

Exercise 1
PDE+Atomistic

Write a program to use SOR to solve the Laplace equation on an NxM rectangular grid with the following boundary conditions:

$$\begin{aligned}u(x,0)&=0 \\ u(x,M)&=0 \\ u(0,y)&=0 \\ u(N,y)&=100\end{aligned}$$

Solve to a tolerance of 10^{-8} . Make a contour plot of your final result.

You can use a weight of 1.75 for the exercise. If you have time, try using different weights. There is a formula for an approximation to the ideal weight for a rectangular region with only Dirichlet boundary conditions:

$$\left(\cos\left(\frac{\pi}{N}\right) + \cos\left(\frac{\pi}{M}\right)\right)^2 \omega^2 - 16\omega + 16 = 0$$