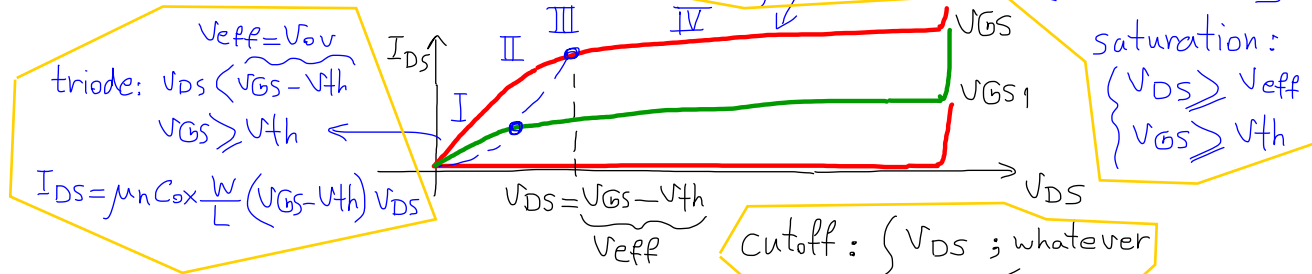


* Mosfet current equations:

$$I_{DS} = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_{th}) V_{DS} - \frac{V_{DS}^2}{2} \right]; \text{ region II}$$

$$I_{DS} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th})^2; \text{ region III}$$

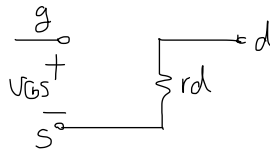
$$I_{DS} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th})^2 \left[1 + \lambda (V_{DS} - V_{eff}) \right]$$



* effective/overdrive voltage is the minimum voltage applied to drain/source junctions of the transistor to ensure it is operating in the saturation or active operating point

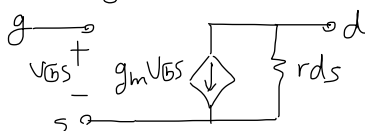
* $V_{eff} \uparrow \Rightarrow$ transistor becomes more linear, signal swing decreases

* region I:



$$r_{DS} = \frac{V_{DS}}{I_{DS}} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th})}$$

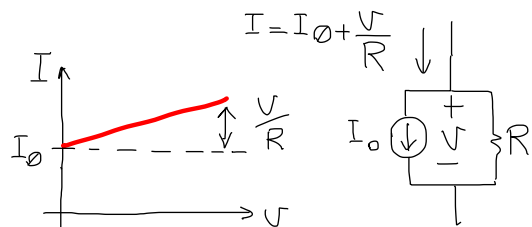
* region IV:



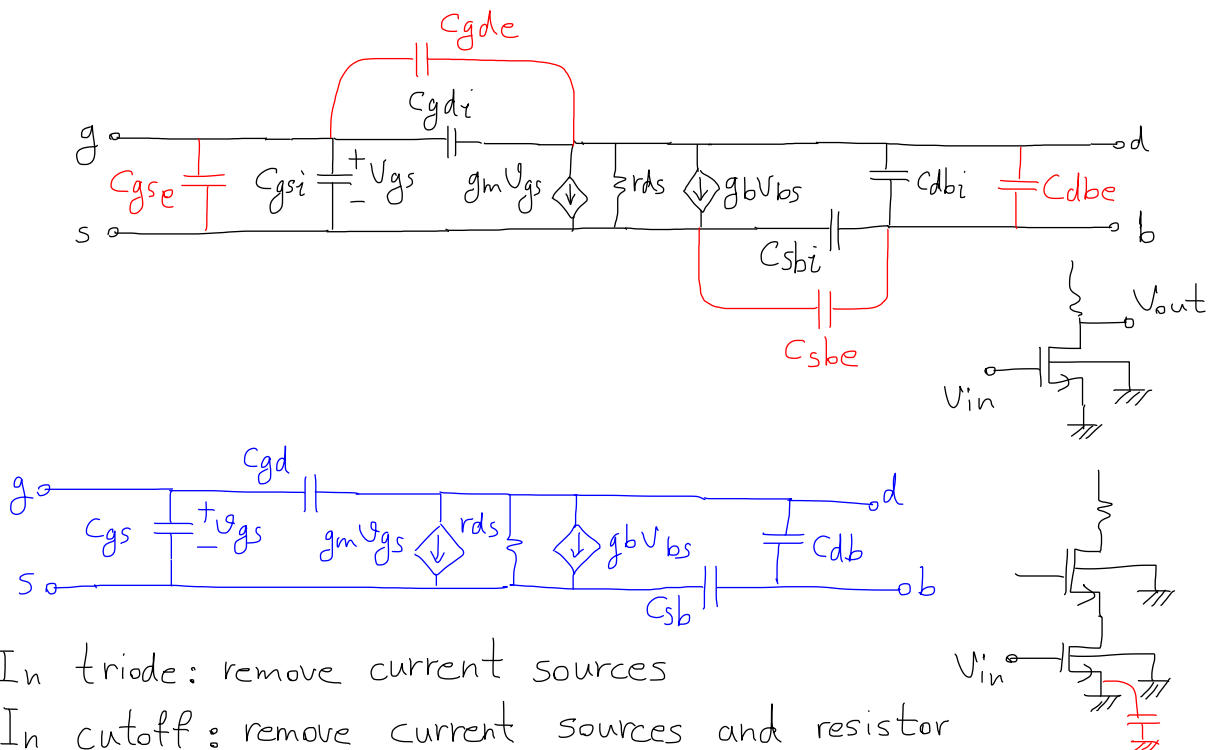
$$\text{transconductance gain} = \frac{I_{out}}{V_{in}}, \lambda \approx 0$$

$$g_m = \frac{\partial I_{DS}}{\partial V_{GS}} = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th})$$

$$r_{DS} = \frac{1}{\frac{\partial I_{DS}}{\partial V_{DS}}} \approx \frac{1}{\lambda I_{DS}}; \lambda [V^{-1}] \text{ Early voltage}$$



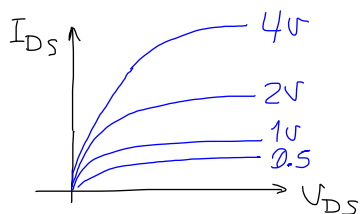
* High Frequency Model of Mosfets in saturation/active :



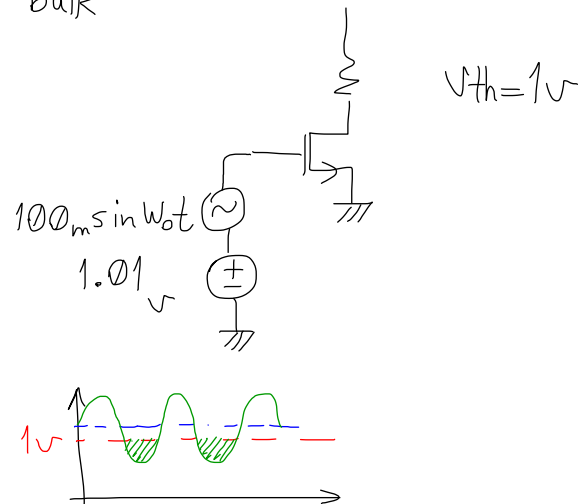
* In triode: remove current sources

* In cutoff: remove current sources and resistor

* $\downarrow g_b V_{bs}$ is modeling the body effect of transistor when source has different voltage than bulk



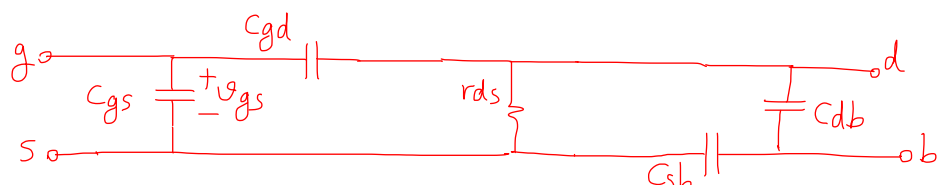
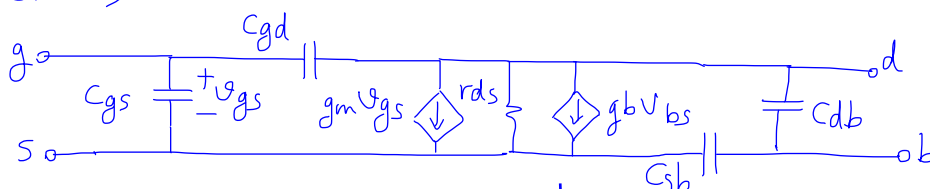
subthreshold \rightarrow low power \rightarrow low current



$$I_{DS} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th})^2 [1 + \lambda (V_{DS} - (V_{GS} - V_{th}))]$$

$$g_m = \frac{\partial I_{DS}}{\partial V_{GS}} \approx \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th})$$

$$r_{ds} = \frac{1}{\frac{\partial I_{DS}}{\partial V_{DS}}} \approx \frac{1}{\lambda I_{DS}}$$



$V_{GS} > V_{th}$
 $V_{DS} > V_{GS} - V_{th}$
 (current source)
 saturation

$$I_{DS} = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th}) V_{DS}$$

$$r_{ds} = \frac{1}{\frac{\partial I_{DS}}{\partial V_{DS}}} = \frac{V_{DS}}{I_{DS}} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th})}$$

