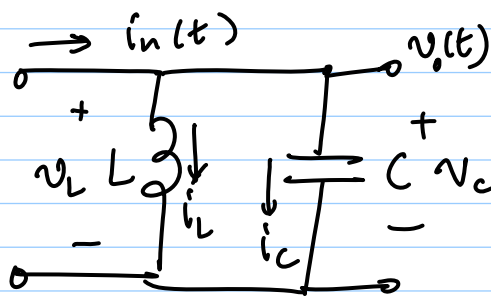


Lecture 32 : VCO Design

ISF



initially, $v_o(t)$ is

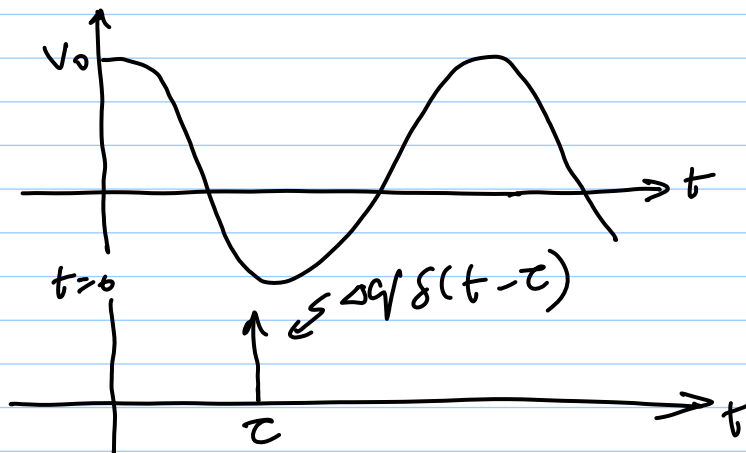
$$v_o(t) = V_o \cos \omega_0 t$$

current pulse @ τ

$$\Rightarrow i_{in}(t) = \Delta q \delta(t - \tau)$$

* Use superposition

because the system is linear



* Current pulse of

$$\Delta q \delta(t - \tau) \Rightarrow \text{charge}$$

of Δq is injected into LC tank

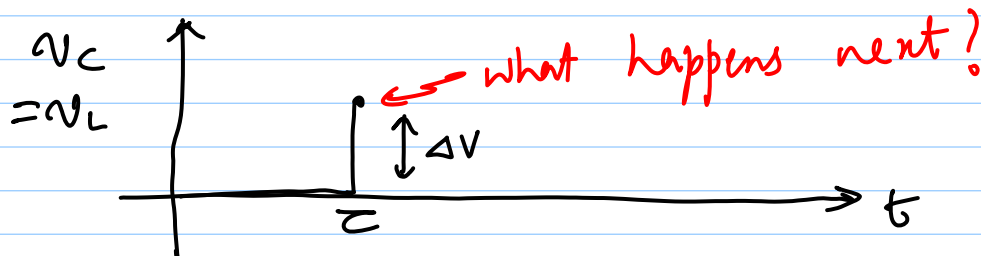
how does current pulse split between L & C?

\rightarrow if any portion of $i_{in}(t)$ pulse flows through L $\Rightarrow v_L = \infty$

\Rightarrow all of $i_{in}(t)$ flows through cap. C

$$i_C = C \frac{dv_C}{dt}$$

$\Rightarrow v_C$ experiences a voltage step due to $i_{in}(t)$

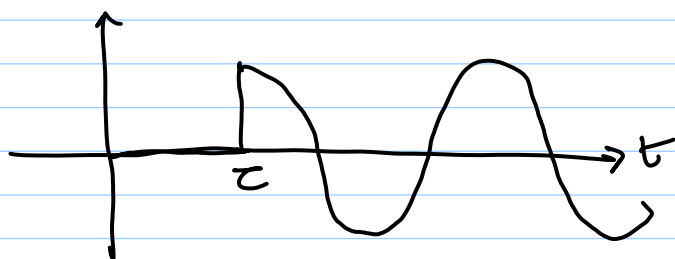


$$\text{charge } q = \int i_n(t) dt = Q_n$$

$$\Rightarrow \Delta q = C \Delta V \Rightarrow \boxed{\Delta V = \frac{\Delta q}{C}}$$

* this initial charge sets up oscillations in the LC system

→ energy slashes back & forth between L & C



$$v_2(t) = \Delta V \cos[\omega_0(t - \tau)]$$

$$v_0(t) = v_1(t) + v_2(t) \quad \{\text{superposition}\}$$

$$= V_0 \cos \omega_0 t + \Delta V \cos \omega_0(t - \tau)$$

$$v_0(t) = V_0 \cos \omega_0 t + \Delta V \cos \omega_0(t - \tau)$$

$$= V_0 \cos \omega_0 t + (\Delta V \cos \omega_0 \tau) \cdot \cos \omega_0 t$$

$$+ (\Delta V \sin \omega_0 \tau) \cdot \sin \omega_0 t$$

$$= (V_0 + \Delta V \cos \omega_0 \tau) \cos \omega_0 t$$

$$+ (\Delta V \sin \omega_0 \tau) \cdot \sin \omega_0 t$$

$$= V \cos(\omega_0 t + \phi)$$

$$V = \sqrt{(V_0 + \Delta V \cos \omega_0 \tau)^2 + (\Delta V \sin \omega_0 \tau)^2}$$

$$\phi = \tan^{-1} \left(\frac{\Delta V \sin \omega_0 \tau}{V_0 + \Delta V \cos \omega_0 \tau} \right)$$

(i) If $\tau = 0 \Rightarrow$ pulse injected @ peak of cosine

$$\sin \omega_0 \tau = 0, \cos \omega_0 \tau = 1$$

$$\Rightarrow V = (V_0 + \Delta V); \phi = 0$$

$$v_o(t) = (V_0 + \Delta V) \cos \omega_0 t$$

\Rightarrow amplitude change, no phase change

(ii) If $\tau = T/4 \Rightarrow$ pulse injected @ zero crossing

$$\sin \omega_0 \tau = 1, \cos \omega_0 \tau = 0$$

$$V = \sqrt{V_0^2 + \Delta V^2} \quad \leftarrow \text{ampl. change}$$

$$\phi = \tan^{-1} \left(\frac{\Delta V}{V_0} \right) \quad \leftarrow \text{phase change}$$

(iii) When is ϕ (phase change) maximum?

$$\phi = \text{max. when } \left. \begin{array}{l} \sin \omega_0 \tau = 1 \\ \cos \omega_0 \tau = 0 \end{array} \right\} \Rightarrow \tau = T/4$$

i.e. pulse injected @ zero-crossing causes max. phase-shift

negative $-g_m$ oscillator (cross-coupled)

$$* f_o = \frac{1}{2\pi\sqrt{LC}} \quad \checkmark$$

$$* V_o = \frac{2}{\pi} I_T R_p$$
$$\approx 0.64 I_T R_p \quad \times$$

$$* \text{Startup condition}$$
$$g_m R_p > 2 \text{ (easier)} \quad \checkmark$$

Colpitts Osc.

$$* f_o = \frac{1}{2\pi\sqrt{L\frac{C_1 C_2}{C_1 + C_2}}} \quad \checkmark$$

$$* V_o = 2 I_T (1 - \frac{1}{n}) R_p$$

$$\frac{1}{n} = \frac{C_2}{C_1 + C_2} \sim 0.2 \text{ for best PN}$$

$$\Rightarrow V_o \approx 1.6 I_T R_p \quad \checkmark$$

$$* \text{Startup condition}$$

$$g_m R_p \left(\frac{1}{n} - \frac{1}{n^2} \right) > 1$$

$$\Rightarrow g_m R_p (0.2 - 0.04) > 1$$

$$\Rightarrow g_m R_p > 6.25 \quad \times$$

-ve g_m Osc.

$$* \text{Tuning range} \quad \checkmark$$

NMOS - good

PMOS - ok

Compl. - ok

$$* \text{Good phase noise} \quad \checkmark$$

(but noise inj. @ zero cross)

$$* \text{differential} \quad \checkmark$$

Colpitts Osc.

$$* \text{Tuning Range poor} \quad \times$$

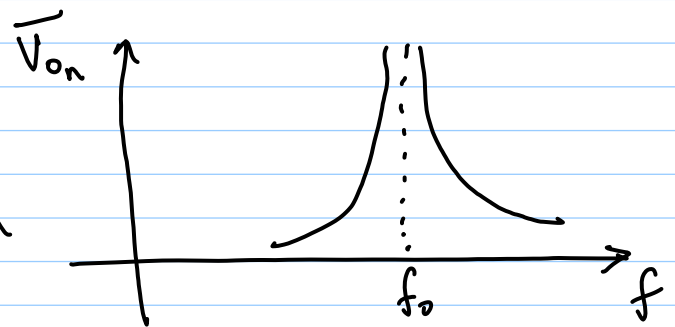
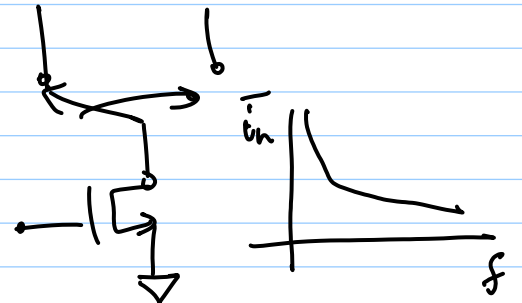
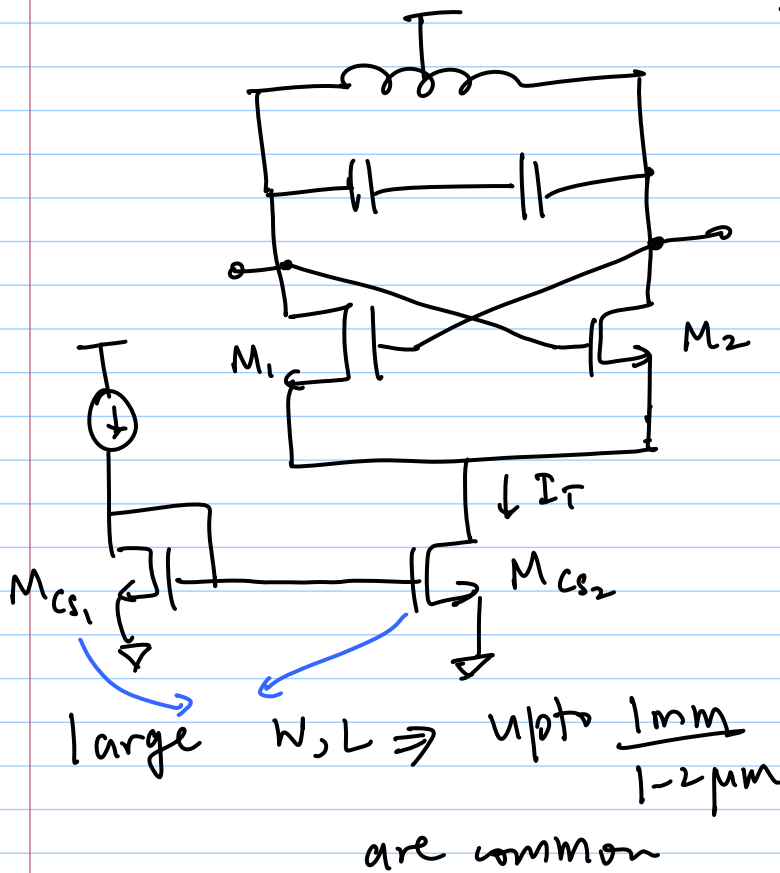
\rightarrow part of cap used to create C_1, C_2 feedback

$$* \text{Better PN (noise inj. @ voltage peaks)} \quad \checkmark$$

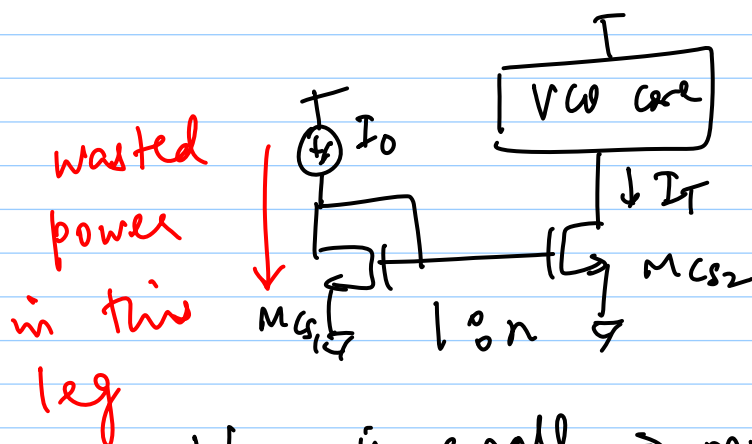
$$* \text{diff. form possible} \quad \checkmark$$

VCO biasing

- * $1/f$ noise up conversion
 \rightarrow tail CS to output
 \Rightarrow looks like a mixer



- * $1/f$ noise from both M_{CS1} & M_{CS2}
- * You may be tempted to have a large CM ratio

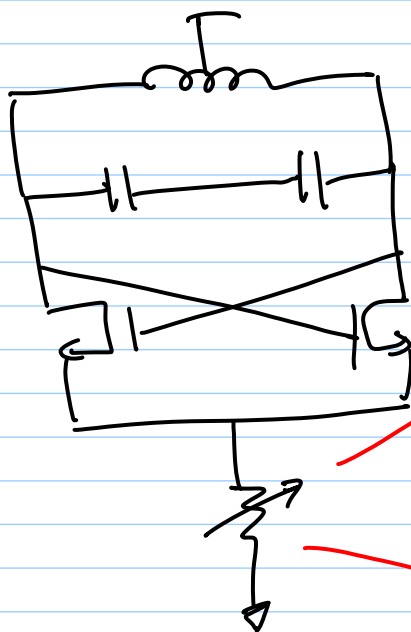


e.g. $I_T = 2\text{mA}$
 $I_0 = 20\mu\text{A}$ (1% of I_T)
 $n = 100$

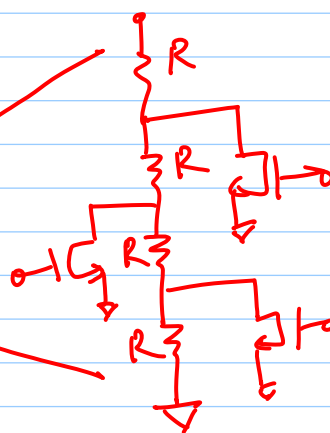
$$\frac{W_{CS1}}{W_{CS2}} = \frac{1}{100}$$

- * W_{CS1} is small \Rightarrow more $1/f$ noise
- * 1% CM ratio \Rightarrow $1/f$ noise gets multiplied
 \Rightarrow $1/f$ noise is dominated by M_{CS1} !

You may be tempted to do this:



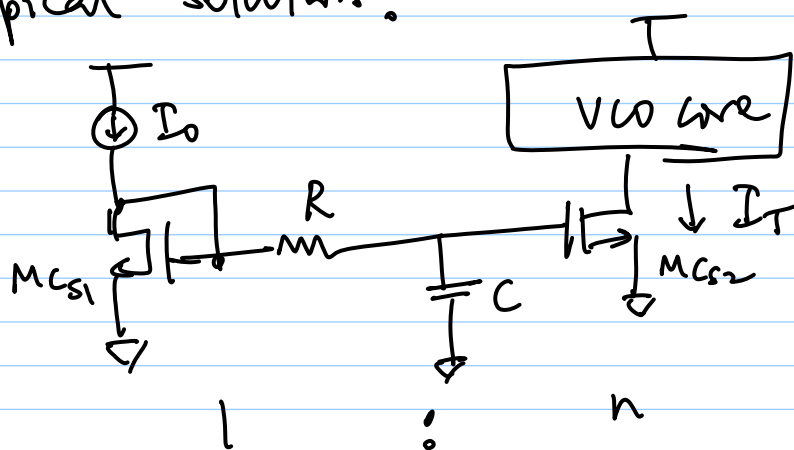
- * Bias can still be tuned
- * $1/f$ noise from CS absent



Problem: Bias current varies a lot over process

Problem: no rejection of common-mode noise from ground node

typical solution:



* $n = 100$
 $\Rightarrow I_D = 0.01 I_T$
 (no wastage of current)

* $1/f$ noise filtered by RC filter!

$$\left. \begin{array}{l} R = 2 \text{ M}\Omega \\ C = 400 \text{ pF} \end{array} \right\} f_{\text{BW}} = \frac{1}{2\pi RC} = 199 \text{ Hz}$$

\rightarrow low enough so $1/f$ noise does not matter

* Why not choose

$$R = 20\text{M}\Omega, C = 40\text{pF}?$$

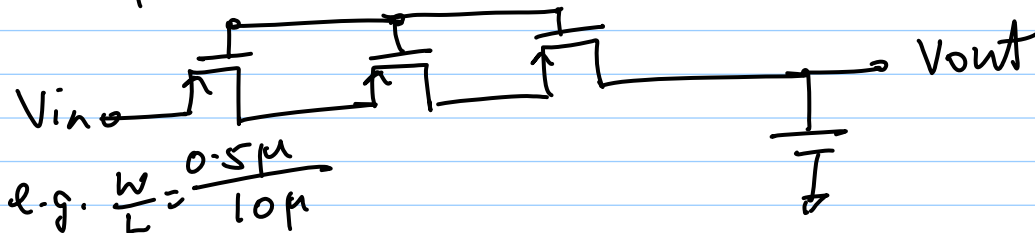
$$f_{\text{BW}} = 199\text{ Hz again}$$

→ Remember $\frac{kT}{C}$ noise!

→ you will see a noise hump which may end up at an inconvenient freq.

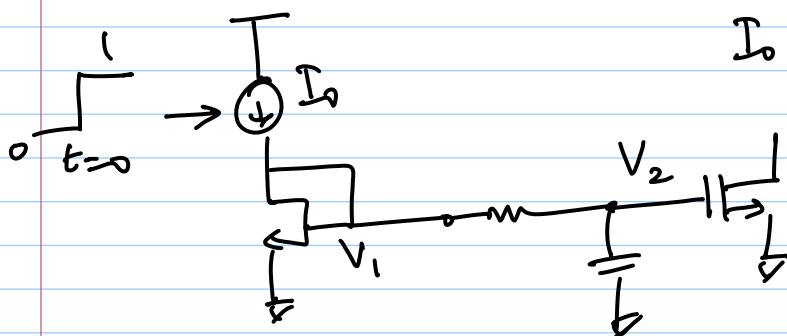
→ R area starts competing with C area

* Implement R with MOSFET (PMOS!)

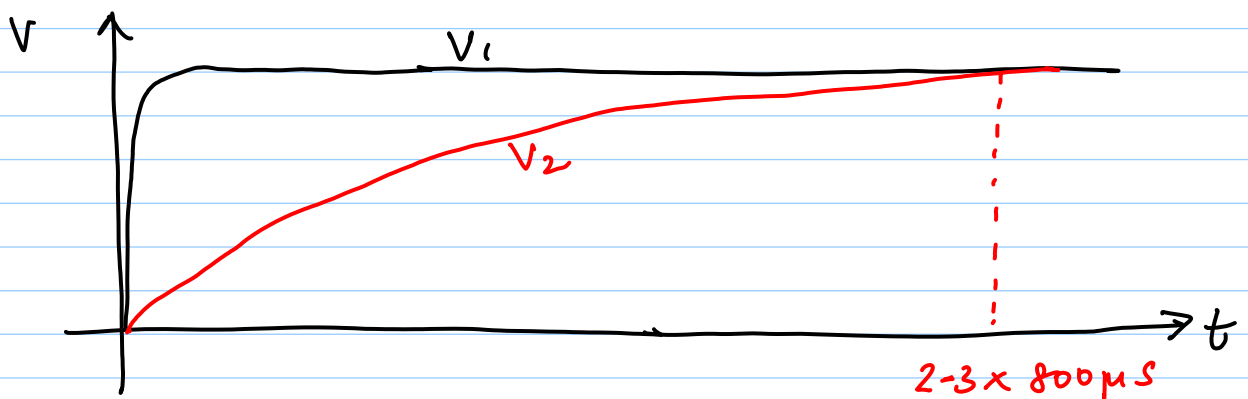


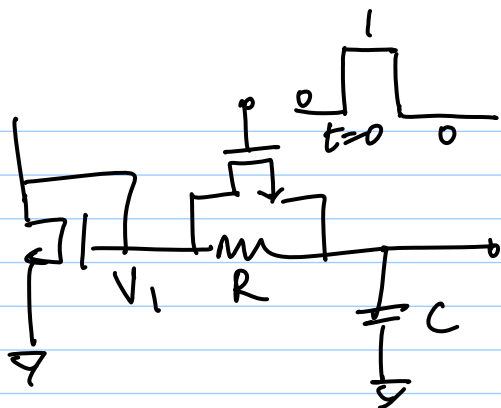
* leads to start-up problem!

$$\tau = RC = 800\mu\text{s}! \leftarrow \text{very large time constant}$$



I_0 turned on @ $t=0$



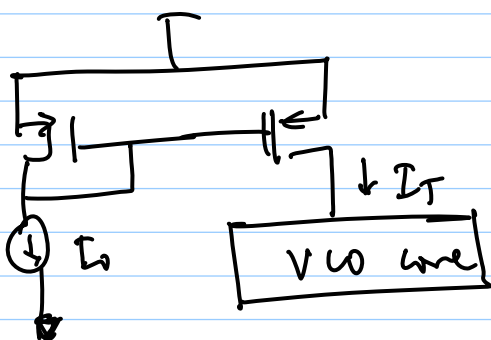


* bypass R till C is charged up (typically in 10-15ps)

* NMOS switch R matters!

* No need for PMOS here ($V_1 \sim 0.5-0.6V$)

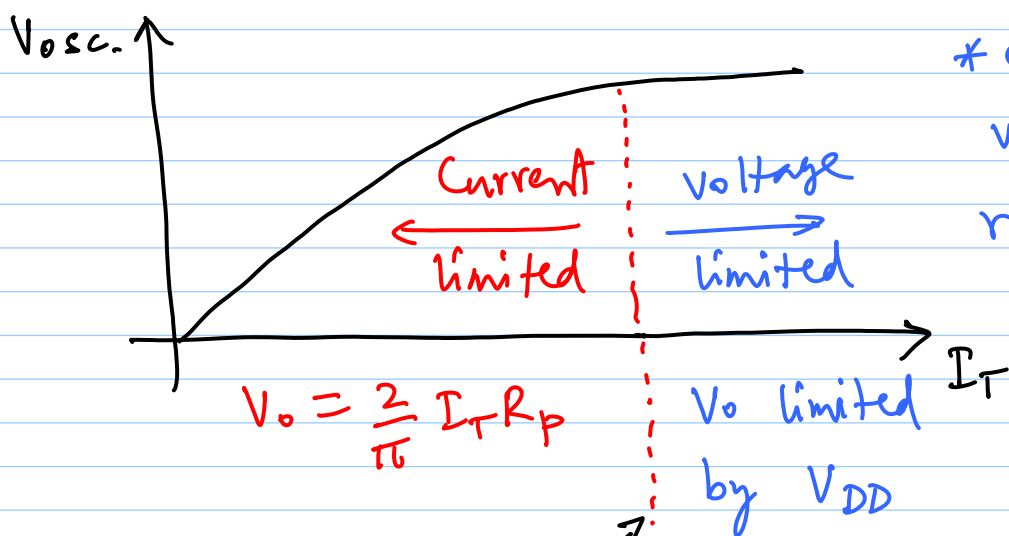
PMOS C-S.



* PMOS may have lower $1/f$ noise

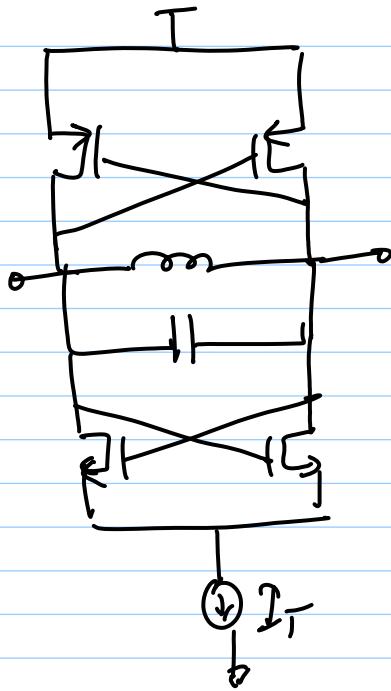
* But 3x as large for same headroom

VCO - regions of operation



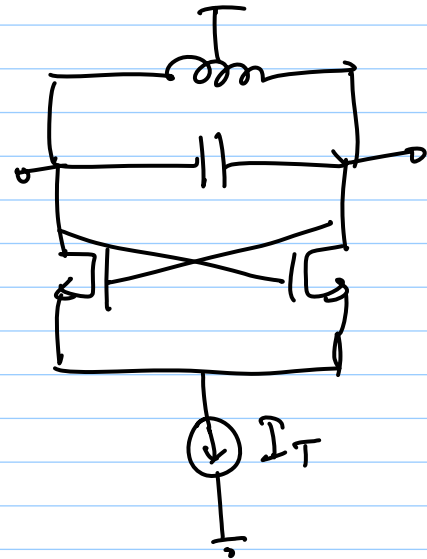
* extra power in voltage limited regime goes into
a) harmonics
b) noise

optimum operating point!



$$\rightarrow V_o = \frac{4}{\pi} I_T R_p$$

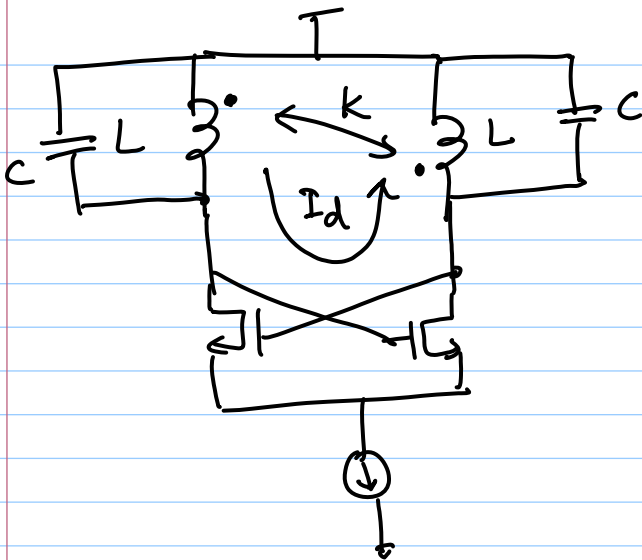
$$\rightarrow V_{o\max} \sim V_{DD}$$



$$\rightarrow V_o = \frac{2}{\pi} I_T R_p$$

$$\rightarrow V_o \text{ can swing above } V_{DD}$$

$$\rightarrow V_o(\max) \sim 2V_{DD}$$



I_d = differential current

$$k = \frac{M}{\sqrt{L_1 L_2}} \quad \left\{ \begin{array}{l} \text{coupling} \\ \text{factor} \end{array} \right\}$$

$$= \frac{M}{L} \text{ here}$$

we want max k ($0 \leq k \leq 1$)

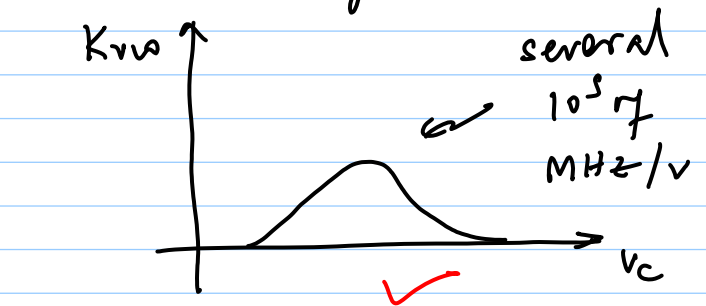
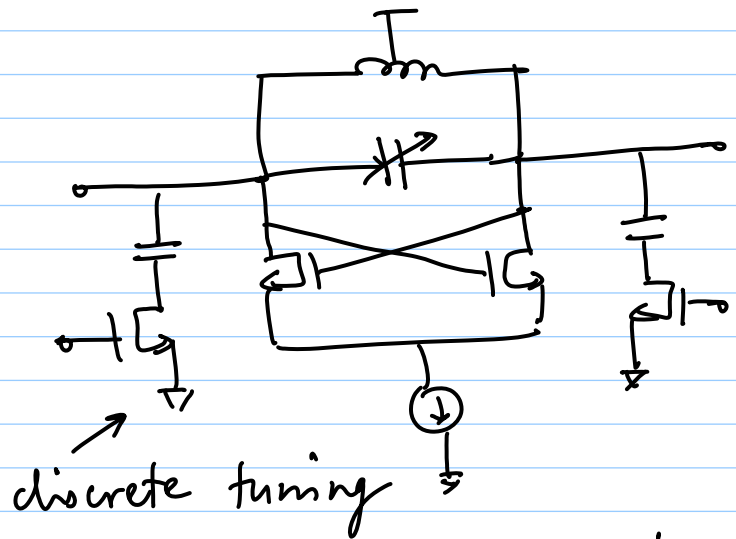
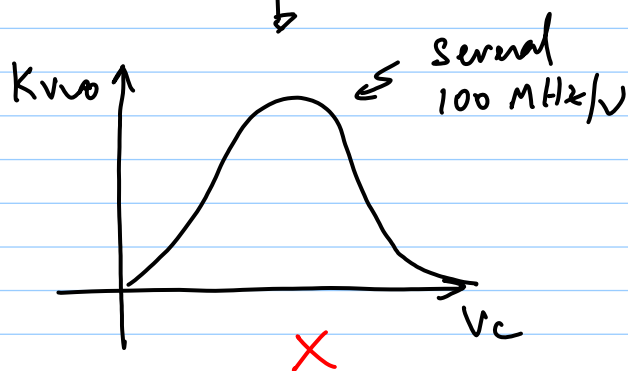
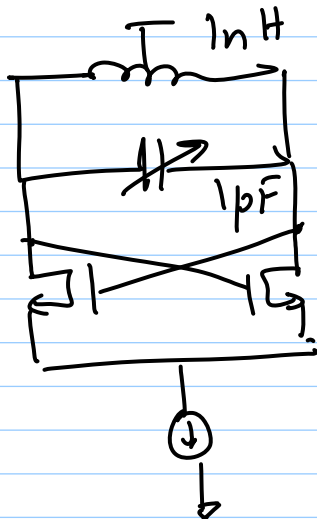
$$L_{\text{eff.}} = (L + M) = L(1+k)$$

$$Q_{\text{eff.}} = \frac{\omega_0 L_{\text{eff.}}}{\gamma} = \frac{\omega_0 L}{\gamma} (1+k) = Q(1+k)$$

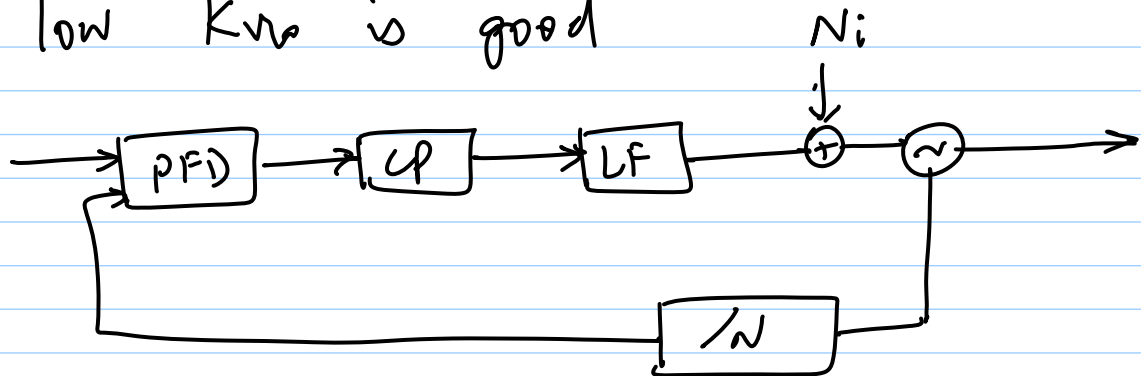
series res. of inductor

If $Q = 10$, you can almost double it to 20!

Tuning \rightarrow continuous (varactor)
 \rightarrow discrete (cap. bank)

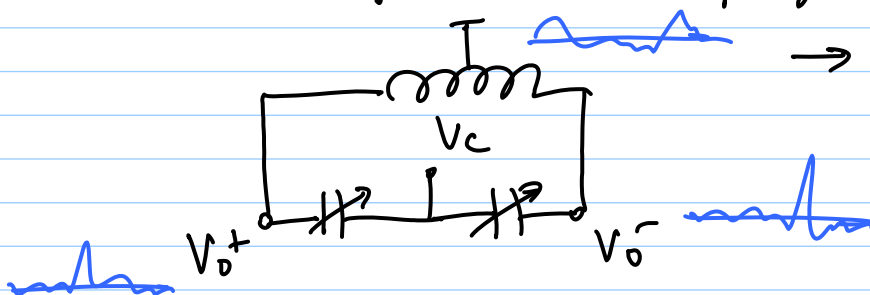


* low K_{vo} is good



\rightarrow noise or spurs coupling @ VCO input do not have a large gain to output

* Effects of noise coupling to A, B

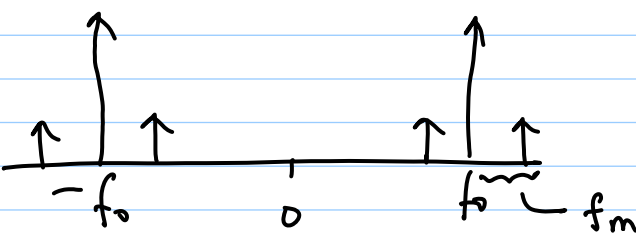


\rightarrow Varactor performs

AM-PM conversion

$$f_0 = \frac{1}{2\pi\sqrt{LC}}$$

$$V_{DD} = \text{[sinusoidal wave]} \quad \Leftarrow \quad f_m \ll f_0$$


$$V_{od} = \text{[discrete spectrum with multiple lines at } f_0 \pm f_m \text{]} \quad \Leftarrow \quad f_m \ll f_0$$


* Need overlap in discrete tuning (PVT variations)

