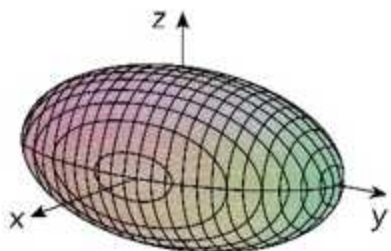


Ellipsoid

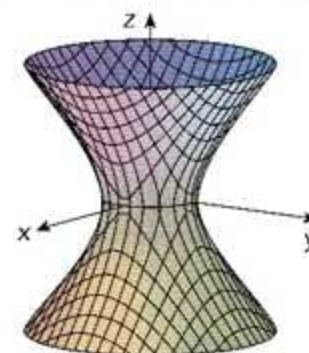


$$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$

"A bunch of ellipses stacked together"

Special case: If $a = b = c$, we have a sphere

Hyperboloid of One Sheet



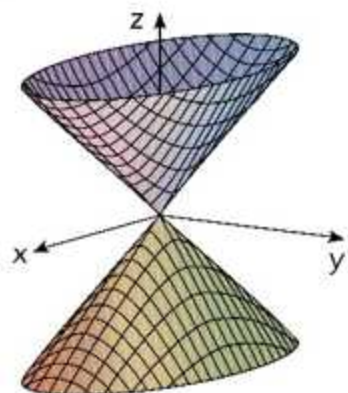
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 1$$

In the xy plane, the traces are ellipses.

In the xz or yz planes, the traces are hyperbolas.

*Whichever variable is negative corresponds to the axis of symmetry

Cone

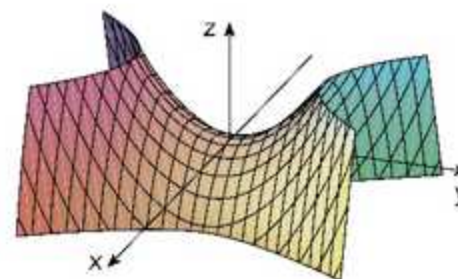


$$\frac{z^2}{c^2} = \frac{x^2}{a^2} + \frac{y^2}{b^2}$$

In the xy plane, the traces are ellipses.

In the xz or yz planes, the traces are hyperbolas, except when $x = 0$ or $y = 0$, then the traces are pairs of lines

Hyperbolic Paraboloid

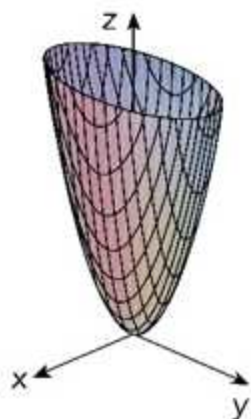


$$\frac{z}{c} = \frac{x^2}{a^2} - \frac{y^2}{b^2}$$

In the xy plane, the traces are hyperbolas.

In the xz or yz plane, the traces are parabolas.

Elliptic Paraboloid

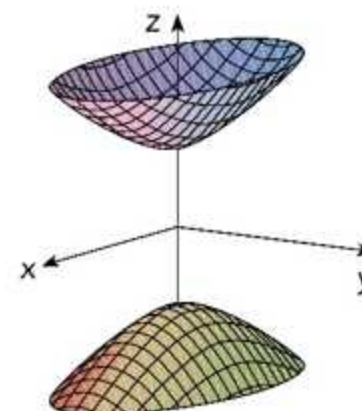


$$\frac{z}{c} = \frac{x^2}{a^2} + \frac{y^2}{b^2}$$

In the xy plane, the traces are ellipses.

In the xz or yz planes, the traces are parabolas.

Hyperboloid of Two Sheets



$$-\frac{x^2}{a^2} - \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$

In the xy plane, the traces are ellipses if $z > c$ or $z < -c$

In the xz or yz planes, the traces are hyperbolas.