CMSC 170 Machine Problem #1

I. Single Goal Mazes

A. Tiny Maze

1. Straight-Line Distance

Path Cost: 8 Nodes Expanded: 15 Frontier size: 1

Path Coordinates:

B. Small Maze

1. Straight-Line Distance

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
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3%	%	%	%	%	%						P	•	•	%							%
4%					%		%	%	%	%	%	%		%	%		%	%	%	%	%
5%		%	%	%	%		%										%				%
6%									%	%	%		%	%	%				%		%
7%	%	%	%	%	%	%	%	%	%	•	•	•		%	%	%	%	%	%		%
8%		•	•	٠	•	٠	٠	•	•	•	%	%									%
9%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%

2. Manhattan Distance

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Path Cost: 8 Nodes Expanded: 15 Frontier size: 1

Path Cost: 19 Nodes Expanded: 57 Frontier size: 4

Path Coordinates:

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(3,11), (3,12), (3,13), (4,13), (5,13), (5,12), (6,12), (7,12), (7,11), (7,10), (8,10), (8,9), (8,8), (8,7), (8,6), (8,5), (8,4), (8,3), (8,2), (8,1)
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2. Manhattan Distance

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
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2%					%	%	%	%	%	%		%		%	%	%	%	%	%		%
3%	%	%	%	%	%						P	•	• (%							%
4%					%		%	%	%	%	%	%	•	%	%		%	%	%	%	%
5%		%	%	%	%		%					•	•				%				%
6%									%	%	%		%	%	%				%		%
7%	%	%	%	%	%	%	%	%	%		•			%	%	%	%	%	%		%
8%	•	•	•	•	•	•	•	•	•	•	%	%									%
9%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%

Path Cost: 19 Nodes Expanded: 54 Frontier size: 5

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(3,11), (3,12), (3,13), (4,13), (5,13), (5,12), (6,12), (7,12), (7,11), (7,10), (8,10), (8,9), (8,8), (8,7), (8,6), (8,5), (8,4), (8,3), (8,2), (8,1)
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C. Medium Maze

1. Straight-Line Distance

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15%
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16%
```

Path Cost: 68 Nodes Expanded: 228 Frontier size: 4

```
(1,34), (1,33), (1,32), (1,31), (1,30), (1,29), (1,28), (1,27), (1,26), (1,25), (2,25), (3,25), (3,26), (3,27), (4,27), (5,27), (6,27), (6,26), (6,25), (6,24), (5,24), (5,23), (5,22), (5,21), (5,20), (6,20), (7,20), (8,20), (8,21), (8,22), (8,23), (8,24), (8,25), (8,26), (8,27), (9,27), (10,27), (11,27), (12,27), (13,27), (14,27), (15,27), (15,26), (15,25), (15,24), (15,23), (15,22), (15,21), (15,20), (15,19), (15,18), (15,17), (15,16), (15,15), (15,14), (15,13), (15,12), (15,11), (15,10), (16,10), (16,9), (16,8), (16,7), (16,6), (16,5), (16,4), (16,3), (16,2), (16,1)
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16%
```

Path Cost: 68

Nodes Expanded: 221

Frontier size: 6

```
(1,34), (1,33), (1,32), (1,31), (1,30), (1,29), (1,28), (1,27), (1,26), (1,25), (2,25), (3,25), (3,26), (3,27), (4,27), (5,27), (6,27), (6,26), (6,25), (6,24), (5,24), (5,23), (5,22), (5,21), (5,20), (6,20), (7,20), (8,20), (8,21), (8,22), (8,23), (8,24), (8,25), (8,26), (8,27), (9,27), (10,27), (11,27), (12,27), (13,27), (14,27), (15,27), (15,26), (15,25), (15,24), (15,23), (15,22), (15,21), (15,20), (15,19), (15,18), (15,17), (15,16), (15,15), (15,14), (15,13), (15,12), (15,11), (15,10), (16,10), (16,9), (16,8), (16,7), (16,6), (16,5), (16,4), (16,3), (16,2), (16,1)
```

D. Big Maze

1. Straight-Line Distance

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
0 %	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%
1 %		0/	0/	0/	0/	0/	0/	%		%		%	0/	0/		•		•	•	•		0/	0/	%		0/	0/	%	0/	0/	0/	0/		%		%
2 % 3 %		%	%	%	%	%	%	%		%		%	%	%		%		% %	%	%		%	%	%		%	%	%	%	% %	%	%		%		%
3 % 4 %	%	%	%	%		%	%	%	%	%		%	%	%		%		%		%		%	%	%		%	%	%	%	%		% %		%	%	%
5 %	/0	/0	/0	%		%	/0	%	/0	%		/0	/0	%		%		%		%		/0	/0	%		%	/0	/0	/0	%		%		/0	/0	%
6 %		%	%	%		%		%		%	•	%	%	%		%	%	%	%	%	•	%	%	%		%		%	%	%		%	%	%		%
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10%		%		%	%	%	%	%		%		%	%	%		%		%		%	%	%		%		%	%	%		%	%	%		%		%
11%		%		%						%		%		%		%		%						%				%		%		%		%		%
12%		%		%		%	%	%	%	%	%	%		%		%	%	%	%	%	%	%	%	%		%	%	%		%		%	%	%		%
13%	0/	%		%	0/	%		0/		0/	0/	%		0/		%	0/	01	0/	0/		%	0/	0/		0/	0/	%		0/	0/	%	0/	00		%
14%	%	%		%	%	%		%		%	%	%	%	%		%	%	%	%	%		%	%	%		%	%	%		%	%	%	%	%		%
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17%		%		%		%		%		76	76	76		76	76	76		76	76	76		76	76	/6		%		%		%		76		76		%
18%	%	%		%	%	%	%	%	%	%		%		%		%	%	%	%	%		%	%	%		%		%	%	%		%	%	%	%	%
19%	/0	/•		,,	,,	/0	70	%	,,,	%		%		%		70	/0	/0	/0	%		/0	/•	%				/0	/0	%		%	/0	70	70	%
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31%	/0	%		%		%	/0	%	/0	%		%	/0	%	/0	/0		/0	/0	%		%	/0	/0		%		%	/0	/0		%		%	/0	%
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34%		%		%		%		%	%	%		%	%	%	•	%	%	%	%	%	%	%		%	%	%	•	%	%	%	•	%	%	%	er No	%
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(30,3), (31,3), (32,3), (33,3), (33,2), (33,1), (34,1), (35,1)
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3 %		70	70	70	70	/0	/0	%		/0		,,		,	•	%		%	70	70	:	/0	/0	%		/0	70	70	70	%	70	%		70		%
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13%	0/	%		%	0/	%		0/		0/	0/	%	0/	0/		%	0/	0/	0/	0/		%	0/	0/		0/	0/	%		0/	0/	%	0/	0/		%
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15% 16%		0/		%		% %		% %		% %	%	%		%	%	% %		%	0/	0/		0/	0/	% %		% %		%		% %		% %		% %		%
17%		%		%		%		%		/0	/0	/0		/6	/0	/0		/0	%	%		%	%	/0		%		%		%		/0		/0		%
18%	%	%		%	%	%	%	%	%	%		%		%		%	%	%	%	%		%	%	%		/o 9/		%	%	%		%	%	%	%	%
19%	/0	/0		/0	/0	/0	/0	%	/0	%		%		%		/0	/0	/0	/0	%		/0	/0	%		/0		/0	/0	%		%	/0	/0	/0	%
20%	%	%	%	%	•	%		%		%	%	%	%	%	%	%	%	%		%	%	%	%	%	%	%	%	%	%	%	•	%		%	%	%
21%				%		%									-			%		%						%				%		%				%
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23%		%				%							%									%						%								%
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30%	%	%		%		%	%	%	%	%		%	%	%	%	%		%	%	%		%	%	%		%		%	%	%		%		%	%	%
31%		%		%		%		%		%		%		%						%		%				%		%				%		%		%
32%		%		%	%	%		%		%		%		%		%	%	%	%	%	%	%	%	%		%		%		%		%		%		%
33%		0/		%		0/		%	0/	0/		%	0/	0/		0/	0/	•	•	•	•	•		•	•	•		•	•	%		•	0/	•		%
34% 35%		%		% %		% %		%	%	%		%	%	%		%	%	%	%	%	76	%		%	%	%		%	%	% %		% %	%	%		%
	0/	% %	0/	% %	9/	% %	9/	0/	0/	0/	0/	0/	0/	%	9/	0/	0/	% %	9/	0/	0/	0/	0/	0/	0/	%	0/	0/	0/	% %	%	% %	0/	0/	P •/	% %
36%	70	76	76	/6	76	76	76	%	76	76	%	%	/0	76	%	%	/0	/0	/6	/0	/0	/6	76	76	/6	76	/6	70	76	76	76	76	%	/0	/0	/0

```
(35,35), (34,35), (33,35), (33,34), (33,33), (33,32), (33,31), (32,31), (31,31), (31,30), (31,29), (32,29), (33,29), (33,28), (33,27), , 33,26), (33,25), (33,24), (33,23), (33,22), (33,21), (33,20), (33,19), (33,18), (33,17), (33,16), (33,15), (32,15), (31,15), (31,16), (31,17), (30,17), (29,17), (29,16), (29,15), (28,15), (27,15), (26,15), (25,15), (24,15), (23,15), (23,16), (23,17), (23,18), (23,19), (23,20), (23,21), (24,21), (25,21), (25,22), (25,23), (24,23), (23,23), (23,24), (23,25), (23,26),
```

```
(23,27), (22,27), (21,27), (21,28), (21,29), (22,29), (23,29), (23,30),
(23,31), (22,31), (21,31), (20,31), (19,31), (18,31), (17,31), (17,32),
(17,33), (17,34), (17,35), (16,35), (15,35), (14,35), (13,35), (12,35),
(11,35), (10,35), (9,35), (8,35), (7,35), (7,34), (7,33), (8,33), (9,33),
(9,32), (9,31), (9,30), (9,29), (10,29), (11,29), (12,29), (13,29), (14,29),
(15,29), (15,28), (15,27), (16,27), (17,27), (18,27), (19,27), (19,26),
(19,25), (18,25), (17,25), (17,24), (17,23), (17,22), (17,21), (17,20),
(17, 19), (17, 18), (17, 17), (17, 16), (17, 15), (17, 14), (17, 13), (16, 13),
(15,13), (15,14), (15,15), (14,15), (13,15), (12,15), (11,15), (10,15),
(9,15), (9,16), (9,17), (9,18), (9,19), (9,20), (9,21), (8,21), (7,21),
(6,21), (5,21), (4,21), (3,21), (2,21), (1,21), (1,20), (1,19), (1,18),
(1,17), (1,16), (1,15), (2,15), (3,15), (3,14), (3,13), (3,12), (3,11),
(4,11), (5,11), (6,11), (7,11), (7,12), (7,13), (8,13), (9,13), (9,12),
(9,11), (9,10), (9,9), (9,8), (9,7), (9,6), (9,5), (9,4), (9,3), (10,3),
(11,3), (12,3), (13,3), (14,3), (15,3), (16,3), (17,3), (18,3), (19,3),
(19,4), (19,5), (20,5), (21,5), (22,5), (23,5), (23,4), (23,3), (24,3),
(25,3), (26,3), (27,3), (27,4), (27,5), (28,5), (29,5), (29,4), (29,3),
(30,3), (31,3), (32,3), (33,3), (33,2), (33,1), (34,1), (35,1)
```

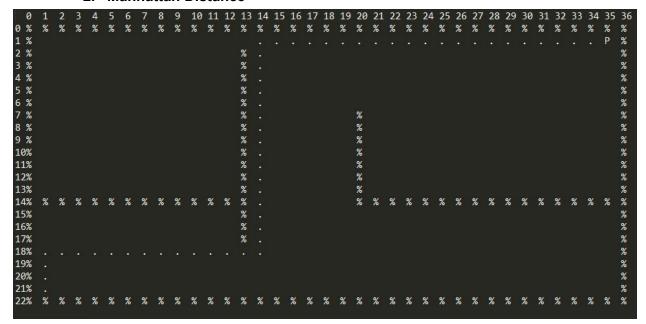
E. Open Maze

1. Straight-Line Distance

Path Cost: 54 Nodes Expanded: 551 Frontier size: 30

```
(1,35), (1,34), (1,33), (1,32), (1,31), (1,30), (1,29), (1,28), (1,27), (1,26), (1,25), (1,24), (1,23), (1,22), (1,21), (1,20), (2,20), (2,19),
```

```
(3,19), (3,18), (4,18), (4,17), (5,17), (5,16), (6,16), (6,15), (7,15), (7,14), (8,14), (9,14), (10,14), (11,14), (12,14), (13,14), (14,14), (15,14), (16,14), (17,14), (18,14), (18,13), (18,12), (18,11), (18,10), (18,9), (18,8), (18,7), (18,6), (18,5), (18,4), (18,3), (19,3), (19,2), (20,2), (20,1), (21,1)
```



Path Cost: 54

Nodes Expanded: 518 Frontier size: 36

```
(1,35), (1,34), (1,33), (1,32), (1,31), (1,30), (1,29), (1,28), (1,27), (1,26), (1,25), (1,24), (1,23), (1,22), (1,21), (1,20), (1,19), (1,18), (1,17), (1,16), (1,15), (1,14), (2,14), (3,14), (4,14), (5,14), (6,14), (7,14), (8,14), (9,14), (10,14), (11,14), (12,14), (13,14), (14,14), (15,14), (16,14), (17,14), (18,14), (18,13), (18,12), (18,11), (18,10), (18,9), (18,8), (18,7), (18,6), (18,5), (18,4), (18,3), (18,2), (18,1), (19,1), (20,1), (21,1)
```

II. Multiple Goal Mazes

A. Tricky Search

1. Straight-Line Distance

```
4
                   5
                                      10 11 12 13 14 15 16 17 18 19
 0
    1
        2
                       6
                                  9
0%
    %
        %
            %
                %
                   %
                       %
                           %
                              %
                                  %
                                          %
                                                     %
                                                            %
                                                                %
                                                                    %
                                      %
                                             %
                                                 %
                                                        %
                                                                       %
                                                                       %
1%
    7
                                                 2
                                                     3
                                                        %
                                                 4
                                                     %
                                                        %
2%
        %
                6
                   %
                       %
                           5
                              %
                                  %
                                          %
                                             %
                                                                %
                                                                       %
    8
            %
                                      1
                                                                       %
4%
                                                                %
                                  %
                                                                       %
3%
    %
        %
            %
                %
                   %
                       %
                           %
                              %
                                      %
                                          %
                                             %
                                                 %
                                                     %
                                                        %
                                                            %
                                                                %
4%
    13 12 11 10 9
                                                                       %
                                      %
                                                     %
                           %
                              %
                                  %
                                          %
                                                 %
5%
                %
                       %
                                             %
                                                            %
                                                                %
                                                                    %
                                                                       %
    %
        %
            %
                   %
```

Path Cost: 68 Nodes Expanded: 110 Frontier size: 24

```
[(3,9), (3,10), (2,10)]
[(2,10), (1,10), (1,11), (1,12), (1,13)]
[(1,13), (1,14)]
[(1,14), (1,13), (2,13)]
[(2,13), (1,13), (1,12), (1,11), (1,10), (1,9), (1,8), (1,7), (2,7)]
[(2,7), (1,7), (1,6), (1,5), (1,4), (2,4)]
[(2,4), (1,4), (1,3), (1,2), (1,1)]
[(1,1), (2,1)]
[(2,1), (3,1), (3,2), (3,3), (3,4), (3,5), (3,6), (3,7), (3,8), (3,9), (3,10),
(3,11), (3,12), (3,13), (3,14), (3,15), (3,16), (2,16), (1,16), (1,17),
(1,18), (2,18), (3,18), (4,18), (5,18), (5,17), (5,16), (5,15), (5,14),
(5,13), (5,12), (5,11), (5,10), (5,9), (5,8), (5,7), (5,6), (5,5)
[(5,5), (5,4)]
[(5,4), (5,3)]
[(5,3), (5,2)]
[(5,2), (5,1)]
```

```
10 11 12 13 14 15 16 17 18 19
 0
            3
                4
                   5
                       6
                                  9
    1
        2
                               8
    %
        %
            %
                %
                   %
                       %
0%
                           %
                              %
                                  %
                                      %
                                          %
                                             %
                                                 %
                                                     %
                                                         %
                                                            %
                                                                %
                                                                    %
                                                                       %
1%
    7
                                                     3
                                                         %
                                                                       %
                                                 2
        %
                   %
                       %
                              %
                                             %
                                                 4
                                                     %
                                                         %
                                                                %
                                                                       %
2%
    8
            %
                6
                           5
                                  %
                                      1
                                          %
                                                                       %
3%
                                                                %
4%
                           %
                                  %
                                      %
                                          %
                                             %
                                                 %
                                                     %
                                                         %
                                                            %
                                                                %
                                                                       %
        %
            %
               %
                   %
                       %
                              %
    %
                                                                       %
5%
    13 12 11 10 9
               %
                           %
                              %
                                  %
                                             %
                                                 %
                                                         %
                                                            %
                                                                %
                                                                       %
6%
        %
                       %
                                      %
                                          %
                                                     %
```

Path Cost: 68 Nodes Expanded: 99 Frontier size: 21

```
[(3,9), (3,10), (2,10)]
[(2,10), (1,10), (1,11), (1,12), (1,13)]
[(1,13), (1,14)]
[(1,14), (1,13), (2,13)]
[(2,13), (1,13), (1,12), (1,11), (1,10), (1,9), (1,8), (1,7), (2,7)]
[(2,7), (1,7), (1,6), (1,5), (1,4), (2,4)]
[(2,4), (1,4), (1,3), (1,2), (1,1)]
[(1,1), (2,1)]
[(2,1), (3,1), (3,2), (3,3), (3,4), (3,5), (3,6), (3,7), (3,8), (3,9), (3,10),
(3,11), (3,12), (3,13), (3,14), (3,15), (3,16), (2,16), (1,16), (1,17),
(1,18), (2,18), (3,18), (4,18), (5,18), (5,17), (5,16), (5,15), (5,14),
(5,13), (5,12), (5,11), (5,10), (5,9), (5,8), (5,7), (5,6), (5,5)
[(5,5), (5,4)]
[(5,4), (5,3)]
[(5,3), (5,2)]
[(5,2), (5,1)]
```

B. Small Search

1. Straight-Line Distance

```
2
              4
                                   10 11 12 13 14 15 16 17 18 19
                            8
       %
              %
                  %
                     %
                         %
                            %
                                %
0%
    %
           %
                                   %
                                       %
                                          %
                                              %
                                                 %
                                                     %
                                                        %
                                                            %
                                                               %
                                                                   %
1%
    13 .
                                                     1
                                                               15 %
                                              3
                                                 2
           %
                                          %
                                              4
                                                 %
                                                     %
2%
    14 %
              12 %
                     %
                         10 %
                                %
                                   5
                                       %
                                                            %
                                                               16 %
3%
       %
           %
                  %
                                   6
                                                            %
                                                               17 %
                     11 9
                            8
                                7
                                %
                                   %
4%
       %
           %
              %
                  %
                     %
                         %
                            %
                                       %
                                          %
                                              %
                                                 %
                                                     %
                                                        %
                                                            %
                                                               %
                                                                  %
    %
```

Path Cost: 48 Nodes Expanded: 69 Frontier size: 33

```
[(1,16), (1,15)]
[(1,15), (1,14)]
[(1,14), (1,13)]
[(1,13), (2,13)]
[(2,13), (1,13), (1,12), (1,11), (1,10), (2,10)]
[(2,10), (3,10)]
[(3,10), (3,9)]
[(3,9), (3,8)]
[(3,8), (3,7)]
[(3,7), (2,7)]
[(2,7), (3,7), (3,6)]
[(3,6), (3,7), (2,7), (1,7), (1,6), (1,5), (1,4), (2,4)]
[(2,4), (1,4), (1,3), (1,2), (1,1)]
[(1,1), (2,1)]
[(2,1), (1,1), (1,2), (1,3), (1,4), (1,5), (1,6), (1,7), (1,8), (1,9), (1,10),
(1,11), (1,12), (1,13), (1,14), (1,15), (1,16), (1,17), (1,18)
[(1,18), (2,18)]
[(2,18), (3,18)]
```

```
3
                   5
                       6
                                      10 11 12 13 14 15 16 17 18 19
0
    1
        2
               4
                              8
                                  9
        %
            %
               %
                   %
                              %
0%
    %
                       %
                           %
                                  %
                                      %
                                         %
                                             %
                                                 %
                                                        %
                                                                   %
                                                     %
                                                            %
                                                                %
                                                                       %
1%
    13 .
                                                        1
                                                            P
                                                                   15 %
                                                 3
                                                     2
                                         %
    14 %
            %
                12 %
                       %
                           10 %
                                  %
                                      5
                                             %
                                                     %
                                                        %
                                                                %
2%
                                                 4
                                                                   16 %
        %
            %
3%
                   %
                       11 9
                              8
                                      6
                                                                %
                                                                   17 %
        %
            %
                   %
                              %
                                      %
                                                                %
                                                                   %
4%
    %
               %
                       %
                          %
                                  %
                                         %
                                             %
                                                 %
                                                     %
                                                        %
                                                            %
                                                                       %
```

Path Cost: 48 Nodes Expanded: 65 Frontier size: 32

```
Path Coordinates:
[(1,16), (1,15)]
[(1,15), (1,14)]
[(1,14), (1,13)]
[(1,13), (2,13)]
[(2,13), (1,13), (1,12), (1,11), (1,10), (2,10)]
[(2,10), (3,10)]
[(3,10), (3,9)]
[(3,9), (3,8)]
[(3,8), (3,7)]
[(3,7), (2,7)]
[(2,7), (3,7), (3,6)]
[(3,6), (3,7), (2,7), (1,7), (1,6), (1,5), (1,4), (2,4)]
[(2,4), (1,4), (1,3), (1,2), (1,1)]
[(1,1), (2,1)]
[(2,1), (1,1), (1,2), (1,3), (1,4), (1,5), (1,6), (1,7), (1,8), (1,9), (1,10),
(1,11), (1,12), (1,13), (1,14), (1,15), (1,16), (1,17), (1,18)
[(1,18), (2,18)]
```

C. Medium Search

[(2,18), (3,18)]

1. Straight-Line Distance

```
30 29 28
                  26 25
                         23 22 21 20 18 17
                                                                           58 59
              27
                                                                    56
                                                                                  60
                                                                                     61
                                                                                         62
                                                                                             63
                                               15
                                                  14
                                                     51
                                                             53
           31
                  50
                      49
                         24
                                        19
                                           16
                                                         52
                                                                54
                                                                    82
                                                                                         80
4%
           45
              44
                  43
                      46
                         47
                                           10
                                              11
                                                         84
                                                             85
                                                                                  76
                                                                                         74
                                                                                             73
                                                  12
                                                                86
                                                                    87
                                                                       88
                                                                           89
                                                                                          103 %
                  42
       38 39 40 41 %
                         98 97
                                                          94 93
                                                                           102 101 100 %
                                                                                          104 105 106 107 108 %
```

Path Cost: 182 Nodes Expanded: 347 Frontier size: 153

```
[(6,15), (6,14)]
[(6,14), (6,13)]
[(6,13), (6,12)]
[(6,12), (6,11)]
[(6,11), (5,11)]
[(5,11), (4,11)]
[(4,11), (4,10)]
[(4,10), (4,9)]
[(4,9), (3,9)]
[(3,9), (4,9), (4,10), (4,11), (4,12)]
[(4,12), (4,13)]
[(4,13), (4,14)]
[(4,14), (3,14)]
[(3,14), (2,14)]
[(2,14), (2,13)]
[(2,13), (2,12)]
[(2,12), (1,12)]
[(1,12), (1,11)]
[(1,11), (2,11)]
[(2,11), (1,11), (1,10)]
[(1,10), (1,9)]
[(1,9), (1,8)]
[(1,8), (1,7)]
[(1,7), (2,7)]
[(2,7), (1,7), (1,6)]
[(1,6), (1,5)]
[(1,5), (1,4)]
[(1,4), (1,3)]
[(1,3), (1,2)]
[(1,2), (1,1)]
[(1,1), (1,2), (1,3), (2,3)]
[(2,3), (3,3)]
[(3,3), (3,2)]
[(3,2), (3,1)]
[(3,1), (4,1)]
[(4,1), (5,1)]
[(5,1), (6,1)]
[(6,1), (6,2)]
[(6,2), (6,3)]
[(6,3), (6,4)]
[(6,4), (6,5)]
[(6,5), (5,5)]
[(5,5), (4,5)]
[(4,5), (4,4)]
[(4,4), (4,3)]
```

```
[(4,3), (4,4), (4,5), (4,6)]
[(4,6), (4,7)]
[(4,7), (3,7)]
[(3,7), (2,7), (2,6)]
[(2,6), (2,5)]
[(2,5), (2,6), (2,7), (1,7), (1,8), (1,9), (1,10), (1,11), (1,12), (2,12),
(2,13), (2,14), (2,15)
[(2,15), (2,16)]
[(2,16), (2,17)]
[(2,17), (2,18)]
[(2,18), (1,18)]
[(1,18), (1,19)]
[(1,19), (1,20)]
[(1,20), (1,21)]
[(1,21), (1,22)]
[(1,22), (1,23)]
[(1,23), (1,24)]
[(1,24), (1,25)]
[(1,25), (1,26)]
[(1,26), (1,27)]
[(1,27), (1,28)]
[(1,28), (1,29)]
[(1,29), (1,28), (1,27), (2,27)]
[(2,27), (3,27)]
[(3,27), (3,28)]
[(3,28), (3,29)]
[(3,29), (4,29)]
[(4,29), (3,29), (3,28), (3,27), (4,27)]
[(4,27), (4,26)]
[(4,26), (4,25)]
[(4,25), (4,24)]
[(4,24), (4,23)]
[(4,23), (3,23)]
[(3,23), (2,23)]
[(2,23), (2,24)]
[(2,24), (2,25)]
[(2,25), (2,24), (2,23), (1,23), (1,22), (1,21), (2,21)]
[(2,21), (1,21), (1,20), (1,19), (2,19)]
[(2,19), (2,18), (2,17), (2,16), (3,16)]
[(3,16), (4,16)]
[(4,16), (4,17)]
[(4,17), (4,18)]
[(4,18), (4,19)]
[(4,19), (4,20)]
[(4,20), (4,21)]
[(4,21), (4,20), (4,19), (5,19)]
[(5,19), (6,19)]
[(6,19), (6,18)]
```

```
[(6,18), (6,17)]
[(6,17), (6,16)]
[(6,16), (6,15), (6,14), (6,13), (6,12), (6,11), (6,10)]
[(6,10), (6,9)]
[(6,9), (6,8)]
[(6,8), (6,7)]
[(6,7), (6,8), (6,9), (6,10), (6,11), (5,11), (4,11), (4,12), (4,13), (4,14),
(3,14), (2,14), (2,15), (2,16), (2,17), (2,18), (2,19), (1,19), (1,20),
(1,21), (1,22), (1,23), (2,23), (3,23), (4,23), (5,23)
[(5,23), (6,23)]
[(6,23), (6,22)]
[(6,22), (6,21)]
[(6,21), (6,22), (6,23), (5,23), (4,23), (4,24), (4,25), (5,25)]
[(5,25), (6,25)]
[(6,25), (6,26)]
[(6,26), (6,27)]
[(6,27), (6,28)]
[(6,28), (6,29)]
```

```
22 21
26 25 24 23
                      20
                          19
                                                                          60
                                                                              61 62 63 64
                                                        55
                                                            56
                                                                   58
                                     15
                                                    53
                                                83
   42 41
                                     11
                                                                           76
                                                                                  74
                                  10
                                         12
                                                    85
                                                        86
                                                           87
                                                84
                                                               88
                                                                                  103 %
                                                                   102 101 100 %
                                                                                  104 105 106 107 108 %
```

Path Cost: 178 Nodes Expanded: 316 Frontier size: 151

```
[(6,15), (6,14)]

[(6,14), (6,13)]

[(6,13), (6,12)]

[(6,12), (6,11)]

[(6,11), (5,11)]

[(5,11), (4,11)]

[(4,11), (4,10)]

[(4,10), (4,9)]

[(4,9), (3,9)]

[(3,9), (4,9), (4,10), (4,11), (4,12)]

[(4,12), (4,13)]
```

```
[(4,13), (4,14)]
[(4,14), (3,14)]
[(3,14), (2,14)]
[(2,14), (2,13)]
[(2,13), (2,12)]
[(2,12), (1,12)]
[(1,12), (1,11)]
[(1,11), (1,10)]
[(1,10), (1,9)]
[(1,9), (1,8)]
[(1,8), (1,7)]
[(1,7), (1,6)]
[(1,6), (1,5)]
[(1,5), (1,4)]
[(1,4), (1,3)]
[(1,3), (1,2)]
[(1,2), (1,1)]
[(1,1), (1,2), (1,3), (2,3)]
[(2,3), (3,3)]
[(3,3), (3,2)]
[(3,2), (3,1)]
[(3,1), (4,1)]
[(4,1), (5,1)]
[(5,1), (6,1)]
[(6,1), (6,2)]
[(6,2), (6,3)]
[(6,3), (6,4)]
[(6,4), (6,5)]
[(6,5), (5,5)]
[(5,5), (4,5)]
[(4,5), (4,4)]
[(4,4), (4,3)]
[(4,3), (4,4), (4,5), (4,6)]
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D. Big Search

1. Straight-Line Distance

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```

Members:

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Contribution of Each Member:

On the first parts of the project, creating the single_goal() function and the single and multiple goal drivers, we coded on Butas's laptop while the other two (Arbuis and Erasmo) helped with ideas, logic, and implementation. Each of us have contributed to refining and fixing errors in the code (in our respective laptops).

On the later parts of the project wherein we focused on fixing, refactoring, and changing some of our implementations, we coded on Arbuis's laptop. Each of us have also contributed to the documentation.