

U T $D_o(\omega)$

$$\Sigma_\sigma = U \langle n_{\sigma'} \rangle$$

$$f(\omega, T) = \frac{1}{\exp(\omega/kBT)+1}$$

Occupation Fluctuation

$$\omega_n = \pi \frac{(2n+1)}{\beta}$$

$$\begin{aligned} \Sigma_{1,\sigma}(\omega/\omega_n) &= U \langle n_{\sigma'} \rangle \\ \Sigma_{2,\sigma}(\omega/\omega_n) &= 0 \end{aligned}$$

$$\delta_{\uparrow,\downarrow} \in [-1, 1]$$

$$\zeta_\sigma(\omega_n) = i\omega_n - \Sigma(\omega_n)$$

$$G_\sigma(\zeta_\sigma) = \zeta_{\sigma'} \int d\omega \frac{D_o(\omega)}{\zeta_\uparrow \zeta_\downarrow - \omega^2}$$

$$\mathcal{G}^{-1}(\omega_n) = G^{-1}(\omega_n) + \Sigma(\omega_n)$$

$$\Sigma_{\text{fluc},\sigma}(\delta_\uparrow, \delta_\downarrow) = \frac{1}{2} U (\langle n_{\sigma'} \rangle + \delta_{\sigma'})$$

$$G_{\text{loc}}^{-1}(\omega_n, \delta_\uparrow, \delta_\downarrow) = \mathcal{G}^{-1}(\omega_n) - \Sigma_{\text{fluc}}(\delta_\uparrow, \delta_\downarrow) - \Sigma_2(\omega_n)$$

$$S_{\text{eff}}(\delta_\uparrow, \delta_\downarrow) = -\sum_{\omega_n} \ln [\det (\mathcal{G}(\omega_n) G_{\text{loc}}^{-1}(\omega_n, \delta_\uparrow, \delta_\downarrow))]$$

$$G_{\text{average}}(\omega_n) = \frac{1}{2} \int d\delta_\uparrow \int d\delta_\downarrow \exp(-S_{\text{eff}}(\delta_\uparrow, \delta_\downarrow)) G_{\text{loc}}(\omega_n)$$

$$\Sigma(\omega_n) = \mathcal{G}^{-1}(\omega_n) - G_{\text{average}}^{-1}(\omega_n) \quad \zeta_\sigma(\omega_n) = i\omega_n - \Sigma(\omega_n)$$

$$G_\sigma(\zeta_\sigma) = \zeta_{\sigma'} \int d\omega \frac{D_o(\omega)}{\zeta_\uparrow \zeta_\downarrow - \omega^2}$$

$$\text{convg} = \int d\omega G_{\text{calc}}(\omega_n) - G_{\text{old}}(\omega_n) < \text{threshold}$$

$$\zeta_\sigma(\omega) = \omega_n + i\eta - \Sigma(\omega_n)$$

$$G_\sigma(\zeta_\sigma) = \zeta_{\sigma'} \int d\omega \frac{D_o(\omega)}{\zeta_\uparrow \zeta_\downarrow - \omega^2}$$

$$\mathcal{G}^{-1}(\omega) = G^{-1}(\omega) + \Sigma(\omega)$$

$$\Sigma_{\text{fluc},\sigma}(\delta_\uparrow, \delta_\downarrow) = \frac{1}{2} U (\langle n_{\sigma'} \rangle + \delta_{\sigma'})$$

$$G_{\text{loc}}^{-1}(\omega, \delta_\uparrow, \delta_\downarrow) = \mathcal{G}^{-1}(\omega) - \Sigma_{\text{fluc}}(\delta_\uparrow, \delta_\downarrow) - \Sigma_2(\omega)$$

$$G_{\text{average}}(\omega) = \frac{1}{2} \int d\delta_\uparrow \int d\delta_\downarrow \exp(-S_{\text{eff}}(\delta_\uparrow, \delta_\downarrow)) G_{\text{loc}}(\omega)$$

$$\Sigma(\omega) = \mathcal{G}^{-1}(\omega) - G_{\text{average}}^{-1}(\omega) \quad \zeta_\sigma(\omega) = \omega_n + i\eta - \Sigma(\omega_n)$$

$$D(\omega) = -\frac{1}{\pi} \text{Im} G(\omega)$$

$$\langle n_\sigma \rangle = \langle n_\sigma \rangle - \frac{1}{2} \sum_\sigma \langle n_\sigma \rangle \quad - \quad \langle n_\sigma \rangle = \int d\omega D_\sigma(\omega) f(\omega, T)$$

$$\begin{aligned} \Sigma_{1,\sigma}(\omega) &= U \langle n_{\sigma'} \rangle \\ \Sigma_2(\omega) &= -\text{hilbert.transform}(\text{Im}\Sigma(\omega)) + i\text{Im}\Sigma(\omega) \end{aligned}$$

$$G_\sigma(\zeta_\sigma) = \zeta_{\sigma'} \int d\omega \frac{D_o(\omega)}{\zeta_\uparrow \zeta_\downarrow - \omega^2}$$

$$D(\omega) = -\frac{1}{\pi} \text{Im} G(\omega)$$