

# MT2002: Statistical Modeling

## Structure of a PyMC Model

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# Parts of a PyMC Model

A PyMC model consists of three core components:

## ① Priors:

- Capture prior knowledge or belief about model parameters.
- Example:  $\theta \sim \text{Beta}(1, 1)$  (uniform prior, no preference for heads or tails).
- Choosing Priors:
  - Use domain knowledge if available.
  - If uncertain, use non-informative or weakly informative priors.

## ② Likelihood:

- Models how data is generated given the parameters.
- Example:  $y \sim \text{Binomial}(n, \theta)$  for coin tosses.
- Choosing Likelihood:
  - Use the data-generating process (e.g., Binomial for binary data).

## ③ Inference Engine (Backend):

- Uses algorithms (e.g., MCMC) to sample from the posterior distribution.
- Handles the computation behind the scenes.
- PyMC automatically selects the method or allows you to customize it.

# Example: Coin Toss Inference with PyMC

**Task:** Estimate the probability of heads ( $\theta$ ) from 7 heads out of 10 tosses.

**Model:** *Notations book p-32*

- **Prior:**  $\theta \sim \text{Beta}(1, 1)$  (uniform distribution).
- **Likelihood:**  $y \sim \text{Binomial}(n = 10, p = \theta)$  (observed data: 7 heads).
- **Inference:** Sample from posterior  $P(\theta \mid \text{data})$  using MCMC.

## Python Code:

```
Observed data: 7 heads in 10 tosses data = [1, 1, 1, 1, 1, 1, 1, 0, 0, 0]
with pm.Model() as
    coin_toss_model: 1. Define Prior  $\theta = \text{pm.Beta}(\text{"theta"}, \alpha = 1, \beta = 1)$ 
    2. Define Likelihood  $y = \text{pm.Binomial}(\text{"y"}, n=10, p=\theta, \text{observed}=\text{data})$ 
    3. Perform Inference  $\text{trace} = \text{pm.sample}()$ 
    Visualize posterior distribution
     $\text{pm.plot\_posterior}(\text{trace}, \text{var\_names} = [\text{"theta"}])$ 
```

# Summary of PyMC Model

## What We Explored:

- **Structure of a PyMC Model:**

- **Priors:** Initial beliefs about parameters.
- **Likelihood:** Relates observed data to parameters.
- **Inference:** Sampling to compute the posterior distribution.

- **What the Model Does:**

- Combines priors and data via Bayes' theorem.
- Provides probabilistic estimates of unknown parameters.

- **What the Model Takes as Input:**

- Observed data (e.g., coin toss results).
- Prior distributions for unknown parameters.

- **What the Model Produces as Output:**

- Posterior distribution of parameters.
- Visualizations (e.g., posterior plots).

- **How It Produces the Output:**

- Uses an inference engine (e.g., MCMC sampling) to sample the posterior.
- Requires sufficient data to infer parameter values effectively.

# Let's create a basic pymc model!

Ready to explore PyMC in-depth?