The CAP Theorem

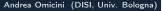
Availability, Consistency, Failure in Distributed Systems Distributed Systems

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Academic Year 2025/2026

- Availability, Consistency, Failure
- CAP at a Glance
- 3 A Brief Detour: Pokémon Go
- Back to CAP: Some Proof
- Building on CAP
- 6 Conclusion



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(Hiding) Failure in Distributed Systems

- being able to keep on providing services in spite of failures is supposed to be one of the main benefit of distributed systems over centralised ones^[Friedman and Birman, 1996]
- intuitive assumption: distributed systems can be designed so that if one component of the system fails – or, it becomes disconnected / partitioned – other components can replace it so as to hide failures from the outside world
 - or at least to reduce the (perceived) impact of failure

Failure & Availability

- when a system can hide (most of) it failures, it is basically (almost)
 always working
 - we say it is highly available
- basic questions in the design of distributed systems: how much failure can a given system sustain before failure is noticed?

Features

What do we expect from a (distributed) systems? [Gilbert and Lynch, 2012]

- we would like them to behave correctly, to give correct replies when queried
 - to be consistent (Correttezza)
- we would like them to work, to make good things happen, to be live
 - to be available (Disponibilitá)
- however, we know systems can actually experience power losses, crashes, network failures, message loss, malicious attacks, Byzantine failures, and so on
 - and be unreliable (Tolleranza alle Partizioni)

Tradeoff

Consistency: Garantisce che il dato restituito sia sempre corretto e aggiornato. Se non si può garantire, il sistema fallisce o blocca l'operazione. Availability: Garantisce che il sistema risponda a una richiesta entro un tempo ragionevole. Il servizio continua a essere erogato (anche se con dati potenzialmente non aggiornati).

il CAP Theorem è la manifestazione più nota di un conflitto universale nell'informatica distribuita: la difficoltà di progettare un sistema che sia allo stesso tempo sempre corretto e sempre reattivo quando il caos (l'inaffidabilità della rete) colpisce.

The idea

"The CAP theorem is one example of a more general tradeoff between safety and liveness in unreliable systems" [Gilbert and Lynch, 2012]



Nei sistemi inaffidabili (cioè tutti i sistemi distribuiti nel mondo reale):

- Massimizzare la Safety (es. garantire una consistenza perfetta) spesso richiede di fermare il progresso del sistema (rendere il servizio non disponibile) quando si verifica un guasto o un'ambiguità, per evitare di prendere decisioni errate.

- Massimizzare la Liveness (es. garantire la massima disponibilità) spesso richiede di sacrificare la Safety (accettare che alcuni dati possano essere obsoleti o

inconsistenti) per permettere al sistema di continuare a funzionare e rispondere.

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Informally I



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Informally II

Secondo il Teorema di CAP, è possibile fornire simultaneamente solo due delle tre seguenti proprietà nelle applicazioni distribuite: Consistenza (C), Disponibilità (A) e Tolleranza alle Partizioni (P).

In short [Shim, 2012]

According to the CAP theorem, it is only possible to simultaneously provide any two of the three following properties in distributed applications: consistency (C), availability (A), and partition tolerance (P).

Consistency: ogni lettura riceve il dato più recente scritto o un errore. Il sistema si comporta come se fosse un singolo nodo, garantendo un unico stato globale. Non permettere mai agli utenti di vedere dati vecchi o contraddittori.

Availability: ogni richiesta a un nodo non guasto riceve una risposta (non un errore o un timeout), garantendo che il servizio sia sempre operativo. Il sistema deve sempre rispondere, anche in caso di problemi.

Partition Tolerance: il sistema deve continuare a funzionare anche se si verifica una partizione di rete, ovvero una rottura della comunicazione tra gruppi di nodi (ad esempio, a causa di un guasto del cavo o di un server che isola una parte del sistema). Poiché le reti reali non sono mai perfette (il fallimento è inevitabile), la Tolleranza alle Partizioni (P) è considerata un requisito obbligatorio per quasi tutti i moderni sistemi distribuiti su larga scala.

Informally III

Less short [Zhao, 2014]

The CAP theorem [...] states that it is impossible to satisfy all three of the following guarantees:

Consistency (C) the replicated data is always consistent with each other

Availability (A) the data is highly available to the users

Partition tolerance (P): the system can continue providing services to its users even when the network partitions

Original Theorem

First formulation by Eric A. Brewer^[Brewer, 2000]

A distributed database potentially features three desirable properties

- Consistency
- Availability
- 3 tolerance towards network Partition

According to the CAP theorem, any shared-data distributed system can have at most two of these three properties

http://apice.unibo.it/xwiki/bin/view/Talk/BrewerPodc2000

An Impossibility Result

- "we repent and renounce"
- ? ... yet, what is actually our sin?
- distributed systems, that's what it is.



Pick Up One... I

... and live with(out) that

- one might forget about tolerance to network partition, so to have consistency and availability
- one might *forget about consistency*, and live with a partition-tolerant and highly-available system
- one might *forget about availability*, and enjoy a system that is both consistent and tolerant to network partition

Pick Up One... II

Note

- the three properties are not exactly of the same sort, both technically and conceptually
 - consistency and availability range over a spectrum of options, whereas partition tolerance can somehow be seen more as an on/off feature
- all of them are *desirable*, yet forfeiting partition tolerance is *not really* an option in real-world systems
- particularly with pervasive systems in the IoT era, where *instability* (of the network) rules^[Grimm et al., 2004]
- → long story short, CAP theorem most often forces us to *choose between* availability and consistency

Example: Location-based Games I

Location-based games

- location-based services [Shekhar et al., 2016] use information about the position of a user / device to provide information, entertainment, security
- location-based games use player's location to evolve and progress the gameplay
 - e.g., BotFighters, GeoZombie^[Prandi et al., 2016], Ingress, Pokémon Go, Harry Potter: Wizards Unite, Minecraft Earth

Example: Location-based Games II

CAP in location-based games: partition tolerance

- since the architecture is built around the notion of millions of players rooming physical space worldwide with their mobile devices (and, playing through them), forfeiting partition tolerance is not an option
 - mobile devices are inherently unstable in their network connectivity
 - players are inherently mobile, and so they can move in and out of network coverage
 - players tend to concentrate in some areas, e.g., during special events
 - scalabilty is a multi-level issue: not just the number of players overall, but also the number of places they can be at, and the number of players at each place
 - e.g., costly disaster at the Chicago 2017 Pokémon Go Fest

Example: Location-based Games III

CAP in location-based games: consistency and availability

- consistency of the game data (goals, situation, achievements, ...) is essential to keep players going (and, into the game)
 - location-based games are usually built around logically-centralised architecture
 - using spatial replication in order to reduce user-perceived latency and improve scalabilty
 - when strong consistency is required, e.g., for in-game transactions, players might be forced to wait for the app servers to confirm the operation
 - by reaching a consistent state overall
- first (and usual) casualty: availability
 - the Spinning Wheel of Death

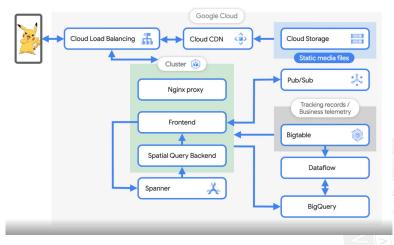


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Catching a Pokémon on Google Cloud I



https://cloud.google.com/blog/topics/developers-practitioners/how-pokémon-go-scales-millions-requests

Catching a Pokémon on Google Cloud II

- when a player opens the Pokémon Go app, all static media are downloaded to his/her personal device
 - which are stored in Cloud Storage
 - Cloud CDN (Content Network Delivery) uses Google's global edge network to serve content closer to users
 - Cloud CDN works with the Cloud Load Balancing (actually, a load balancer) to cache and serve user content
- user requests are sent to NGINX reverse proxy
 - which sends this traffic to the Frontend game service
 - hosted on Google Kubernetes Engine (GKE)
- the Spatial Query Backend handle the location-based features
 - keeps a cache sharded by location
 - the cache and service decides which Pokémon is shown on the map, what gyms and PokéStops are around, which is the time zone, ...

Catching a Pokémon on Google Cloud III

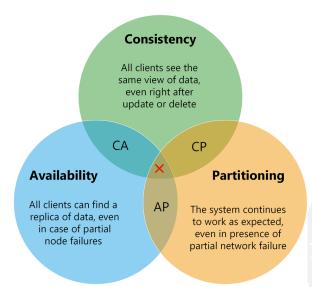
- when a player catches a Pokémon, the Frontend (GKE) sends an event to Google Spanner
 - when the write request is completed, a response is sent back to the device
 - Spanner is strongly consistent
- every player's actions is recorded in the Bigtable NoSQL database service
 - as a Protobuf representation
 - for logging and tracking data
 - also as a message to a Pub/Sub topic for the analysis pipeline
- multiple players in the same geographical region are kept in sync by determinism of the Pokémon Go maps
 - even if multiple players are on different machines, but in the same physical location, all players' inputs would be the same
- all the servers are in sync with settings changes and event timings in order for all players to feel like they are part of a shared world

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One Way to See CAP



From Brewer's Conjecture to CAP Theorem

Going formal

- Brewer's first results required some proof, possibly formal
- for a proof, a more precise formulation of the conjecture is required
- a proof was soon provided [Gilbert and Lynch, 2002]
 - with some limitations
- then, several others followed
- first step for us to sketch a proof: defining the main concepts

Consistency, Availability, Network Partition I

Availability [Gilbert and Lynch, 2002]

- "For a distributed system to be continuously available, every request received by a non-failing node in the system must result in a response"
- if the system is available, we got responses



Consistency, Availability, Network Partition II

Consistency [Gilbert and Lynch, 2002]

- a consistent service is modelled as an atomic data object
- where
 - operations are totally ordered, and
 - each operation occurs in a single instant of time
- ! here, the meaning of *consistent* is unlike ACID properties, since it encompasses both A and C there
- among the many consequences, consistency implies that all read operations over a distributed shared memory occurring after a write operation completes must return the value of either this write operation or a later one
- if the system is consistent, we got correct responses

Consistency, Availability, Network Partition III

Network partition [Gilbert and Lynch, 2002]

- "When a network is partitioned, all messages sent from nodes in one component of the partition to nodes in another component are lost"
- "And, any pattern of message loss can be modelled as a temporary partition separating the communicating nodes at the exact instant the message is lost"

In short, and roughly...

- if node A send a message to node B, the network is *partitioned* if the message does not make it to B
- availability is when B receives the message and responds
- consistency is when B response is correct

Theorem I

Three different sorts of systems

The proof is given for three sorts of network

- asynchronous network with message loss
- asynchronous network without message loss
- partially synchronous network with local clocks

For teaching purposes, we focus here on the asynchronous model, where

- there is no single clock
- nodes act based on local computation and message received

Theorem II

Theorem^[Gilbert and Lynch, 2002]

"It is impossible in the asynchronous network model to implement a read/write data object that guarantees the following properties:

- availability
- atomic consistency

in all fair executions (including those in which messages are lost)"

Proof[Gilbert and Lynch, 2002]

Assumptions

- atomicity, availability, and partition tolerance are all fulfilled
 - proof by contradiction attacks just that
- nodes in the network can be partitioned into two disjoint, non-empty sets G_1, G_2
- atomic object o has initial value v_0
 - o is expected to be consistent through G_1 , G_2
- α_1 executes a single write $v_1 \neq v_0$ of o in G_1
 - α_1 is the only request in that time
 - during α_1 no message are received—from G_1 to G_2 , from G_2 to G_1
- ullet no messages from G_1 are received in G_2
- α_2 executes a single read of o in G_2
 - during α_2 no message are received—from G_1 to G_2 , from G_2 to G_1

Proof[Gilbert and Lynch, 2002]

Q.E.D.

- due to availability, α_1 completes $(v_0 \rightarrow v_1)$, and α_2 does, too
- executing α_1 and α_2 , G_2 just sees α_2 , and must return v_0
- this obviously violates consistency as defined above
 - which is basically a sort of atomic consistency

Next in Line...

- Building on CAP



What do we Make out of an Impossibility Result?

Should we stop distributing computational systems?

- in the same way we stopped using axiomatic systems after Gödel? [Gödel, 1931]
 - of course we did not
- ! negative results just set the boundaries, and make us understand the very limits of our reach
- so that an impossibility result from computer science becomes a leverage for specific and effective computer engineering methods and practices

Switching Strategy based on Partition Tolerance

A very simple scheme

- Brewer himself later elaborated on his CAP theorem^[Brewer, 2012]
 - (i) when the network is partitioned, a distributed system should choose a tradeoff between consistency and availability
 - (ii) when there is no partition, a system can feature both consistency and availability

ACID vs. BASE I

Beyond ACID^[Fox et al., 1997]

- ACID (Atomicity, Consistency, Isolation, and Durability) semantics might be too strong
 - "The design space for network services can be partitioned according to the data semantics that each service demands."
 - "For other Internet services, however, the primary value to the user is not necessarily strong consistency or durability, but rather high availability of data"

ACID vs. BASE II

Towards BASE[Fox et al., 1997]

- "Stale data can be temporarily tolerated as long as all copies of data eventually reach consistency after a short time"
- "Soft state, which can be generated at the expense of additional computation or file I/O, is exploited to improve performance; data is not durable"
- "Approximate answers (based on stale data or incomplete soft state) delivered quickly may be more valuable than exact answers"

BASE

- Basically Available
- Soft state
- Eventual consistency

Beyond BASE

Data consistency for Cloud [Birman et al., 2012]

- most cloud services nowadays adopts BASE
 - e.g. eBay, Amazon DynamoDB
 - ! Amazon S3 allows for strong read-after-write consistency
 - ! Amazon DynamoDB writes are eventually consistent, reads too—but strongly-consistent reads can be configured (and, they are more costly)
- and try to mask inconsistencies from users
- steps ahead are leading to new models, based on, e.g., new data-consistency models
- ! further details in the literature—at the end of the slides

Overall

CAP today^[Brewer, 2012]

The modern CAP goal should be to maximise combinations of consistency and availability that make sense for the specific application. Such an approach incorporates plans for operation during a partition and for recovery afterward, thus helping designers think about CAP beyond its historically perceived limitations

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Lessons Learnt

- in the design and development of distributed systems, we have typically to choose between a responsive system and a fully-consistent one, when network fails
- in any case, we can leverage on the CAP theorem to design your system with different features depending on the overall system status
- ACID is generally a thing to know and understand, yet less stringent models could be both theoretically and practically useful in real-world distributed systems—e.g., BASE

The CAP Theorem Availability, Consistency, Failure in Distributed Systems Distributed Systems

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