

Structured light systems

Tutorial 1: 9:00 to 12:00

Monday May 16 2011

Hiroshi Kawasaki & Ryusuke Sagawa

Today

Structured light systems

- Part I (Kawasaki@Kagoshima Univ.)
 - Calibration of Structured light systems
- Part II (Sagawa@AIST Japan)
 - Structured light systems for moving object

Self-introduction

- Name: Hiroshi Kawasaki
- From: Kagoshima National University, Japan
- Research interest: 3D scanning, photo-realistic CG



Overview

- Introduction
 - shape acquisition system
- Basic problems of Structured light system
 - Calibration
 - Correspondences
- Online calibration for light sectioning method
- Auto calibration for projector camera system

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Shape acquisition

- Passive method
 - ☺ Only camera
 - ☹ Unstable
 - ☹ Sparse
- Active method
 - ☺ Dense
 - ☺ Stable
 - ☹ Lighting and mechanical devices

Shape acquisition

- Passive method

- ☹ Only camera

- ☹ Unstable

- ☹ Sparse

- Active method

- 😊 Dense

- 😊 Stable

- ☹ Lighting and mechanical devices

Active scanner

1. Time-of-flight based technique

2. Stereo based technique

Active scanner

1. Time-of-flight based technique
2. Stereo based technique



Active scanner

1. Time-of-flight based technique
2. Stereo based technique



- ☺ Precision and stability
- ☹ High cost (precision devices)
- ☹ Long scanning time



Active scanner

1. Time-of-flight based technique
2. Stereo based technique

Possibility of

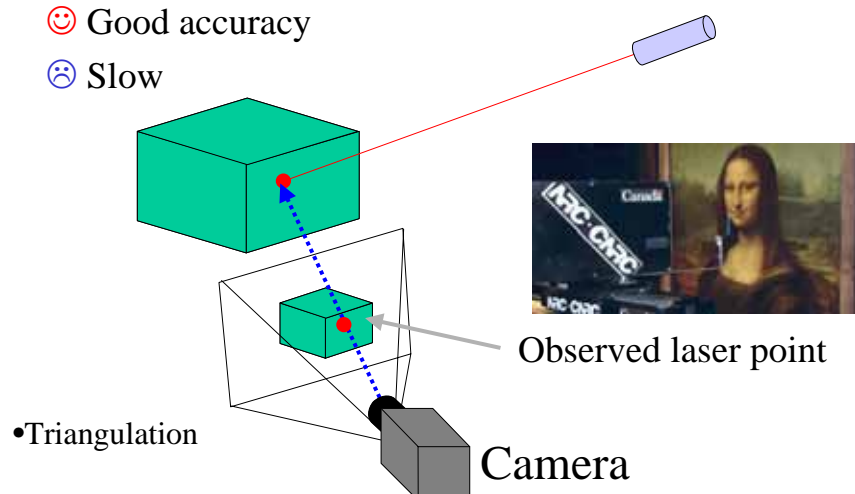
- ☺ cost efficiency
- ☺ precision
- ☺ short scanning time

by **computer vision** techniques

Stereo based active scan

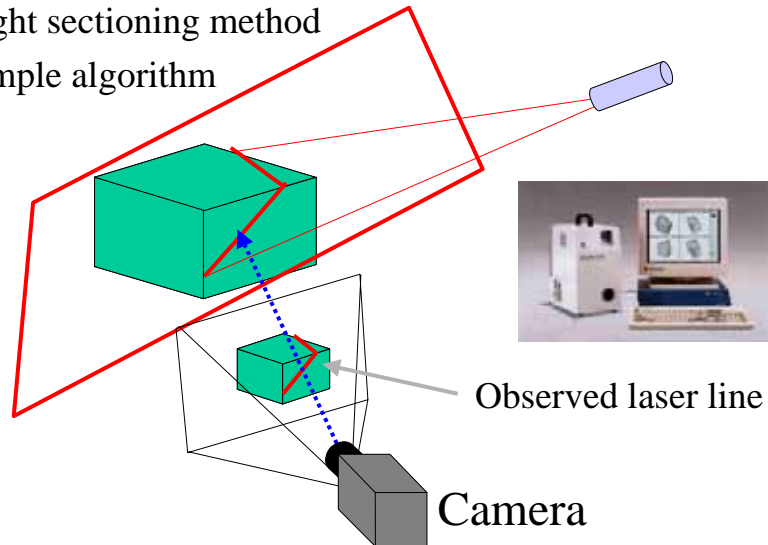
- Camera + **point** laser projector

- ☺ Easy to make
- ☺ Good accuracy
- ☹ Slow



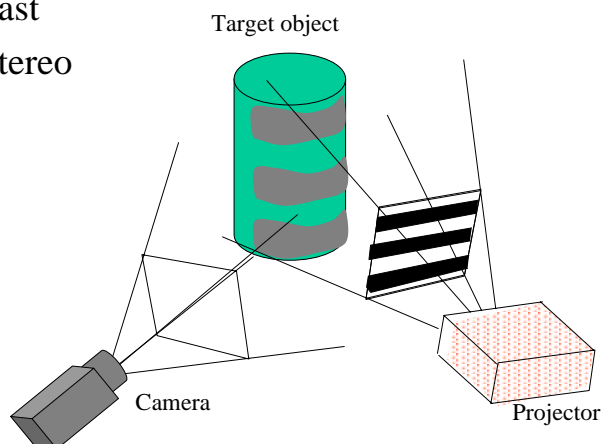
Stereo based active scan

- Camera + **line laser** projector
 - Light sectioning method
 - Simple algorithm



Stereo based active scan

- Camera + **video** projector
 - Projector camera system
 - Fast
 - Stereo



Stereo based active scan

- Camera + **point** laser projector
 - No structure on light
- Camera + **line laser** projector
 - Light sectioning method
 - Simple algorithm
- Camera + **video** projector
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Stereo based active scan

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Basic problems of Structured light system

- Calibration of structured light
- Correspondences

Basic problems of Structured light system

- Calibration of structured light → Part I
- Correspondences → Part II

Calibration of structured light

- Calibration of light source (Intrinsic)
- Calibration between light source and camera (Extrinsic)

Calibration of structured light

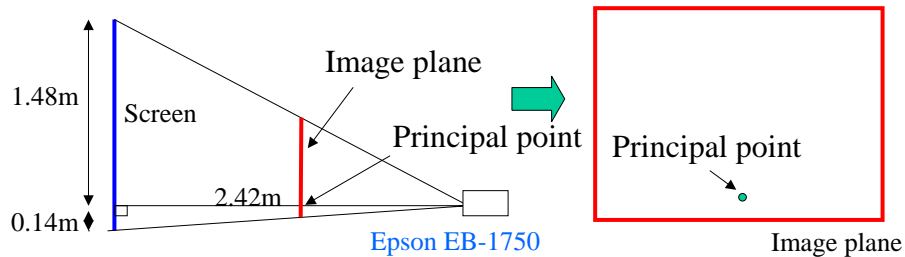
- Calibration of light source (Intrinsic)
- Calibration between light source and camera (Extrinsic)

Question

- Model of light source?
- Algorithm?
 - Projector cannot capture image
 - Calibration box or plane?

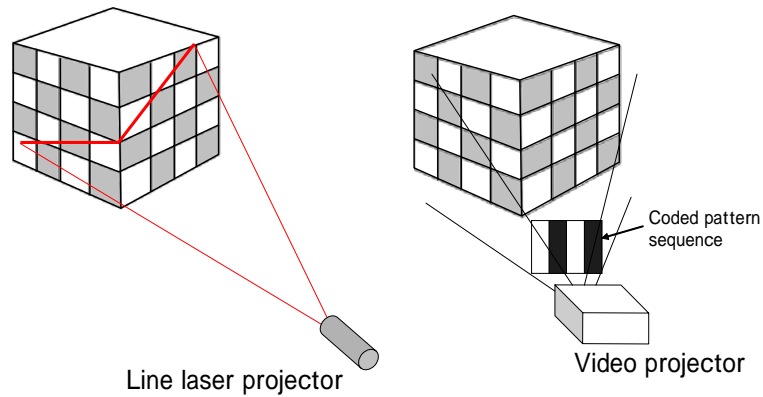
Model of light source

- Line laser projector
 - Plane in 3D
- Video projector
 - Pinhole camera model
 - Principal point is placed bottom



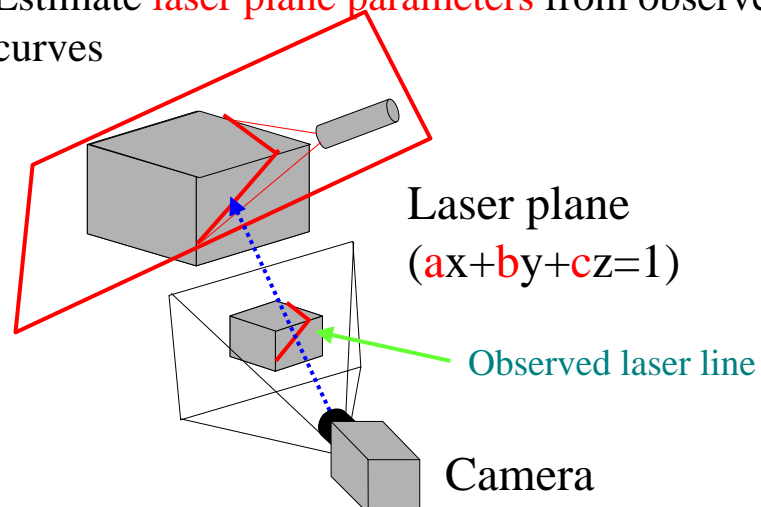
Basic approach

- Using calibration object



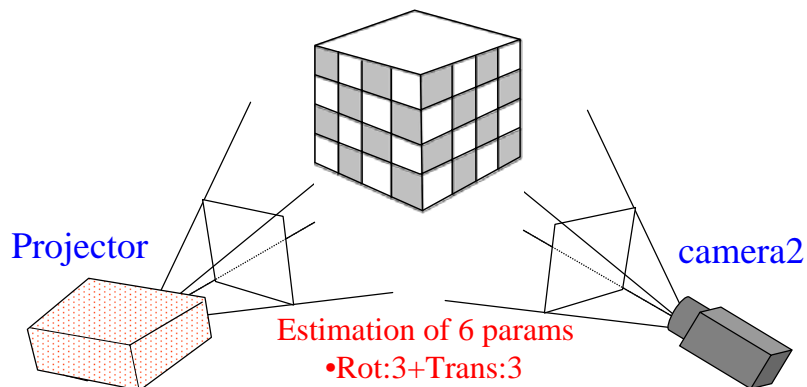
Calibration of laser plane

- Light sectioning method (triangulation)
- Estimate **laser plane parameters** from observed curves

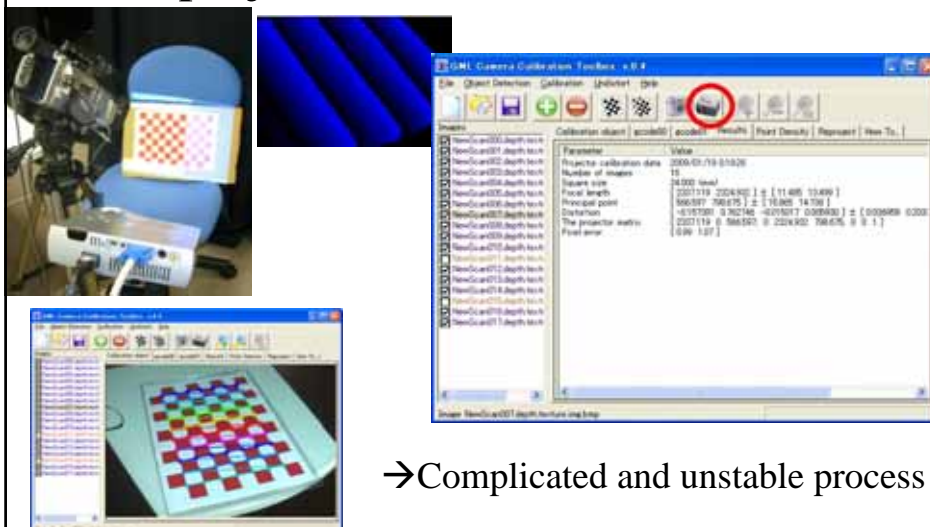


Calibration of projector camera system

- Stereo method
- Estimate camera parameter



Example of calibration [projector calibration toolbox]

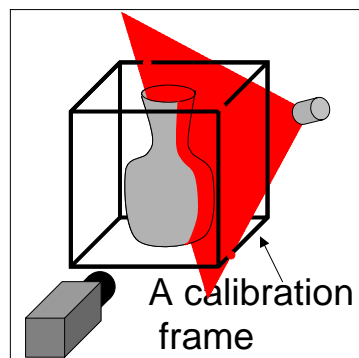


Overview

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Online calibration

- Calibration object in a scene
 - Frame [Chu et.al. 3DIM01]
 - Planes [David 2006 <http://www.rob.cs.tu-bs.de/news/david>]

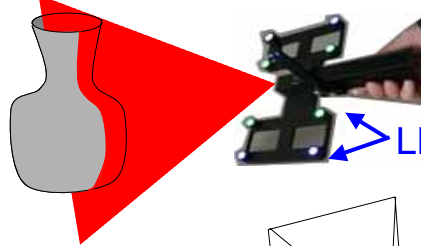


Online calibration

- Calibration object on the projector

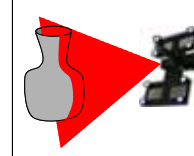
[Furukawa and Kawasaki 3DIM03]

- Attach LEDs

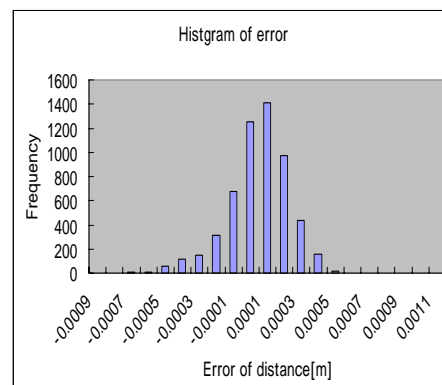
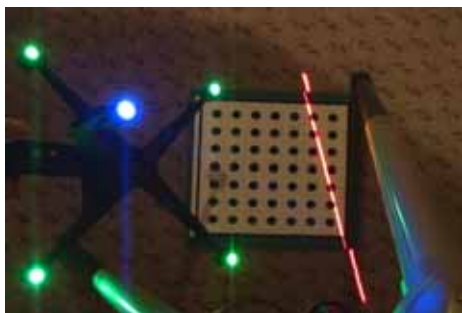


Captured image

- Both laser and LEDs are in a image



Capturing sequence and precision

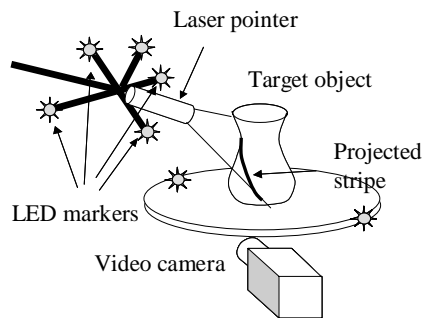


=0.00017(m)

Extension

Entire shape acquisition with **rotation table**

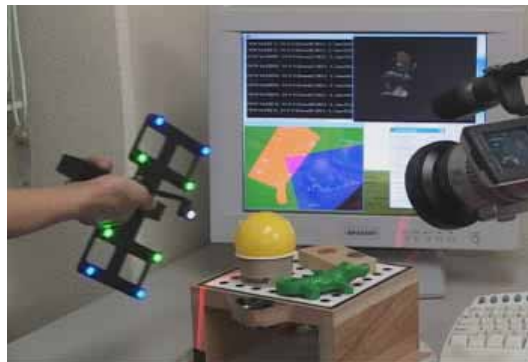
[Furukawa and Kawasaki 3DPVT04]



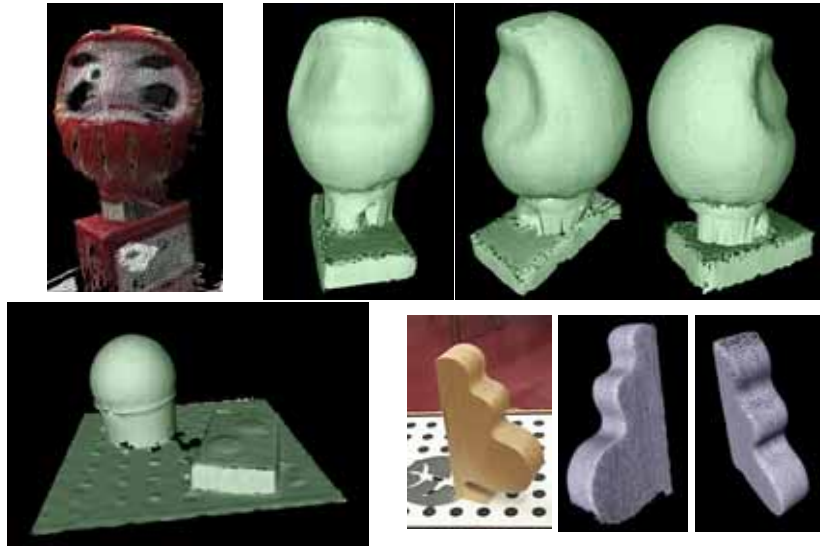
Extension

Entire shape acquisition with **rotation table**

[Furukawa and Kawasaki 3DPVT04]



Rotation table results

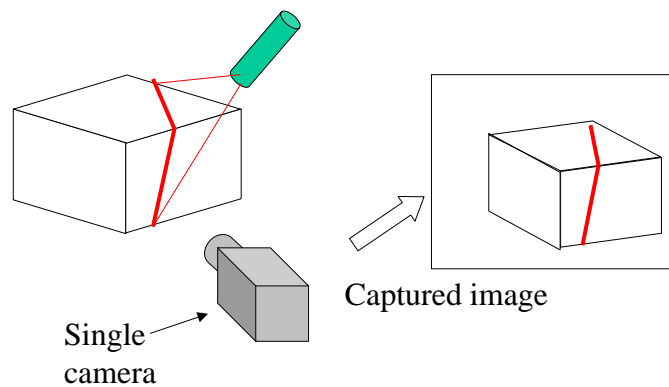


Previous method

- Pre-calibration
 - Hard calibration (fixed system)
 - Use motor and precision devices
- Online-calibration
 - Frames or planes are required [david'06]
 - LED markers required [kawasaki'03]

Can we eliminate **all** additional devices ?

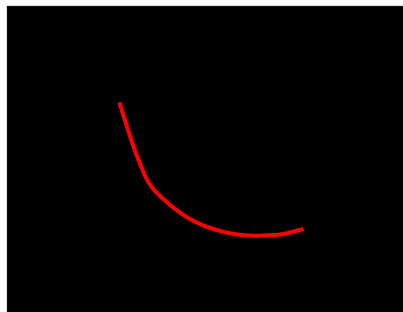
Self-calibration of laser plane without any additional devices



System configuration

Problem 1

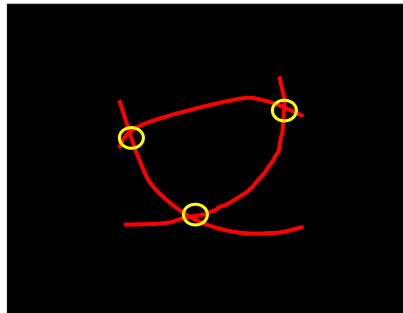
- Can we reconstruct shape from the following image?



NO!

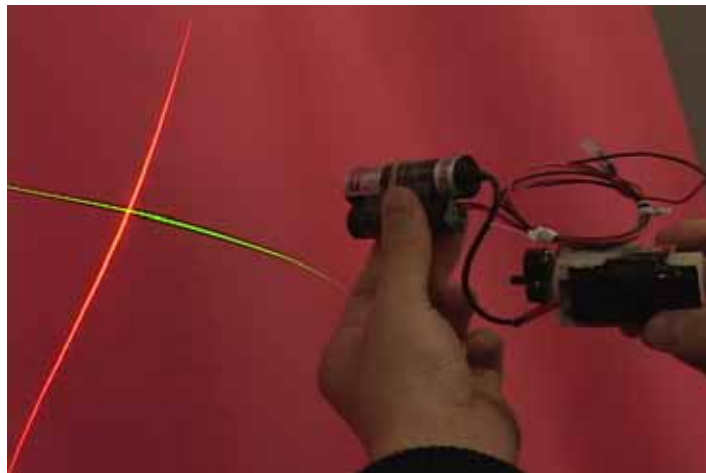
Problem 2

- How about this?

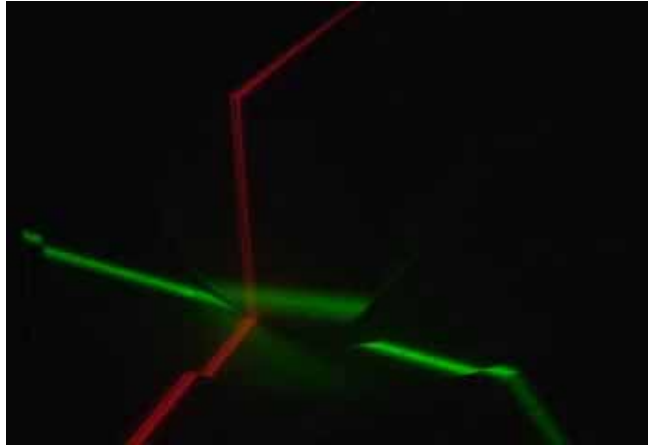


Maybe?

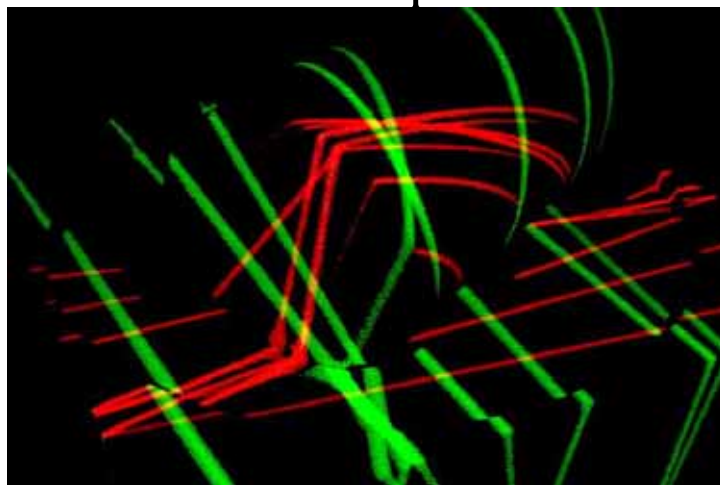
Example of line laser projector
(cross pattern by two lasers)



Can you imagine the shape?



Is it possible to reconstruct the
3D shape?

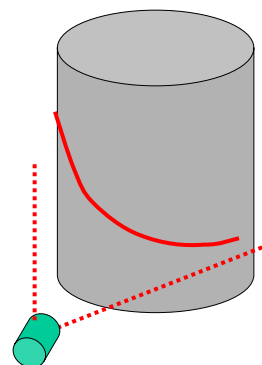
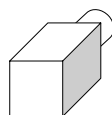
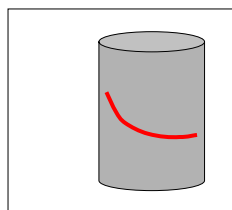


True shape



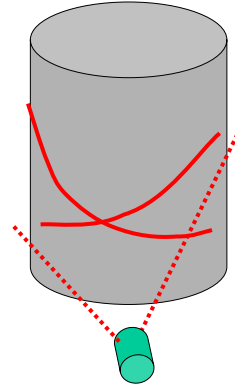
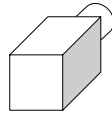
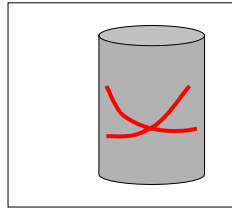
Problem definition

Camera Image



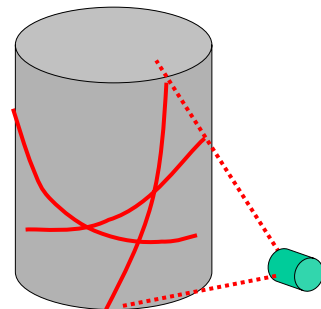
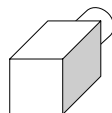
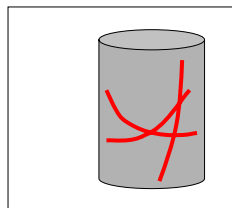
Problem definition

Accumulated Images



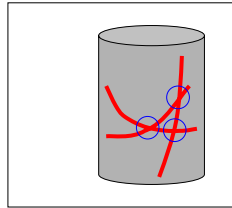
Problem definition

Accumulated Images

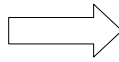


Self-calibration of planes

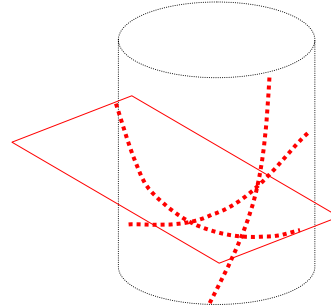
Temporally accumulated camera images



Intersections

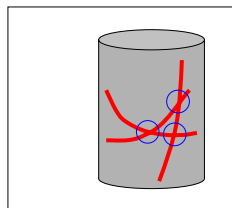


Estimation of laser planes

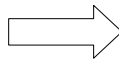


Self-calibration of planes

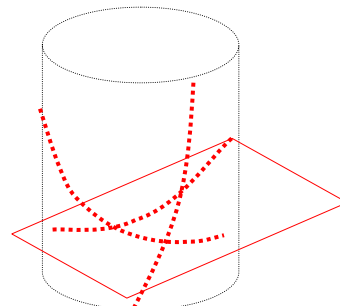
Temporally accumulated camera images



Intersections

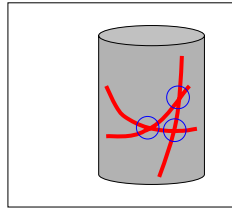


Estimation of laser planes

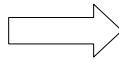


Self-calibration of planes

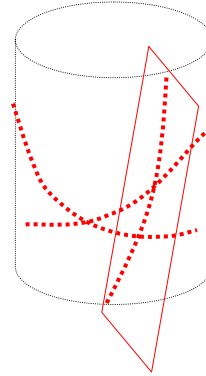
Temporally accumulated camera images



Intersections



Estimation of laser planes



Outline of Self-calibration and 3D reconstruction

Detect laser lines from video



Constraint equations from intersections



3D shape reconstruction by solving the simultaneous equations

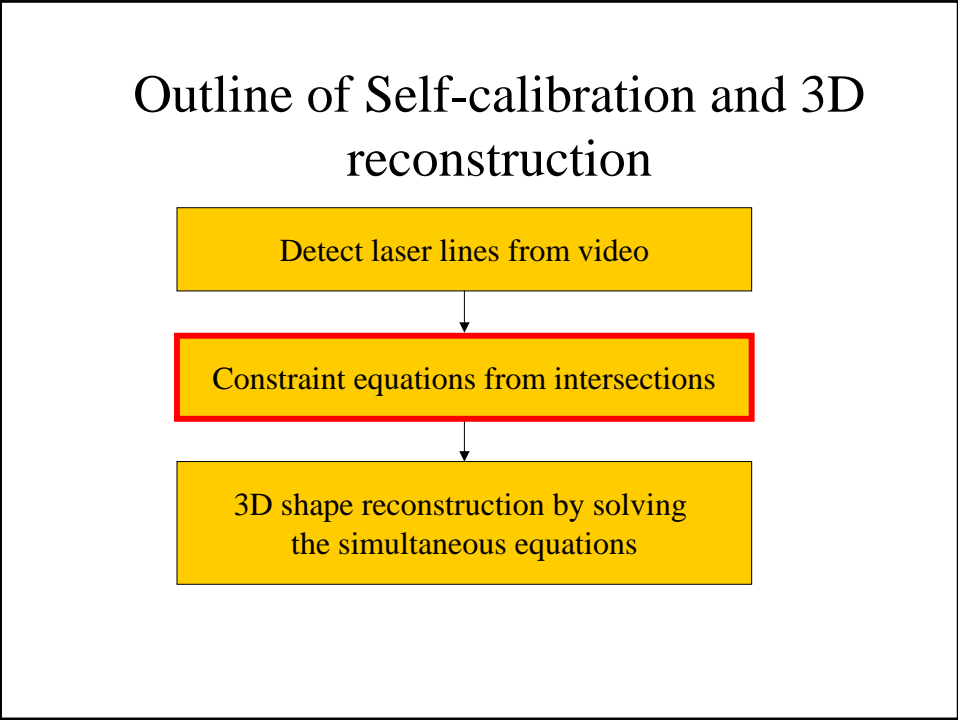

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graph TD; A[Detect laser lines from video] --> B[Constraint equations from intersections]; B --> C[3D shape reconstruction by solving the simultaneous equations];
```

Outline of Self-calibration and 3D reconstruction

Detect laser lines from video

Constraint equations from intersections

3D shape reconstruction by solving the simultaneous equations



Constraints from intersections (coplanar constraint)

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = -z \begin{pmatrix} \alpha u \\ \alpha v \\ -1 \end{pmatrix}$$

$$a_1 x + b_1 y + c_1 z + 1 = 0$$

$$a_2 x + b_2 y + c_2 z + 1 = 0$$

(u, v)

Constraints from intersections (coplanar constraint)

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = -z \begin{pmatrix} \alpha u \\ \alpha v \\ -1 \end{pmatrix}$$

$$a_1 x + b_1 y + c_1 z + 1 = 0$$

$$a_2 x + b_2 y + c_2 z + 1 = 0$$

(u, v)

Constraints from intersections (coplanar constraint)

$$-a_1^*u - b_1^*v + c_1 + t = 0$$

$$-a_2^*u - b_2^*v + c_2 + t = 0$$

$$-a_1^*u + a_2^*u - b_1^*v + b_2^*v + c_1 - c_2 = 0$$

3*2 Unknowns

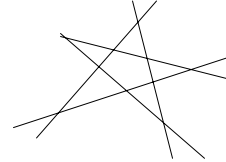
Number of intersections: M

Number of equations: M

Number of planes: N

Number of unknown params: $3N$

5 plains
9 intersections



Usually, Intersection number $M \gg$ plane number $N(\text{unknown})$

Matrix form

$$\begin{pmatrix} u_1 & v_1 & 1 & -u_2 & v_2 & -1 & 0 & 0 & 0 & \vdots \\ u_2 & v_2 & 1 & 0 & 0 & 0 & u_2 & v_2 & -1 & \vdots \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \vdots \end{pmatrix} \begin{pmatrix} a_1 \\ b_1 \\ c_1 \\ a_2 \\ b_2 \\ c_2 \\ a_3 \\ b_3 \\ c_3 \\ \vdots \end{pmatrix} = \mathbf{0}$$

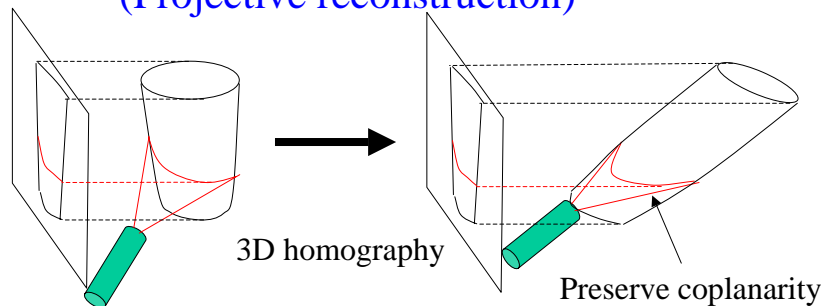
$$\mathbf{L}\mathbf{x} = \mathbf{0}$$

\mathbf{L} : $3N \times M$ matrix (Intersection num M , Plane num N)

Reconstruction from coplanarity

$$\mathbf{L}\mathbf{x} = \mathbf{0}$$

Solution \mathbf{x} has 4 degrees of freedom
(Projective reconstruction)



The 4 DOFs → Found in other research areas.

e.g. Polyhedra analyses in single view reconstruction

Generalized Bas-Relief Ambiguity in photometric stereo

Shape from coplanarity

Sort eigen values after SVD of \mathbf{L}

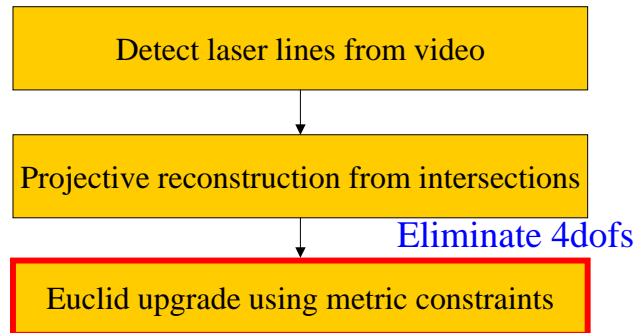
$$\mathbf{U} \begin{pmatrix} \Sigma_1 & 0 \\ 0 & \Sigma_2 \\ 0 & 0 \end{pmatrix} \mathbf{V}^\perp \mathbf{x} = \mathbf{0}$$

$\underbrace{\hspace{1.5cm}}_{3n-4} \quad \underbrace{\hspace{1.5cm}}_{4 \text{ columns}}$

$\Sigma_1 \ \Sigma_2$ Square diagonal matrix

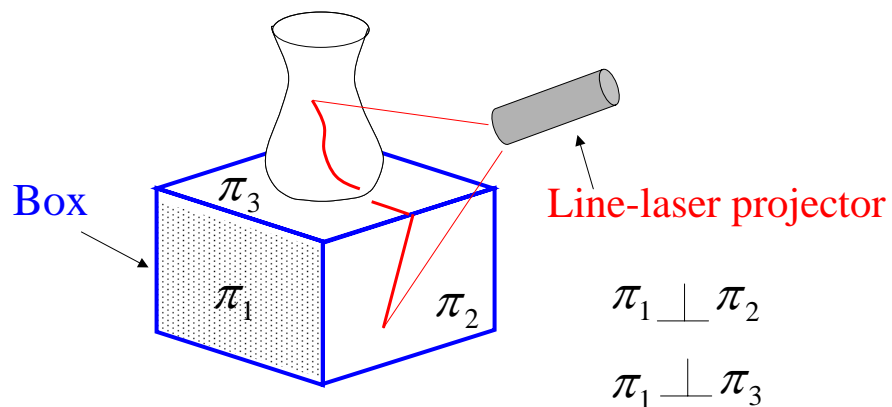
$$\Sigma_2 \approx \mathbf{0} \quad (\text{if no errors})$$

Outline of Self-calibration and 3D reconstruction



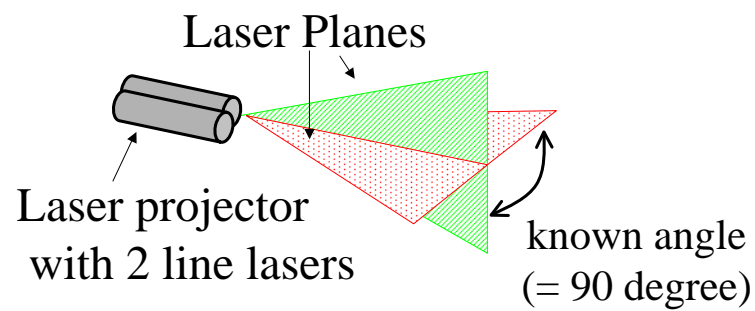
Upgrade to Euclidean solution-1

- Metric constraints from the captured scene



Upgrade to Euclidean solution-2

- Metric constraints from laser planes

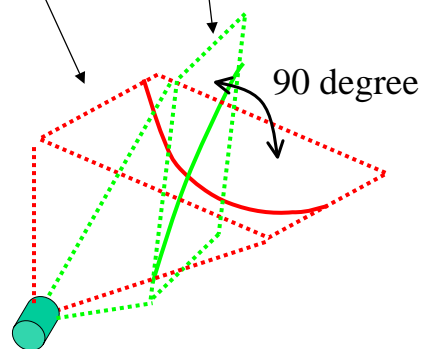


Formulation of metric constraints

Constraints from orthogonality

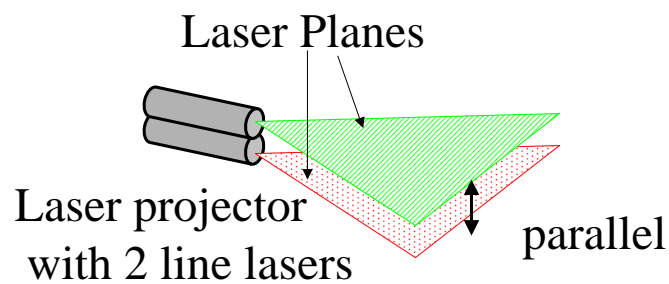
$$ax + by + cz + 1 = 0 \quad dx + ey + fz + 1 = 0$$

$$ad + be + cf = 0$$



Upgrade to Euclidean solution-3

- Another metric constraints from laser planes



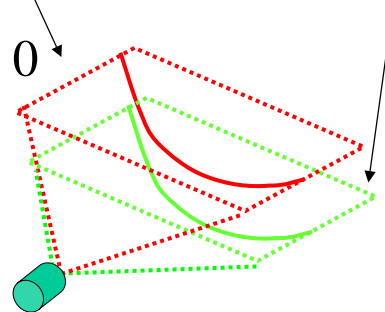
Formulation of metric constraints

Constraints of parallelism

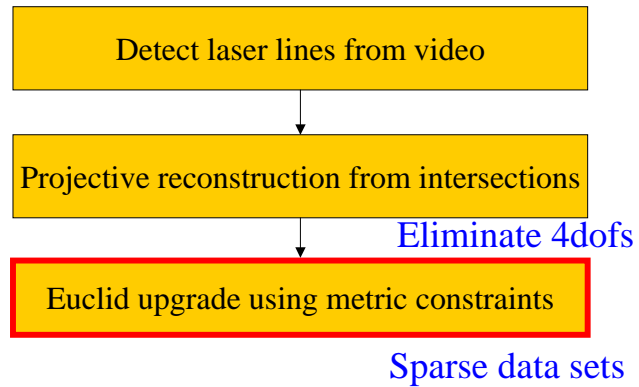
$$ax + by + cz + 1 = 0$$

$$dx + ey + fz + 1 = 0$$

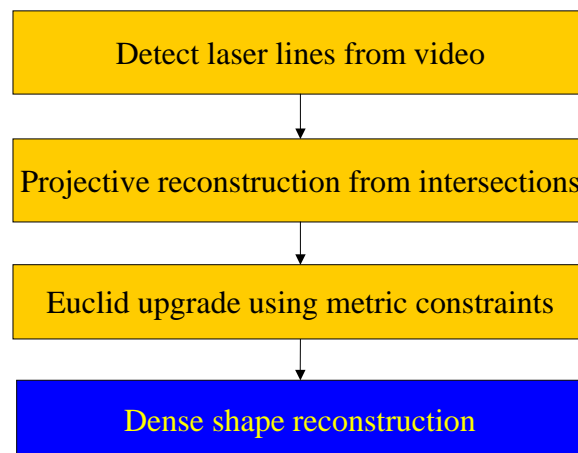
$$(a, b, c) \otimes (d, e, f) = 0$$



Outline of Self-calibration and 3D reconstruction

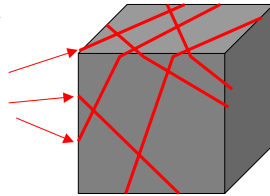


Outline of Self-calibration and 3D reconstruction

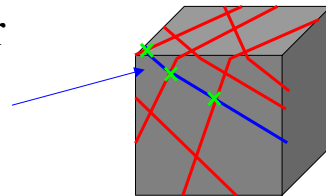


Dense Reconstruction

Small number of
laser planes are
reconstructed.

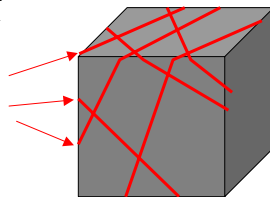


Another laser
plane
estimated by
plane fitting.

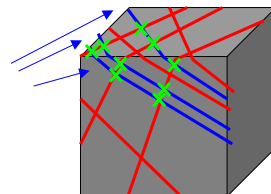


Dense Reconstruction

Small number of
laser planes are
reconstructed.



Iterate same
process for all
laser planes.



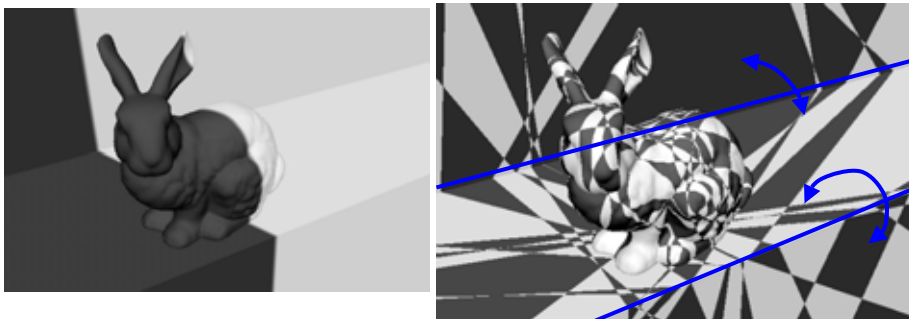
Experiments

- Simulation data
- Real data

Simulation data 1

- Randomly project single line laser

20 lasers and 200 intersections

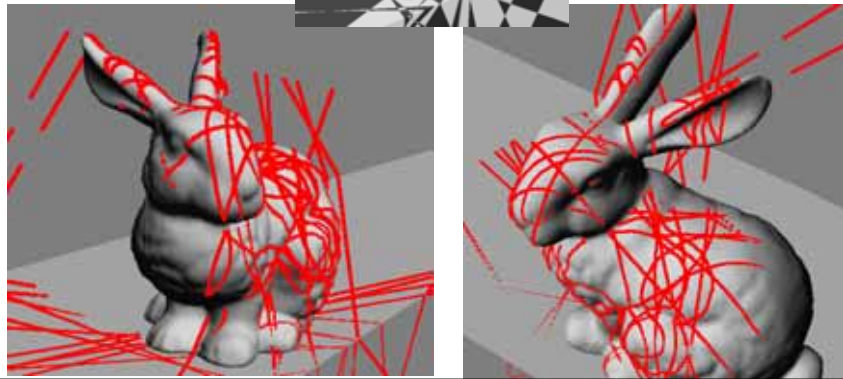


Require 3 metric constraints for Euclidean solution up to scale

Simulation data 1 – result



View 3D data



Simulation data

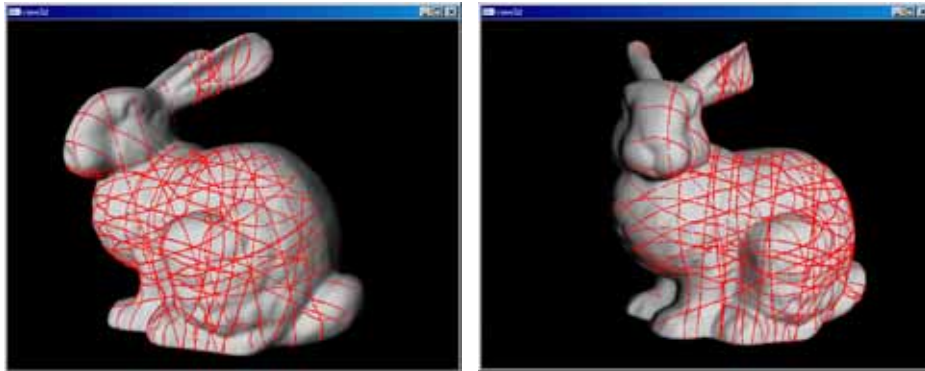
- Randomly project **cross line laser**



Image number:20
Plane number:40
Intersection number:613
Metric constraints:20

Simulation data – result

[View 3D data](#)

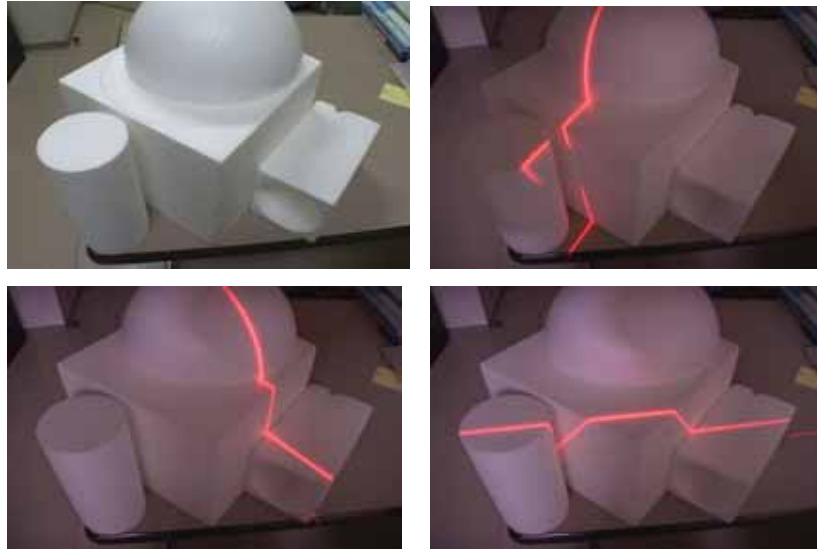


Experiment -- Real data 1

- Single line laser

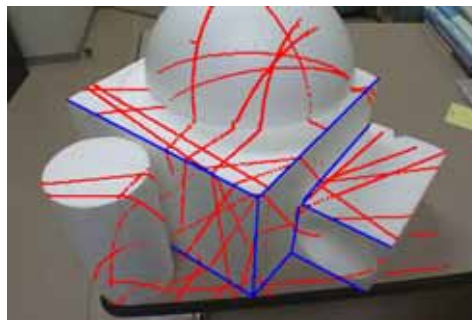


Real data 1

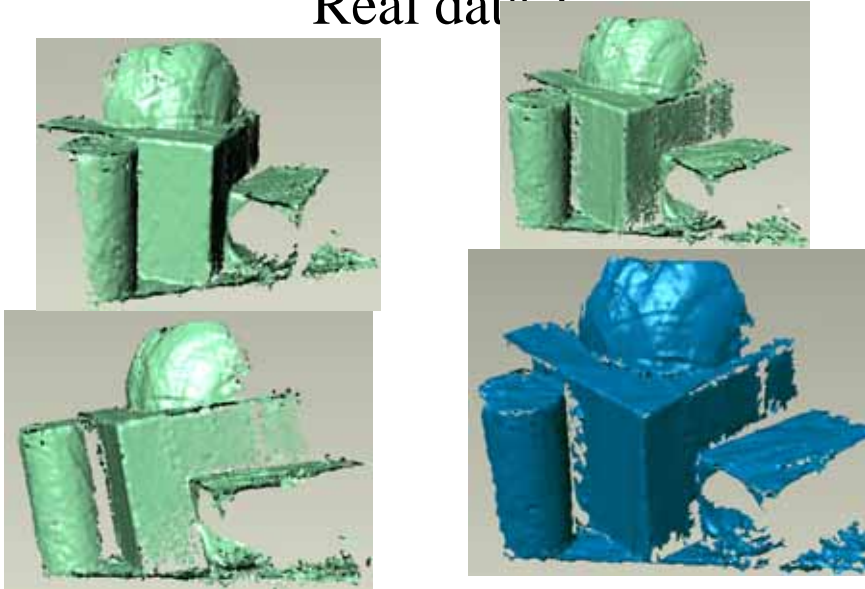


Experiment -- Real data 1

- Red --- detected laser lines
- Blue --- constraints from scene



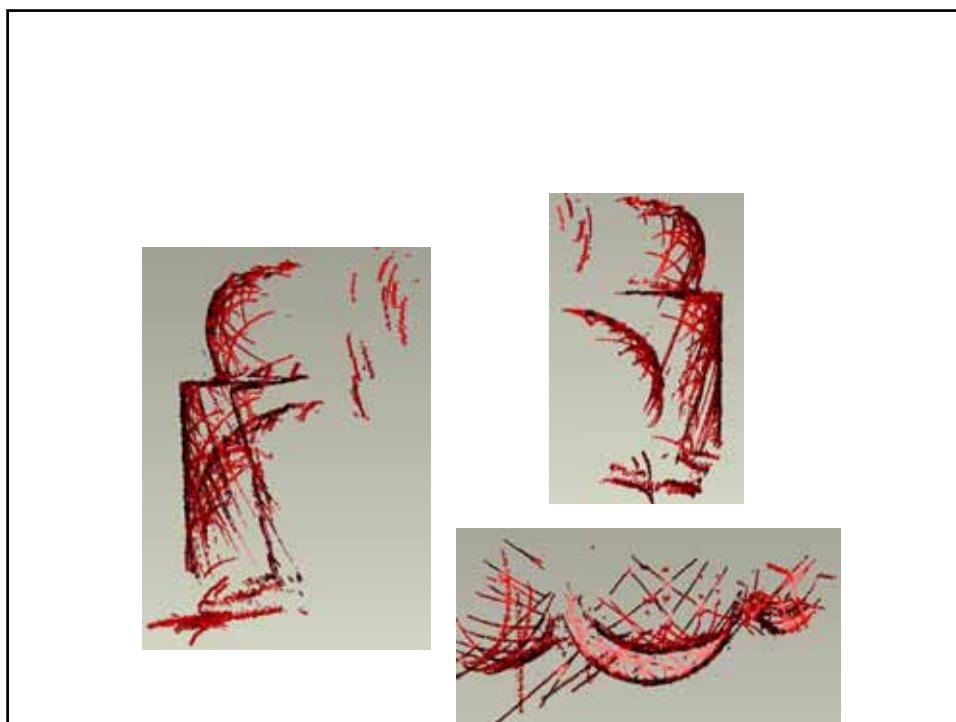
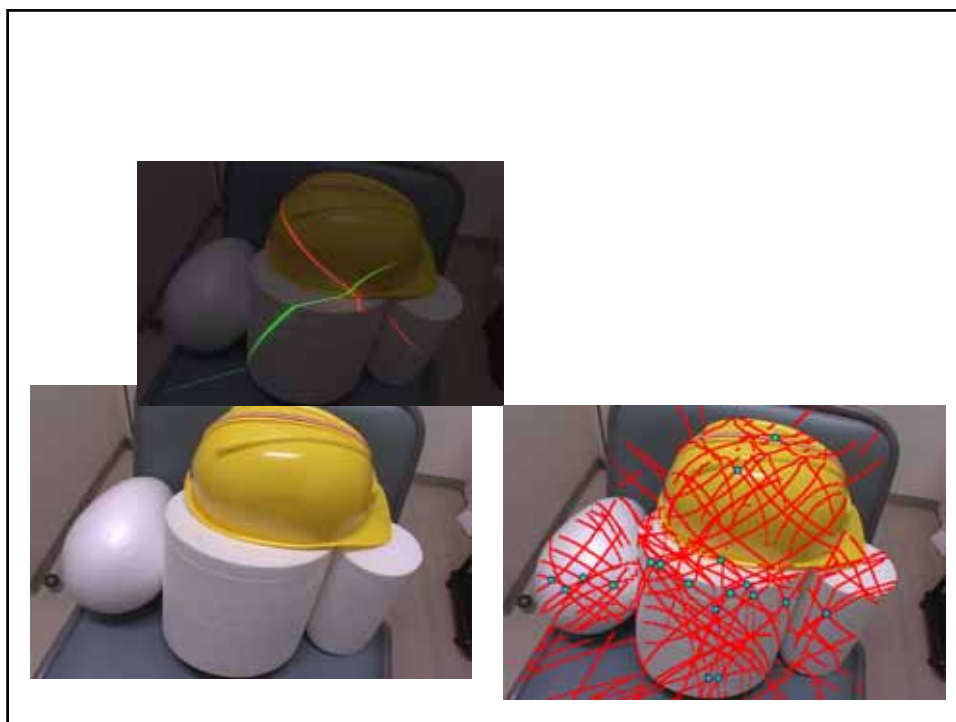
Real data 1

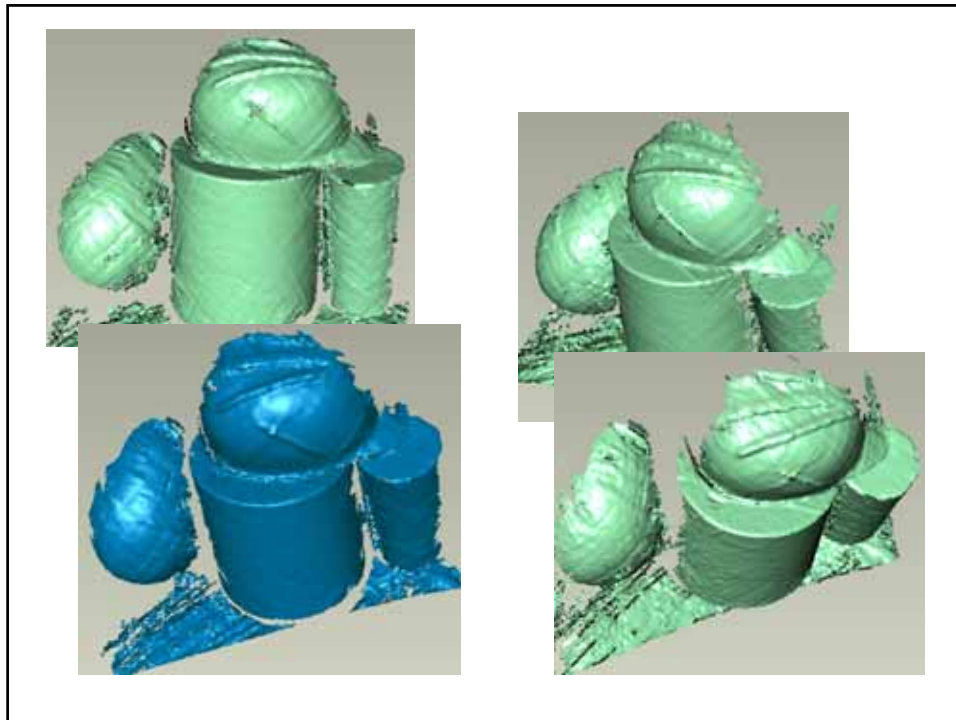


Experiment -- Real data 2

- Cross line laser





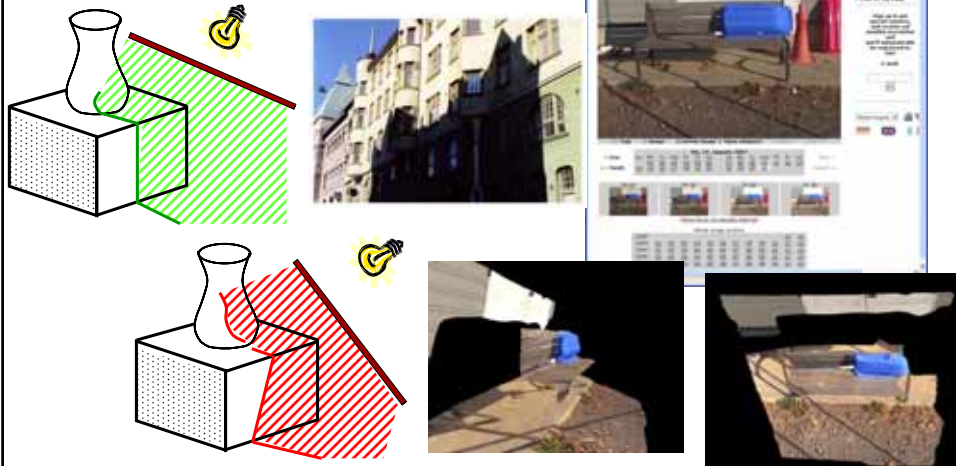


Proposed method

- Only require a line laser and a single camera
 - General solution for “Shape from Coplanarity”
 - Any other applications?

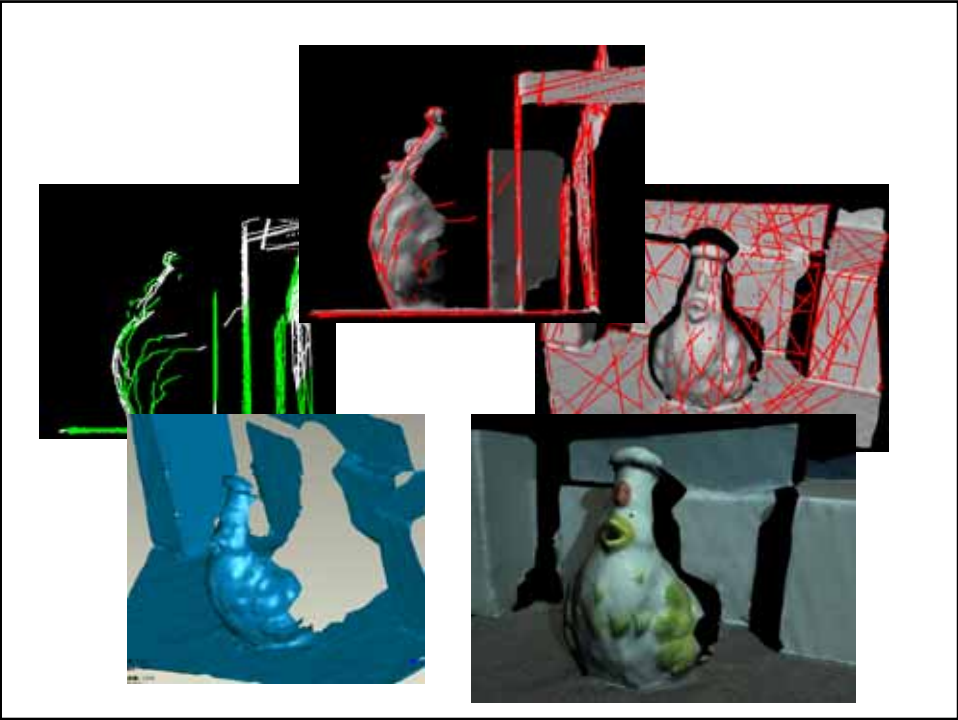
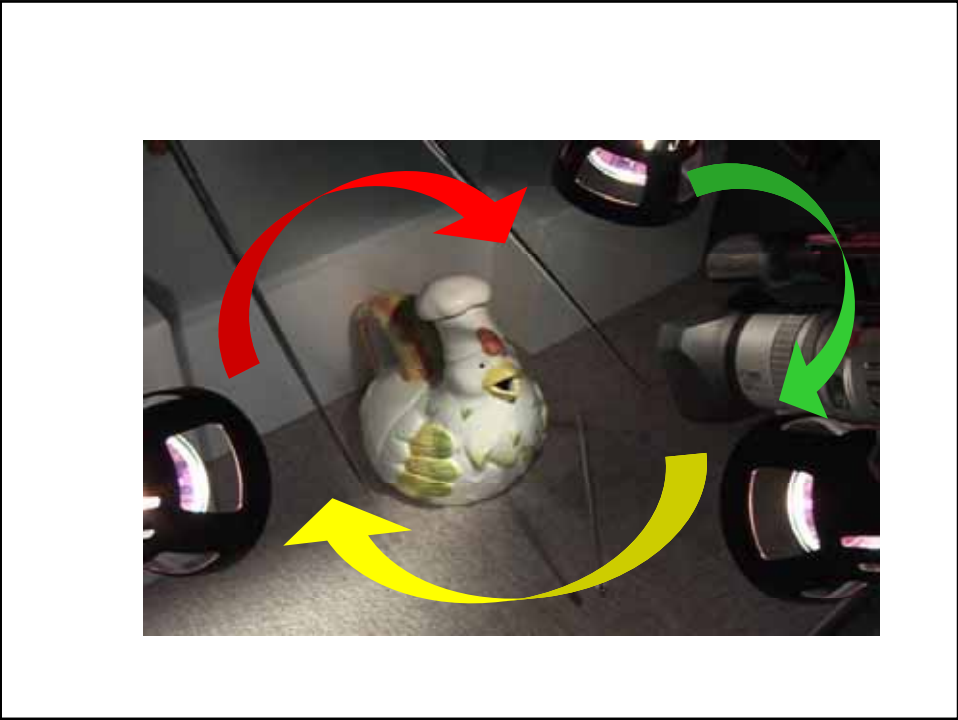
Other applications

- Shape from cast shadow



Shape from cast shadow





Other applications

- Single view reconstruction



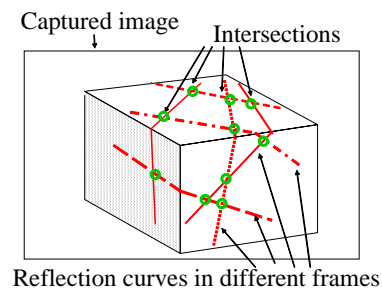
Other applications

- Single view reconstruction



Summary of self-calibration of light sectioning method

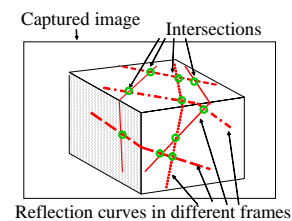
- Temporal accumulation
 - Self-calibration of 3D planes from observed curves
 - Takes long times
 - Need manual steps



→ Can we make enough intersections at one time?

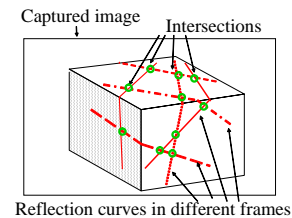
Self-calibration for 3D scanner

- Solution
 - A. Temporal accumulation

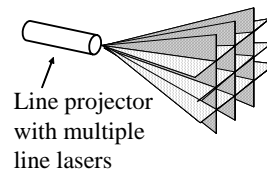


Self-calibration for 3D scanner

- Another solution
 - A. Temporal accumulation

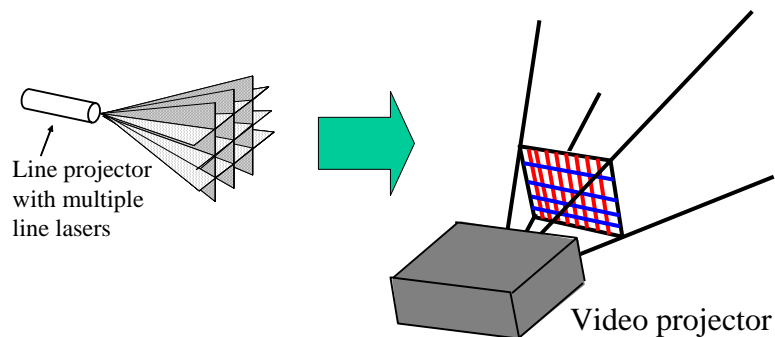


- B. Many laser projectors



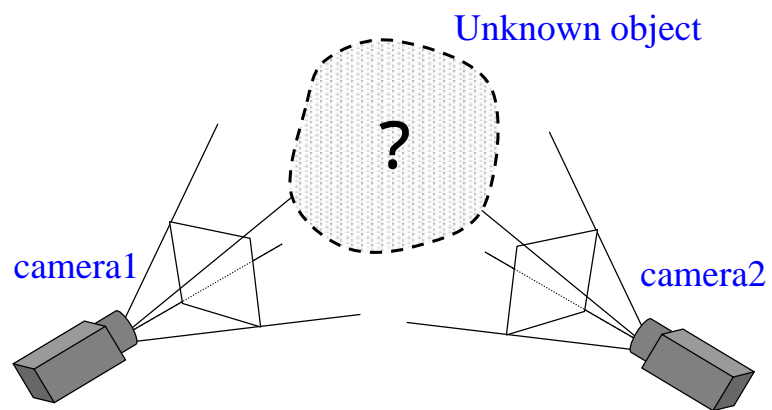
Self-calibration for Coded Structured light

- Use many laser projectors

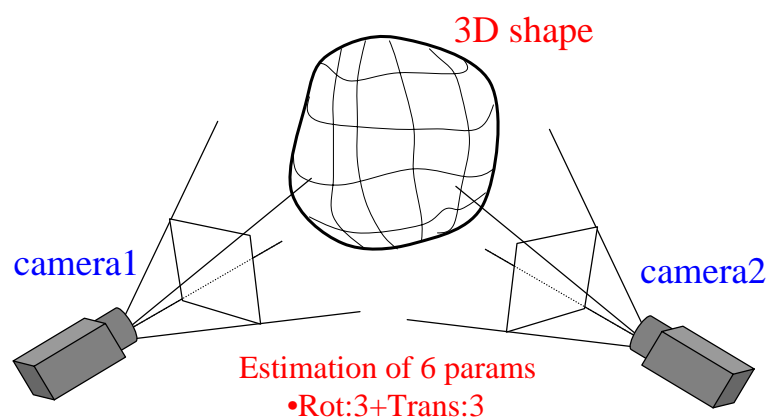


Equivalent: As many lasers as pixel resolution

Self calibration



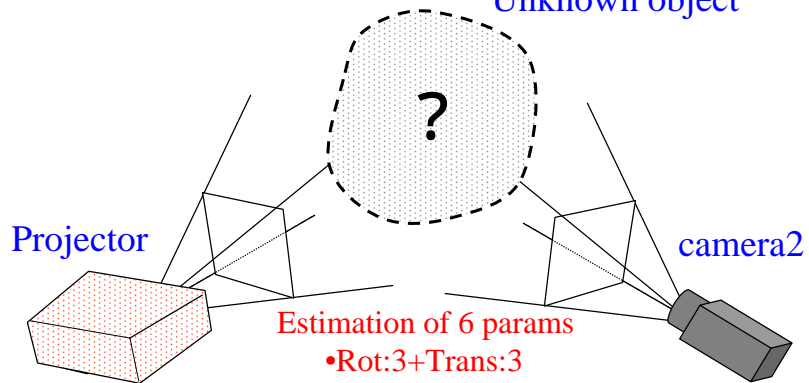
Self calibration



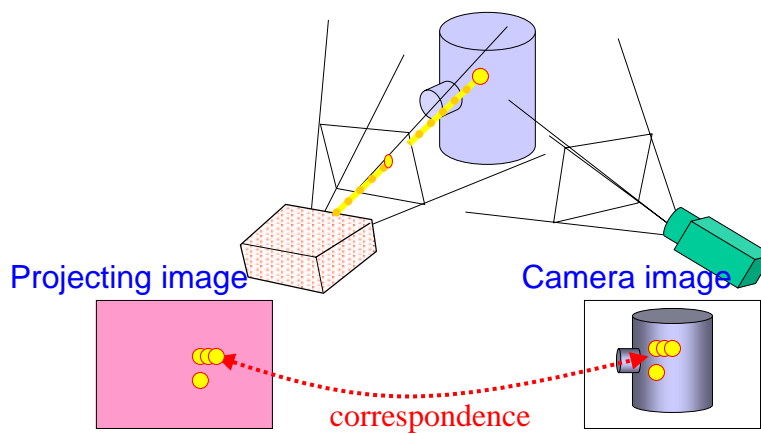
Self calibration of projector camera system

Replace camera to **projector**

Unknown object

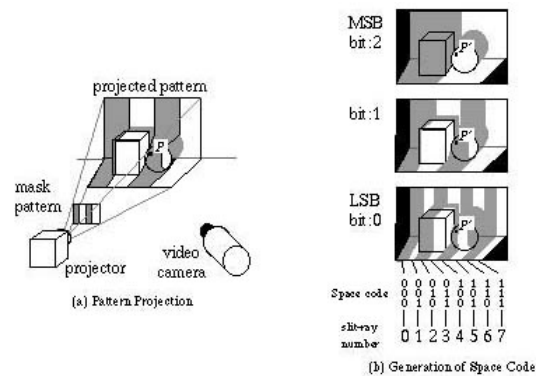


Self calibration of pro-cams



Actual implementation

- Gray code method['86 Inokuchi]

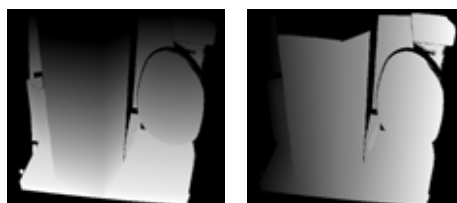


Structured light example

- Projecting patterns → two directions



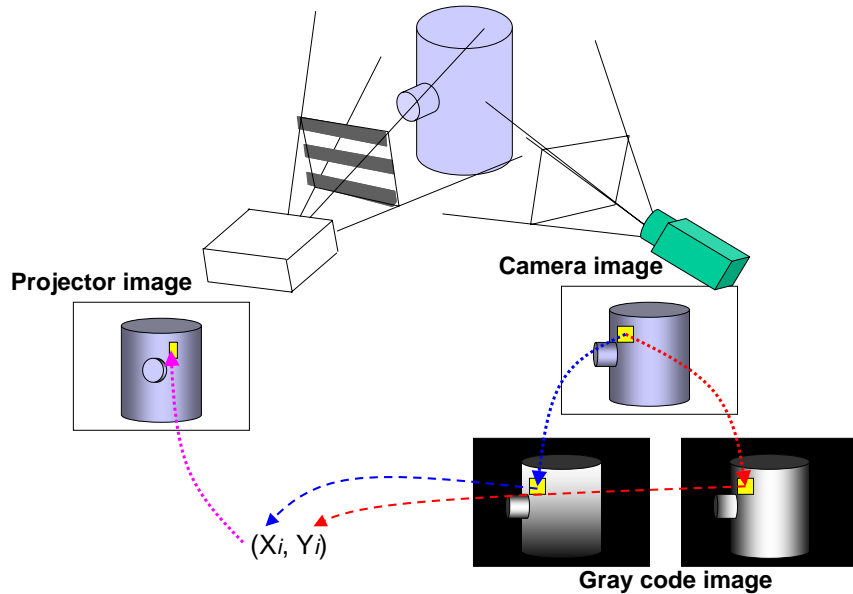
- Acquired coded images



vertical

horizontal

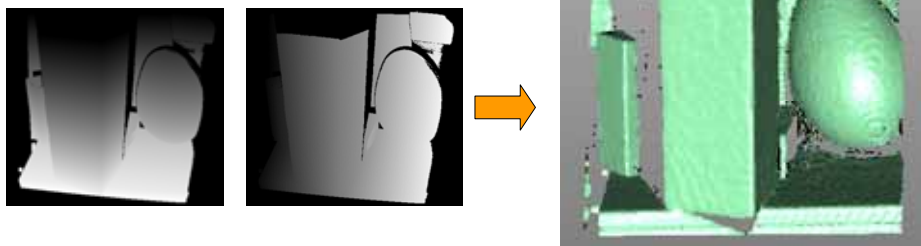
Correspondences from decoded images



Self-calibration for Coded Structured light

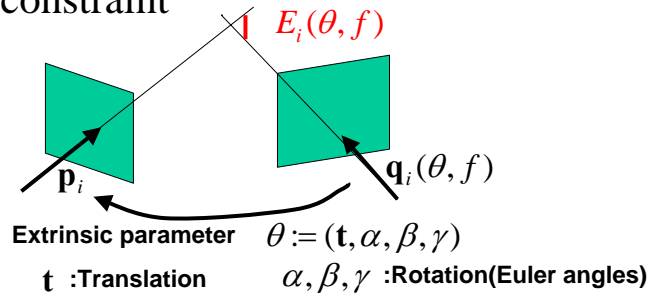
- problem definition -

- Input :- **camera params** (focal length, etc.)
- **two index images**
- Output :- **6 params** (R&T)
- **3D shape**



Non-linear optimization

- Epipolar constraint



$$E_i(\theta, f) := |\mathbf{t} \cdot N(\mathbf{p}_i \times \mathbf{q}_i(\alpha, \beta, \gamma, f))|$$

Using $F(\theta, f) := \sum_i \{E_i(\theta, f)\}^2$ as a minimizing function.
 \rightarrow **Re-projection** error in real algo.

Solving epipolar constraints

- Gauss-Newton method

$$\mathbf{x} := (\theta, f),$$

$$\mathbf{y}(\mathbf{x}) := (\tilde{E}_1(\mathbf{x}), \tilde{E}_2(\mathbf{x}), \dots, \tilde{E}_k(\mathbf{x}))^t$$

$$\text{minimize } \sum_i \{\tilde{E}_i(\theta, f)\}^2 = \|\mathbf{y}(\mathbf{x})\|^2 = \mathbf{y}(\mathbf{x})^t \mathbf{y}(\mathbf{x})$$

$$\mathbf{x}_{k+1} = \mathbf{x}_k + \Delta \mathbf{x}_k,$$

$$\Delta \mathbf{x}_k = - \left\{ \left(\frac{\partial \mathbf{y}(\mathbf{x}_k)}{\partial \mathbf{x}} \right)^t \left(\frac{\partial \mathbf{y}(\mathbf{x}_k)}{\partial \mathbf{x}} \right) \right\}^{-1} \left(\frac{\partial \mathbf{y}(\mathbf{x}_k)}{\partial \mathbf{x}} \right)^t \mathbf{y}(\mathbf{x}_k)$$

Demo

Extended techniques

- Wide range reconstruction by pivot scanning
- Simultaneous reconstruction method

Extended techniques

- Wide range reconstruction by pivot scanning
- Simultaneous reconstruction method

Wide view scanning

Pivot scanning (use multiple scenes)

1. Initial 3D reconstruction



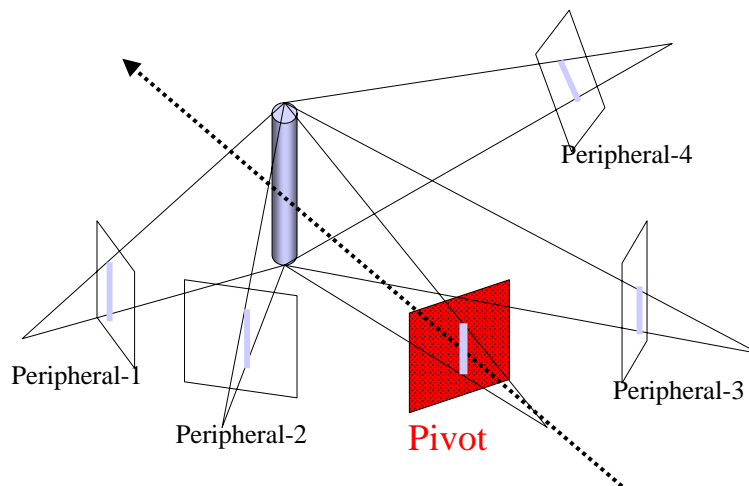
2. Move camera (or projector) freely



3. Apply bundle adjustment

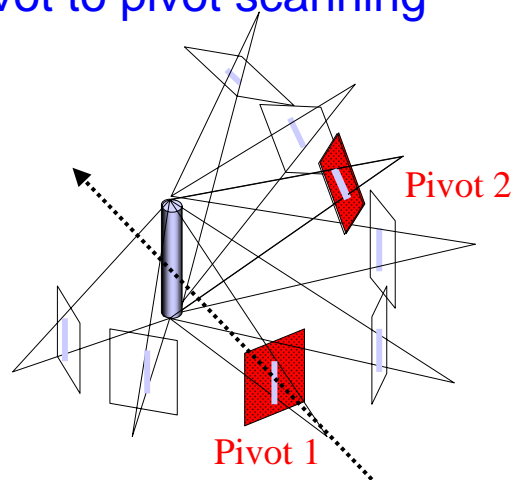
Pivot scanning

Fix **pivot** device and move **peripheral** device arbitrarily



More wide view scanning

Pivot to pivot scanning



Bundle adjustment for pivot scanning

- Configuration of single camera-projector pair
 - Only epipolar constraints are available
 - Can be unstable if the projections of the camera and the projector are nearly orthogonal
- Configuration of pivot scanning
 - Constraints between multiple views can be used

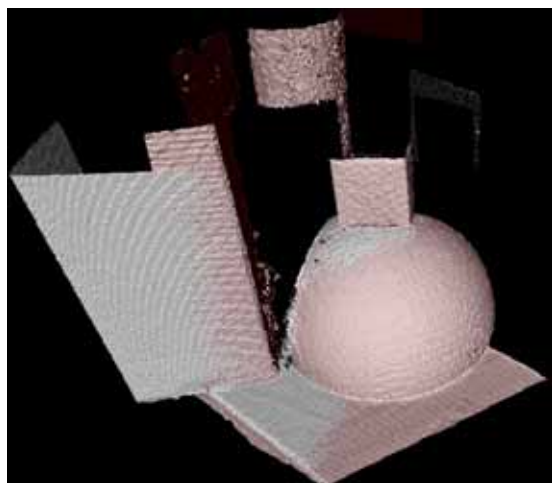
Dense correspondences



**Simple algorithm to enforce multi-view constraints
to correct errors of self-calibration**

Result – pivot to pivot

- No alignment algorithm applied



1+2 result

Demo movie

- Pivot scan



Extended techniques

- Wide range reconstruction by pivot scanning
- Simultaneous reconstruction method

Simultaneous reconstruction

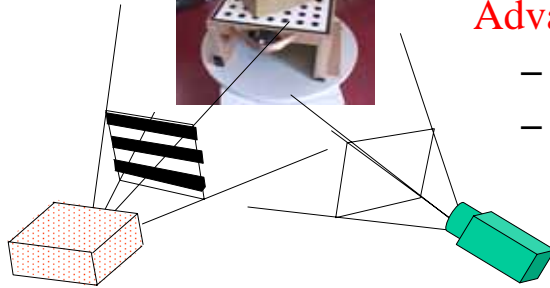
- Capture multiple scenes
- 3D reconstruction simultaneously



Multiple depths for single pixel

Advantage

- Consistent scaling
- Improving result
 - Redundant input



Demo movie

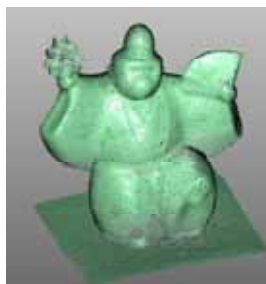
- Simultaneous scan



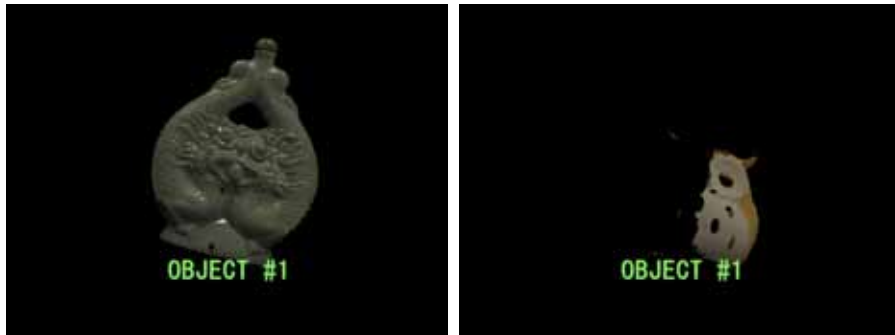
Results (1)



Results (2)



Final results



- With
- Fast mesh integration [Furukawa and Kawasaki 3DIM '05]
 - seamless texture [Inose, kawasaki *et.al.* '06 '07]

Conclusion

- Introduction of structured light system
- Explain calibration problem
- Self calibration techniques for
 - Light sectioning method
 - Projector camera system

Discussion

- Calibration of **light sectioning method** and **procam system** is different
- Once correspondences are obtained, self-calibration is possible
 - **Correspondence** is an essential problem

In the next tutorial (part II)...

- Explain about correspondence problem
- Scanning techniques for moving object

Thanks

- Any question?