

- Instructions:**
1. This is a CLOSED TEXTBOOK and OPEN CLASS NOTES examination.
  2. Attempt all **4 problems**. Each part, e.g. (a), (b), (c), carries the same weight.
  3. Derive/Prove each answer or give reference to a fact covered in class/textbook.
  4. Only faculty calculators are allowed.
  5. Write your answers on both sides of this exam paper.

**Problem 1: Image Processing Elements**

Assume you are given an grey scale intensity image  $I(x,y)$  that is 1000 by 1000 pixels in size and uses standard 8-bits per pixel representation (e.g., a larger image of Lena used in Lab 3).

- (a) First explain how a digital camera works to capture and store such an image using charged coupled devices.
- (b) Consequently, explain how a night vision camera (discussed in class) can make a low intensity image acquired at night to be visible on a display screen. Use your own words and system diagram to explain signal processing involved.
- (c) Finally, you know that the face in the given image is located in a rectangular area for  $x=600, 601, \dots, 800$  and  $y= 500, 501, \dots, 699, 700$ . Write a short MATLAB script which will make the person's face un-recognizable in this provided picture. Comment/explain how and why your Matlab script works. (**HINT:** Use either sub-sampling of the face region or excessive quantization.)

## Problem 2: Signal Processing for Wireless Communication

(a) Consider a  $(16, 5, 8)$  binary linear Reed-Muller code used by NASA for transmission of data from their early Mars probes. Given its generator matrix

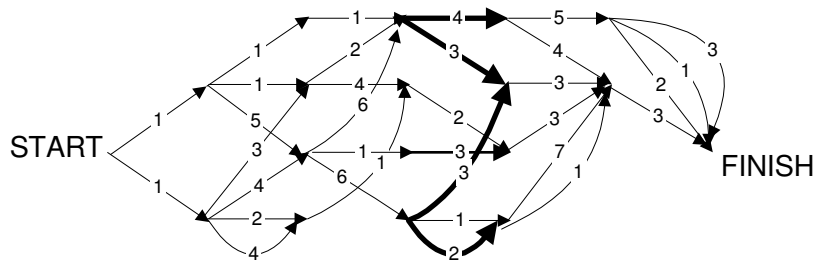
$$\mathbf{G} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 1 & 1 \end{pmatrix}.$$

Decode all erasures in the following received codeword that contains erasures:

(1 1 1 E<sub>1</sub> E<sub>2</sub> 1 0 E<sub>3</sub> E<sub>4</sub> E<sub>5</sub> E<sub>6</sub> 0 0 1 1 E<sub>7</sub>)

(Hint: Note the symmetry of the parity checks 1, 2, ..., 9 for this code.)

(b) Use the Viterbi algorithm to find first the shortest path and then also the longest path from *Start to Finish* in the decoding trellis below. (The edge labels correspond to distances in your decoding metric). Document each step of your add-compare-store process, i.e., your survivor paths, their ‘growth’ and elimination, etc.



**Problem 3: Digital Signal Processing**

Consider a discrete-time echo system that has an impulse response  $h[0] = 0.5$ ,  $h[1] = -1$  and  $h[2] = 0.5$ , while  $h[n] = 0$  for all other values of  $n$ .

- (a) Sketch a finite shift register structure of this system and write down the input-output equation between input signal  $x[n]$  and output signal  $y[n]$ .
- (b) Describe a linear, time-invariant inverse system that recovers  $x[n]$  from  $y[n]$  (i.e., eliminates the echo) and sketch its block diagram.
- (c) Determine if the systems in parts (a) and (b) are each causal and/or BIBO stable. Fully justify your reasoning.

#### Problem 4: FPGA Hardware for Signal Processing

Given the following structure AND assuming the design compiles, determine the output sequence when the input sequence is [00101100].

**EXTRA CREDIT:** Will this design actually compile? Why or Why not? State your reasoning.

