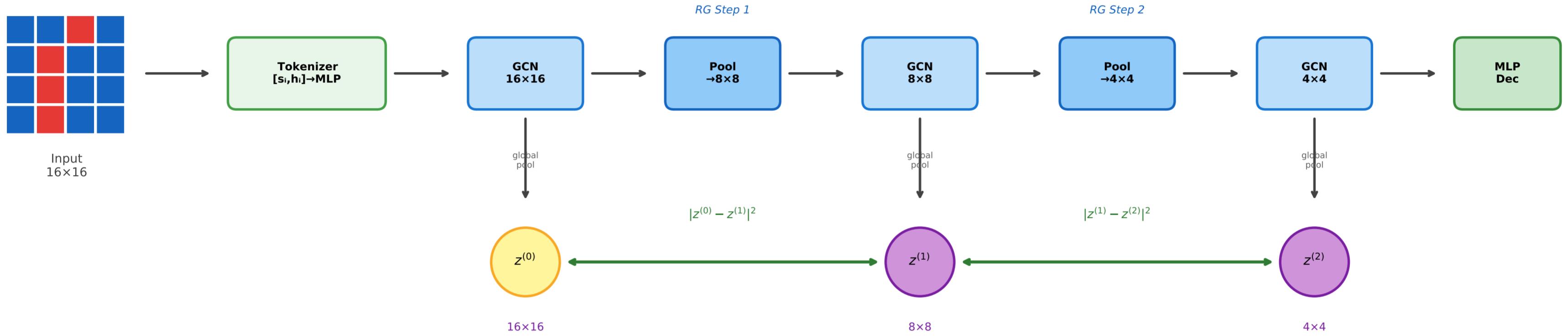


GNN-VAE with Multi-Scale RG Encoder

Each RG level outputs its own latent z



Latent Computation at Each Level:

Level 0 (16×16):

$$h^{(0)} = \text{GCN}(x_{16 \times 16})$$

$$\mu^{(0)}, \sigma^{(0)} = \text{Linear}(\text{GlobalPool}(h^{(0)}))$$

$$z^{(0)} = \mu^{(0)} + \sigma^{(0)} \cdot \varepsilon$$

Level 1 (8×8):

$$h^{(1)} = \text{GCN}(\text{Pool}(h^{(0)}))$$

$$\mu^{(1)}, \sigma^{(1)} = \text{Linear}(\text{GlobalPool}(h^{(1)}))$$

$$z^{(1)} = \mu^{(1)} + \sigma^{(1)} \cdot \varepsilon$$

Level 2 (4×4):

$$h^{(2)} = \text{GCN}(\text{Pool}(h^{(1)}))$$

$$\mu^{(2)}, \sigma^{(2)} = \text{Linear}(\text{GlobalPool}(h^{(2)}))$$

$$z^{(2)} = \mu^{(2)} + \sigma^{(2)} \cdot \varepsilon$$

Total Loss: $\mathcal{L} = \mathcal{L}_{\text{recon}} + \beta \cdot \mathcal{L}_{\text{KL}} + \lambda_{\text{RG}} \cdot \mathcal{L}_{\text{RG}}$

$$\mathcal{L}_{\text{RG}} = \frac{1}{2}(|z^{(0)} - z^{(1)}|^2 + |z^{(1)} - z^{(2)}|^2)$$

GCN Layer

Pooling (RG)

□ $z^{(0)}$ (Fine)

□ $z^{(i)}$ (Coarse)

□ Decoder