

Section 8: Semiconductors and Quantum Information

Monday, November 29, 2021 10:07 PM

(I) Why Quantum?

a) Solve problems that are hard for classical computers:

- Search large databases (Grover's Algorithm)
- Factor primes and break RSA (Shor's Algorithm)
- Quantum simulation: you need a quantum system to simulate a quantum system
↑
best

b) Secure Communications and networks

- Quantum Key Distribution: measurement disturbs the system, so you can easily detect eavesdroppers
- Quantum networks: interface many quantum computers to share entanglement as resource for computing, distributed precision sensors

c) Interesting science + engineering

- Need to make fantastic classical devices along the way → will help existing applications

- Plus, interesting phenomena inherent

(II) Qubits

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a) Analogy

Consider a spinning coin:



Is it in heads? tails?

In some sense, it is both at the same time.

But when you measure it by slapping the coin down on the table, you only ever get one result — heads or tails.

Let's say you measure heads. Does that actually mean it was in heads the whole time? No.

In quantum mechanics, it truly is both states at once — it is in a superposition.

You might describe the state as

$$\Psi = \frac{1}{\sqrt{2}} \Psi_{\text{heads}} + \frac{1}{\sqrt{2}} \Psi_{\text{tails}}$$

Moreover, the act of measurement illustrates another phenomenon — measurement collapse.

You measure out some observable, and you can only get certain values out. After measuring, the quantum state is fundamentally

measuring, the quantum state is fundamentally altered — it collapses to the state which corresponds to the value of the observable you just measured.

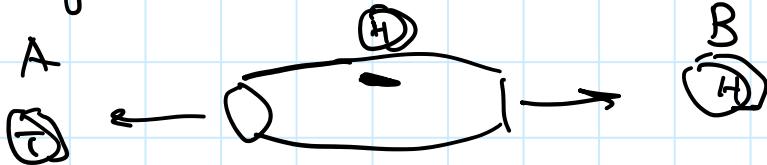
$$\psi^{\text{out}} = \psi_{\text{heads}} \quad (\text{if you measured heads})$$

We could have also called the states "0" and "1", in analogy to a classical bit. This forms the basic unit of quantum information — a quantum bit or "qubit", can be realized by a quantum system that can take on two states, ψ_0 or ψ_1 , or any superposition thereof.

$$\psi = c_0 \psi_0 + c_1 \psi_1$$

Let's stretch the analogy a little bit more.

Suppose you have a magical canon that splits a coin in two, and ejects the two halves across the room.



You don't know what the result on any individual side will be — but you do know that the results are correlated. If side A measures tails, you know

If side A measures tails, you know
side B has heads & if A measures heads,
B has tails.

Is the state just a superposition like
before then? Not exactly. You could
have the result

$$\psi_0^A \psi_1^B$$

but also get

$$\psi_1^A \psi_0^B$$

So you have a superposition of two coin
states,

$$\psi = \frac{1}{\sqrt{2}} \psi_0^A \psi_1^B + \frac{1}{\sqrt{2}} \psi_1^A \psi_0^B$$

We can't describe each coin individually
— we have to describe both at the same
time. This is entanglement.

It turns out that superposition and entanglement
are some of the most fundamental quantum
resources that enable quantum computing
and quantum information to tackle problems
that would be otherwise impossible for
classical computers.

6) Math

A qubit is a two-level quantum system,

A qubit is a two-level quantum system, described by two orthogonal basis states.

$$"1" \longrightarrow \psi_1 \rightarrow |1\rangle$$

$$"0" \longrightarrow \psi_0 \rightarrow |0\rangle$$

Earlier we called these basis states ψ_0 and ψ_1 . By convention, we will now refer to them as $|0\rangle$ and $|1\rangle$ (Dirac notation).

The qubit is generally described by a superposition (linear combination) of these basis states:

$$|\psi\rangle = c_0|0\rangle + c_1|1\rangle$$

And entanglement is when a many-body state cannot be factored into individual single-qubit states.

$$|\psi\rangle = \frac{1}{\sqrt{2}} (|00\rangle + |01\rangle)$$

$$= \frac{1}{\sqrt{2}} |0\rangle (|0\rangle + |1\rangle) \quad \text{Not entangled!}$$

$$|\psi\rangle = \frac{1}{\sqrt{2}} (|00\rangle + |11\rangle) \quad \text{entangled!}$$

In other words, qubits are vectors in the vector subspace \mathbb{C}^2 such that the length is 1. ($|c_0|^2 + |c_1|^2 = 1$)

c) Manipulating Qubits

Classical logic: AND, NOR, NOT ...

Can think similarly for qubits — develop quantum logic gates.

Single qubit operations should be able to transform one qubit state to another valid qubit state. This means it preserves length, aka a rotation!

Thus, single qubit rotations can be described by 2×2 unitary matrices.

Ex: NOT = X gate

$$X = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

Other things: multi-qubit gates, memory, measurement...

(II) What do you need to make a quantum computer?

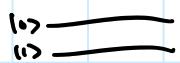
a) Di Vincenzo's Criteria

1. Scalable physical system w/ well characterized qubit
2. Ability to initialize qubit state
 - ↳ i.e. set all qubits to $|0\rangle|0\rangle|0\rangle\dots$
3. Long decoherence times
 - ↳ Roughly, usable time before system is no longer usable
4. "Universal" set of quantum gates
 - ↳ to a theorist, usually means something like "CNOT gate set"
 - ↳ to an experimentalist, usually means something like arbitrary single qubit rotations and a two-qubit entangling gate

5. Measurement

b) Example systems

- Photons

- ↳ polarization \longleftrightarrow 
- ↳ path 
- ↳ time bin 
- ↳ frequency bin 

- Electrons

- ↳ spin 
- ↳ charge 

- Atom
 - ↳ excited state vs ground state
- $1s$
— $1g$

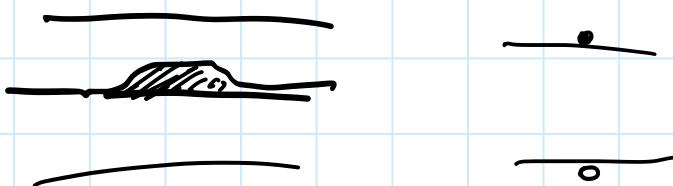
(III) What role can semiconductors play?

Why semiconductors?

- ↳ Primarily a scalability argument
- ↳ General approach: use "artificial atoms" in the solid-state

a) Quantum Dots

Essentially, as close to particle in a (3D)
box we can get:



$$H = H_e + H_h + H_c$$

↑ ↑ ↑
 electron hole Coulomb

$$H_e = -\frac{\hbar^2}{2m_e} \nabla^2 + V_e(\vec{r})$$

$$H_h = -\frac{\hbar^2}{2m_h} \nabla^2 + V_h(\vec{r})$$

$$H_c = -\frac{e^2}{4\pi\epsilon} \frac{1}{|r_e - r_h|}$$

To first order ignore Coulomb potential.

Potential modeled as:

$$V(x, y, z) = \left(\frac{1}{2} m_{eff} \omega_0^2 (x^2 + y^2) \right) z \leq L$$

$$\psi(x, y, z) = \begin{cases} \frac{1}{2} m_{\text{eff}} \omega_0^2 (x^2 + y^2) & z \leq L \\ 0 & z > L \end{cases}$$

(Infinite well in z -direction, locally)
Harmonic in xy

$$\Rightarrow E_{e/h} = (n_x + n_y + 1) \hbar \omega_0 + \frac{1}{2m_{\text{eff}}} \left(\frac{\pi b n_z}{L} \right)^2$$

Use as:

- Single photon source

↳ highest "purities" in solid state

("single-photon ness", > 99% in GaAs)

↳ many of the first impressive displays
of quantum protocols with optics,
cavity QED, etc.

↳ Challenge: no two QDs exactly the
same, controllable fabrication \rightarrow
nontrivial

- Spin/electron qubit

↳ e.g., work by Anne Fahey

b) Defects ("Color centers")

- Missing or replaced atoms in crystal

↳ Diamond ($\text{NV}, \text{SiV}, \text{GeV}, \text{S}_2\text{V}$)

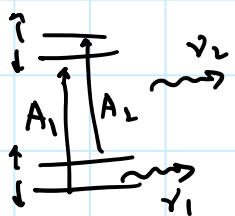
↳ SiC ($\text{V}_{\text{Si}}, \text{VV}_{\text{Si}}, \text{N}_{\text{C}}\text{V}_{\text{Si}}$)

$\hookrightarrow \text{SiC} \quad (\text{V}_{\text{S}\ddot{\text{O}}}, \text{V}_{\text{c}\text{V}_{\text{S}\ddot{\text{O}}}}, \text{N}_{\text{c}}\text{V}_{\text{S}\ddot{\text{O}}})$
 $\hookrightarrow \text{Si} \quad (\text{P donors, T centers})$

- "Color" \rightarrow luminescent

Most studied defects don't just fluoresce,
but also have spin (magnetic) properties

Simplified picture:



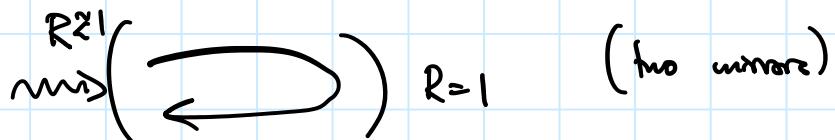
\Rightarrow use Spin as qubit, and interface
interface with photons (map qubit
from spin to photon) to send for
distances for communications

\Rightarrow use as memories (can interface with
long-lived nuclear spins)

- Challenges: relatively dim, controllable creation, local environmental inhomogeneities

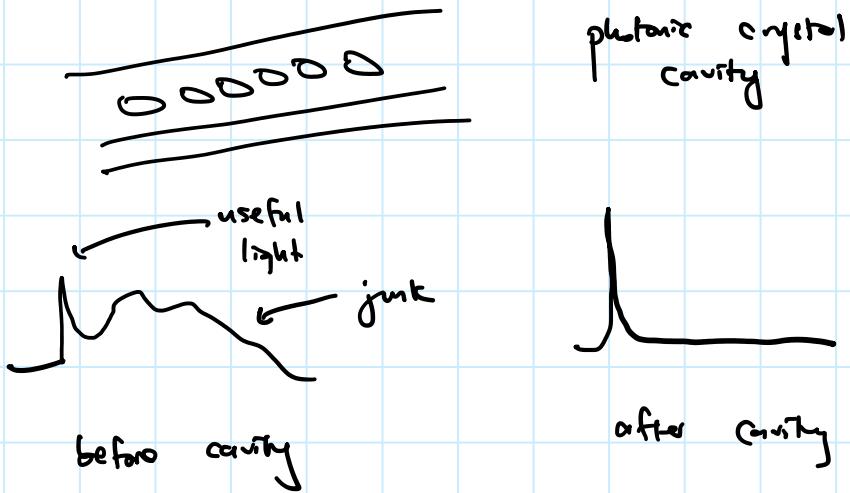
c) Nonfabricated devices

- Cavities



Light circulates in cavity many times,
enhances light-matter interaction (more chances
to hit atom/atom-like system).

Especially enhanced if electric field mostly
in small volume \Rightarrow nanofabrication!



Put in cold center, quantum dot ... or
even other platforms!

Heterogeneous integration with atoms, exotic emitters

(e.g. Er : Y₂O₃) ... take advantage of
mature and scalable fab!

- Other material "kubos"?
 - mechanical strain / acoustics
 - electric field (Stark tuning)
 - electrically -driven single photons?
(usually, optically driven)
 - chemical functionalization?
 - And much more!