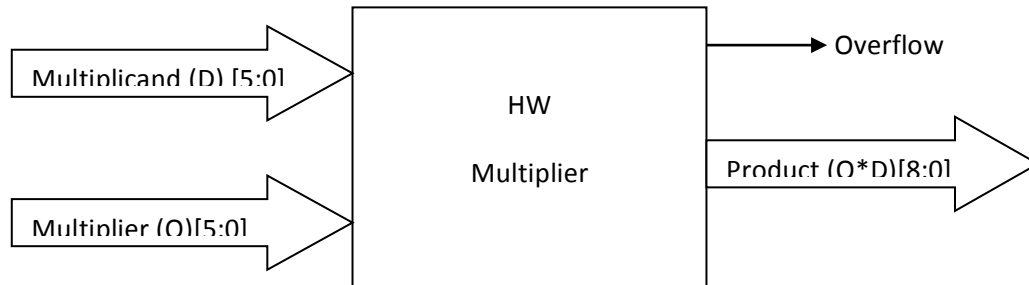


The studies will be presented after 2 weeks (Lab sections). **Each group must present their own study. The group members have to work together and each member must know each step of the study.**

For this laboratory assignment, you will use Altera Quartus II software and DE-115 FPGA kit and design a hardware floating point multiplier that has the Input/output definitions below. You should design the circuit first, then use verilog-HDL and DE-115 kit to implement your design.



All numbers in this assignment are in the IEEE 754 binary floating-point format and the inputs and output have 6 and 9 bits respectively. The FP format has three areas: the MSB represents the sign of the number (0: positive, 1: negative), the exponential part and the mantissa.

The area lengths for the inputs:

S-1bit	E-2 bits	M-2 bits
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The area lengths for the output:

S-1bit	E-3 bits	M-5 bits
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The formula to convert the number from IEEE 754 format to decimal is given as:

$$\text{For the numbers at input: } n_{input} = (-1)^S \cdot (1 + M \cdot 2^{-2}) \cdot (2^{E-1})$$

$$\text{For the numbers at output: } n_{output} = (-1)^S \cdot (1 + M \cdot 2^{-5}) \cdot (2^{E-3})$$

The formulas are different since area sizes are not same for input and output numbers.

Some examples:

Ex1: If the FP formatted number at **input** is: 01011 =>

The first bit is sign bit hence number is positive.

1. Exponential area is E=10b. $2^{2-1}=2$
2. Mantissa, M=11b. $1+3 \cdot 2^{-2}=1.75$
3. The number: $+ 2 \cdot 1.75 = 3,5$

Ex2: If the number at the **input** is 11101 =>

The first bit is sign bit hence number is negative.

1. Exponential area is E=11b. $2^{3-1}=4$
2. Mantissa, M=01b. $1+1 \cdot 2^{-2}=1.25$
3. The number: $- 4 \cdot 1.25 = -5$

Ex3: If the number at the **output** is 111100011 =>

The first bit is sign bit hence number is negative.

1. Exponential area is E=111b. $2^{7-3}=2^4$
2. Mantissa, M=00011b. $1+3 \cdot 2^{-5}=1.09375$
3. The number: $- 2^4 \cdot 1.09375 = -17.5$

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Multiplication procedure for floating point numbers:

The floating point formatted inputs Q and D will be multiplied.

Step1: Same sign bits => positive result, otherwise => negative result.

Step2: normalize the exponentials by subtracting 01b, then sum them. Add 01b to the sum. $E_{result} = E_D - 1 + E_Q - 1$.

Step3: multiply the mantissa areas as shown in the following formula: $M_{result} = 1.M_Q * 1.M_D$. In the formula, all the numbers are binary and the mantissa areas are used as fractional parts.

Possible results:

- 1) $M_{result} = 1x.xxxx$ => move the radix point one place to the left and increase the exponent by 1. After operation, $M_{result} = 1.xxxxx$ and $E_{result} = E_D - 1 + E_Q - 1 + 1$.
- 2) $M_{result} = 01.xxxx$ => no manipulation is needed.

Step4: E_{result} should be increased by 3 and converted to binary, use only fractional part of M_{result} ($M=xxxxx$) and use sign bit at MSB position:

Multiplication result in FP format: SEEEMMMMM

Multiplication Example:

Let us multiply the numbers in Ex1 and Ex2: $(Q=01011)*(D=11101) = ?$

Step1: sign bits are not same => resulted sign bit: 1

Step2: $E_Q=10b=2$, $E_D=11b=3$ => $E_{result} = 3+2-2=3$.

Step3: $M_Q=11b$ and $M_D=01b$ =>

1.11
1.01
*-----
111
000
111
+-----
10.0011

$M_{result}=10.0011$ => the radix point should be moved to the one place left. Therefore E_{result} should be increased by one.

After Step3: $E_{result}=3+1 = 4$ and $M_{result}=1.00011$

Step4: increase E_{result} by 3 and convert it to binary: $E_{result}=111$. Use only fractional part for $M_{result}=00011$. The multiplication result in FP format: Product=111100011.

Overflows:

If the result's exponential area exceeds 3 bits an overflow is occurred. The result's Sign bit defines the type of overflow (positive or negative).

Overflow example:

$11111*01111=?$

Step1: result is neg., **Step2:** $E=3-1+3-1=4$,

Step3: $1.11*1.11=11.0001$ => radix point should be moved to one place left and E should be increased by 1 => $M=1.10001$ and $E=5$.

Step4: $E = 5+3=8=1000b$ and $M=10001$. The exponential area has four bits=> overflow = 1, $S=1$, $E=000$ and $M=10001$. The result: Ov=1, Product=100010001.