

# EE141-Spring 2010 Digital Integrated Circuits

Lecture 8 Wires Transistors

EECS141

Lecture #8

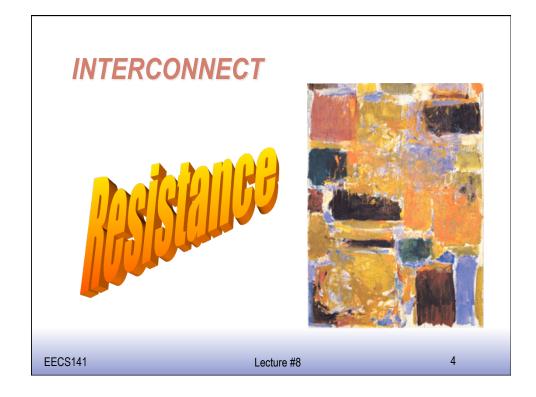
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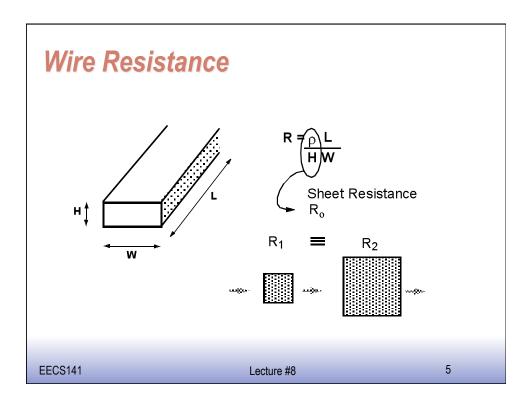
#### **Administrativia**

- □ Hw 3 due today HW 4 to be posted
- □ No Lab next week
- □ Extra review session Th at 6:30pm

#### **Class Material**

- □ Last lecture
  - Logical Effort + Wires
- □ Today's lecture
  - Wiring (cntd) Transistor models
- □ Reading (Ch 3, 4)



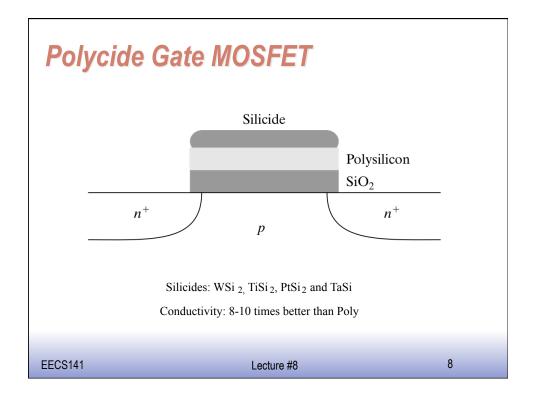


### Interconnect Resistance

Material	ρ (Ω-m)
Silver (Ag)	$1.6 \times 10^{-8}$
Copper (Cu)	$1.7 \times 10^{-8}$
Gold (Au)	$2.2 \times 10^{-8}$
Aluminum (Al)	$2.7 \times 10^{-8}$
Tungsten (W)	$5.5 \times 10^{-8}$

# **Dealing with Resistance**

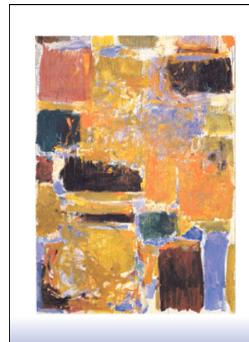
- Use Better Interconnect Materials
  - e.g. copper, silicides
- More Interconnect Layers
  - reduce average wire-length
- □ Selective Technology Scaling
  - (More later)



## **Sheet Resistance**

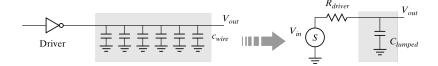
Material	Sheet Resistance (Ω/□)
n- or p-well diffusion	1000 - 1500
$n^+$ , $p^+$ diffusion	50 – 150
$n^+$ , $p^+$ diffusion with silicide	3 – 5
$n^+$ , $p^+$ polysilicon	150 – 200
$n^+$ , $p^+$ polysilicon with silicide	4 – 5
Aluminum	0.05 - 0.1

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# Interconnect Modeling

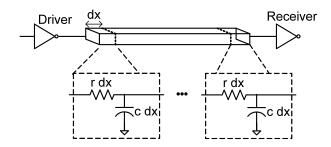
# The Lumped Model



What to do with the resistance?

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### The Distributed RC-line



- · Analysis method:
  - Break the wire up into segments of length dx
  - Each segment has resistance (r dx) and capacitance (c dx)

#### The Distributed RC-line

$$\bigvee_{in} \underbrace{r \ dx}_{c \ dx} \underbrace{r \ dx}_{c \ dx} \underbrace{\bigvee_{i+1} r \ dx}_{c \ dx} \underbrace$$

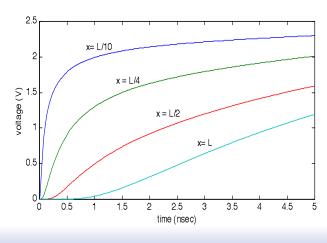
$$I_{C} = c\Delta L \frac{\partial V}{\partial t} = \frac{\left(V_{i-1} - V_{i}\right) - \left(V_{i} - V_{i+1}\right)}{r\Delta L} \longrightarrow rc\frac{\partial V}{\partial t} = \frac{\partial^{2}V}{\partial x^{2}}$$

The diffusion equation

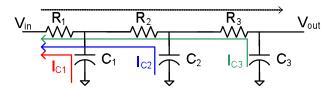
$$\tau = \frac{L^2}{2}rc$$

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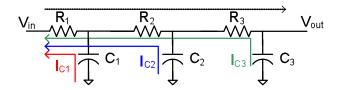
#### Simplified Model: Elmore Delay



- "Elmore delay": approximation for delay of arbitrary (complex) RC circuits
- To find "Elmore time constant":
  - For each capacitor, draw path of current from cap to input
  - $\bullet$  Multiply C by sum of R's on current path that are common with path from  $V_{in}$  to  $V_{out}$
  - Add up RC products from all capacitors

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#### Simplified Model: Elmore Delay



$$\tau_{Elmore} = R_1 C_1 + (R_1 + R_2) C_2 + (R_1 + R_2 + R_3) C_3$$

#### Wire Model

Model the wire with N equal-length segments:

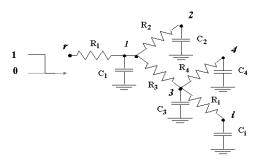
$$\tau_{DN} = \left(\frac{L}{N}\right)^2 (rc + 2rc + \dots + Nrc) = (rcL^2) \frac{N(N+1)}{2N^2} = RC \frac{N+1}{2N}$$

For large values of N:

$$\tau_{DN} = \frac{RC}{2} = \frac{rcL^2}{2}$$

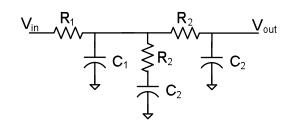
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#### Elmore Delay - Extended



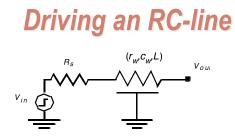
$$\begin{split} R_{ik} &= \sum R_j \Rightarrow (R_j \in [path(s \rightarrow i) \cap path(s \rightarrow k)]) \\ \tau_{Di} &= \sum_{k=1}^{N} C_k R_{ik} \end{split}$$

# Another Elmore Delay Example



$$au_{Elmore} =$$

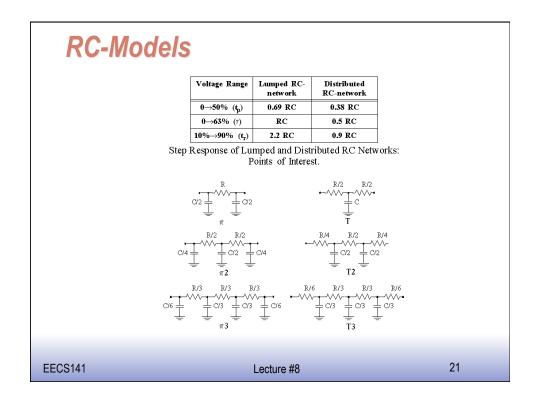
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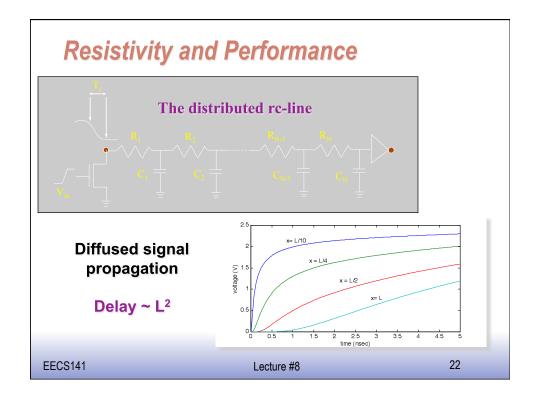


$$\tau_D = R_s C_w + \frac{R_w C_w}{2} = R_s C_w + 0.5 r_w c_w L^2$$

$$t_p = 0.69R_s C_w + 0.38R_w C_w$$

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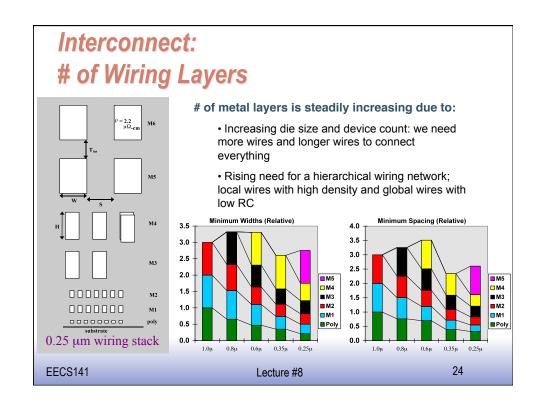


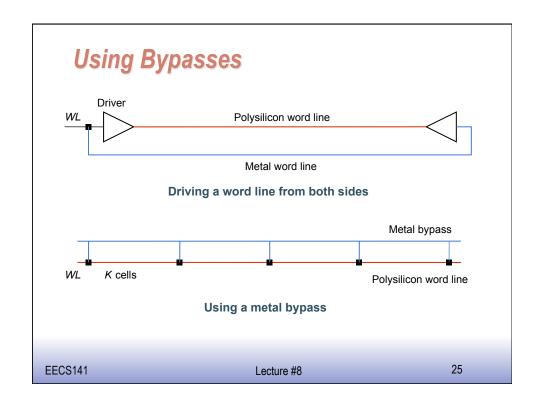
#### The Global Wire Problem

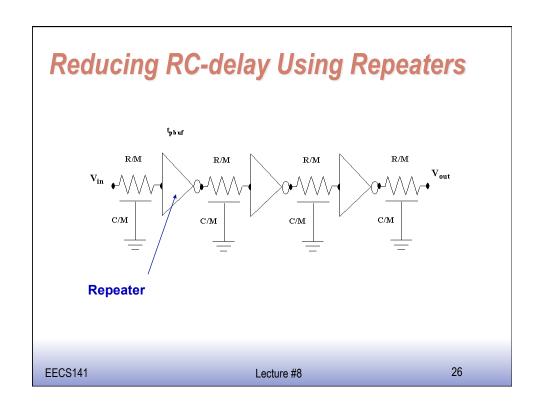
$$T_d = 0.377 R_w C_w + 0.693 (R_d C_{out} + R_d C_w + R_w C_{out})$$

#### **Challenges**

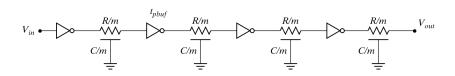
- □ No further improvements to be expected after the introduction of Copper (superconducting, optical?)
- Design solutions
  - Use of fat wires
  - Efficient chip floorplanning
  - Insert repeaters







#### Repeaters



$$t_p = m \left( 0.69 \frac{R_d}{s} \left( s \gamma C_d + \frac{cL}{m} + s C_d \right) + 0.69 \left( \frac{rL}{m} \right) \left( s C_d \right) + 0.38 rc \left( \frac{L}{m} \right)^2 \right)$$

$$\begin{split} m_{opt} = L \sqrt{\frac{0.38rc}{0.69R_dC_d(\gamma+1)}} = \sqrt{\frac{t_{pwire(unbuffered)}}{t_{p1}}} \\ s_{opt} = \sqrt{\frac{R_dc}{rC_d}} \end{split}$$

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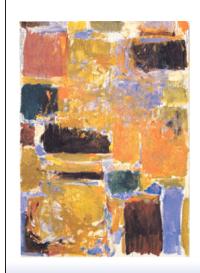
#### Repeater Insertion (Revisited)

Taking the repeater loading into account

$$\begin{split} m_{opt} &= L \sqrt{\frac{0.38rc}{0.69R_dC_d(\gamma+1)}} = \sqrt{\frac{t_{pwire(unbuffered)}}{t_{p1}}} \\ s_{opt} &= \sqrt{\frac{R_dc}{rC_d}} \end{split}$$

For a given technology and a given interconnect layer, there exists an optimal length of the wire segments between repeaters. The delay of these wire segments is independent of the routing layer!

$$L_{crit} = \frac{L}{m_{opt}} = \sqrt{\frac{t_{p1}}{0.38rc}} \qquad t_{p,\,crit} = \frac{t_{\dot{p},\,min}}{m_{opt}} = 2 \bigg( 1 + \sqrt{\frac{0.69}{0.38(1+\gamma)}} \bigg) t_{p1}$$

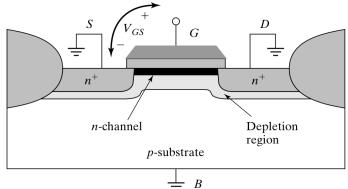


### **MOS Transistor**

What do digital IC designers need to know?

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# Threshold Voltage: Concept



- With positive gate bias, electrons pulled toward the gate
- With large enough bias, enough electrons will be pulled to "invert" the surface (p→n type)
- Voltage at which surface inverts: "magic" threshold voltage V<sub>T</sub>

# The Threshold Voltage

□ Threshold

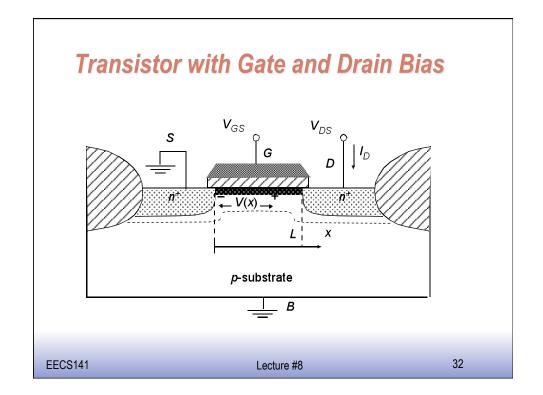
$$V_{T} = \varphi_{FB} + 2\varphi_{F} + \frac{Q_{B}}{C_{ox}} \leftarrow \text{Depletion charge}$$

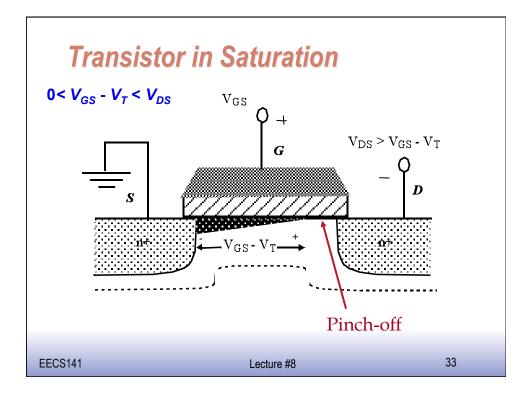
$$V_{T} = V_{T0} + \gamma \cdot \left( \sqrt{|2\varphi_{F} + V_{SB}|} - \sqrt{2\varphi_{F}} \right)$$

□ Fermi potential

$$\phi_F = \phi_T \cdot \ln \frac{N_A}{n_i}$$

 $2\Phi_F$  is approximately 0.6V for p-type substrates  $\gamma$  is the body factor  $V_{70}$  is approximately 0.45V for our process





#### Saturation

 $\square$  For  $(V_{GS} - V_T) \le V_{DS}$ , the effective drain voltage and current saturate:

$$V_{DS,eff} = \left(V_{GS} - V_{T}\right)$$

$$V_{DS,eff} = (V_{GS} - V_T)$$

$$I_D = \frac{k'_n}{2} \cdot \frac{W}{L} \cdot (V_{GS} - V_T)^2$$

- □ Of course, real drain current isn't totally independent of  $V_{\rm DS}$ 
  - For example, approx. for channel-length modulation:

$$I_D = \frac{k'_n}{2} \cdot \frac{W}{L} \cdot (V_{GS} - V_T)^2 \cdot (1 + \lambda \cdot V_{DS})$$

### **Modes of Operation**

**Cutoff:** 

$$V_{GS} - V_T < 0$$
  $I_D = 0$ 

Linear (Resistive):  

$$V_{GS} - V_T > V_{DS}$$
  $I_D = k_n' \cdot \frac{W}{L} \cdot \left[ (V_{GS} - V_T) \cdot V_{DS} - \frac{V_{DS}^2}{2} \right]$ 

Saturation:

$$0 < V_{GS} - V_T < V_{DS} \qquad I_D = \frac{k'_n}{2} \cdot \frac{W}{L} \cdot (V_{GS} - V_T)^2 \cdot (1 + \lambda \cdot V_{DS})$$

