

We are given the equations:

$$x_1 + t_1 \cdot dx_1 = x_2 + t_2 \cdot dx_2 \quad (1)$$

$$y_1 + t_1 \cdot dy_1 = y_2 + t_2 \cdot dy_2 \quad (2)$$

To solve for  $t_1$  and  $t_2$ , we rearrange each equation to isolate  $t_1$  and  $t_2$ :  
From the first equation:

$$t_1 = \frac{x_2 - x_1 + t_2 \cdot dx_2}{dx_1} \quad (3)$$

From the second equation:

$$t_1 = \frac{y_2 - y_1 + t_2 \cdot dy_2}{dy_1} \quad (4)$$

Now, equate the expressions for  $t_1$  from both equations:

$$\frac{x_2 - x_1 + t_2 \cdot dx_2}{dx_1} = \frac{y_2 - y_1 + t_2 \cdot dy_2}{dy_1} \quad (5)$$

$$(x_2 - x_1 + t_2 \cdot dx_2) \cdot dy_1 = (y_2 - y_1 + t_2 \cdot dy_2) \cdot dx_1 \quad (6)$$

Expanding and rearranging, we get:

$$x_2 \cdot dy_1 - x_1 \cdot dy_1 + t_2 \cdot dx_2 \cdot dy_1 = y_2 \cdot dx_1 - y_1 \cdot dx_1 + t_2 \cdot dy_2 \cdot dx_1 \quad (7)$$

$$t_2 \cdot (dx_2 \cdot dy_1 - dy_2 \cdot dx_1) = y_2 \cdot dx_1 - y_1 \cdot dx_1 - x_2 \cdot dy_1 + x_1 \cdot dy_1 \quad (8)$$

Solving for  $t_2$ :

$$t_2 = \frac{y_2 \cdot dx_1 - y_1 \cdot dx_1 - x_2 \cdot dy_1 + x_1 \cdot dy_1}{dx_2 \cdot dy_1 - dy_2 \cdot dx_1} \quad (9)$$

Substitute  $t_2$  into one of the original equations to find  $t_1$ :

$$t_1 = \frac{x_2 \cdot dy_2 - x_1 \cdot dy_2 - y_2 \cdot dx_2 + y_1 \cdot dx_2}{dx_1 \cdot dy_2 - dy_1 \cdot dx_2} \quad (10)$$

Thus, the solutions for  $t_1$  and  $t_2$  are:

$$t_1 = \frac{x_2 \cdot dy_2 - x_1 \cdot dy_2 - y_2 \cdot dx_2 + y_1 \cdot dx_2}{dx_1 \cdot dy_2 - dy_1 \cdot dx_2} \quad (11)$$

$$t_2 = \frac{y_2 \cdot dx_1 - y_1 \cdot dx_1 - x_2 \cdot dy_1 + x_1 \cdot dy_1}{dx_2 \cdot dy_1 - dy_2 \cdot dx_1} \quad (12)$$