

Direct Measurement of the Higgs Boson Total Width at a Muon Collider

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In the light of the discovery of a 126 GeV Standard Model-like Higgs boson at the LHC, we evaluate the achievable accuracies for direct measurements of the width, mass and the s -channel resonant production cross section of the Higgs boson at a proposed muon collider. We find that with a beam energy resolution of $R = 0.01\%$ (0.003%) and integrated luminosity of 0.5 fb^{-1} (1 fb^{-1}), a muon collider would enable us to determine the SM-like Higgs width to 0.85 MeV (0.30 MeV) by combining two complementary channels of the WW^* and $b\bar{b}$ final states. A non-SM Higgs with a broader width is also studied. The unparalleled accuracy potentially attainable at a muon collider would test the Higgs interactions to a high precision.

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Introduction

The discovery of a Higgs boson at the LHC [1, 2] completes the simple structure of the Standard Model (SM). Yet, a profound question remains: Is this rather light, weakly-coupled boson nothing but a SM Higgs or it is a first manifestation of a deeper theory? While the LHC certainly will take us to a long journey to seek for new physics beyond the SM, it would be very important to determine the Higgs boson's properties as accurately as possible at the LHC and future collider facilities, whether or not there are other particles directly associated with the Higgs sector observed at the LHC.

Of all properties of the Higgs boson, its total decay width (Γ_h) is perhaps of the most fundamental importance since it characterizes the overall coupling strength. Once it is determined, the partial decay widths to other observable channels would be readily available. Because of the broad spread of the partonic energy distribution, limited energy-momentum resolution for final state particles and the large SM backgrounds in the LHC environment, there is essentially no way to measure its total width or any partial width to a desirable accuracy without additional theoretical assumptions [3, 4]. Assuming an upper limit for a Higgs coupling, such as that of hWW , then an upper bound for the total width can be inferred [5]. At an International Linear Collider (ILC) optimized for Higgs boson studies, the hZZ coupling, and thus the partial decay width $\Gamma(h \rightarrow ZZ)$ can be measured to a good accuracy [6]. The total decay width then may be indirectly determined. At a muon collider, however, due to the much stronger coupling for the Higgs to the muons than to the electrons, an s -channel production of a Higgs boson [7] will likely lead to clear signal for several channels and thus its total decay width may be directly measured by fitting its scanned data.

In this Letter, we propose a realistic scanning and fitting procedure to determine the Higgs boson width at a muon collider. We demonstrate the complementarity for the two leading signal channels $h \rightarrow b\bar{b}$, WW^* . The combined results lead to a highly accurate determination for the width, mass and the s -channel production cross

section. This is undoubtedly invaluable for determining the Higgs interactions and testing the theory of the electroweak symmetry breaking to an unparalleled precision.

Resonant Profile for a Higgs Boson

For a resonant production $\mu^+\mu^- \rightarrow h$ and a subsequent decay to a final state X with a collider c.m. energy $\sqrt{\hat{s}}$, the Breit-Wigner formula reads

$$\sigma(\mu^+\mu^- \rightarrow h \rightarrow X) = \frac{4\pi\Gamma_h^2 \text{Br}(h \rightarrow \mu^+\mu^-) \text{Br}(h \rightarrow X)}{(\hat{s} - m_h^2)^2 + \Gamma_h^2 m_h^2}. \quad (1)$$

where Br denotes the corresponding decay branching fraction. At a given energy, the cross section is governed by three parameters: m_h for the signal peak position, Γ_h for the line shape profile, and the product $B \equiv \text{Br}(h \rightarrow \mu^+\mu^-) \text{Br}(h \rightarrow X)$ for the event rate.

In reality, the observable cross section is given by the convolution of the energy distribution delivered by the collider. Assume that the $\mu^+\mu^-$ collider c.m. energy (\sqrt{s}) has a flux distribution $dL(\sqrt{s})/d\sqrt{\hat{s}} = \frac{1}{\sqrt{2\pi}\Delta} \exp[-\frac{(\sqrt{\hat{s}} - \sqrt{s})^2}{2\Delta^2}]$, with a Gaussian energy spread $\Delta = R\sqrt{s}/\sqrt{2}$, where R is the percentage beam energy resolution, then the effective cross section is

$$\begin{aligned} \sigma_{\text{eff}}(s) &= \int d\sqrt{\hat{s}} \frac{dL(\sqrt{\hat{s}})}{d\sqrt{\hat{s}}} \sigma(\mu^+\mu^- \rightarrow h \rightarrow X) \\ &\propto \begin{cases} \Gamma_h^2 B / [(s - m_h^2)^2 + \Gamma_h^2 m_h^2] & (\Delta \ll \Gamma_h), \\ B \exp[-\frac{(m_h - \sqrt{s})^2}{2\Delta^2}] (\frac{\Gamma_h}{\Delta}) / m_h^2 & (\Delta \gg \Gamma_h). \end{cases} \quad (2) \end{aligned}$$

For $\Delta \ll \Gamma_h$, the line shape of a Breit-Wigner resonance can be mapped out by scanning over the energy as given in the first equation. For $\Delta \gg \Gamma_h$ on the other hand, the physical line shape is smeared out by the Gaussian distribution of the beam energy spread and the signal rate will be determined by the overlap of the Breit-Wigner and the luminosity distributions, as seen in the second equation above.

Unless stated otherwise, we focus on the SM Higgs boson with the mass and total width as

$$m_h = 126 \text{ GeV}, \quad \Gamma_h = 4.21 \text{ MeV}. \quad (3)$$

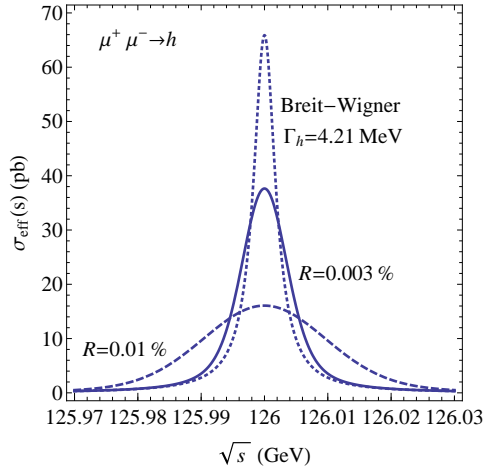


FIG. 1: Effective cross section for $\mu^+\mu^- \rightarrow h$ versus the collider energy \sqrt{s} for the SM Higgs boson production with $m_h = 126$ GeV. A Breit-Wigner line shape with $\Gamma_h = 4.21$ MeV is shown (dotted curve). The solid and dashed curves compare the two beam energy resolutions of Cases A and B.

Width (MeV)		R (%)	$\mu^+\mu^- \rightarrow h$ σ_{eff} (pb)	$h \rightarrow b\bar{b}$		$h \rightarrow WW^*$	
Br $_{b\bar{b}}$	Br $_{WW^*}$			σ_{Sig}	σ_{Bkg}	σ_{Sig}	σ_{Bkg}
SM: 4.2 [9]		0.01	16	7.6	15	3.7	0.051
56%	23%	0.003	38	18		5.5	
Exotic: 42		0.01	18	2.6		1.3	
18%	7.3%	0.003	20	3.0		1.5	

TABLE I: Effective cross sections (in pb) at the resonance $\sqrt{s} = m_h$ for two choices of beam energy resolutions R and two leading decay channels. The SM Higgs and exotic Higgs width, as well as the branching fractions in the SM are also listed.

For definitiveness in this study, we assume two sets of representative values for the machine parameters [8]

Case A : $R = 0.01\%$ ($\Delta = 8.9$ MeV), $L = 0.5$ fb $^{-1}$, (4)

Case B : $R = 0.003\%$ ($\Delta = 2.7$ MeV), $L = 1$ fb $^{-1}$. (5)

We see that their corresponding beam energy spread Δ are comparable to the Higgs total width. In Fig. I, we show the effective cross section versus the $\mu^+\mu^-$ collider c.m. energy for the SM Higgs boson production. A pure Breit-Wigner resonance is shown by the dotted curve. The solid and dashed curves include the convolution of the luminosity distribution for the two beam energy resolutions and integrated over \sqrt{s} . For simplicity, we have taken the branching fractions $h \rightarrow \mu^+\mu^-$ to be the SM value and to the final state $h \rightarrow X$ to be 100%. The beam energy resolution manifests its great importance in comparison between the solid and dashed curves in this figure.

Width Determination for the SM Higgs Boson

An excellent beam energy resolution for a muon collider would make a direct determination of the Higgs boson width possible in contrast to the situations in the

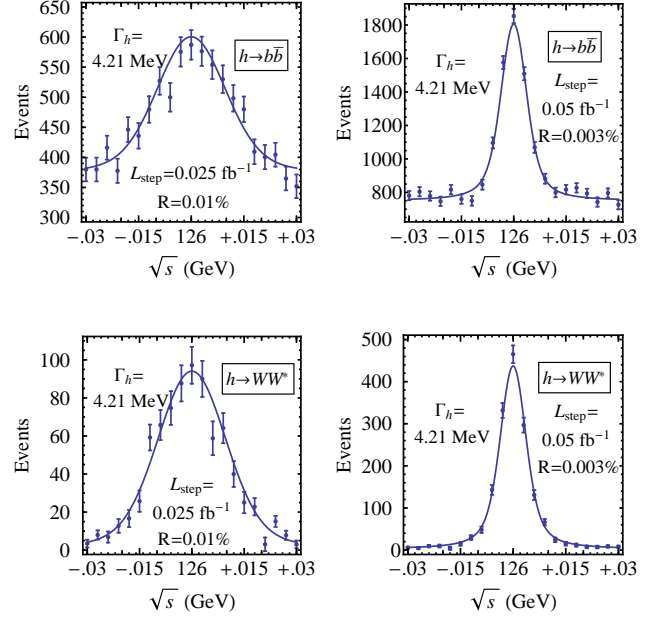


FIG. 2: Number of events of the Higgs signal plus backgrounds and statistical errors expected for Cases A and B as a function of the collider energy \sqrt{s} in $b\bar{b}$ and WW^* final states with a SM Higgs $m_h = 126$ GeV and $\Gamma_h = 4.21$ MeV.

LHC and ILC. Because of the expected narrow width for a SM Higgs boson, one still needs to convolute the idealistic Breit-Wigner resonance with the realistic beam energy spectrum as illustrated in Eq. (2). We first calculate the effective cross sections at the peak for the two cases of energy resolutions A and B. We tablet the results along with the input SM parameters (the first two rows) in Table I. We further evaluate the signal and SM background for the leading channels

$$h \rightarrow b\bar{b}, \quad WW^*. \quad (6)$$

For a given beam resolution, we assume that a scan procedure over the collider c.m. energy \sqrt{s} is available. The current Higgs mass statistical error is about 0.4 GeV [1, 2] with an integrated luminosity of about 10 fb $^{-1}$. Toward the end of the LHC run with about 100 times more luminosity accumulated, it is conceivable to improve the statistical error of the mass determination by about an order of magnitude. Then the systematic errors would have to be controlled to a best level. It was argued that an ILC could reach a similar or better accuracy [10]. We thus proceed to scan over the energy in the range

$$126 \text{ GeV} \pm 30 \text{ MeV} \text{ in } 20 \text{ scanning steps.} \quad (7)$$

The energy scanning step is set at 3 MeV, roughly the same size of the Δ and Γ_h .

We first generate ideal data in accordance with a Breit-Wigner resonance at this mass convoluted with Gaussian

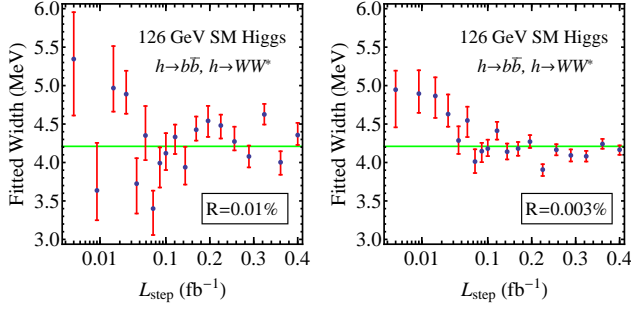


FIG. 3: Fitted values and errors for the SM Higgs width versus the luminosity per step with the scanning scheme as specified in Eq. (7).

distribution of the beam energy integrated over \sqrt{s} , as discussed before. We impose a polar angle acceptance for the final state particles,

$$10^\circ < \theta < 170^\circ. \quad (8)$$

Tightening up the polar angle to $20^\circ - 160^\circ$ will further reduce the signal by 4.6%, and the background by 6.7% (15%) for the $b\bar{b}$ (WW^*) final states. We assume a 60% single b -tagging efficiency and require at least one tagged b jet for the $b\bar{b}$ final state. The backgrounds are assumed to be flat with cross sections evaluated right at 126 GeV using Madgraph5 [11]. The background rate of $\mu^+\mu^- \rightarrow Z^*/\gamma^* \rightarrow b\bar{b}$ is 15 pb and the rate of $\mu^+\mu^- \rightarrow WW^* \rightarrow 4$ fermions is only 51 fb, as shown in Table I. While the $b\bar{b}$ final state has a larger signal rate than that for WW^* by about a factor of three, the latter has a much improved signal (S) to background (B) ratio, about 100:1 near the peak.

The results are shown by the solid curves in Fig. 2, for Cases A and B as in Eq. (4) (left panels) and Eq. (5) (right panels). The $b\bar{b}$ and WW^* final states are separately shown by the upper and lower panels, respectively. These data are then randomized with a Gaussian fluctuation with standard deviation \sqrt{N} , where N is the number of events expected for a given integrated luminosity, summing both signal and background. The simulated events over the scanning points are plotted with statistical errors for the assumed integrated luminosity as in Eqs. (4) and (5).

We adopt a χ^2 -fit over the scanning points with three model independent free parameters in the theory Γ_h , B and m_h by minimizing the χ^2 . The fitted curves have no appreciable difference from the theoretical expectation as in Fig. 2. The fitting accuracies for the Higgs properties can be illustrated by the one standard deviation range, denoted by $\delta\Gamma_h$, δB and δm_h . To see the effects from the available luminosity, we show our results for the SM Higgs width determination in Fig. 3 for both cases by varying the luminosity. The achievable accuracies with the scanning scheme as specified in Eq. (7) by combining

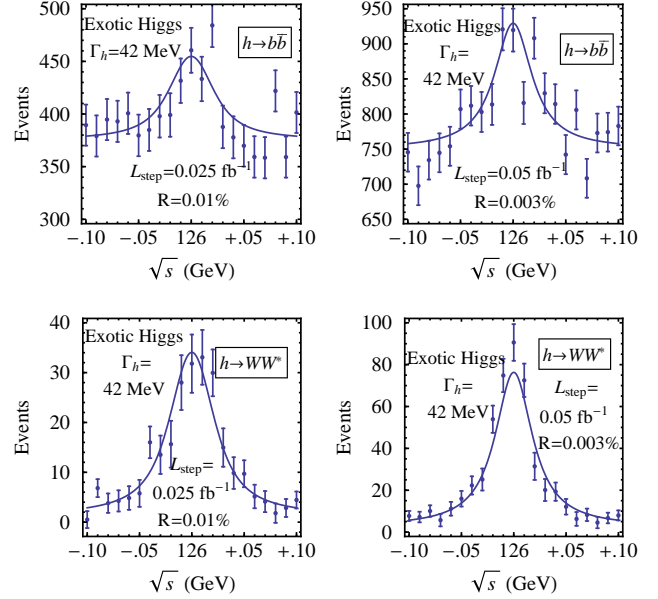


FIG. 4: Number of events of the Higgs signal plus backgrounds and statistical errors expected for Cases A and B as a function of the collider energy \sqrt{s} in $b\bar{b}$ and WW^* final states with an exotic Higgs $m_h = 126$ GeV and $\Gamma_h = 42$ MeV.

two leading channels is summarized in Table II for three representative luminosities per step.

$\Gamma_h = 4.21$ MeV	L_{step} (fb $^{-1}$)	$\delta\Gamma_h$ (MeV)	δB	δm_h (MeV)
Case A $R = 0.01\%$	0.005	1.5	13%	0.51
	0.025	0.85	6.1%	0.32
	0.2	0.34	2.2%	0.13
Case B $R = 0.003\%$	0.01	0.61	8.3%	0.40
	0.05	0.30	3.8%	0.13
	0.2	0.17	2.0%	0.10

TABLE II: Fitting accuracies for one standard deviation range of $\delta\Gamma_h$, δB and δm_h of the SM Higgs with the scanning scheme as specified in Eq. (7) for three representative luminosities per step.

Width Determination for a Broader Higgs Boson

We now explore the unique feature of the direct width measurement for a broader resonance at a muon collider. For definitiveness, we still work with a Higgs-like particle with a mass at 126 GeV, but with a total width of ten times larger than that of the SM value, $\Gamma_h = 42$ MeV. To be conservative in accordance with the current LHC observation, we would like to keep the LHC signal of this particle unchanged.

In Fig. 4, we present the similar analyses as in Fig. 2 for a broader Higgs. There are two features of this figure comparing to the SM Higgs in Fig. 2. First, the increase of Higgs width requires a broader scan range to reconstruct the Breit-Wigner resonant distribution. We choose

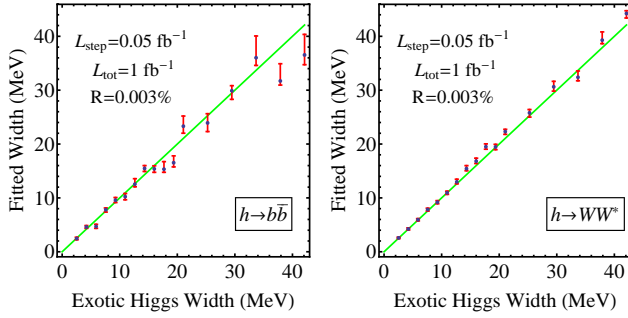


FIG. 5: Fitted values and errors for the Higgs width versus the input values. The step size is set as rounded half integer value between 3 MeV – 10 MeV in accordance to the Higgs width 0.6 – 10 times the SM value.

$\Gamma_h = 2.5 - 42 \text{ MeV}$	$\delta\Gamma_h \text{ (MeV)}$	δB	$\delta m_h \text{ (MeV)}$
$b\bar{b}$	0.5 – 6.8	6% – 20%	0.2 – 2
WW^*	0.3 – 1.3	5% – 10%	0.1 – 1

TABLE III: Fitting accuracies for the exotic Higgs properties. The scanning scheme is the same as in Fig. 5.

to scan the same number of 20 scan steps with a step size of 10 MeV, while keeping the same total integrated luminosity. It is seen from the figure that the physical line shape of the Higgs boson is essentially mapped out by the scanning. Secondly, since the signal rate at the LHC is governed by partial widths to initial (i) and final (f) states $\propto \Gamma_i \Gamma_f / \Gamma_h$, the rate could be kept the same when increasing the Higgs total width by a factor κ while scaling the partial widths up by a factor $\sqrt{\kappa}$. This would correspondingly reduce the cross section for the signal at muon collider as seen in Eq. (1). Under this constraint, the results for the branching fractions and the effective peak cross sections of a broader Higgs at a muon collider are listed in Table I in the last two rows.

Although a larger Higgs width would be easier to resolve with a fine energy resolution, it is a practical concern when larger range of the scanning energy is needed with a fixed total luminosity. In Fig. 5, we explore this issue by plotting the width determination with statistical errors for a fixed total luminosity at 1 fb^{-1} and varying Higgs widths. The events from the $b\bar{b}$ channel and WW^* channel are shown individually. It turns out that a smaller width could receive better accuracies in the

scanning process due to the larger signal rate than that at a larger width as commented above. We summarize the fitting accuracies in Table III.

Discussions and Conclusions

The direct measurement of the Higgs width with high precision will be invaluable to explore new physics through this “Higgs lamp post”. For instance, varying the parameters $\tan \beta$, M_A in the Minimal Supersymmetric Model (MSSM) within the current LHC constraints, the SM-like Higgs width could change by 20% [12]. Models with Higgs invisible decays would increase the width. Generic Higgs multiplet models allow an increase in total width, as illustrated in the triplet Georgi-Machacek model [13]. Composite Higgs models also alter the Higgs width from the SM value.

The mass and cross section can be simultaneously determined along with the Higgs width to a high precision. The results obtained are largely free from theoretical uncertainties. Uncertainties of the signal evaluation do not alter the width and mass fitting. The major systematic uncertainty comes from our knowledge of beam properties [8].

Moreover, our study on the width and mass measurements can be applicable to new particles predicted in many theories. For example, the CP-odd and the other CP-even Higgs states in MSSM and in Two-Higgs-Doublet-Models may all be suitably studied at a muon collider. The achievable high accuracy would help to resolve nearly degenerate Higgs states.

In conclusion, the newly observed Higgs-like particle at the LHC strongly motivates a muon collider as the Higgs factory. We proposed methods and evaluated the attainable accuracy to directly measure the Higgs width by scanning and fitting the s -channel resonance. The unparalleled precision would test the Higgs interactions to a high precision and undoubtedly take us to a deeper understanding of the EWSB sector.

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