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NAIVE BAYES CLASSIFIER

No	Color	Type	Origin	Stolen
1	Red	Sports	Domestic	Yes
2	Red	Sports	Domestic	No
3	Red	Sports	Domestic	Yes
4	Yellow	Sports	Domestic	No
5	Yellow	Sports	Imported	Yes
6	Yellow	SUV	Imported	No
7	Yellow	SUV	Imported	Yes
8	Yellow	SUV	Domestic	No
9	Red	SUV	Imported	No
10	Red	Sports	Imported	Yes

New Instance = (Red, SUV, Domestic) →
(Yes or No)

$$p(\text{yes}) = \frac{5}{10} = 0.5$$

$$p(\text{No}) = \frac{5}{10} = 0.5$$

Color	Yes	No
Red	3/5	2/5
Yellow	2/5	3/5

↙ 5 Yes samples ↘ 5 No samples

(2)

Type	No	Yes
Sports	2/5	4/5
SUV	3/5	3/5

Type	Yes	No
Sports	4/5	2/5
SUV	1/5	3/5

Origin	Yes	No
Domestic	2/5	3/5
Imported	3/5	2/5

$$P(\text{Yes} | \text{New Instance}) = P(\text{Yes}) \times$$

$$P(\text{Color} = \text{Red} | \text{Yes}) \times$$

$$P(\text{Type} = \text{SUV} | \text{Yes}) \times$$

$$P(\text{Origin} = \text{Domestic} | \text{Yes})$$

$$P(\text{Yes} | \text{New Instance}) = \frac{5}{10} \times$$

$$\frac{3}{5} \times \frac{1}{5} \times \frac{2}{5} = 0.024$$

(3)

$$P(\text{No} | \text{New Instance}) = P(\text{No}) \times$$

$$P(\text{Color} = \text{Red} | \text{No}) \times$$

$$P(\text{Type} = \text{SUV} | \text{No}) \times$$

$$P(\text{Origin} = \text{Domestic} | \text{No})$$

$$P(\text{No} | \text{New Instance}) = \frac{5}{10} \times \frac{2}{5} \times \frac{3}{5} \times \frac{3}{5}$$

$$= 0.072$$

$$P(\text{No} | \text{New Instance}) \rightarrow$$

$$P(\text{Yes} | \text{New Instance})$$

$$- x - x -$$