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EXTENDS Workflow Validation
 T ... The set of all tasks T
t^* ... The predicate indicating the repeatability of a task t
t^* \stackrel{\Delta}{=} Task(t).repeatable e.g. \$"XRAY"* = true\$
 destr(t) ... The predicate indicating the destructiveness of a task t
destr(t) \stackrel{\triangle}{=} Task(t).group = "destructive" | e.g. \$destr("IVI") = true\$
 non_destr(t) ... The predicate indicating the non-destructiveness of a task t
non\_destr(t) \stackrel{\triangle}{=} Task(t).group = "non-destructive" e.g. <math>non\_destr(EVI") = true
 A \prec B, B \succ A ... The partial order relation between tasks
A \prec B \stackrel{\Delta}{=} ConRel[A, B] e.g. $"EVI" \prec "XRAY"$
B \succ A \triangleq ConRel[A, B] e.g. \$"IVI" \succ "XRAY"\$
 A \leq B, B \succeq A ... The reflexive transitive closure over the partial order relation
A \leq B \stackrel{\triangle}{=} TransConRel[A, B] e.g. \$"EVI" \leq "IVI" \$
B \succ A \stackrel{\triangle}{=} TransConRel[A, B] e.g. $"IVI" \succ "EVI"$
 A \vdash B, B \dashv A ... The relation describing whether one task requires another task
A \vdash B \stackrel{\triangle}{=} RequiresRel[A, B] e.g. \$"XRAY" \vdash "EVI"\$
B \dashv A \stackrel{\Delta}{=} RequiresRel[A, B] e.g. \$"XRAY" \dashv "IVI"\$
 W$ ... the sequence of workflow tasks W
W \stackrel{\Delta}{=} Workflow \ e.g. \ \$W = ("EVI", "IVI", "EVI") \$
 T(W) ... The set of all workflow tasks T(W)
T(W) \stackrel{\triangle}{=} RAN(W) e.g. T(W) = \{ EVI'', IVI'' \}
 \, \$\, W \setminus \neq \, \setminus \neq t \$\, \dots The amount of occurrences of task t in the given workflow sequence
W \# \# t \stackrel{\Delta}{=} Count(W, t) e.g. \$W \setminus \neq \setminus \neq \text{``EVI''} = 2\$
 W @ t \ldots The set of all indexes of a task t in the given workflow sequence
W @@ t \stackrel{\triangle}{=} Indexes(W, t) e.g. \$W @@ "EVI" = \setminus \{1, 3 \setminus \}\$
 W \simeq \hat{t} \ . . . The first index of a task t in the given workflow sequence
W^{\hat{t}} \stackrel{\triangle}{=} FirstIndex(W, t) | e.g. $W \string^\string^ "IVI" = 2$
 W \ ... The last index of a task t in the given workflow sequence
W \$\$ t \stackrel{\triangle}{=} LastIndex(W, t) e.g. \$W \ \$ ``\& ``EVI" = 3\$
All tasks must be known
KnownTaskConstraint \triangleq
    \forall t - w \in T(W): \exists t \in T: t - w = t
Non-repeatable tasks must not be repeated
RepeatabilityConstraint \triangleq
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Destructive tasks must come after non-destructive ones

 $\forall t \in T: t \in T(W) \land \neg t^* \Rightarrow W \# \# t < 1$

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DestructiveOrderConstraint \triangleq
     \forall d, n \in T:
         d \neq n \land d \in T(W) \land n \in T(W) \land destr(d) \land non\_destr(n) \Rightarrow W^{\hat{}}d > W \$\$ n
Task order must adhere to (transitive) partial order
PartialOrderConstraint \triangleq
     \forall a, b \in T:
         a \neq b \land a \leq b \land a \in T(W) \land b \in T(W) \land (\neg a^* \lor \neg b^*) \Rightarrow W \$\$ a < W^{\hat{}}b
Required tasks must be done before / after dependent tasks
MandatoryDependencyConstraint \triangleq
     \forall a, b \in T:
          \land \ a \neq b \land a \preceq b \land a \vdash b \land a \in T(\mathit{W}) \ \Rightarrow \ b \in T(\mathit{W}) \land \mathit{W} \$\$ \ a < \mathit{W} \$\$ \ b
          \land a \neq b \land a \leq b \land a \dashv b \land b \in T(W) \Rightarrow a \in T(W) \land W^{\hat{}}a < W^{\hat{}}b
Required tasks must be done in between dependent tasks, in case of repetition
MandatoryRepetitionConstraint \triangleq
     \forall a, b \in T:
         \wedge
               \land a \neq b \land a \leq b \land a \vdash b \land a \in T(W) \land b \in T(W)
               \Rightarrow \forall i, j \in (W@@a): i < j \Rightarrow \exists k \in (W@@b): i < k \land k < j
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 $\land a \neq b \land a \leq b \land a \dashv b \land a \in T(W) \land b \in T(W)$

 $\Rightarrow \forall i, j \in (W@@b): i < j \Rightarrow \exists k \in (W@@a): i < k \land k < j$