_2} \\
 Z + \frac{i_2}{i_2}
 \end{bmatrix}
 H
 \begin{bmatrix}
 i_1 \\
 i_2
 \end{bmatrix}
 Z + = -1$$

```
1 ZpZp = Zp1 * Zp2

2 3 4 5 (dag(ZpZp)' * H * ZpZp)[] 6 inner(ZpZp', H, ZpZp) 7 inner(ZpZp, apply(H, ZpZp))
```

$$\begin{array}{ll} 1 & D, \, U = \operatorname{eigen}(H) \\ 2 & \operatorname{diag}(D) \end{array}$$

$$\begin{bmatrix}
 Z + & i_1' \\
 Z + & i_2'
 \end{bmatrix}
 H
 \begin{bmatrix}
 i_1 & Z + \\
 i_2 & Z +
 \end{bmatrix}
 = -1$$

$$\approx [-\sqrt{2}, -1, 1, \sqrt{2}]$$

```
1  ZpZp = Zp1 * Zp2
2
3
4
5  (dag(ZpZp)' * H * ZpZp)[]
6  inner(ZpZp', H, ZpZp)
7  inner(ZpZp, apply(H, ZpZp))
```

```
\begin{array}{ll} 1 & D, \, U = eigen(H) \\ 2 & diag(D) \end{array}
```

$$= \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{H} \mathbf{I}_{2} \mathbf{U} \mathbf{U}$$

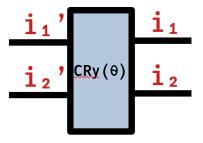
$$= \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \mathbf{U} \mathbf{U} \mathbf{U}$$



```
import ITensors: op
2
    function op(
     ::OpName"CRy",
     ::SiteType"S=1/2":
6
     c = \cos(\theta/2)
     s = \sin(\theta/2)
   return
10
11
   1 \ 0 \ 0
12 0 1 0 0
  00c-s
13
14 	 0.0 s c
15
16
    end
```

```
Controlled-Ry (CRy) rotation gate CRy(\theta)
```

```
import ITensors: op
    function op(
     ::OpName"CRy".
     ::SiteType"S=1/2";
     c = \cos(\theta/2)
     s = \sin(\theta/2)
    return
10
11
    1000
12
   0\ 1\ 0\ 0
13
   0~0~\mathrm{c} -s
14 	 0.0 s c
15
16
    end
```



1 CH = op("CRy", i1, i2;
2
$$\theta = \pi/2$$
)

Controlled-Hadamard gate
$$CH = CRy(\theta = \pi/2)$$

1 CH = op("CRy", i1, i2;
2
$$\theta = \pi/2$$
)

Tutorial: Custom two-site operators

1 CH = op("CRy", i1, i2;
2
$$\theta = \pi/2$$
)

$$|\mathrm{Z+Z-}\rangle = |\mathrm{Z+}\rangle_1|\mathrm{Z-}\rangle_2$$

$$CH|Z+Z-\rangle = |Z+X-\rangle$$

true

Tutorial: Custom two-site operators

1 CH = op("CRy", i1, i2;
2
$$\theta = \pi/2$$
)

$$\begin{array}{c|c}
i_1' \\
i_2'
\end{array}
\xrightarrow{\text{CRy}(n/2)}
\begin{array}{c|c}
i_1 \\
i_2
\end{array}
=
\begin{array}{c|c}
i_1' \\
i_2'
\end{array}
\text{CH}
\begin{array}{c|c}
i_1 \\
i_2
\end{array}$$

$$Z + \frac{i_1}{i_2}, CH \frac{i_1}{i_2} Z + = 1$$

```
1 function E(\psi)

2 \psi H \psi = inner(\psi', H, \psi)

3 \psi \psi = inner(\psi, \psi)

4 return \psi H \psi / \psi \psi

5 end
```

Function to minimize: Expectation value of the energy.

$$E(\psi) = \langle \psi | H | \psi \rangle / \langle \psi | \psi \rangle$$

```
1 function E(\psi)

2 \psi H \psi = inner(\psi', H, \psi)

3 \psi \psi = inner(\psi, \psi)

4 return \psi H \psi / \psi \psi

5 end
```



```
1 function E(\psi)

2 \psi H \psi = inner(\psi', H, \psi)

3 \psi \psi = inner(\psi, \psi)

4 return \psi H \psi / \psi \psi

5 end
```

```
1 function minimize(f, \partial f, x;

2 nsteps, \gamma)

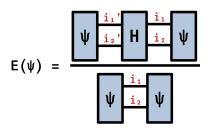
3 for n in 1:nsteps

4 x = x - \gamma * \partial f(x)

5 end

6 return x

7 end
```



Simple gradient descent. Must provide function f(x) to minimize and $\partial f(x)$, the gradient of f at x. γ is the gradient descent step size.

```
1 function E(\psi)

2 \psi H \psi = inner(\psi', H, \psi)

3 \psi \psi = inner(\psi, \psi)

4 return \psi H \psi / \psi \psi

5 end
```

```
1 function minimize(f, \partial f, x;

2 nsteps, \gamma)

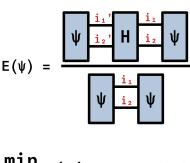
3 for n in 1:nsteps

4 x = x - \gamma * \partial f(x)

5 end

6 return x

7 end
```



$$_{\psi}^{\mathsf{min}}\mathsf{E}(\psi) \qquad \partial_{\psi}\!\mathsf{E}(\psi)$$

```
1 \psi_0 = (\mathrm{Zp1} * \mathrm{Zm2} + 2 \mathrm{Zm1} * \mathrm{Zp2})/\sqrt{2}
3
4 \mathrm{E}(\psi_0)
5
6 \mathrm{using} \ \mathrm{Zygote} : \mathrm{gradient}
7 \partial \mathrm{E}(\psi) = \mathrm{gradient}(\mathrm{E}, \ \psi)[1]
8
9 \mathrm{norm}(\partial \mathrm{E}(\psi_0))
```

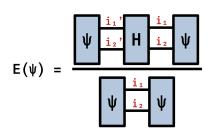
$$|\psi_0\rangle = (|\mathbf{Z}+\mathbf{Z}+\rangle + |\mathbf{Z}-\mathbf{Z}-\rangle)/\sqrt{2}$$

 ≈ -1

Using Zygote for automatic differentation of the energy.

$$\approx 2$$

```
1 \psi_0 = (\mathrm{Zp1} * \mathrm{Zm2} + 2 \mathrm{Zm1} * \mathrm{Zp2})/\sqrt{2}
3 4 \mathrm{E}(\psi_0)
5 6 using Zygote: gradient 7 \partial \mathrm{E}(\psi) = \mathrm{gradient}(\mathrm{E}, \psi)[1]
8 9 \mathrm{norm}(\partial \mathrm{E}(\psi_0))
```



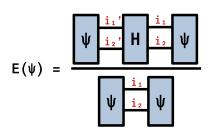
```
1 \psi_0 = (\mathrm{Zp1} * \mathrm{Zm2} + 2 \mathrm{Zm1} * \mathrm{Zp2})/\sqrt{2}
3
4 \mathrm{E}(\psi_0)
5
6 \mathrm{using} Zygote: gradient
7 \partial \mathrm{E}(\psi) = \mathrm{gradient}(\mathrm{E}, \psi)[1]
8
9 \mathrm{norm}(\partial \mathrm{E}(\psi_0))
```

```
1 \psi = \underset{\text{nsteps}=10, \ \gamma=0.1)}{\text{minimize}} (E, \partial E, \psi_0;

2 \text{nsteps}=10, \ \gamma=0.1)

3 4 E(\psi_0), \underset{\text{norm}}{\text{norm}} (\partial E(\psi_0))

5 E(\psi), \underset{\text{norm}}{\text{norm}} (\partial E(\psi))
```



Minimize over ψ : $E(\psi) = \langle \psi | H | \psi \rangle / \langle \psi | \psi \rangle$

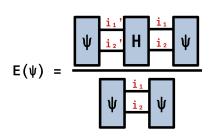
$$\begin{array}{l} (-1, 2) \\ (-1.4142131, 0.0010865277) \\ \approx (-\sqrt{2}, 0) \end{array}$$

```
1 \psi_0 = (\mathrm{Zp1} * \mathrm{Zm2} + 2 \mathrm{Zm1} * \mathrm{Zp2})/\sqrt{2}
3
4 \mathrm{E}(\psi_0)
5
6 \mathrm{using} Zygote: gradient
7 \partial \mathrm{E}(\psi) = \mathrm{gradient}(\mathrm{E}, \psi)[1]
8
9 \mathrm{norm}(\partial \mathrm{E}(\psi_0))
```

```
1 \psi = \underset{\text{minimize}(E, \partial E, \psi_0;}{\text{msteps}=10, \gamma=0.1}

3 E(\psi_0), \underset{\text{norm}(\partial E(\psi_0))}{\text{norm}(\partial E(\psi))}

5 E(\psi), \underset{\text{norm}(\partial E(\psi))}{\text{norm}(\partial E(\psi))}
```



$$_{\psi}^{\min}\mathsf{E}(\psi)\qquad\partial_{\psi}\mathsf{E}(\psi)$$

```
# Circuit as a vector of gates:
     U(\theta, i1, i2) = [
     op("Ry", i1; \theta = \theta[1]),
     op("Ry", i2; \theta = \theta[2]),
    op("CX", i1, i2),
     op("Ry", i1; \theta = \theta[3]),
      op("Ry", i2; \theta = \theta[4]),
 8
10
11
```

```
# Circuit as a vector of gates:
     U(\theta, i1, i2) = [
      op("Ry", i1: \theta = \theta[1]),
     op("Ry", i2; \theta = \theta[2]),
     op("CX", i1, i2),
      op("Ry", i1; \theta = \theta[3]),
      op("Ry", i2; \theta = \theta[4]),
 8
 9
10
11
```

```
# PastaQ notation:

u(\theta, j1, j2) = [

("Ry", j1, (; \theta=\theta[1])),

("Ry", j2, (; \theta=\theta[2])),

("CNOT", j1, j2),

("Ry", j1, (; \theta=\theta[3])),

("Ry", j2, (; \theta=\theta[4]),

]

U(\theta, i1, i2) =

buildcircuit(u(\theta, 1, 2), [i1, i2])
```

```
# Circuit as a vector of gates:
     U(\theta, i1, i2) = [
      op("Ry", i1; \theta = \theta[1]),
       op("Ry", i2; \theta = \theta[2]),
     op("CX", i1, i2),
       op("Ry", i1; \theta = \theta[3]),
      op("Ry", i2; \theta = \theta[4]),
 8
 9
10
11
```

$$\frac{\mathbf{i}_{1}, \mathbf{i}_{2}}{\mathbf{i}_{2}, \mathbf{i}_{2}} = \frac{\mathbf{i}_{1}, \mathbf{i}_{2}}{\mathbf{i}_{2}, \mathbf{i}_{2}} = \frac{\mathbf{i}_{1}, \mathbf{i}_{2}}{\mathbf{i}_{2}, \mathbf{i}_{2}} \times \mathbf{CX} \times \mathbf{i}_{1}, \mathbf{k}_{y(\theta_{1})} \times \mathbf{i}_{2}$$

$$\frac{\mathbf{i}_{1}, \mathbf{k}_{y(\theta_{1})}}{\mathbf{i}_{2}} \times \mathbf{i}_{2}, \mathbf{k}_{y(\theta_{2})} \times \mathbf{i}_{2}$$

$$\frac{\mathbf{i}_{1}, \mathbf{k}_{y(\theta_{1})}}{\mathbf{i}_{2}} \times \mathbf{i}_{2}, \mathbf{k}_{y(\theta_{2})} \times \mathbf{i}_{2}$$

```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 3 4 function \mathrm{E}(\theta)

5 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta), \psi_0)

6 return \mathrm{inner}(\psi_\theta, \mathrm{H}, \psi_\theta)

7 end
```

References state:

$$|0\rangle = |Z+Z+\rangle$$

Find θ that minimizes:

$$E(\theta) = \langle 0 | U(\theta)^{\dagger} H U(\theta) | 0 \rangle$$
$$= \langle \theta | H | \theta \rangle$$

```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 3 4 function \mathrm{E}(\theta)

5 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta), \psi_0)

6 return \mathrm{inner}(\psi_\theta, \mathrm{H}, \psi_\theta)

7 end
```

$$E(\theta) = \begin{bmatrix} \mathbf{i}_{1} \\ \mathbf{i}_{2} \end{bmatrix} + \begin{bmatrix} \mathbf{i}_{1$$

```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 3 4 function \mathrm{E}(\theta)

5 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta), \psi_0)

6 return \mathrm{inner}(\psi_\theta, \mathrm{H}, \psi_\theta)

7 end
```

```
1 \theta_0 = [0, 0, 0, 0]

2 \theta = \underset{\text{minimize}}{\text{minimize}}(E, \partial E, \theta_0;

3 \text{nsteps}=40, \gamma=0.5)

4 E(\theta_0), \underset{\text{norm}}{\text{norm}}(\partial E(\theta_0))

6 E(\theta), \underset{\text{norm}}{\text{norm}}(\partial E(\theta))
```

$$\frac{\min}{\Theta} \mathsf{E}(\Theta) \qquad \qquad \partial_{\theta} \mathsf{E}(\Theta)$$

```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 3 4 function \mathrm{E}(\theta)

5 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta), \psi_0)

6 return \mathrm{inner}(\psi_\theta, \mathrm{H}, \psi_\theta)

7 end
```

```
E(\theta) = \begin{bmatrix} \mathbf{i}_{1} \\ \mathbf{i}_{2} \end{bmatrix}, \quad \mathbf{H} \begin{bmatrix} \mathbf{i}_{1} \\ \mathbf{i}_{2} \end{bmatrix}
```

```
1 \theta_0 = [0, 0, 0, 0]

2 \theta = \underset{\text{minimize}(E, \partial E, \theta_0; \\ \text{nsteps}=40, \gamma=0.5)}{\text{solution}}

5 E(\theta_0), \underset{\text{norm}(\partial E(\theta_0))}{\text{norm}(\partial E(\theta))}

6 E(\theta), \underset{\text{norm}(\partial E(\theta))}{\text{norm}(\partial E(\theta))}
```

$$(-1, \sqrt{3}/2)$$

 $(-1.4142077, 0.0017584116)$
 $\approx (-\sqrt{2}, 0)$

```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 \psi = (\mathrm{ZpZp} + \mathrm{ZmZm}) / \sqrt{2}

3 4 5 6 function F(\theta)

7 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta, \mathrm{i1, i2}), \psi_0)

8 return -abs(inner(\psi, \psi_\theta))^2

9 end
```

Reference state:

$$|0\rangle = |Z+Z+\rangle$$

Target state:

$$|\psi\rangle = (|\mathrm{Z}+\mathrm{Z}+\rangle + |\mathrm{Z}-\mathrm{Z}-\rangle)/\sqrt{2}$$

Find θ that minimizes:

$$F(\theta) = -|\langle \psi | U(\theta) | 0 \rangle|^2$$

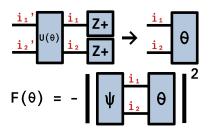
```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 \psi = (\mathrm{ZpZp} + \mathrm{ZmZm}) / \sqrt{2}

3 4 5 6 function F(\theta)

7 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta, \mathrm{i1}, \mathrm{i2}), \psi_0)

8 return -abs(inner(\psi, \psi_\theta))^2 end
```



```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 \psi = (\mathrm{ZpZp} + \mathrm{ZmZm}) / \sqrt{2}

3 4 5 6 function F(\theta)

7 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta, \mathrm{i1}, \mathrm{i2}), \psi_0)

8 \mathrm{return} -abs(inner(\psi, \psi_\theta))^2

9 \mathrm{end}
```

```
F(\theta) = - \begin{bmatrix} \psi & \frac{1}{12} & \theta \end{bmatrix}^{2}
```

```
1 \theta_0 = [0, 0, 0, 0]

2 \theta = \underset{\text{minimize}}{\text{minimize}}(F, \partial F, \theta_0; \\ 3 \quad \text{nsteps} = 50, \gamma = 0.1)

4 

5 F(\theta_0), \underset{\text{norm}}{\text{norm}}(\partial F(\theta_0))

6 F(\theta), \underset{\text{norm}}{\text{norm}}(\partial F(\theta))
```

$$\frac{\min}{\theta} F(\theta) \qquad \partial_{\theta} E(\theta)$$

```
1 \psi_0 = \mathrm{Zp1} * \mathrm{Zp2}

2 \psi = (\mathrm{ZpZp} + \mathrm{ZmZm}) / \sqrt{2}

3 4 5 6 function F(\theta)

7 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta, \mathrm{i1}, \mathrm{i2}), \psi_0)

8 return -abs(inner(\psi, \psi_\theta))^2 9 end
```

```
\frac{\mathbf{i}_{1}'}{\mathbf{i}_{2}'} \mathbf{U}(\theta) \qquad \mathbf{i}_{1} \qquad \mathbf{Z} + \qquad \mathbf{i}_{1} \qquad \mathbf{B}
\mathsf{F}(\theta) = - \qquad \mathbf{\Psi} \qquad \mathbf{i}_{2} \qquad \mathbf{B}
```

```
1 \theta_0 = [0, 0, 0, 0]

2 \theta = \underset{\text{minimize}(F, \partial F, \theta_0; \\ \text{nsteps}=50, \gamma=0.1)}{\text{steps}=50, \gamma=0.1}

5 F(\theta_0), \underset{\text{norm}(\partial F(\theta_0))}{\text{norm}(\partial F(\theta))}

6 F(\theta), \underset{\text{norm}(\partial F(\theta))}{\text{norm}(\partial F(\theta))}
```

$$\approx$$
 (-0.5, 0.5)
 \approx (-0.9938992, 0.07786879)
 \approx (-1, 0)

```
1  n = 30

2  i = [Index(2, "S=1/2")]

3  for j in 1:n]

4  Zp = MPS(i, "Z+")

6  Zm = MPS(i, "Z-")

7  |Z+Z+...Z+\rangle

|Z-Z-...Z-\rangle

8  maxlinkdim(Zp)  1 (product state)
```

1
$$\psi = (\mathrm{Zp} + \mathrm{Zm})/\sqrt{2}$$
2
3
4 $\mathrm{maxlinkdim}(\psi)$

$$\begin{array}{l}(|Z+Z+\ldots Z+\rangle+\\|Z-Z-\ldots Z-\rangle)/\sqrt{2}\end{array}$$

2 (entangled state)

1
$$\psi = (\mathrm{Zp} + \mathrm{Zm})/\sqrt{2}$$
2
3
4 $\mathrm{maxlinkdim}(\psi)$

$$\frac{\frac{1}{1}}{\frac{1}{1}} = \frac{\frac{1}{1}}{\frac{1}{1}} \frac{\mathbb{Z} + \frac{1}{1}}{\frac{1}{1}} \frac{\mathbb{Z} - \frac{1}{1}}{\mathbb{Z} + \frac{1}{1}} = \frac{\frac{1}{1}}{\frac{1}{1}} \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}} + \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}} = \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}} + \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}} + \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}} + \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}} = \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}} + \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}} + \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}} + \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}} = \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}} + \frac{\mathbb{V}_{1}}{\mathbb{V}_{1}}$$

1
$$\psi = (\mathrm{Zp} + \mathrm{Zm})/\sqrt{2}$$
2
3
4 $\mathrm{maxlinkdim}(\psi)$

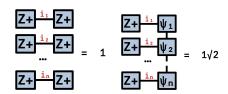
- 1 inner(Zp, Zp)
- $2 \quad inner(Zm, Zp)$
- $3 \quad \text{norm}(\psi)$
- 4 $\operatorname{inner}(\operatorname{Zp}, \psi)$

$$\begin{split} \langle Z + | Z + \rangle &\approx 1 \\ \langle Z - | Z + \rangle &\approx 0 \\ ||\psi\rangle| &\approx 1 \\ \langle Z + |\psi\rangle &\approx 1/\sqrt{2} \end{split}$$

1
$$\psi = (\mathrm{Zp} + \mathrm{Zm})/\sqrt{2}$$
2
3
4 $\mathrm{maxlinkdim}(\psi)$

1 inner(Zp, Zp)
2 inner(Zm, Zp)
3 norm(ψ)
4 inner(Zp, ψ)

$$\begin{array}{c} \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \\ \dots \\ \frac{\mathbf{i}_{n}}{\mathbf{i}_{n}} \end{array} \downarrow = \begin{array}{c} \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{n}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{n}}{\mathbf{i}_{2}} \end{array} = \begin{array}{c} \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \end{array} = \begin{array}{c} \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \end{array} = \begin{array}{c} \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \end{array} = \begin{array}{c} \frac{\mathbf{i}_{1}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}_{2}}{\mathbf{i}_{2}} \\ \frac{\mathbf{i}$$

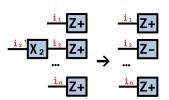


$$j = n/2$$

$$X_{j}$$

$$X_{j}|Z + Z + \dots Z + \rangle = |Z + Z + \dots Z - \dots Z + \rangle$$

$$|Z + Z + \dots Z - \dots Z + \rangle$$



```
1  j = n \div 2

2  X_j = op("X", i[j])

3  4  X_j Zp = apply(X_j, Zp)

5  6

7  state = [k == j ? "Z-" : "Z+" for k in 1:n]

9  X_j Zp = MPS(i, state)
```

```
 \begin{array}{ll} 1 & \operatorname{maxlinkdim}(\mathbf{X}_{j}\mathbf{Z}\mathbf{p}) \\ 2 & \operatorname{inner}(\mathbf{Z}\mathbf{p}, \, \mathbf{X}_{j}\mathbf{Z}\mathbf{p}) \\ 3 & \operatorname{inner}(\mathbf{X}_{j}\mathbf{Z}\mathbf{p}, \, \operatorname{apply}(\mathbf{X}_{j}, \, \mathbf{Z}\mathbf{p})) \end{array}
```

```
\begin{array}{l}
1 \text{ (product state)} \\
\approx 0 \\
\approx 1
\end{array}
```

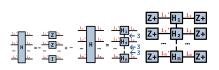
Tutorial: n-site operators with MPO

```
1  function ising(n; h)
2  H = OpSum()
3  for j in 1:(n - 1)
4  H -= "Z", j, "Z", j + 1
5  end
6  for j in 1:n
7  H += h, "X", j
8  end
9  return H
10  end
```

```
n sites H = -\sum_{j}^{n-1} Z_{j} Z_{j+1} + h \sum_{j}^{n} X_{j}
```

Tutorial: n-site operators with MPO

```
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8  end
9  return H
10  end
```

```
1  h = 0.5
2  H = MPO(ising(n; h=h), i)
3  maxlinkdim(H)
4  Zp = MPS(i, "Z+")
5  inner(Zp', H, Zp)
6
```

$$\begin{aligned} \langle Z+Z+...Z+|H|Z+Z+...Z+\rangle \\ \approx -(n-1) = -29 \end{aligned}$$

```
1 \psi_0 = \text{MPS}(i, \text{"Z+"}) |0\rangle = |\text{Z+Z+...Z+}\rangle
2 3 \psi = \underset{\text{minimize}(E, \partial E, \psi_0; \\ \text{nsteps}=50, \gamma=0.1, \\ \text{maxdim}=10, \text{cutoff}=1e-5)} Minimize over \psi: \langle \psi | H | \psi \rangle / \langle \psi | \psi \rangle
6 7 E_{dmrg}, \psi_{dmrg} = \underset{\text{dmrg}(H, \psi_0; \\ \text{nsweeps}=10, \\ \text{maxdim}=10, \text{cutoff}=1e-5)} DMRG solves: H | \psi \rangle \approx | \psi \rangle
```

```
1 \psi_0 = \text{MPS}(i, "Z+")

2 \psi = \text{minimize}(E, \partial E, \psi_0;

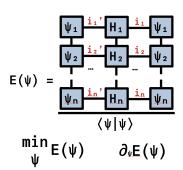
4 \text{nsteps}=50, \gamma=0.1,

5 \text{maxdim}=10, \text{cutoff}=1\text{e-5})

6 E_{dmrg}, \psi_{dmrg} = \text{dmrg}(H, \psi_0;

8 \text{nsweeps}=10,

9 \text{maxdim}=10, \text{cutoff}=1\text{e-5})
```



```
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8 \text{nsweeps}=10,

9 \text{maxdim}=10, \text{cutoff}=1\text{e-5})
```

```
E(\psi) = \frac{\psi_{1} \frac{i_{1}'}{H_{1}} \frac{i_{1}}{\psi_{1}}}{\psi_{1} \frac{i_{2}'}{H_{2}} \frac{i_{2}}{\dots} \frac{\psi_{2}}{\dots}} (\psi|\psi)
\min_{\psi} E(\psi) \quad \partial_{\psi}E(\psi)
```

```
1 \max \lim \dim(\psi_0)

2 \max \lim \dim(\psi)

3 \max \lim \dim(\psi_{dmrg})

4 E(\psi_0), \operatorname{norm}(\partial(\psi_0))

5 E(\psi), \operatorname{norm}(\partial E(\psi))

6 E(\psi_{dmrg}), \operatorname{norm}(\partial E(\psi_{dmrg}))
```

```
= 1 (product state)

= 3 (entangled state)

= 2 (entangled state)

\approx (-29, 5.4772256)

\approx (-31.0317917, 0.06673780)

\approx (-31.0356110, 0.02413237)
```

Tutorial: n-site circuit optimization

```
1 Ry_layer(\theta, i) = [op("Ry", i[j]; \theta=\theta[j]) for j in 1:n]
2 CX_layer(i) = [op("CX", i[j], i[j+1]) for j in 1:2:(n-1)]
```

Tutorial: n-site circuit optimization

```
1 Ry_layer(\theta, i) = [op("Ry", i[j]; \theta = \theta[j]) for j in 1:n]
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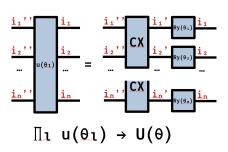
```
\begin{array}{lll} & \textbf{function} \ U(\theta, \ i; \ nlayers) \\ 2 & n = length(i) \\ 3 & U_{\theta} = Ry\_layer(\theta[1:n], \ i) \\ 4 & \textbf{for} \ l \ in \ 1: (nlayers - 1) \\ 5 & \theta_{l} = \theta[(1:n) \ .+ \ l * \ n] \\ 6 & U_{\theta} = [U_{\theta}; \ CX\_layer(i)] \\ 7 & U_{\theta} = [U_{\theta}; \ Ry\_layer(\theta_{l}, \ i)] \\ 8 & \textbf{end} \\ 9 & \textbf{return} \ U_{\theta} \\ 10 & \textbf{end} \end{array}
```

```
U(\theta) = Ry_1(\theta_1) \dots Ry_n(\theta_n)
* CX_{1,2} \dots CX_{n-1,n}
* Ry_1(\theta_{n+1}) \dots Ry_n(\theta_{2n})
* ...
```

Tutorial: n-site circuit optimization

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```

```
\begin{array}{ll} \textbf{function} \ U(\theta, \, i; \, nlayers) \\ \textbf{2} & \textbf{n} = \textbf{length}(i) \\ \textbf{3} & \textbf{U}_{\theta} = \textbf{Ry\_layer}(\theta[1:n], \, i) \\ \textbf{4} & \textbf{for} \ l \ in \ 1: (nlayers - 1) \\ \textbf{5} & \theta_l = \theta[(1:n) \ .+ \ l * \ n] \\ \textbf{6} & \textbf{U}_{\theta} = [\textbf{U}_{\theta}; \ \textbf{CX\_layer}(i)] \\ \textbf{7} & \textbf{U}_{\theta} = [\textbf{U}_{\theta}; \ \textbf{Ry\_layer}(\theta_l, \, i)] \\ \textbf{8} & \textbf{end} \\ \textbf{9} & \textbf{return} \ \textbf{U}_{\theta} \\ \textbf{10} & \textbf{end} \\ \end{array}
```



```
1 \psi_0 = \text{MPS}(i, "Z+")

2 \text{nlayers} = 6

3 \text{function E}(\theta)

4 \psi_\theta = \text{apply}(\text{U}(\theta, i; \text{nlayers}), \psi_0)

5 \text{return inner}(\psi_\theta', \text{H}, \psi_\theta)

6 \text{end}

7 \theta_0 = \text{zeros}(\text{nlayers} * \text{n})

9 \theta = \text{minimize}(\text{E}, \partial \text{E}, \theta_0; \text{nsteps} = 20, <math>\gamma = 0.1)
```

$$|0\rangle = |Z+Z+...Z+\rangle$$

Minimize over θ : $|\theta\rangle = U(\theta)|0\rangle$ $E(\theta) = \langle \theta|H|\theta\rangle$

```
1 \psi_0 = \text{MPS}(i, "Z+")

2 \text{nlayers} = 6

3 \text{function E}(\theta)

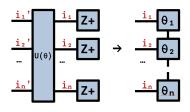
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6 \text{end}

7 \theta_0 = \text{zeros}(\text{nlayers} * n)

9 \theta = \text{minimize}(E, \partial E, \theta_0; \text{nsteps} = 20, \gamma = 0.1)
```



```
1 \psi_0 = \mathrm{MPS}(\mathrm{i}, \text{"Z+"})

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3 \mathrm{function} \ \mathrm{E}(\theta)

4 \psi_\theta = \mathrm{apply}(\mathrm{U}(\theta, \mathrm{i}; \mathrm{nlayers}), \psi_0)

5 \mathrm{return} \ \mathrm{inner}(\psi_\theta', \mathrm{H}, \psi_\theta)

6 \mathrm{end}

7 \theta_0 = \mathrm{zeros}(\mathrm{nlayers} * \mathrm{n})

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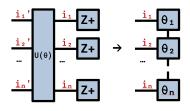
10 \mathrm{nsteps} = 20, \gamma = 0.1
```

```
1 \operatorname{maxlinkdim}(\psi_0)

2 \operatorname{maxlinkdim}(\psi_{\theta})

3 \operatorname{E}(\theta_0), \operatorname{norm}(\partial \operatorname{E}(\theta_0))

4 \operatorname{E}(\theta), \operatorname{norm}(\partial \operatorname{E}(\theta))
```



```
1 (product state)
2 (entangled state)
(-29, 5.773335)
(-31.017062, 0.000759)
```

```
\psi_0 = MPS(i, "Z+")
        nlayers = 6
        function E(\theta)
          \psi_{\theta} = \text{apply}(U(\theta, i; \text{nlayers}), \psi_0)
          return inner(\psi_{\theta}', H, \psi_{\theta})
        end
        \theta_0 = \text{zeros}(\text{nlayers} * \text{n})
        \theta = \text{minimize}(E, \partial E, \theta_0);
                nsteps=20, \gamma=0.1)
10
        \operatorname{maxlinkdim}(\psi_0)
        \operatorname{maxlinkdim}(\psi_{\theta})
        \mathbf{E}(\theta_0), \mathbf{norm}(\partial \mathbf{E}(\theta_0))
        E(\theta), norm(\partial E(\theta))
```

```
E(θ)
```

 $\partial_{\theta} E(\theta)$

▶ More AD, make ITensor fully differentiable (have some work to do, like tensor decompositions and general network contractions, more MPS/MPO functions. You will find bugs!).

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