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# EE288 Data Conversions/Analog Mixed-Signal ICs

## Spring 2018

### Lecture 10: SC and Bootstrapped Clock Circuits

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ENG-259

# Course Schedule – Subject to Change

Date	Topics
24-Jan	Course introduction and ADC architectures
29-Jan	Converter basics: AAF, Sampling, Quantization, Reconstruction
31-Jan	ADC dynamic performance metrics, Spectrum analysis using FFT
5-Feb	ADC & DAC static performance metrics, INL and DNL
7-Feb	OPAMP and bias circuits review
12-Feb	SC circuits review
14-Feb	Sample and Hold Amplifier - Reading materials
19-Feb	Flash ADC and Comparators: Regenerative Latch
21-Feb	Comparators: Latch offset, preamp, auto-zero
26-Feb	<del>Finish Flash ADC</del>
28-Feb	DAC Architectures - Resistor, R-2R
5-Mar	DAC Architectures - Current steering, Segmented
7-Mar	DAC Architectures - Capacitor-based
12-Mar	SAR ADC with bottom plate sampling
14-Mar	SAR ADC with top plate sampling
19-Mar	Midterm Review
21-Mar	Midterm exam
26-Mar	Spring break
28-Mar	Spring break
2-Apr	Pipelined ADC stage - comparator, MDAC, x2 gain
4-Apr	Pipelined ADC bit sync and alignment using Full adders
9-Apr	Pipelined ADC 1.5bit vs multi-bit structures
11-Apr	Fully-differential OPAMP and Switched-capacitor CMFB
16-Apr	Single-slope ADC
18-Apr	Oversampling & Delta-Sigma ADCs
23-Apr	Second- and higher-order Delta-Sigma Modulator.
25-Apr	Hybrid ADC - Pipelined SAR
30-Apr	Hybrid ADC - Time-Interleaving
2-May	ADC testing and FoM
7-May	Project presentation 1
8-May	Project presentation 2
14-May	Final Review
20-May	Project Report Due by 6 PM

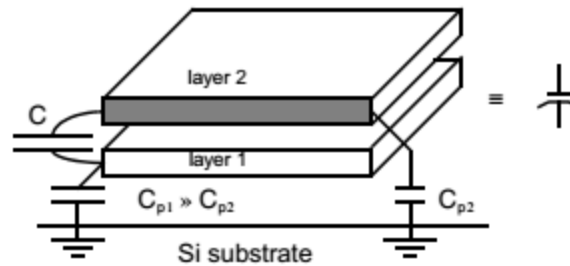
**S&H and  
Bootstrap circuits**



**\*Midterm Exam dates  
are approximate and  
subject to change  
with reasonable notice.**

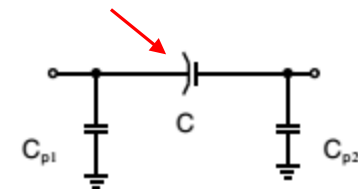
# Basic Building Blocks of Switched-Capacitor Circuits

- OPAMP (OTA)
- Capacitor
- Switch
- Clock



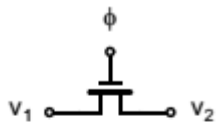
(a)

**Bottom Plate**

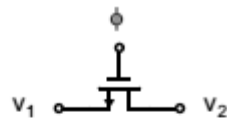


$$C_{p1} > C_{p2}$$

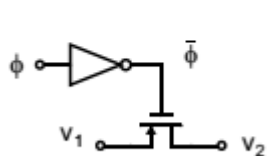
(b)



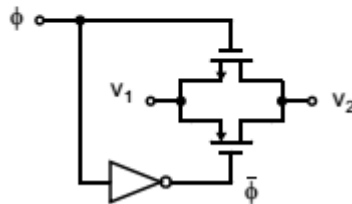
(a)



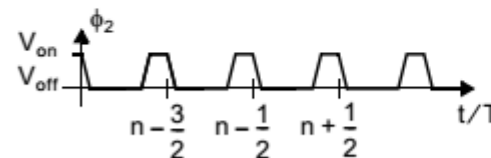
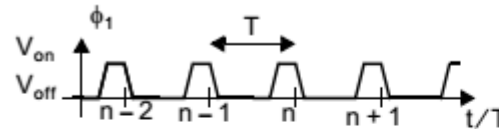
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(c)

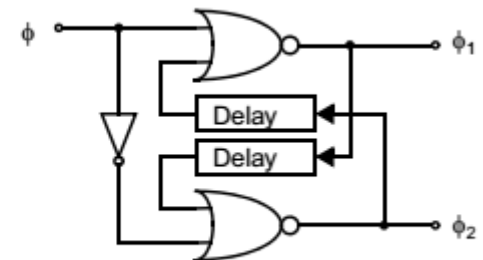


(d)



(a)

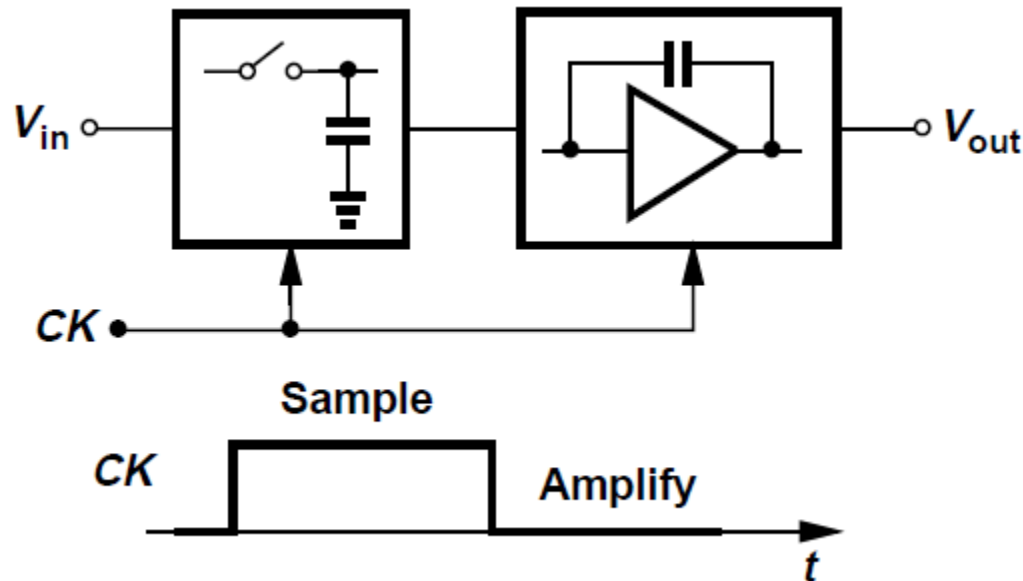
$$f_s \equiv \frac{1}{T}$$



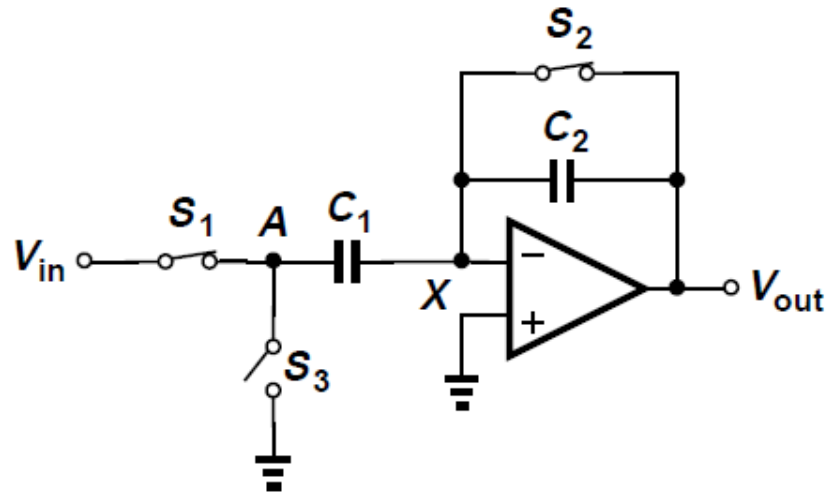
(b)

# General Considerations

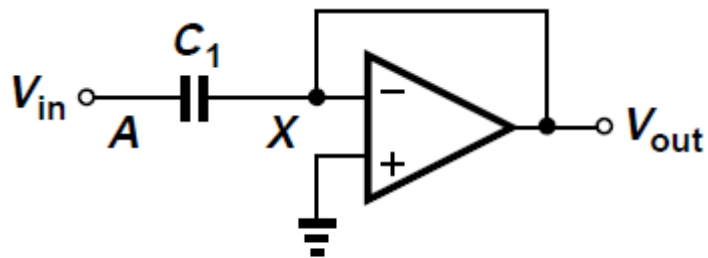
- Switched-capacitor amplifiers operate in **two phases**: **Sampling and Amplification**
- Clock needed in addition to analog input  $V_{in}$



# SC Amplifier



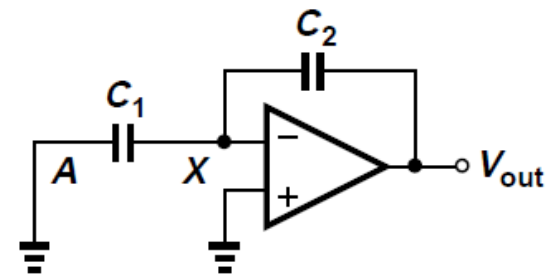
**$S_1, S_2$  on,  $S_3$  off**



(a)

**Sampling Phase**

**$S_1, S_2$  off,  $S_3$  on**

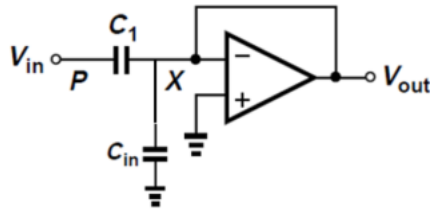


(b)

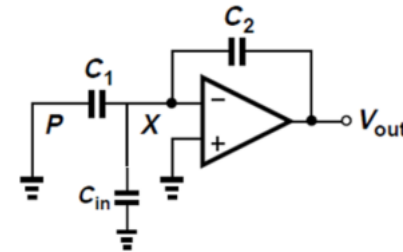
**Amplifying Phase**

# SC Amplifier

Ø1



Ø2



$$Q_1 = C_1(0 - V_{in})$$

$$Q_2 = (C_1 + C_{in})V_x + C_2(V_x - V_{out})$$

$$V_x = \frac{V_{out}}{-A}$$

$$Q_1 = Q_2$$

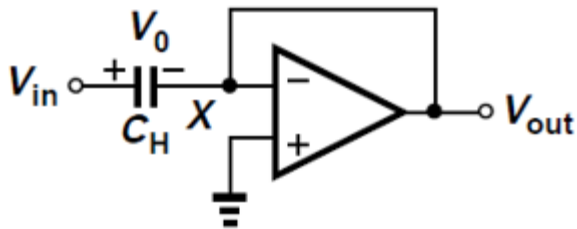
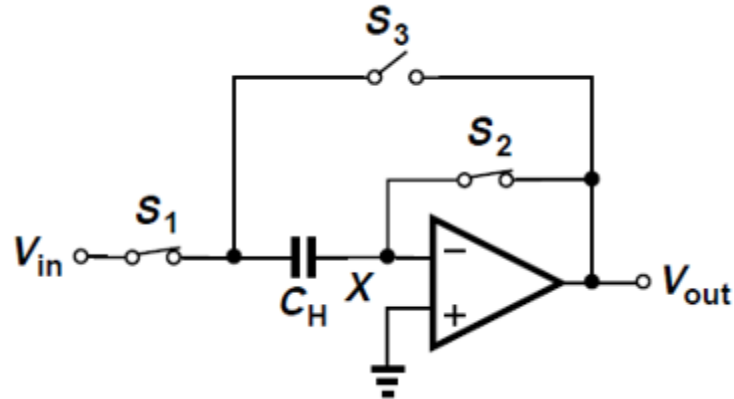
$$C_1(0 - V_{in}) = (C_1 + C_{in})V_x + C_2(V_x - V_{out}) = (C_1 + C_{in})\left(\frac{V_{out}}{-A}\right) + C_2\left(\frac{V_{out}}{-A} - V_{out}\right)$$

$$-C_1V_{in} = -C_1\frac{V_{out}}{A} - C_{in}\frac{V_{out}}{A} - C_2\frac{V_{out}}{A} - C_2V_{out}$$

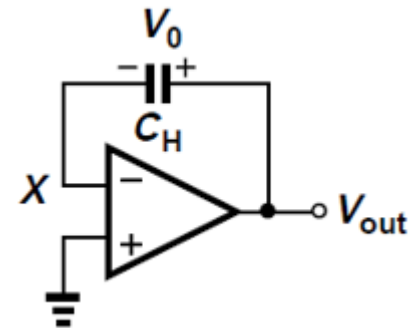
$$C_1V_{in} = \left(\frac{C_1 + C_{in} + C_2}{A} + C_2\right)V_{out} = C_2\left(\frac{C_1 + C_{in} + C_2}{C_2A} + 1\right)V_{out} = C_2\left(\frac{1}{\beta A} + 1\right)V_{out}$$

$$\frac{V_{out}}{V_{in}} = \frac{C_1}{C_2\left(\frac{1}{\beta A} + 1\right)} \approx \frac{C_1}{C_2}\left(1 - \frac{1}{\beta A}\right)$$

# Sample and Hold Amplifier – Flip Around S/H



**Sample**

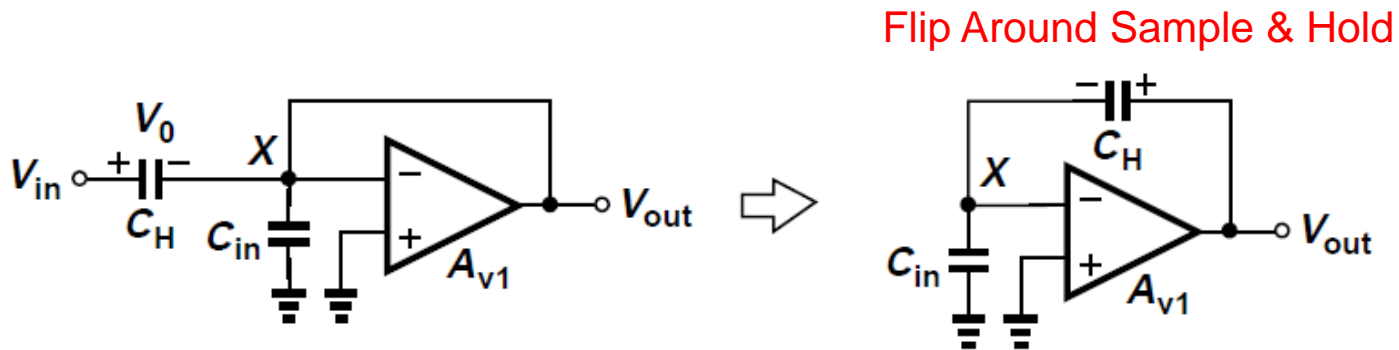


**Amplify**

# Flip Around S/H

## Precision Considerations:

- Output in amplification mode



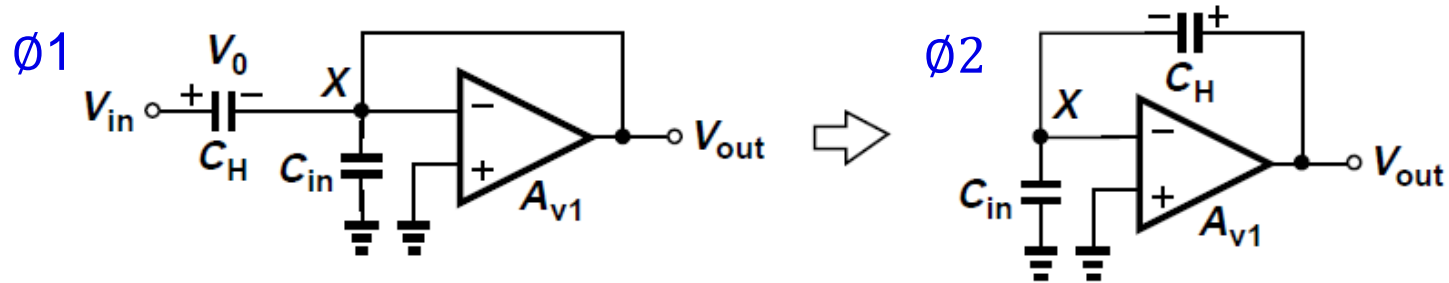
$$V_{out} = \frac{V_0}{1 + \frac{1}{A_{v1}} \left( \frac{C_{in}}{C_H} + 1 \right)}$$

$$\approx V_0 \left[ 1 - \frac{1}{A_{v1}} \left( \frac{C_{in}}{C_H} + 1 \right) \right]$$

Derive this using charge conservation



# Flip Around S/H



Charge conservation during ø1 and ø2

During ø1, total charge at node X is  $Q1 = C_H(0 - V_{in})$

During ø2, total charge at node X is  $Q2 = C_{in}V_x + C_H(V_x - V_{out})$

Let  $Q1 = Q2$

$$-V_{in}C_H = C_{in}V_x + C_H(V_x - V_{out}) = (C_{in} + C_H)V_x - C_HV_{out}$$

$$V_x(-A_{v1}) = V_{out}$$

$$-V_{in}C_H = (C_{in} + C_H)(-V_{out}/A_{v1}) - C_HV_{out}$$

$$V_{in}C_H = (C_{in} + C_H)(V_{out}/A_{v1}) + C_HV_{out}$$

$$V_{in}C_H = [(C_{in} + C_H)/A_{v1} + C_H]V_{out}$$

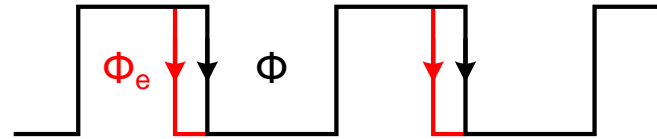
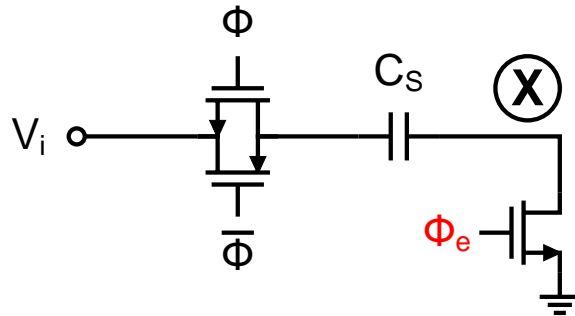
$$V_{in} = [(C_{in} + C_H)/(C_H A_{v1}) + 1]V_{out}$$

$$V_{out}/V_{in} = 1 / [(C_{in} + C_H)/(C_H A_{v1}) + 1] = 1 / [1 + 1/(\beta A_{v1})]$$

$$V_{out} \approx V_0 \left[ 1 - \frac{1}{\beta A_{v1}} \right] \quad \leftarrow \quad \text{To reduce gain error, Increase } \beta A_v$$

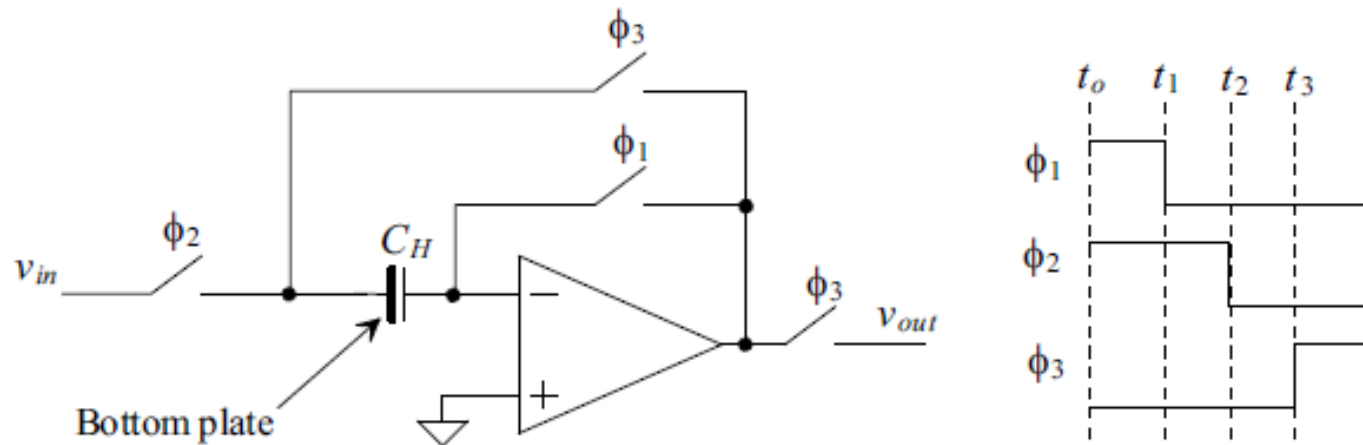
$$\beta = \frac{C_H}{C_H + C_{in}}$$

# Bottom-Plate Sampling

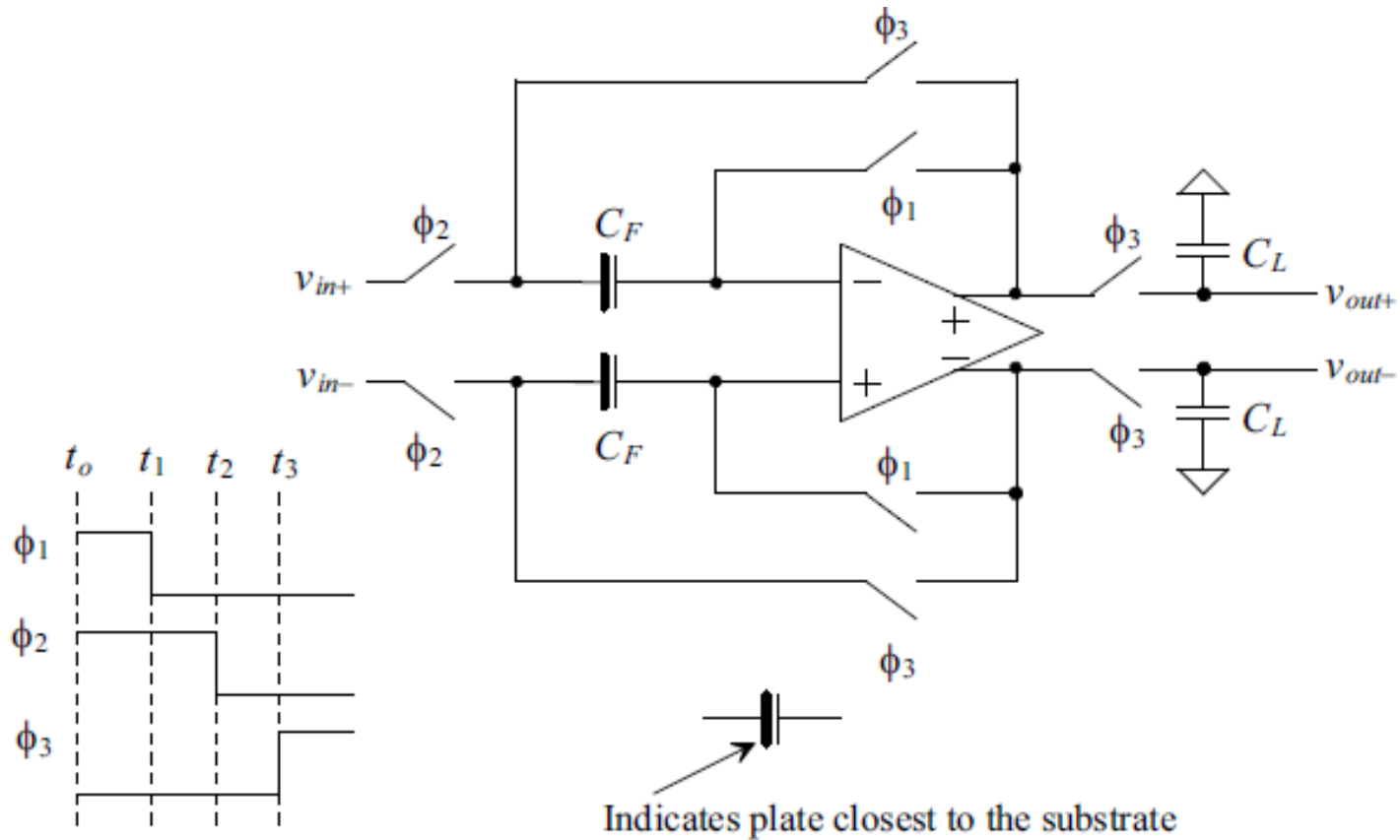


- AC-ground switch opens slightly earlier than input switches
- Signal-independent CF and CI of switch  $\Phi_e$  to the first order!
- Input switch can be further bootstrapped
- Typical for applications of more than 8-bit resolution
- Less tracking bandwidth due to more switches in series
- Signal swing at node X is not entirely zero!

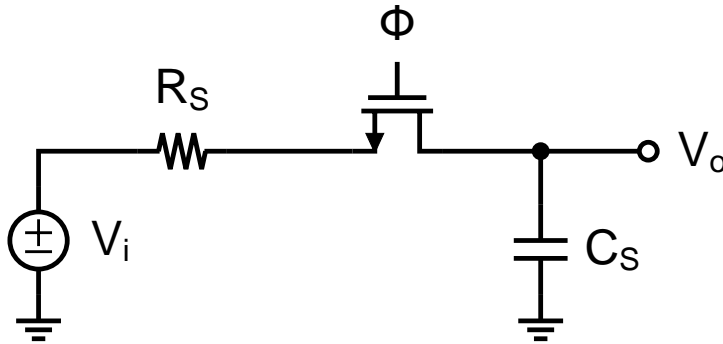
# SHA Timing for Bottom Plate Sampling



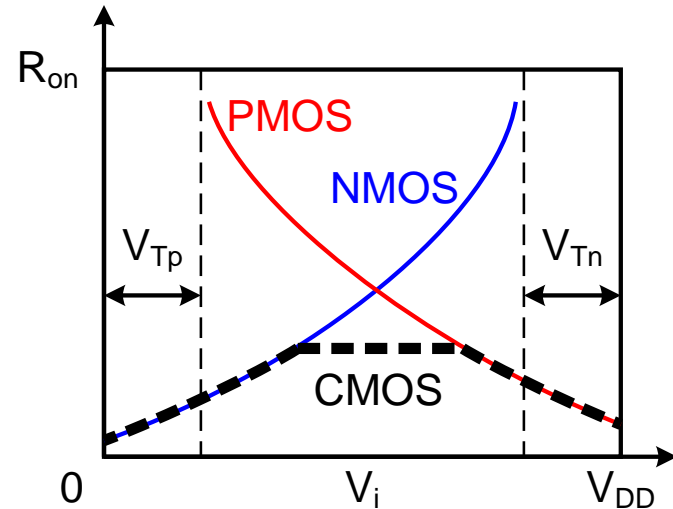
# Fully Differential S/H



# Recap: Signal-Dependent Switch $R_{on}$

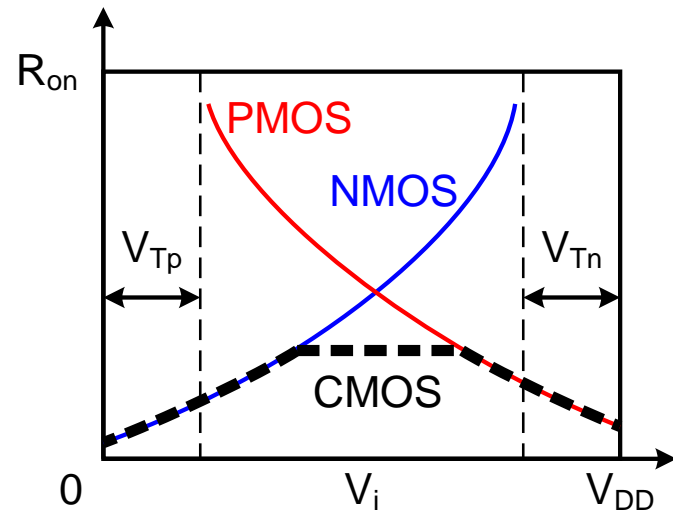
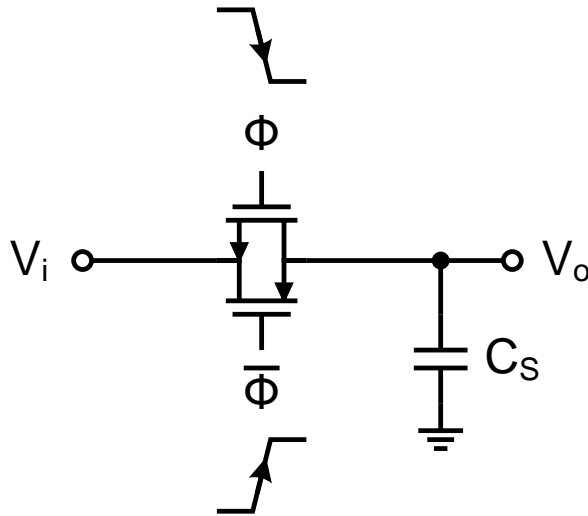


$$R_{on}^{-1} = \mu C_{ox} \frac{W}{L} (V_{DD} - V_{th} - V_i)$$



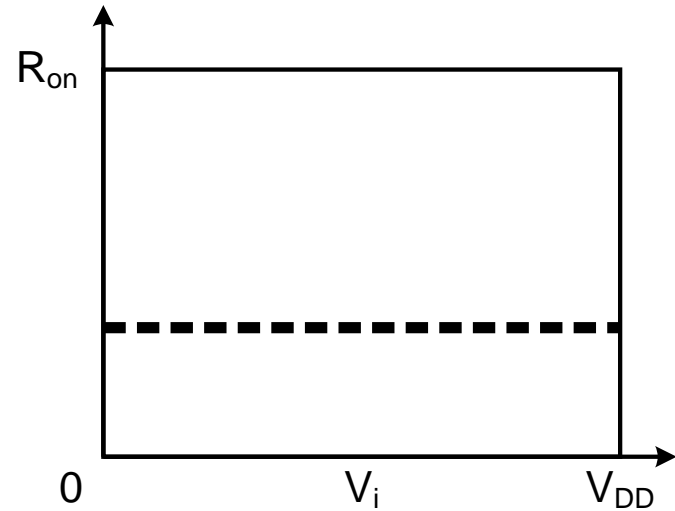
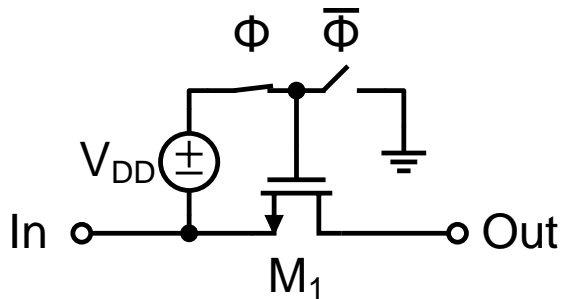
- Signal-dependent  $R_{on} \rightarrow$  signal-dependent TBW  $\rightarrow$  extra waveform distortion
- Neither signal-dependent  $R_{on}$  nor dispersion is of concern if TBW is sufficiently large ( $\gg f_{in}$ , depending on the target accuracy)

# Recap: CMOS Switch



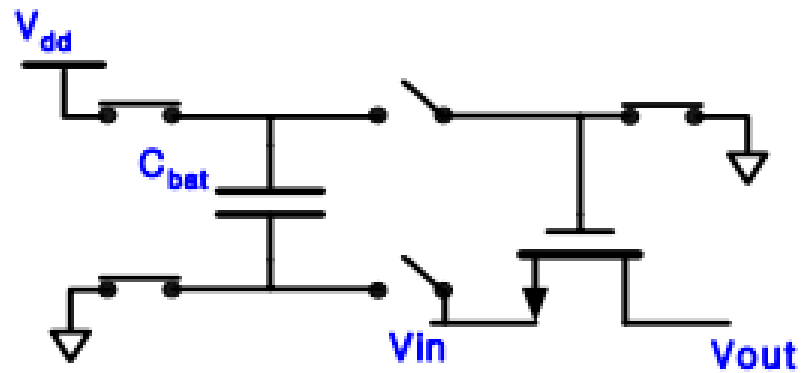
- $R_{on}$  still depends on  $V_{in}$  and is sensitive to N/P mismatch
- Large parasitic cap due to PMOS switch for symmetric  $R_{on}$
- Clock rising/falling edge alignment

# Clock Bootstrapping

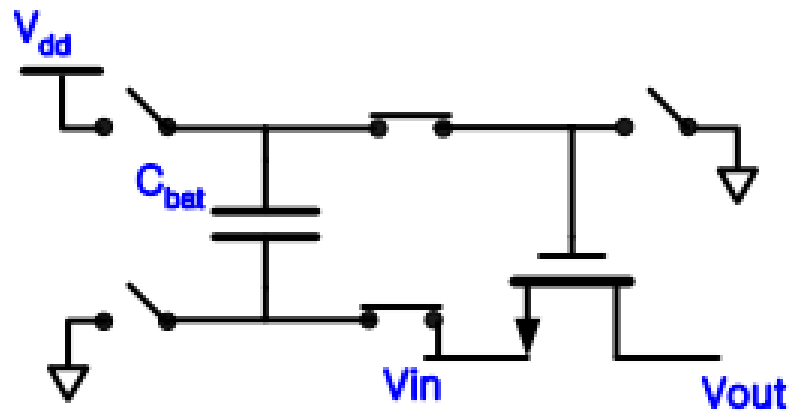


- Constant gate overdrive voltage  $V_{GS} = V_{DD}$  for the switch
- $R_{on}$  is not dependent on  $V_{in}$  to the first order (body effect?)
- NMOS device only with less parasitic capacitance

# Clock Bootstrapping



(a)



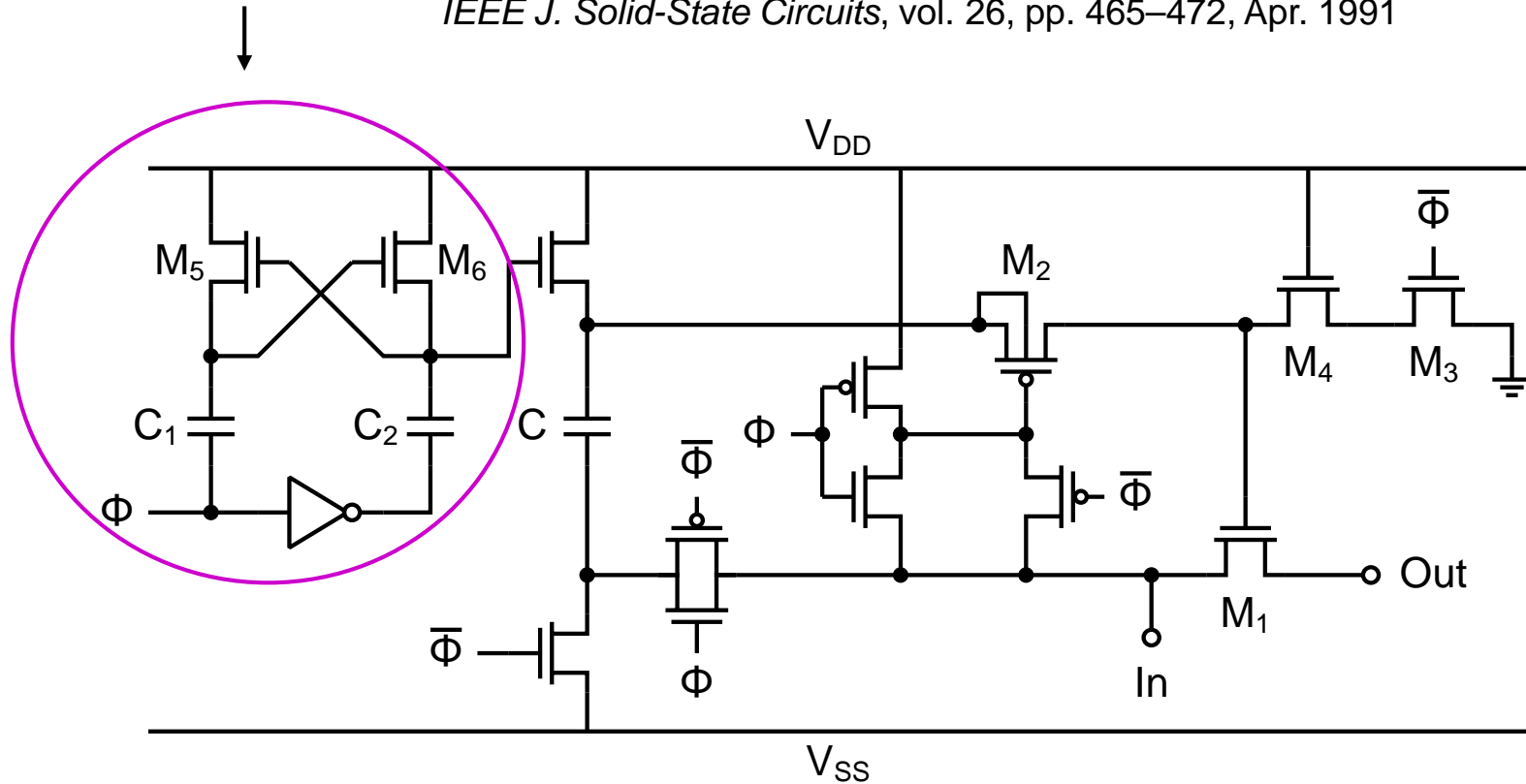
(b)



# Clock Bootstrapping

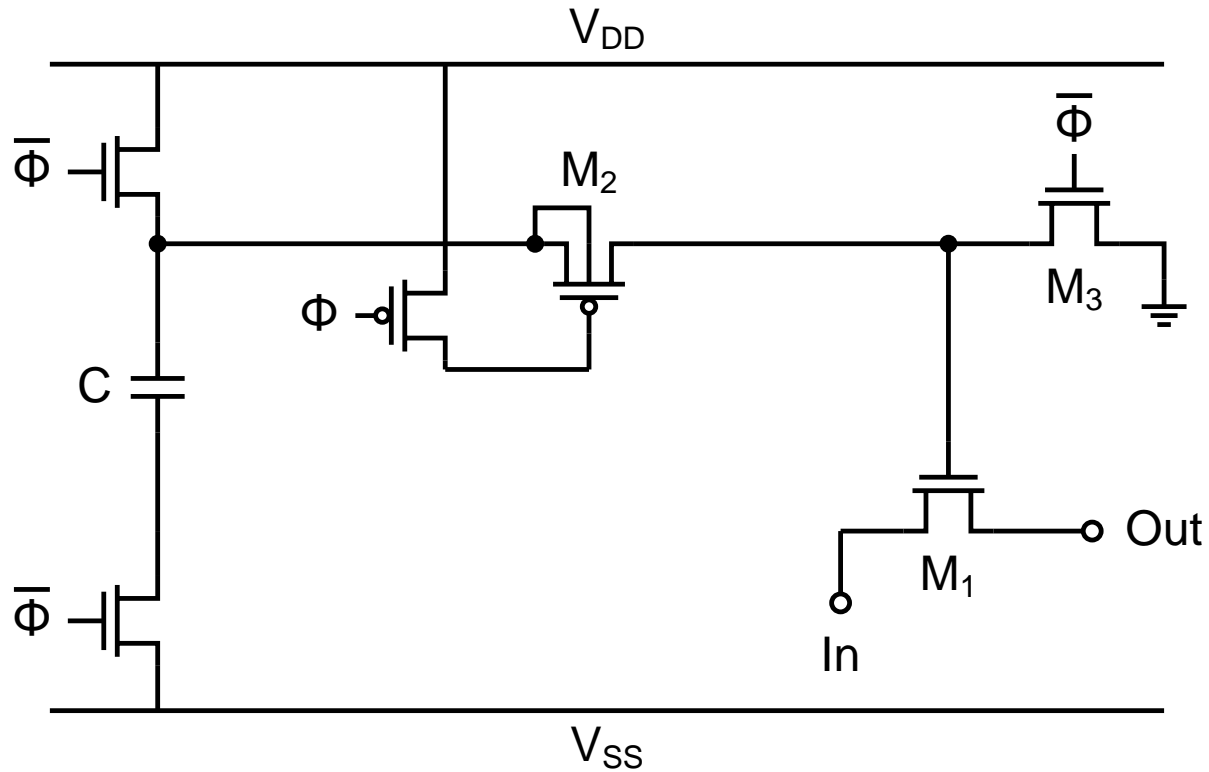
## Nakagome Charge Pump

Y. Nakagome et al., "An experimental 1.5 V 64 Mb dram,"  
*IEEE J. Solid-State Circuits*, vol. 26, pp. 465–472, Apr. 1991

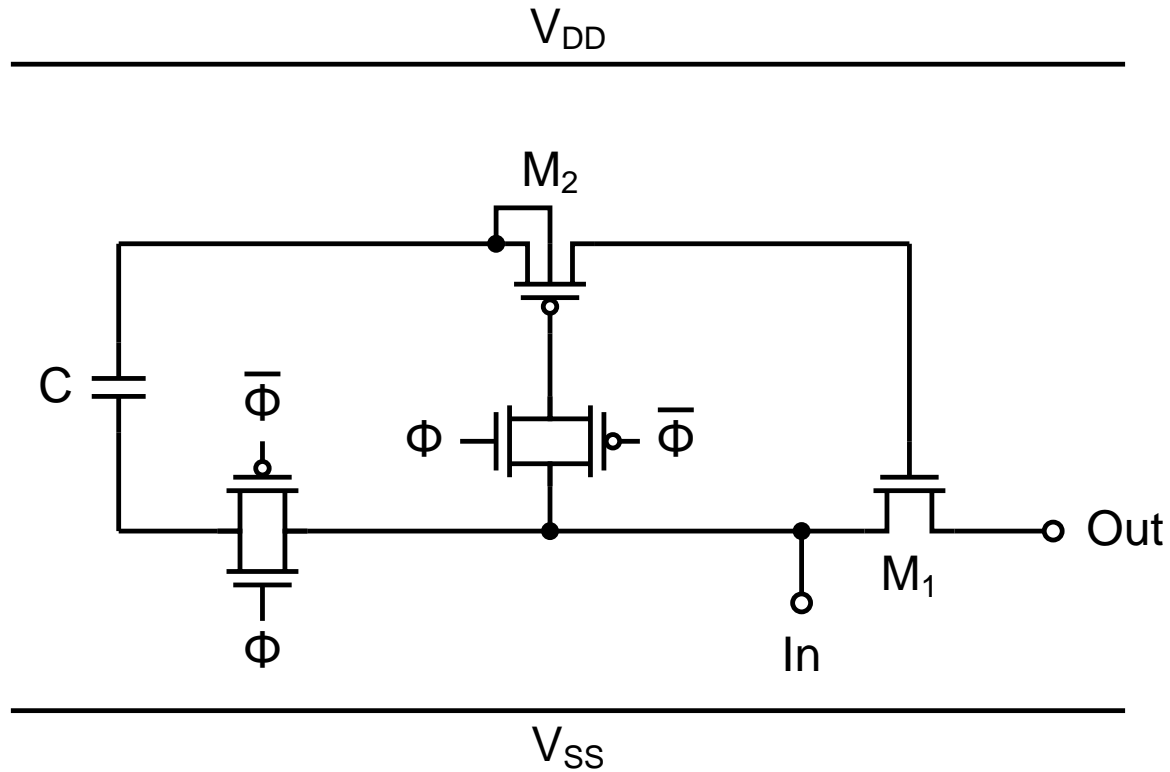


Ref: A. M. Abo and P. R. Gray, "A 1.5-V, 10-bit, 14.3-MS/s CMOS pipeline ADC,"  
*IEEE Journal of Solid-State Circuits*, vol. 34, issue 5, pp. 599-606, 1999.

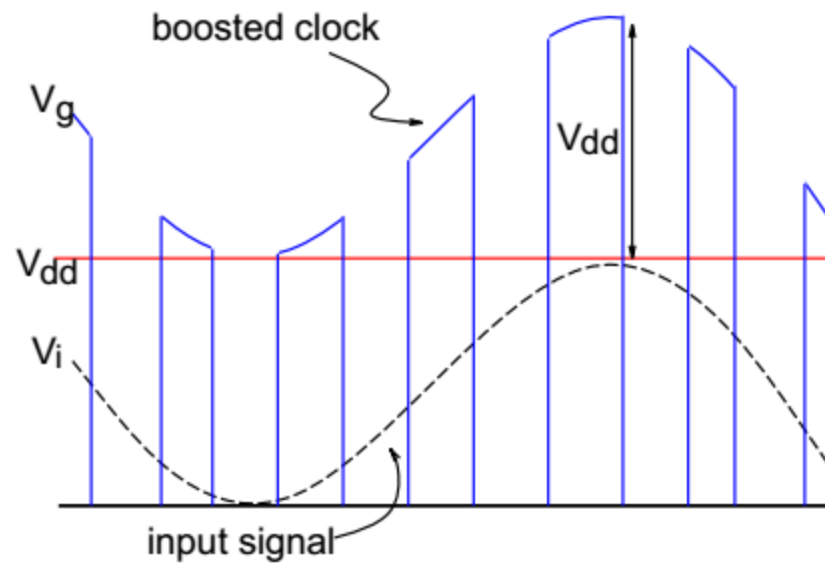
# Clock Bootstrapping ( $\Phi=0$ )



# Clock Bootstrapping ( $\Phi=1$ )

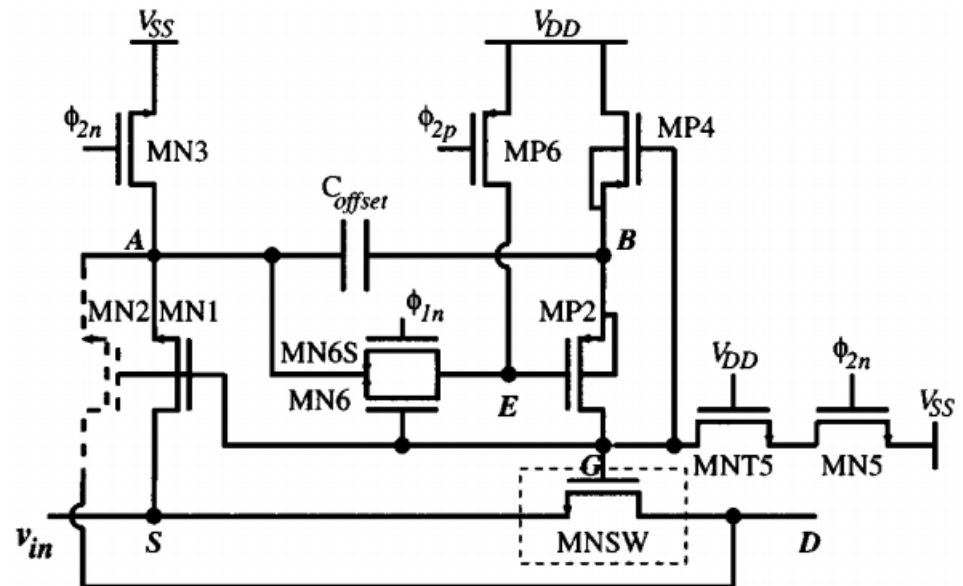
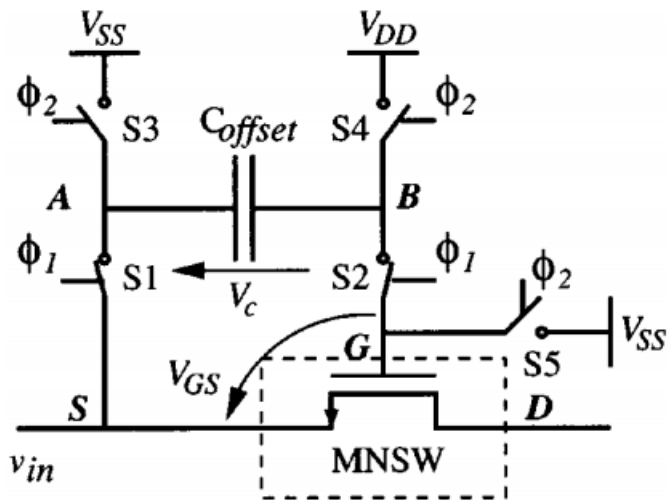


# Clock Bootstrapping



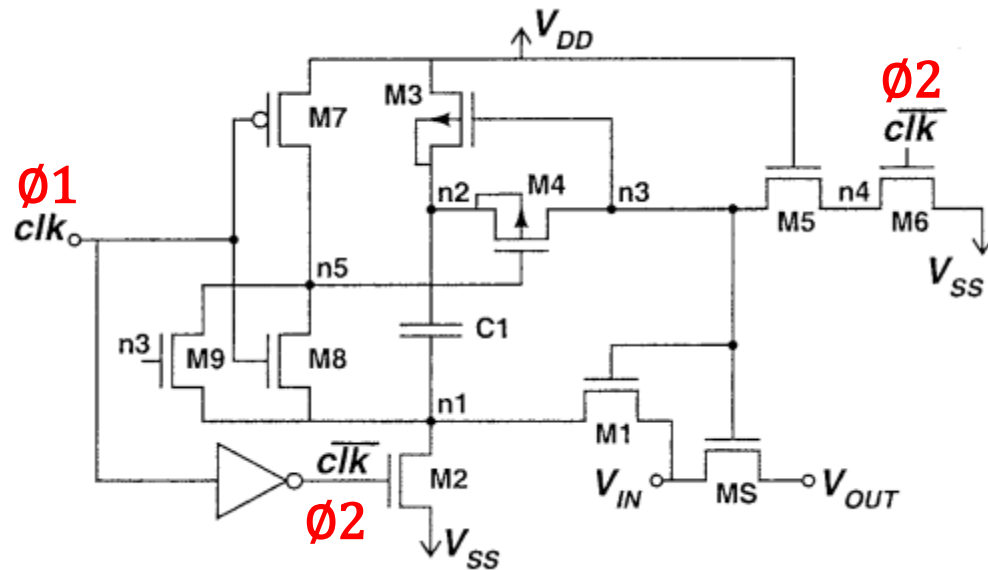
# Another Clock Bootstrap Circuit

Mohamed Dessouky and Andreas Kaiser, "Very Low-Voltage Digital-Audio  $\Delta\Sigma$  Modulator with 88-dB Dynamic Range Using Local Switch Bootstrapping,"  
*IEEE J. Solid-State Circuits*, vol. 36, pp. 349–355, Mar. 2001

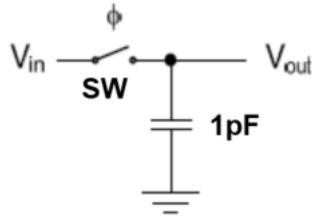


# Another Clock Bootstrap Circuit

M. Waltari, et.al., "A Self-Calibrated Pipeline ADC with 200 MHz IF-Sampling Frontend,"  
*Analog Integrated Circuits and Signal Processing*, vol. 37, pp. 201–213, 2003



# Homework #3 on 10-bit S/H



## SW types

- ideal\_swn from ee288lib
- CMOS TG – nmos2v & pmos2v
- Bootstrapped – nmos2v & pmos2v

VDD = 1.8V

- Sampling clock  $\phi$ ,  $f_s = 100$  MHz with 1.8V square wave.
- ideal\_clock in ee288lib
- Input sine wave signal range 0.4V ~ 1.4V
- Input signal frequency at  $f_{in} = (\text{cycles}/N) * f_s$   
where cycles=7 and N=64 for 64-point FFT

Summary of what you need to submit electronically:

1. Schematics of your design – use white background
2. Transient simulation results showing all relevant signal waveforms
3. FFT spectrum plots for different switch types
4. Summary table showing the ENOB, SNR, SFDR for all cases
5. Summary of what you learned on this homework problem