

A function  $f(x, y)$  is said to have a removable discontinuity at  $(x_0, y_0)$  if

$\lim_{(x,y) \rightarrow (x_0,y_0)} f(x, y)$  exists but  $f$  is not continuous at  $(x_0, y_0)$ , either because  $f$  is not defined at  $(x_0, y_0)$  or because  $f(x_0, y_0)$  differs from the value of the limit.

1. Determine whether  $f(x, y)$  has a removable discontinuity at  $(0, 0)$ .

$$f(x, y) = \frac{x^2}{x^2 + y^2}$$

$$f(x, y) = \begin{cases} x^2 + 7y^2, & \text{if } (x, y) \neq (0, 0) \\ -4, & \text{if } (x, y) = (0, 0) \end{cases}$$

2.

Find  $\nabla \cdot (\nabla \times \mathbf{F})$ .

$$\mathbf{F}(x, y, z) = e^{xz}\mathbf{i} + 3xe^y\mathbf{j} - e^{yz}\mathbf{k}$$

3. Find  $\nabla \times (\nabla \times \mathbf{F})$ .

$$\mathbf{F}(x, y, z) = xy\mathbf{j} + xyz\mathbf{k}$$