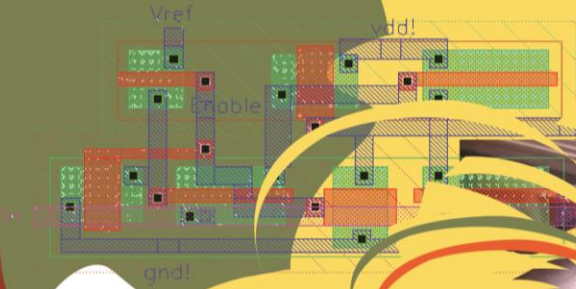


IC RESISTORS

Lecture 1

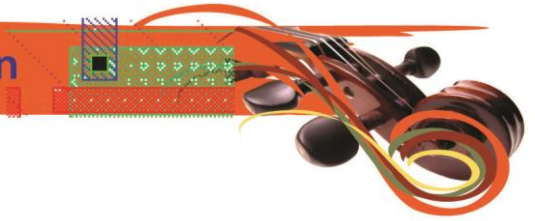
Advanced Digital IC Design

Khosrow Ghadiri

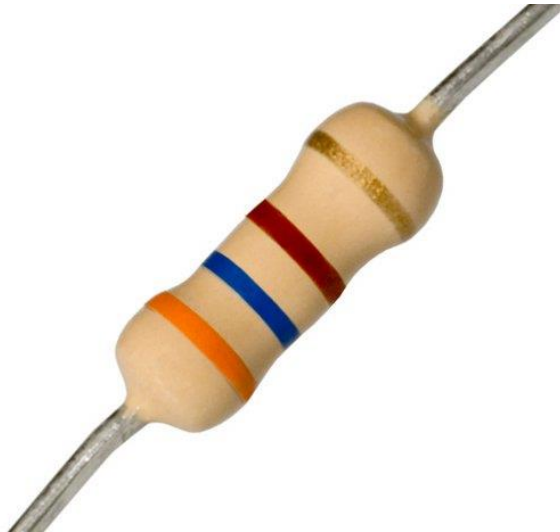




- IC passive components modeling and fabrication
 - IC resistors
 - IC inductors
 - IC capacitors



- **Discrete resistors:** are made from wires wound around a cylinder of carbon film layers.

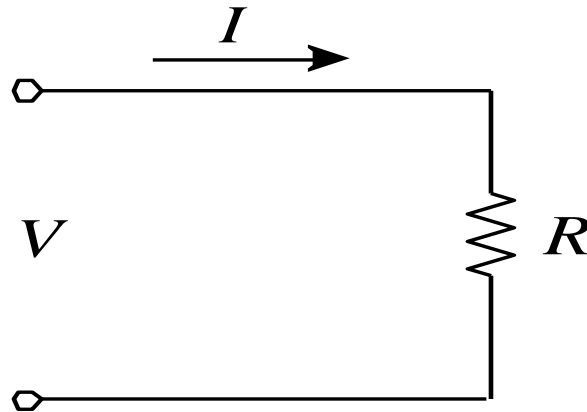


- **Integrated-circuit resistors:** are made from doped semiconductors, polysilicon film and connected to each other or other part of IC circuit with metallization using good conductors like aluminum.

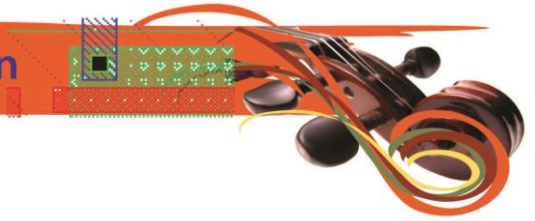


- Resistors follow **Ohm's law** that states the resistance in ohm Ω of resistors is directly proportional to voltage applied V in volts across the resistor and indirectly proportional to current, I in ampere flows through the resistor.

$$R = \frac{V}{I}$$

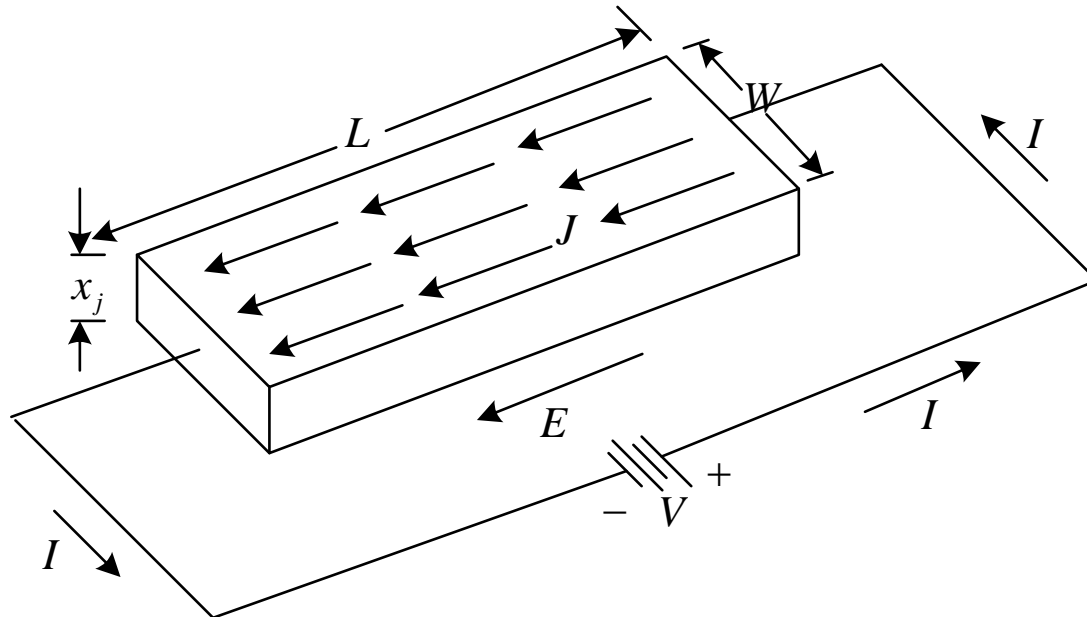


- Resistance of a resistor is defined as a ratio of voltage across it over current through it.



- The Resistance is also directly related to resistivity ρ in $\Omega\text{-cm}$ of the material of which the resistor is made of and its length, L in cm and indirectly proportional to its cross sectional area $A = x_j W$ in cm^2 .

$$R = \rho \frac{L}{x_j W}$$





- The resistivity is also inversely proportional to the conductivity.

$$\rho = \frac{1}{\sigma}$$

- The electric field:

$$E = \frac{V}{L}$$

- The drift current density

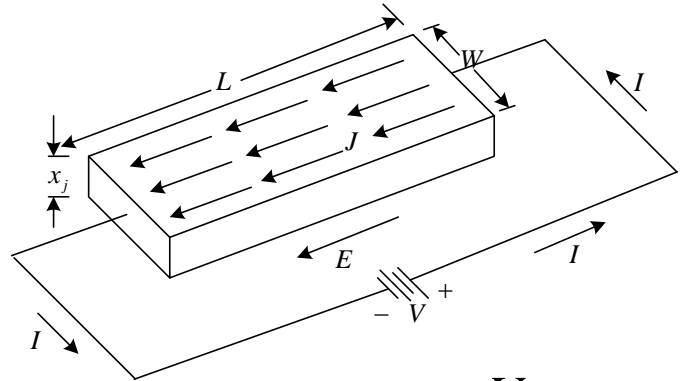
$$J = J_n(\text{drift}) + J_p(\text{drift}) = qn\mu_n E + qp\mu_p E = q(n\mu_n + p\mu_p) \frac{V}{L}$$

- The drift current

$$I = J.A = q(n\mu_n + p\mu_p) \frac{V}{L} (Wx_j) = q(n\mu_n + p\mu_p) \frac{Wx_j}{L} V$$

- The resistance can be rewritten in terms of sheet resistance as

$$R = \frac{V}{I} = \frac{1}{q(n\mu_n + p\mu_p)x_j} \frac{L}{W} = R_s \frac{L}{W} = R_s N_s$$





- The resistivity is also inversely proportional to the conductivity.

$$\rho = \frac{1}{\sigma}$$

- The sheet resistance is defined as a ratio of resistivity over junction depth x_j in integrated circuit,

$$R_s = \frac{\rho}{x_j} = \frac{1}{\sigma x_j}$$

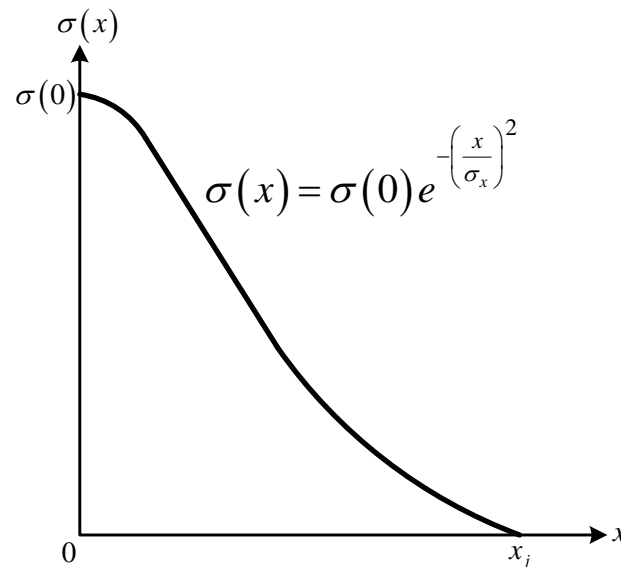
- and expressed in Ω/\square .
- Resistance can be rewritten in terms of sheet resistance as

$$R = R_s \frac{L}{W} = R_s N_s$$

- Where $N_s = L/W$ is the length-to-width ratio and is called **the number of squares** and is unit-less

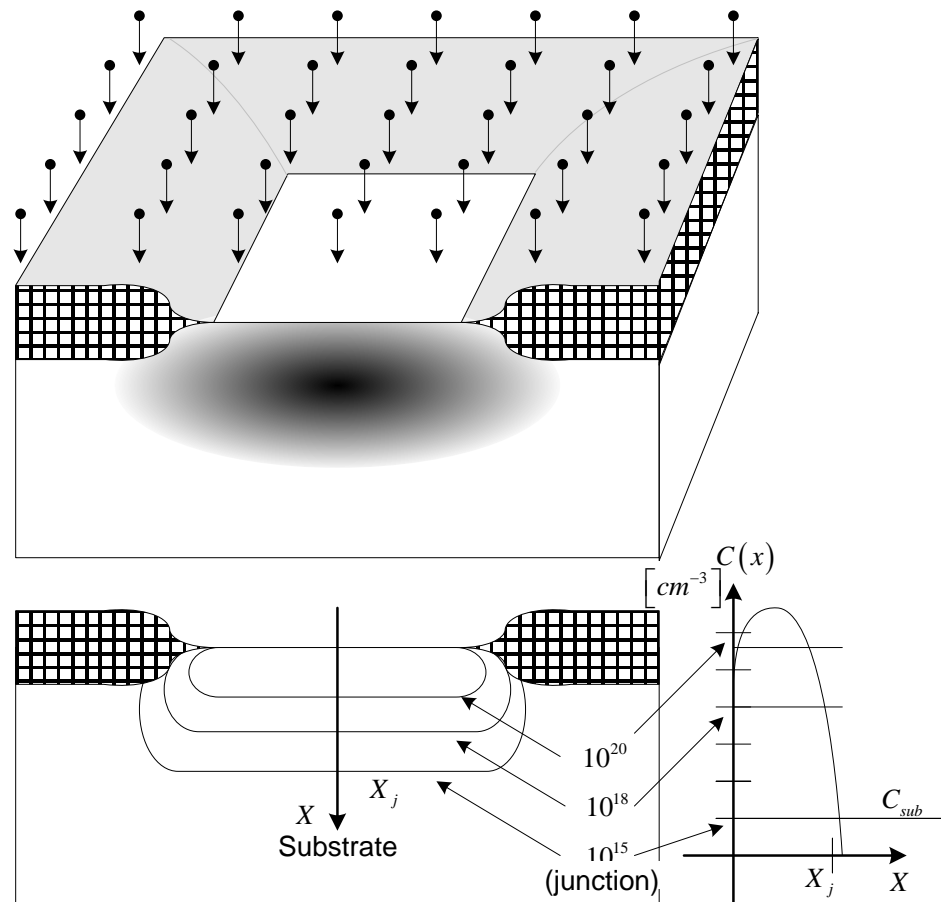


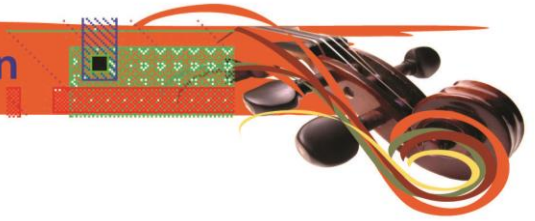
- Distribution models
 - Gaussian
 - Dual Pearson IV
 - Monte Carlo
- Resistivity $\rho(x)$ is not uniform in integrated circuit. Resistivity is smallest at surface, increasing inside the material due to diffusion, or stating in another way, conductivity is highest at surface, reducing inside material.



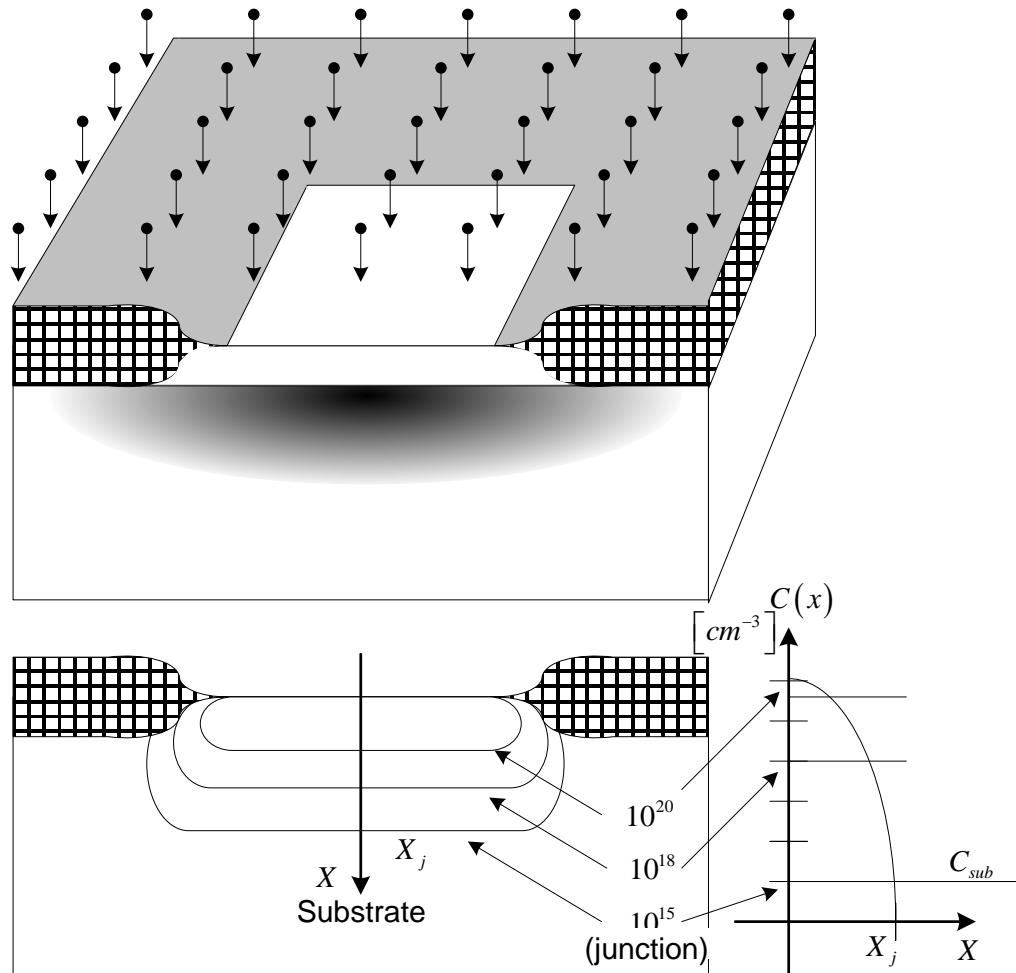


- Gaussian distribution resulting from ion implantation





- Gaussian distribution resulting from annealing





- Impurity Concentration profile
- Gaussian distribution resulting from ion implantation. The impurity is shown implanted completely below the wafer surface $x = 0$
- The projected range, or expected value which is function of the ion energy plus mass and atomic number of impurity as well as target material

R_p = Projected range

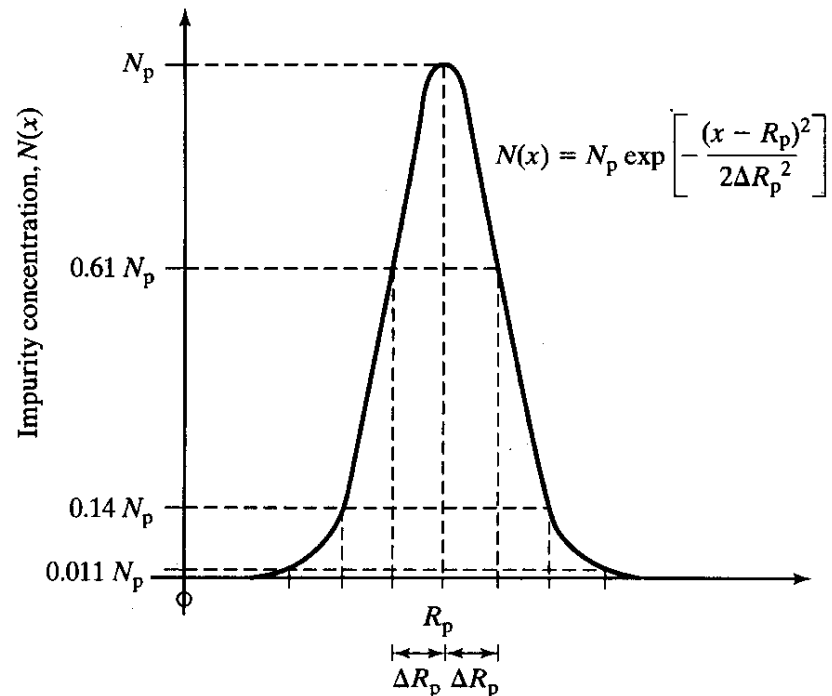
ΔR_p = Straggle = standard deviation

N_p = The peak concentration @ $x = R_p$

$$Q = \text{dose} = \int_0^{\infty} N(x) dx = \sqrt{2\pi} N_p \Delta R_p$$

$$N(x) = N_p e^{-\frac{(x-R_p)^2}{2\Delta R_p^2}}$$

$$N_p = \sqrt{2\pi} N_p \Delta R_p$$





- The conductivity profile is a normalized Gaussian distribution resulting from ion implantation.

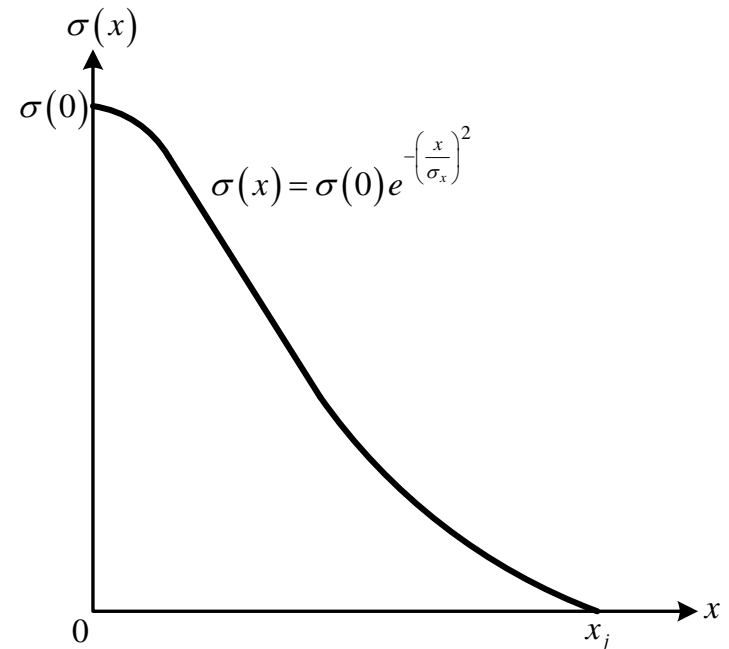
$$\sigma(x) = \sigma(0) e^{-\left(\frac{x}{\sigma_x}\right)^2}$$

- The expected value is zero
- The standard deviation is

σ_x = standard deviation

- The peak-value is

$\sigma(x)$ = the peak conductivity @ $x=0$



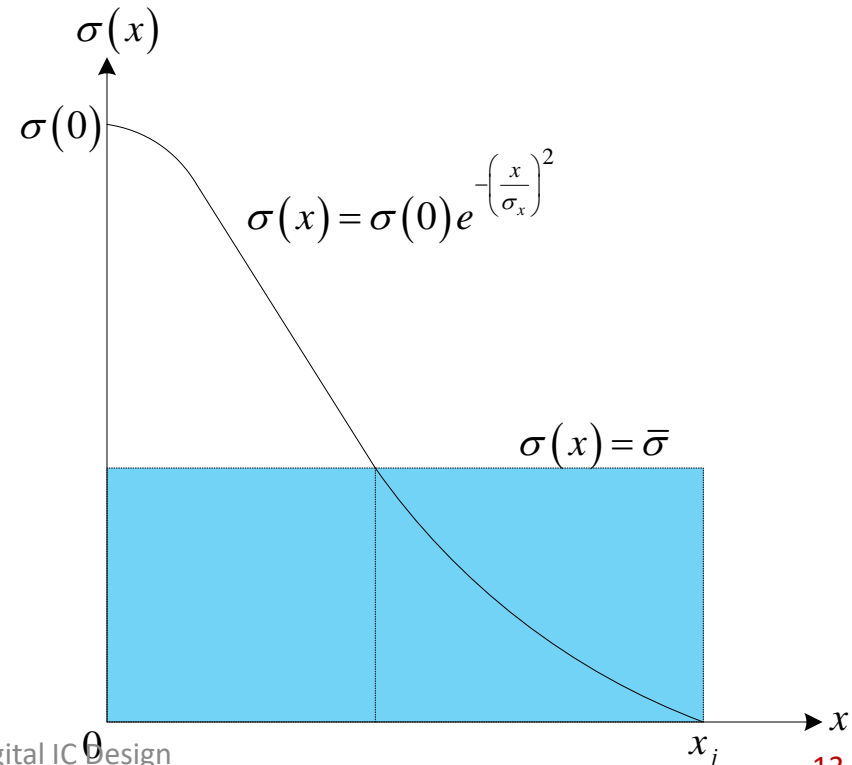


- The average conductivity is a single value for the conductivity that will provide the most suitable uniform conductivity approximation of the real conductivity dependence.
- The average conductivity $\bar{\sigma}$ is shown in dashed line, can be found by equating the rectangular area $\bar{\sigma}x_j$ and enclosed area:

$$\int_0^{x_j} \sigma(x) dx \simeq \int_0^{\infty} \sigma(x) dx$$

$$\bar{\sigma} \simeq \frac{1}{x_j} \int_0^{\infty} \sigma(x) dx$$

$$R_s = R_{\square} = 1/\bar{\sigma}x_j$$





- A single Pearson distribution $P(x)$ is characterized by four parameters position of the peak R_p , the straggle ΔR_p , the skewness which is indicating the tilting of the profile δ , and kurtosis β which indicates the flatness at the top of the profile.
- The concentration

$$n(x) = n(0) \exp[P(x)]$$

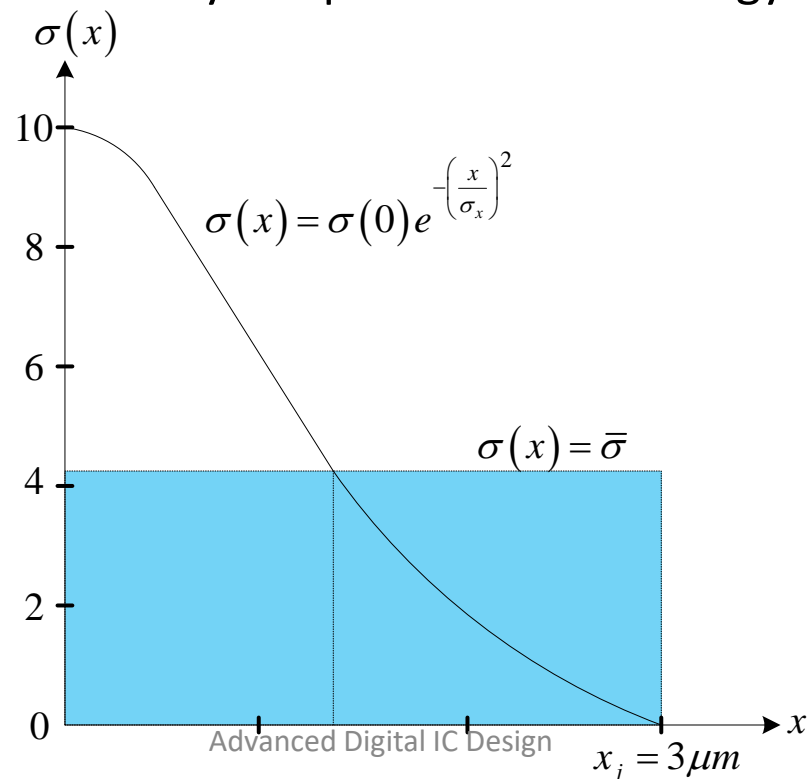
- The Pearson type IV

$$P(x) = \frac{1}{2b_2} \ln(b_2 x^2 + b_1 x + b_0) - \frac{\frac{b_1}{b_2} + 2a_0}{\sqrt{4b_2 b_0 - b_1^2}} \arctan \frac{2b_2 x + b_1}{\sqrt{4b_2 b_0 - b_1^2}}$$



■ **Problem:**

- A) Find the average conductivity for the layer shown in figure, given the standard deviation is $\sqrt{2}$
- B) Design a $100k\Omega$ resistor using this layer, given the minimum dimension achievable by the particular technology is $1\mu m$.





■ **Solution:**

- A) The average conductivity:

$$\bar{\sigma} = \frac{10(\Omega - cm)^{-1}}{3\mu m} \int_0^\infty e^{-\frac{x^2}{2}} dx$$

- The so called Laplace integral is:

$$\int_0^\infty e^{-\frac{x^2}{2}} dx = \sqrt{\frac{\pi}{2}} \mu m$$

- Then the average conductivity is:

$$\bar{\sigma} = \frac{10(\Omega - cm)^{-1}}{3\mu m} \left(\sqrt{\frac{\pi}{2}} \mu m \right) = 4.18(\Omega - cm)^{-1}$$

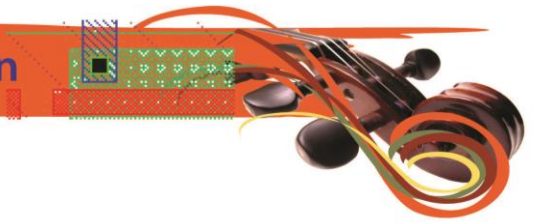
- B) The sheet resistance:

$$R_s = R_\square = \frac{1}{\bar{\sigma} x_j} = \frac{1}{4.18(\Omega - cm)^{-1} \times 3 \times 10^{-4} cm} = 797.4 \Omega/\square$$

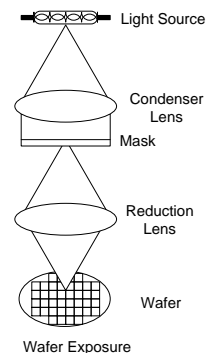
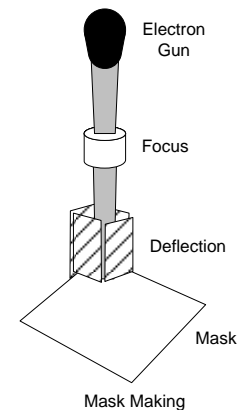
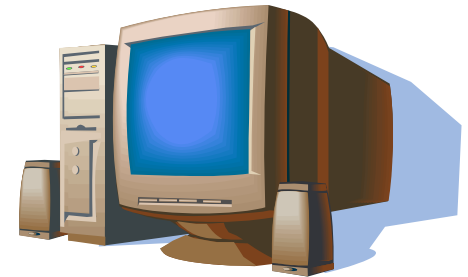
$$\frac{L}{W} = \frac{R}{R_s} = \frac{100,000}{797.4} = 125 \Rightarrow L = 125W = 125\mu m$$

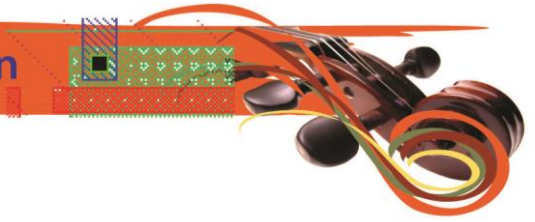


- The fundamental unit of IC manufacturing: Silicon wafer.
- The typical wafer diameter: 20 cm in 1990's, \$50.00, 150 chips.
- The maximum wafer diameter: 30 cm in 2014.
- Development of 45 cm wafer is in horizon.
- A lot: A group of around 24 wafers undergoes the same sequence of fabrication process.
- DRAM: 200 steps
- A typical complex IC chip area: 1.5cmX1.5cm
- A typical IC: Several millions electronic devices
- A typical cost of wafer: \$2000.00.
- The yield of mature process: how many of the chip work: %90
- A typical IC package: In plastic Dual-in-line (DIP)/ Wire bonds
- A typical IC for cellular phone/laptop package: encapsulated in low-profile surface mount package or mount directly mounted on the circuit board using a flip-chip technique/ Electroplated solder bumps.

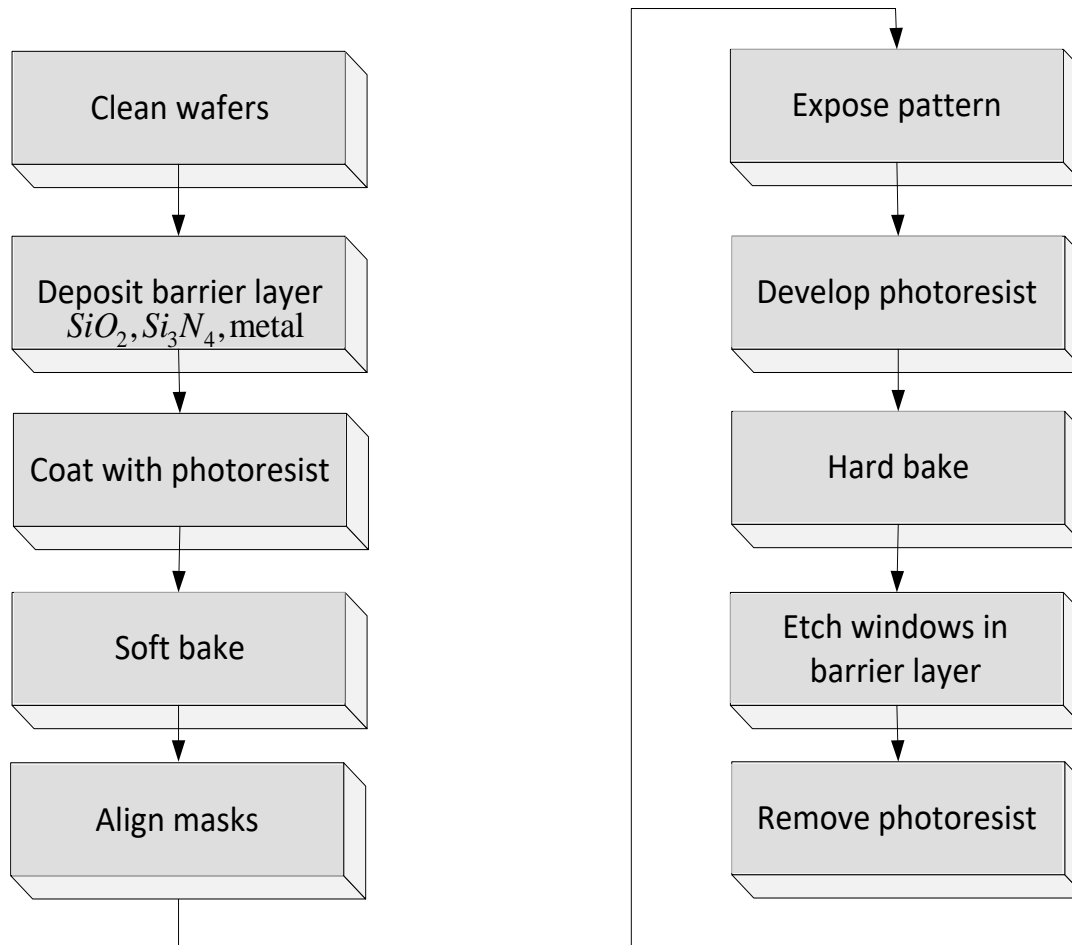


- Photolithography can be divided into three steps:
 - Design using CAD system
 - Layout
 - Simulation
 - Design Rule Verification
 - Mask making
- Wafer exposure
 - The patterns transfer form mask to photo resist
 - Chemical or plasma etching to transfer the
 - pattern from the photo resist to burrier material
 - on the surface of wafer.





- The various steps of basic photolithographic process

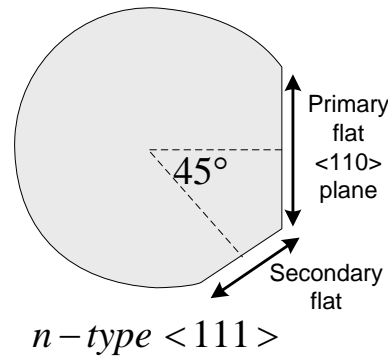
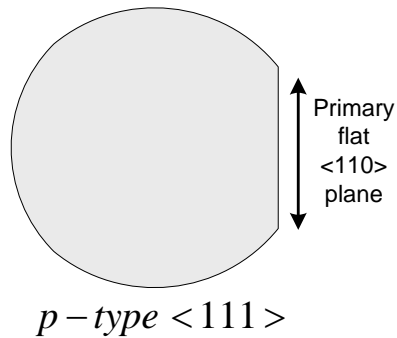
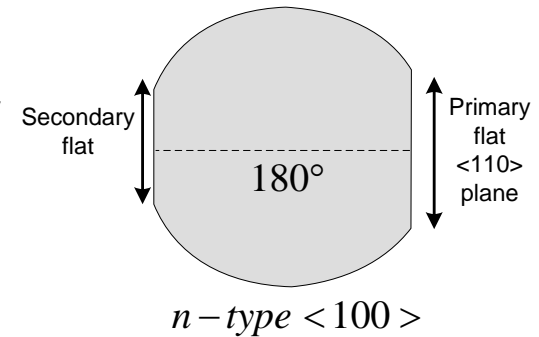
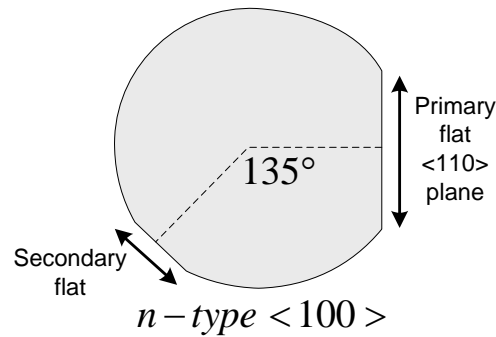
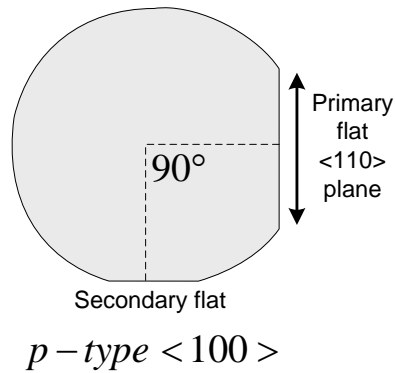




- n or p-type silicon wafer are available with a specified resistivity
- Typically the growing crystal is doped with boron, phosphorous or arsenic. Arsenic and antimony is used for low resistivity (high concentration) n-type crystal.
- The thickness $250\mu m \leq t \leq 500\mu m$
- The diameter $200mm(8\text{ inch}) \leq d \leq 300mm(12\text{ inch})$ (wafers with diameter of 1,1.5,2,3,4,5 and 6 inches have been used at various stages in history of solid state devices).
- The diameter of wafer is chosen in order to withstand the mechanical and thermal strain during the process steps. (for example a 6 to 8 inch diameter semiconductor wafer needs to be about $500\mu m$ thick.

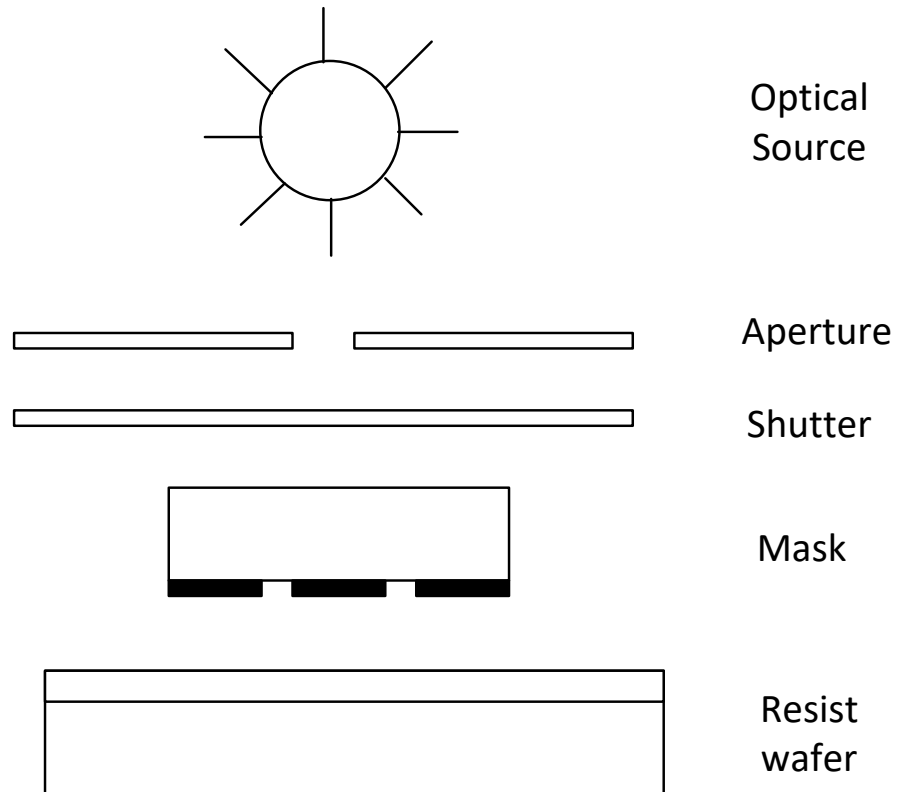


■ Schematic of a simple lithographic exposure system



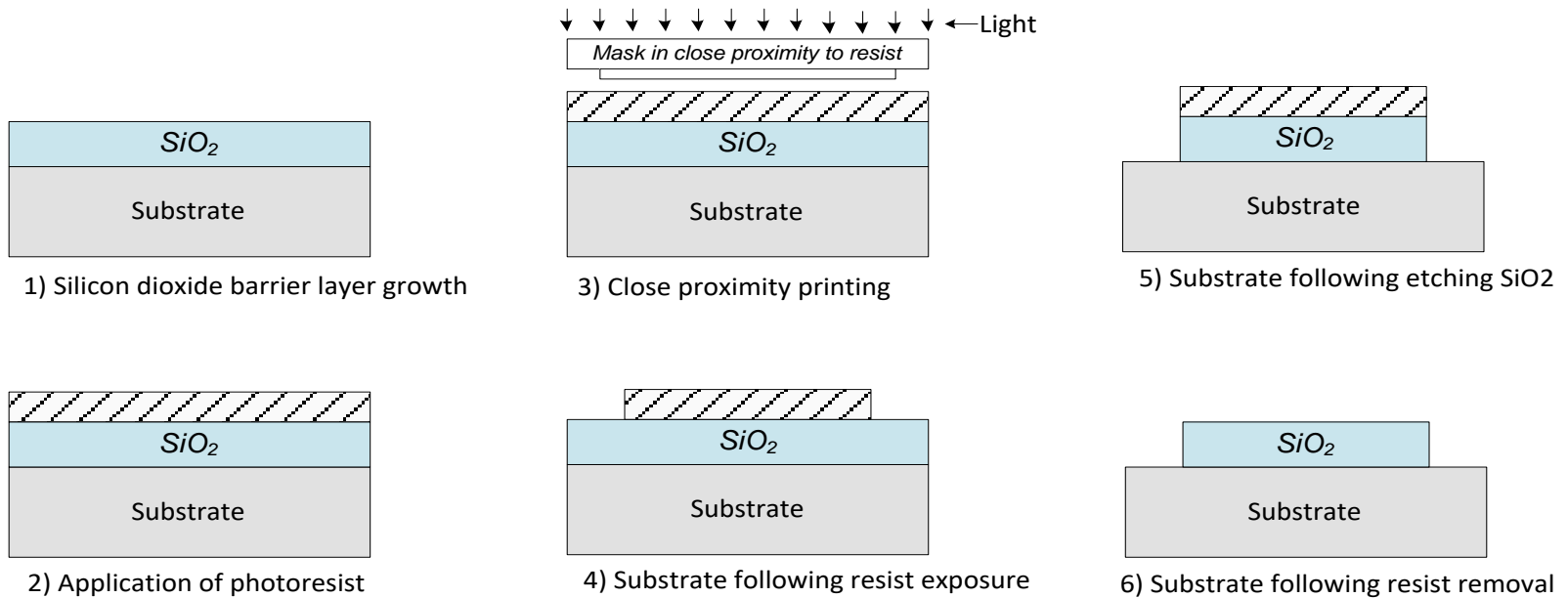


- Schematic of a simple lithographic exposure system



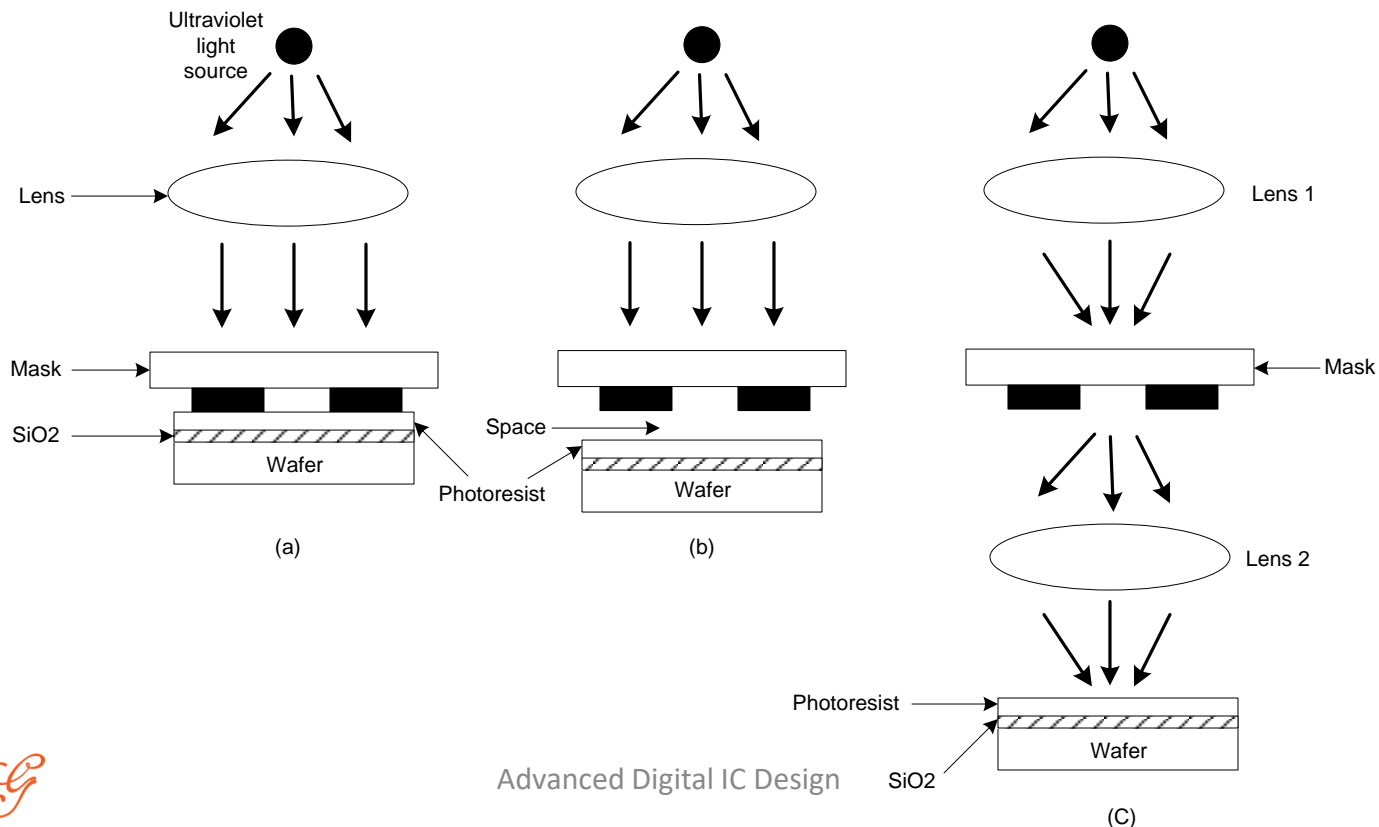


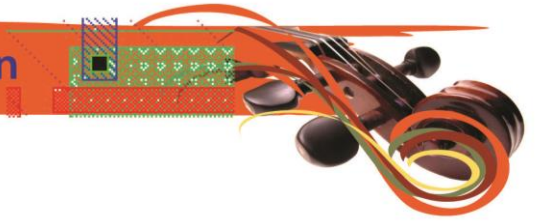
■ Schematic of a simple lithographic exposure system





- (a) Contact printing, in which wafer is in intimate contact with mask,
- (b) proximity printing, in which wafer and mask are in close proximity
- (c) projection printing, in which light source is scanned across the mask and focused on the wafer.





- The resistivity is also inversely proportional to the conductivity.

$$\rho = \frac{1}{\sigma}$$

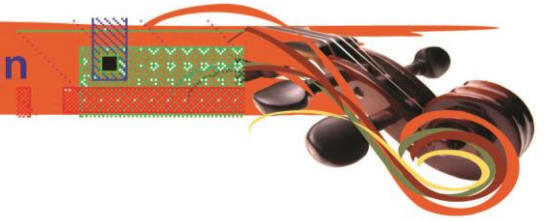
- The sheet resistance is defined as a ratio of resistivity ρ over junction depth x_j in integrated circuit,

$$R_s = \frac{\rho}{x_j} = \frac{1}{\sigma x_j}$$

- and expressed in Ω/cm
- Resistance can be rewritten in terms of sheet resistance as

$$R = R_s \frac{L}{W} = R_s N_s$$

- Where $N_s = L/W$ is the length-to-width ratio and is called **the number of squares**



- The Sheet resistance for frequently used materials in IC.

MATERIAL	THICKNESS (x_j)	SHEET RESISTANCE
n ⁺ -Polysilicon	500 nm	$R_s = 20 \Omega/cm$
Aluminum	1000 nm	$R_s = 0.07 \Omega/cm$
Silicided polysilicon		$R_s = 5 \Omega/cm$
Silisided source/drain diffusion		$R_s = 3 \Omega/cm$



- The Change from run-to-run, chip-to-chip is largely due to ion-implanter.
- The doping concentration N_D can be expressed as:

$$N_D = \bar{N}_D (1 \pm \varepsilon_{N_D})$$

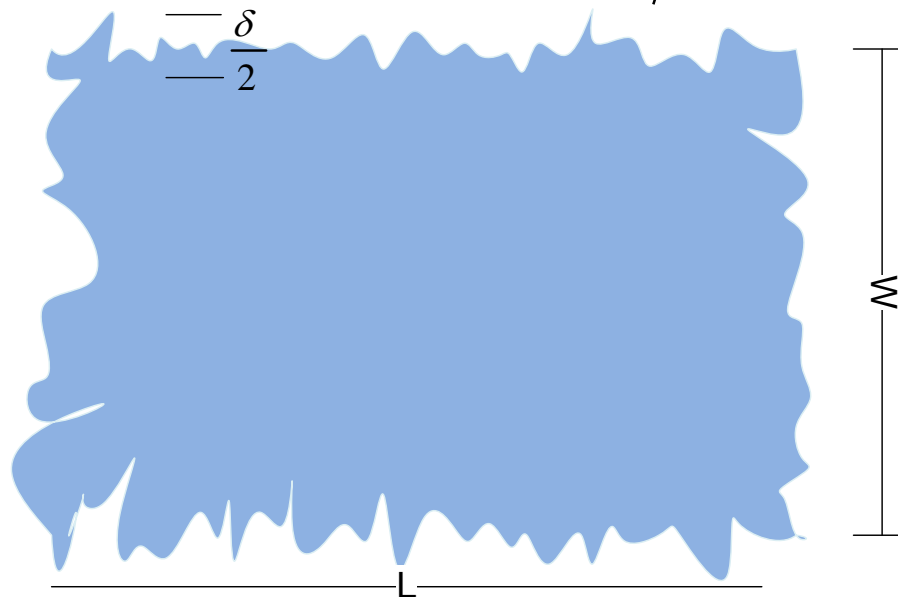
- Where \bar{N}_D is the average doping and ε_{N_D} is the normalized uncertainty.
- For example:

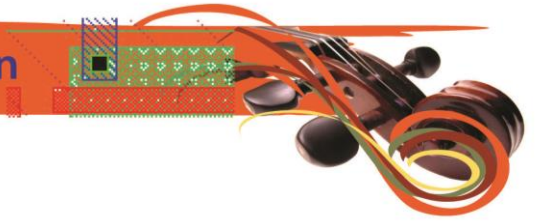
Doping concentration defined by an average of $\bar{N}_D = 10^{17} \text{ cm}^{-3}$
and normalized uncertainty of $\varepsilon_{ND} = 0.025$ means that

$$N_D = (10^{17} \text{ cm}^{-3})(1 \pm 0.025) = 10^{17} \pm 2.5 \times 10^{15} \text{ cm}^{-3}$$



- Mobility Variation are due to random local variation in Crystal defects
- Ignoring Coupling between doping concentration and mobility variation
- The resistor thickness x_j variation is due to time and local wafer temperature variation during the furnace annealing process
- The lateral dimensions of the resistor are affected by random linewidth variations from the pattern transfer processes.
- The uncertainty on one edge is defined as $\delta/2$





- Sheet Resistance

$$W = \bar{W} \pm \delta/2 \pm \delta/2 = \bar{W} \pm \delta$$

$$L = \bar{L} \pm \delta/2 \pm \delta/2 = \bar{L} \pm \delta$$

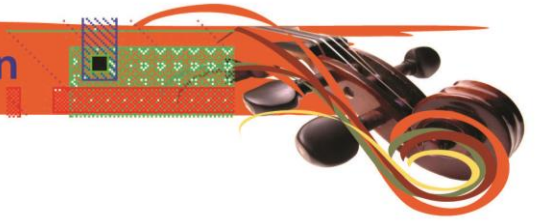
- Uncertainty from each edge:

$$W = \bar{W} (1 \pm \delta/\bar{W}) = \bar{W} (1 \pm \varepsilon_W)$$

$$L = \bar{L} (1 \pm \delta/\bar{L}) = \bar{L} (1 \pm \varepsilon_L)$$

$$E_W = \delta/\bar{W} \quad E_L = \delta/\bar{L}$$

$$\bar{R} = \frac{1}{q\bar{N}_D (1 + \varepsilon_{N_D}) \bar{\mu}_n (1 + \varepsilon_{\mu_n}) \bar{\chi}_j (1 + \varepsilon_{x_j})} \left[\frac{\bar{L} (1 + \varepsilon_L)}{\bar{W} (1 + \varepsilon_W)} \right]$$



- Sheet Resistance
- The average resistance

$$\bar{R} = \frac{1}{qN\bar{d}\bar{\mu}_n\bar{\chi}_j}\left(\frac{\bar{L}}{\bar{W}}\right)$$

- Substitution for each term that is subject to manufacturing is

$$\bar{R} = \frac{1}{q\bar{N}_D(1+\varepsilon_{N_D})\bar{\mu}_n(1+\varepsilon_{\mu_n})\bar{\chi}_j(1+\varepsilon_{x_j})}\left[\frac{\bar{L}(1+\varepsilon_L)}{\bar{W}(1+\varepsilon_W)}\right]$$

- The average resistance

$$\varepsilon_R = \sqrt{\varepsilon_{N_D}^2 + \varepsilon_{\mu_n}^2 + \varepsilon_{x_j}^2 + \varepsilon_L^2 + \varepsilon_W^2}$$

- Uncertainty up to 0.1