

*Effects of dynamical evolution on the internal  
kinematical properties of star clusters*

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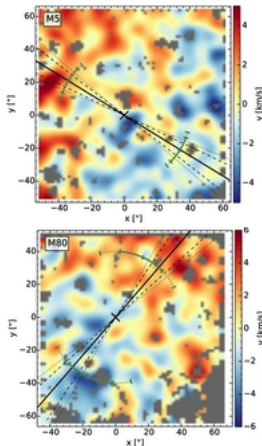
May 24 2016

# *Globular Clusters*

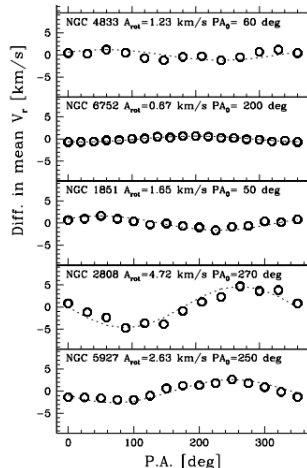


M15 (ESA/Hubble)

# Observations of Internal Kinematics of GCs



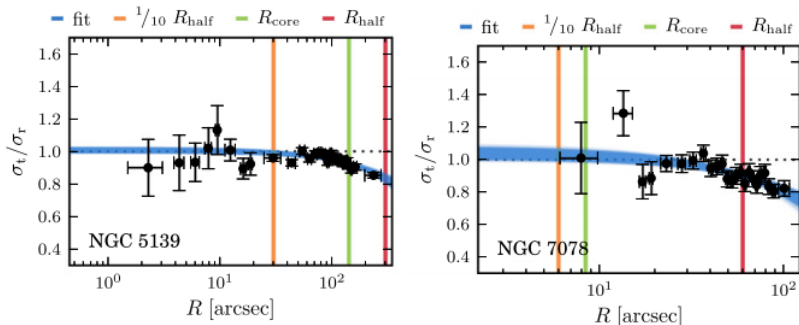
Fabricius et al. 2014, McDonald  
Observatory



Lardo et al. 2015, ESO/VLT

Measurements of Internal Rotation in GCs

# Observations of Internal Kinematics of GCs

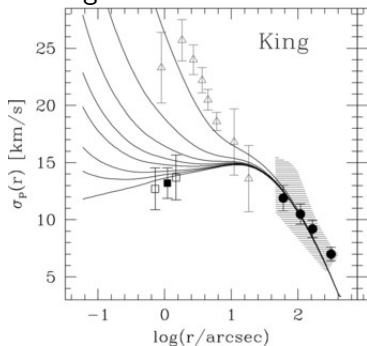


Bellini et al. 2014, Watkins et al. 2015, HSTPROMO

Measurements of Velocity Anisotropy - GCs generally have mildly radially anisotropic velocity distributions near the half-mass radius

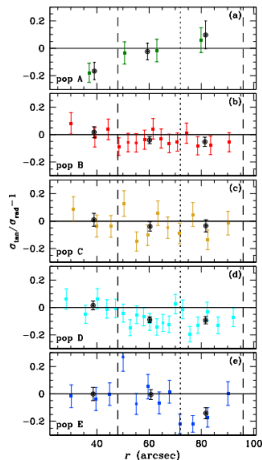
# Observations of Internal Kinematics of GCs

Velocity Dispersion as a potential signature for IMBHs



Lanzoni et al. 2013, ESO/VLT

Kinematical Differences between Multiple Stellar Populations



Bellini et al. 2015, HST (see also Richer et al. 2013)

# *Dynamical Evolution of Kinematical Properties*

Survey of  $N$ -body simulations studying the long-term evolution of the internal kinematics of star clusters

- ▶ Velocity anisotropy (Tiongco et al. 2016)
- ▶ The role of prograde/retrograde stellar orbits on rotation curve (Tiongco et al., submitted)
- ▶ Evolution of rotating clusters in an external tidal field (Tiongco et al., in prep.)
- ▶ Evolution of rotation in multiple population clusters (Tiongco et al., in prep.)

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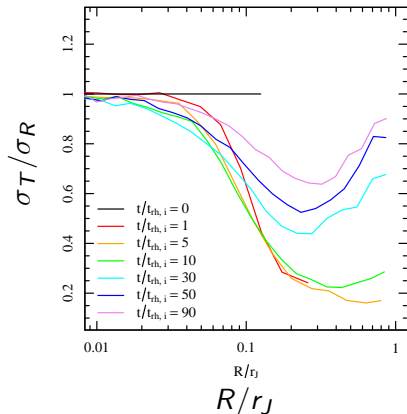
## *Method and Initial Conditions*

- ▶ NBODY6+GPU (Nitadori & Aarseth 2012)
- ▶ Tidally limited
- ▶ King  $W_0 = 7$
- ▶ Rotating cluster models by Varri & Bertin 2012
- ▶ Models evolved through violent relaxation in tidal field
- ▶ Explore evolution for different initial filling factors  $r_h/r_J$  and different virial ratios



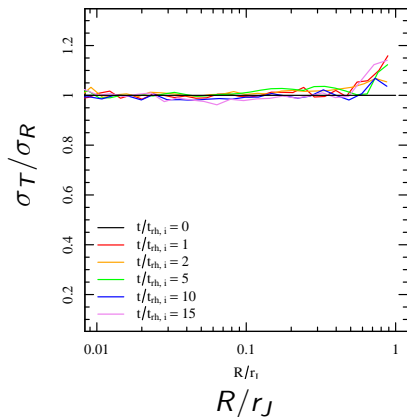
# Evolution of Velocity Anisotropy

See also pioneering works by Giersz & Heggie 1994,1997,2011, Spurzem & Aarseth 1996, Takahashi et al. 1997, Takahashi & Lee 2000, Baumgardt & Makino 2003



- ▶ Initially isotropic, underfilling clusters develop strong radial anisotropy
- ▶ Profile developed: isotropic core, radially anisotropic intermediate region that peaks at  $0.2-0.4r_J$ , outer regions decreasing radial anisotropy
- ▶ System evolves toward an isotropic velocity distribution as mass is lost

# Evolution of Velocity Anisotropy

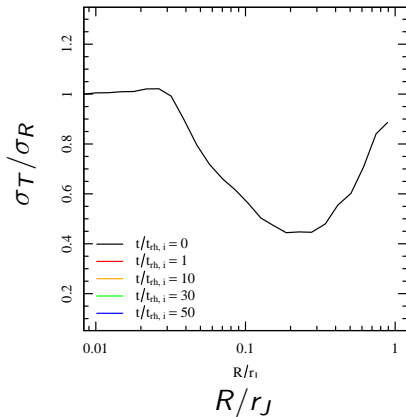


King model ( $r_h/r_J=0.116$ )

Tiongco et al. 2016

- ▶ Degree of radial anisotropy developed decreases as models become more filling
- ▶ Isotropic, tidally filling clusters do not develop significant radial anisotropy

# Evolution of Velocity Anisotropy

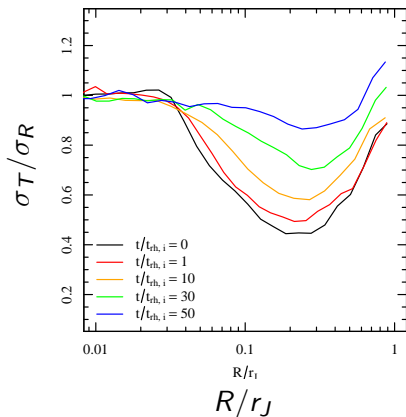


- ▶ Models that first undergo violent relaxation begin their long-term evolution with a profile that has an isotropic core, radially anisotropic intermediate region that peaks at  $0.2-0.4r_J$ , outer regions decreasing radial anisotropy

Violent relaxation model ( $r_h/r_J=0.036$ )

Tiongco et al. 2016, see also Vesperini et al. 2014

# Evolution of Velocity Anisotropy

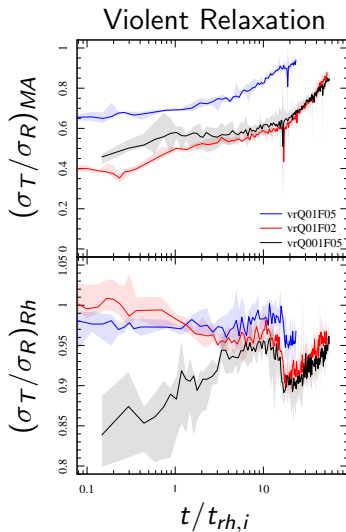
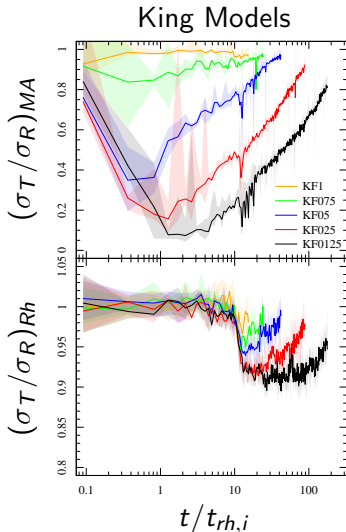


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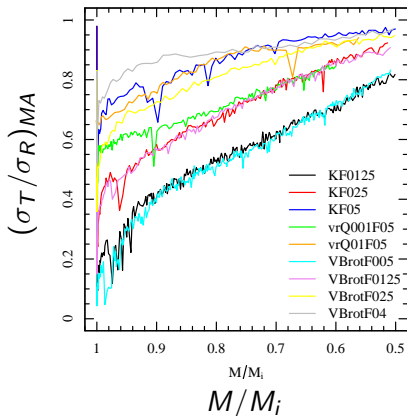
- ▶ Models that first undergo violent relaxation begin their long-term evolution with a profile that has an isotropic core, radially anisotropic intermediate region that peaks at  $0.2-0.4r_J$ , outer regions decreasing radial anisotropy
- ▶ Subsequent evolution is toward an isotropic velocity distribution

# Evolution of Velocity Anisotropy



Value of maximum radial anisotropy and its location over time

# Evolution of Velocity Anisotropy

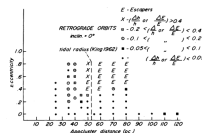
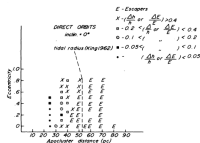


Underfilling models

- ▶ Underfilling models need to lose significant mass in order to erase the strong anisotropy developed
- ▶ Relation between amount of mass lost, strength (or lack of) of radial anisotropy, and dynamical history/initial cluster properties

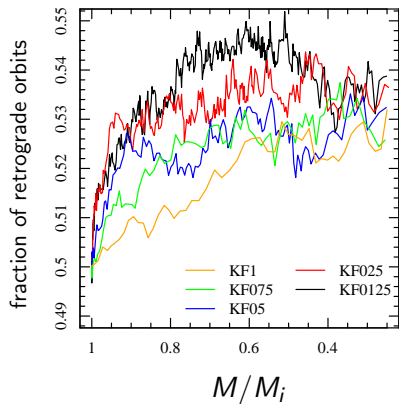
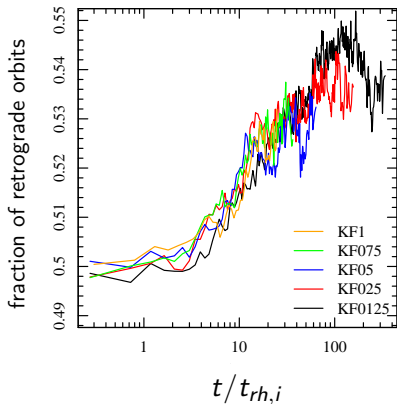
# Role of Prograde and Retrograde Stellar Orbits

- ▶ Prograde orbits are less stable and preferentially lost compared to retrograde orbits (see e.g. Hunter 1967, Hénon 1969,1970, Keenan & Innanen 1975, Fukushige & Heggie 2000, Domingos et al. 2006, Ernst et al. 2007, Zotos 2015)
- ▶ Net effect should be a retrograde rotating cluster



Keenan & Innanen 1975

# *Role of Prograde and Retrograde Stellar Orbits*



Tiongco et al., submitted

**King models:** Fraction of retrograde orbits increases until it reaches a plateau

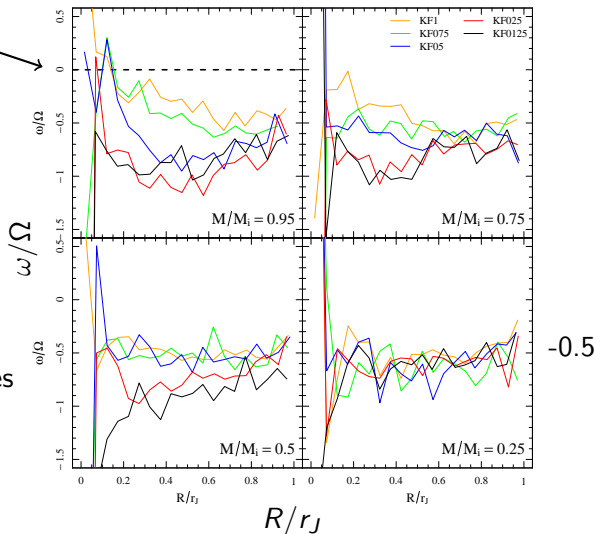


# Development of Internal Rotation

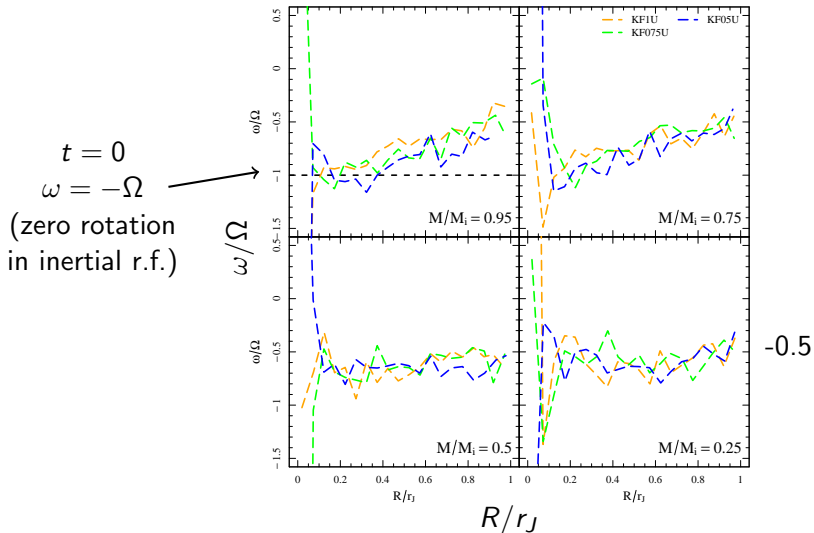
$t = 0$   
 $\omega = 0$   
 (zero rotation  
 in co-rotating r.f.)

$\Omega =$   
 angular velocity  
 of cluster orbit

Filling vs.  
 Underfilling differences

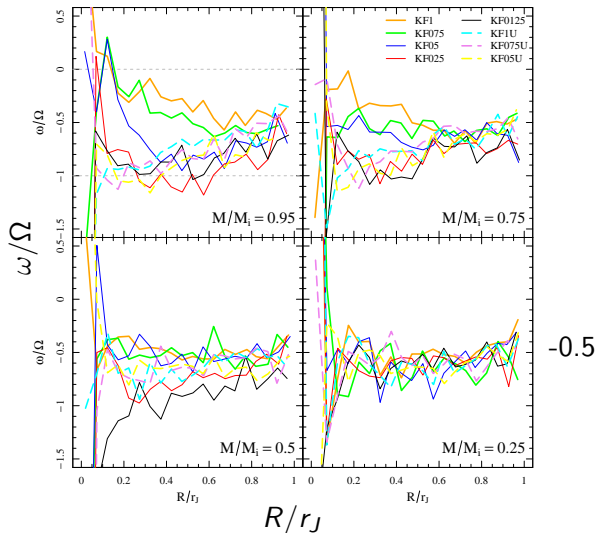


# Development of Internal Rotation



# Development of Internal Rotation

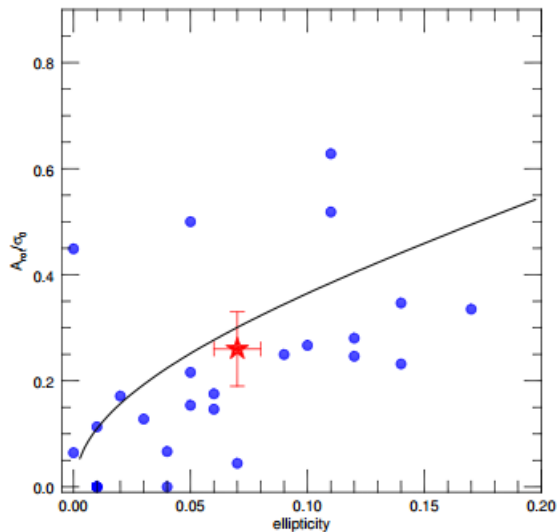
All profiles  
eventually reach an  
approximately solid  
body rotation of  
 $\omega/\Omega \approx -0.5$  in the  
outer regions  
 $R > 0.1r_J$



## *Conclusions*

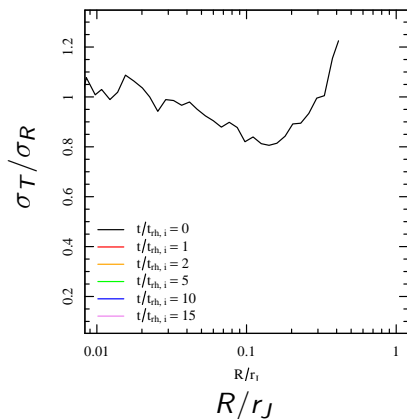
- ▶ Current cluster kinematical properties contain imprints of cluster initial properties and dynamical history
- ▶ Presence of radial velocity anisotropy increasing with radius may indicate initial compactness, though significant mass loss will erase this signature
- ▶ Non-rotating clusters become retrograde rotating in their outer regions due primarily to the preferential loss of prograde orbiting stars

## *Backup Slides*



Kacharov et al. 2014, Bellazzini et al. 2014 ESO/VLT

## Backup Slides

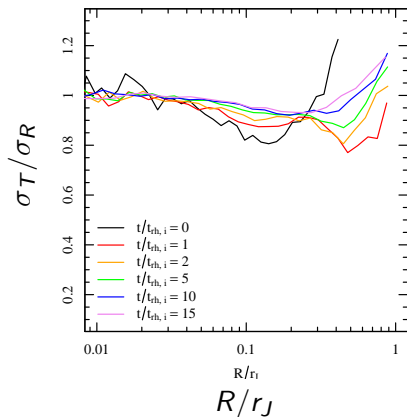


Rotating model ( $r_h/r_J=0.116$ )

Tiongco et al. 2016

- ▶ Rotating models by Varri & Bertin 2012
- ▶ Initial anisotropy profile: isotropic core, radially anisotropic near  $r_h$ , then becomes tangentially anisotropic outwards

## Backup Slides

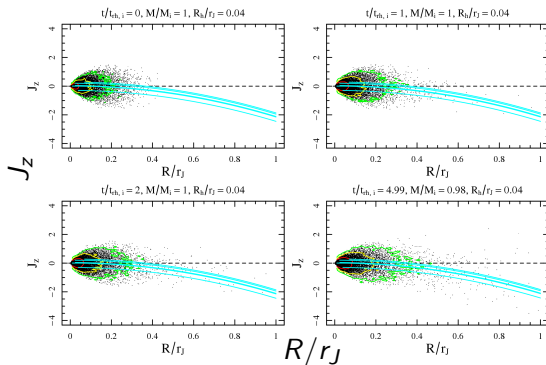


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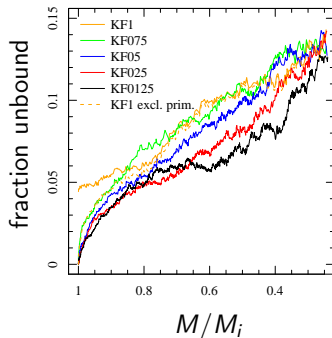
Tiongco et al., submitted

- Expansion of underfilling clusters causes orbits of stars in outermost regions to slow down w.r.t. to the reference frame, thus more likely to be retrograde



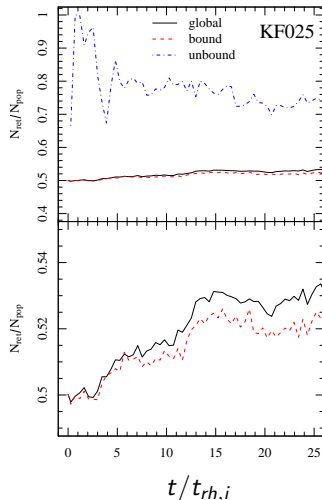
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Tiongco et al., submitted

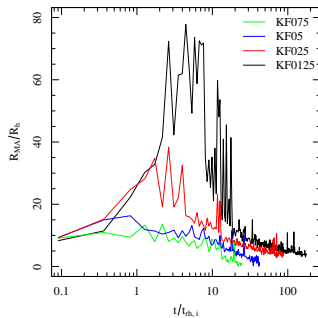
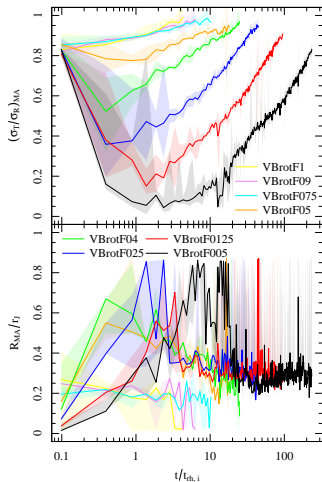


Fraction of potential escapers ( $E > E_{crit}$  within  $r_J$ ) increases until almost 15%  
see also Baumgardt 2001, Küpper et al. 2010

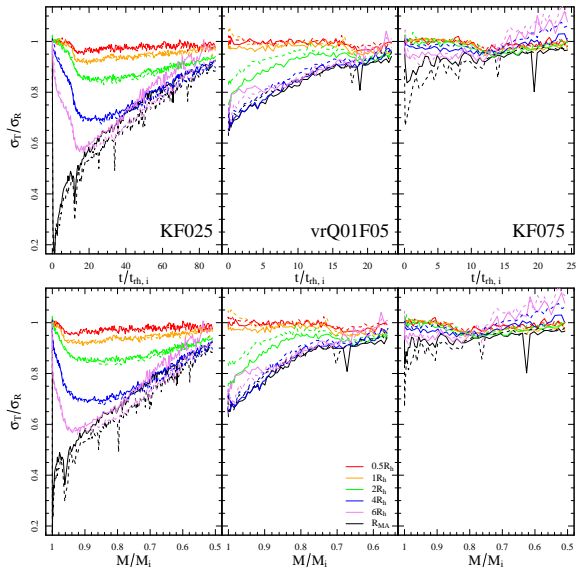
fraction of retrograde orbits



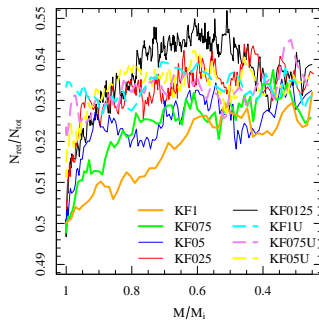
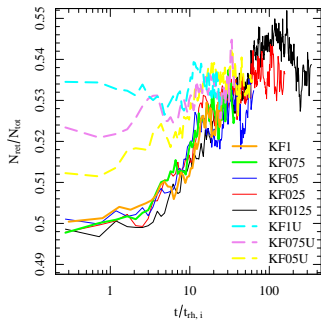
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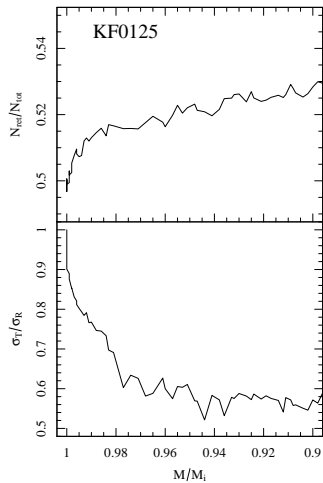
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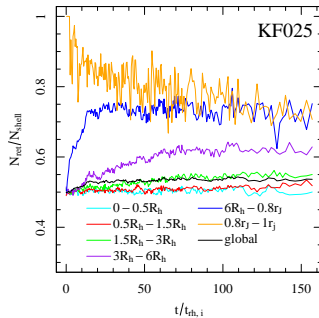
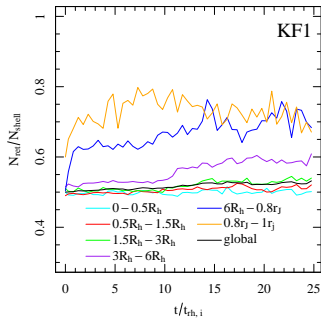
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