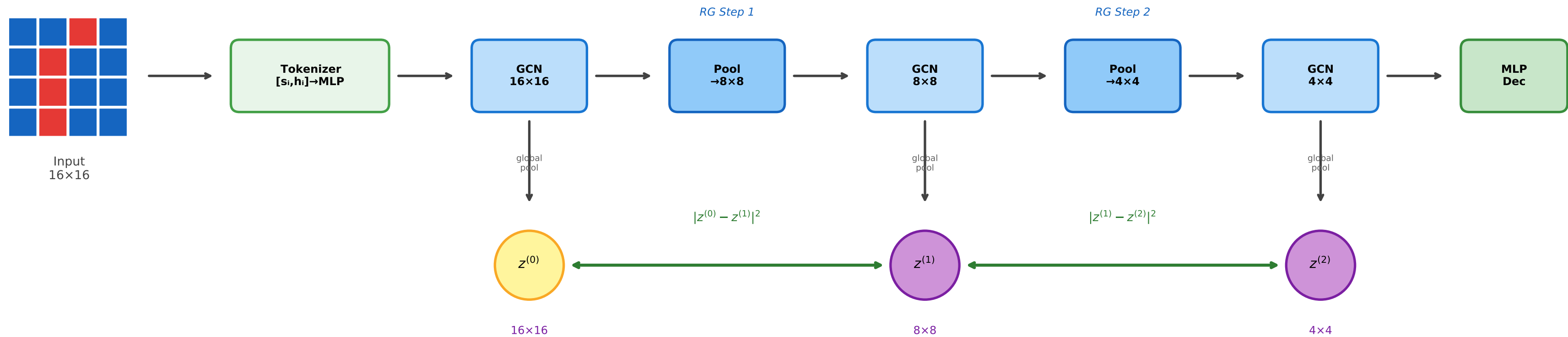


GNN-VAE with Multi-Scale RG Encoder

Each RG level outputs its own latent z



Latent Computation at Each Level:

Level 0 (16x16):

$$h^{(0)} = GCN(X_{16 \times 16})$$

$$\mu^{(0)}, \sigma^{(0)} = Linear(GlobalPool(h^{(0)}))$$

$$z^{(0)} = \mu^{(0)} + \sigma^{(0)} \cdot \varepsilon$$

Level 1 (8x8):

$$h^{(1)} = GCN(Pool(h^{(0)}))$$

$$\mu^{(1)}, \sigma^{(1)} = Linear(GlobalPool(h^{(1)}))$$

$$z^{(1)} = \mu^{(1)} + \sigma^{(1)} \cdot \varepsilon$$

Level 2 (4x4):

$$h^{(2)} = GCN(Pool(h^{(1)}))$$

$$\mu^{(2)}, \sigma^{(2)} = Linear(GlobalPool(h^{(2)}))$$

$$z^{(2)} = \mu^{(2)} + \sigma^{(2)} \cdot \varepsilon$$

$$\text{Total Loss: } \mathcal{L} = \mathcal{L}_{recon} + \beta \cdot \mathcal{L}_{KL} + \lambda_{RG} \cdot \mathcal{L}_{RG}$$

$$\mathcal{L}_{RG} = \frac{1}{2} (|z^{(0)} - z^{(1)}|^2 + |z^{(1)} - z^{(2)}|^2)$$

