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Basics of Neural Network Programming

Vectorizing Logistic Regression

Vectorizing Logistic Regression

$$\begin{aligned} \Rightarrow \underline{z^{(1)}} &= \underline{w^T x^{(1)} + b} \\ \Rightarrow \underline{a^{(1)}} &= \sigma(z^{(1)}) \end{aligned}$$

$$\begin{aligned} \underline{z^{(2)}} &= \underline{w^T x^{(2)} + b} \\ \underline{a^{(2)}} &= \sigma(z^{(2)}) \end{aligned}$$

$$\begin{aligned} \underline{z^{(3)}} &= \underline{w^T x^{(3)} + b} \\ \underline{a^{(3)}} &= \sigma(z^{(3)}) \end{aligned}$$

$$\underline{X} = \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ | & | & & | \\ | & | & & | \\ | & | & & | \end{bmatrix}$$

$$\begin{matrix} (n_x, m) \\ \mathbb{R}^{n_x \times m} \end{matrix}$$

$$\underline{w^T} \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ | & | & & | \\ | & | & & | \end{bmatrix}$$

$$\underline{Z} = \begin{bmatrix} z^{(1)} & z^{(2)} & \dots & z^{(m)} \end{bmatrix} = \underline{w^T X} + \begin{bmatrix} b & b & \dots & b \end{bmatrix}_{1 \times m} = \begin{bmatrix} \underline{w^T x^{(1)} + b} & \underline{w^T x^{(2)} + b} & \dots & \underline{w^T x^{(m)} + b} \end{bmatrix}_{1 \times m}$$

$$\Rightarrow \underline{Z} = \text{np.dot}(w.T, X) + \underline{b}$$

"Broadcasting"

$$\underline{A} = \begin{bmatrix} a^{(1)} & a^{(2)} & \dots & a^{(m)} \end{bmatrix} = \sigma(\underline{Z})$$



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Vectorizing Logistic Regression's Gradient Computation

Vectorizing Logistic Regression

$$dz^{(1)} = a^{(1)} - y^{(1)}$$

$$dz^{(2)} = a^{(2)} - y^{(2)}$$

.....

$$dZ = \begin{bmatrix} dz^{(1)} & dz^{(2)} & \dots & dz^{(m)} \end{bmatrix} \quad \leftarrow$$

$1 \times m$

$$A = [a^{(1)} \dots a^{(m)}], \quad Y = [y^{(1)} \dots y^{(m)}]$$

$$\rightarrow dZ = A - Y = \begin{bmatrix} a^{(1)} - y^{(1)} & a^{(2)} - y^{(2)} & \dots \end{bmatrix}$$

$$\rightarrow dw = 0$$

$$dw += \frac{x^{(1)} dz^{(1)}}{m}$$

$$dw += \frac{x^{(2)} dz^{(2)}}{m}$$

\vdots

$$dw /= m$$

$$db = 0$$

$$db += dz^{(1)}$$

$$db += dz^{(2)}$$

$$\vdots$$

$$db += dz^{(m)}$$

$$db /= m$$

$$db = \frac{1}{m} \sum_{i=1}^m dz^{(i)}$$

$$= \frac{1}{m} \text{np.sum}(dZ)$$

$$dw = \frac{1}{m} X dZ^T$$

$$= \frac{1}{m} \begin{bmatrix} x^{(1)} & \dots & x^{(m)} \\ 1 & & 1 \end{bmatrix} \begin{bmatrix} dz^{(1)} \\ \vdots \\ dz^{(m)} \end{bmatrix}$$

$$= \frac{1}{m} \left[\underbrace{x^{(1)} dz^{(1)}}_{n \times 1} + \dots + \underbrace{x^{(m)} dz^{(m)}}_{n \times 1} \right]$$

Implementing Logistic Regression

$J = 0, dw_1 = 0, dw_2 = 0, db = 0$

for $i = 1$ to m :

$$z^{(i)} = w^T x^{(i)} + b \leftarrow$$

$$a^{(i)} = \sigma(z^{(i)}) \leftarrow$$

$$J += -[y^{(i)} \log a^{(i)} + (1 - y^{(i)}) \log(1 - a^{(i)})]$$

$$dz^{(i)} = a^{(i)} - y^{(i)} \leftarrow$$

$$\left[\begin{array}{l} dw_1 += x_1^{(i)} dz^{(i)} \\ dw_2 += x_2^{(i)} dz^{(i)} \end{array} \right] \quad dw += x^{(i)} * dz^{(i)}$$

$$db += dz^{(i)}$$

$$J = J/m, dw_1 = dw_1/m, dw_2 = dw_2/m$$

$$db = db/m$$

for iter in range(1000): \leftarrow

$$Z = w^T X + b$$

$$= \text{np.dot}(w.T, X) + b$$

$$A = \sigma(Z)$$

$$dZ = A - Y$$

$$dw = \frac{1}{m} X dZ^T$$

$$db = \frac{1}{m} \text{np.sum}(dZ)$$

$$w := w - \alpha dw$$

$$b := b - \alpha db$$