Cheat Sheet ICPC

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Cheat Sheet ICPC Versi Satu Titik Nol

1 Dijkstra

```
int main () {
   int n.m:
   cin >> n >> m;
   vector<pii> adj[10005];
   for (int i=1;i<=m;i++) {
   int x,y,w;
   cin >> x >> y >> w;
   adj[x].pb(mp(w,y));
   int s,e;
   cin >> s >> e;
   priority_queue<pii,vector<pii>,greater<pii> > d;
   int vis[10005];
   for (int i=1;i<=n;i++) vis[i]=INT_MAX;</pre>
   vis[s]=0;
   d.push(mp(0,s));
   while (!d.empty()) {
   pii cur=d.top();
   d.pop();
   for (int i=0;i<adj[cur.se].size();i++) {</pre>
     pii next=adj[cur.se][i];
     if (vis[cur.se]+next.fi<vis[next.se]) {</pre>
       vis[next.se]=vis[cur.se]+next.fi;
       d.push(mp(vis[next.se],next.se));
     }
   }
   if (vis[e]==INT_MAX) cout << "NO" << endl; else cout <<</pre>

    vis[e] << endl;
</pre>
   return 0;
```

2 MST

```
int main () {
   int n,m;
   cin >> n>> m:
   vector<pii> adj[10005];
   for (int i=1;i<=m;i++) {
     int u,v,w;
     cin >> u >> v >> w;
     adj[u].pb(mp(w,v));
     adj[v].pb(mp(w,u));
   bool MST[10005]:
   memset (MST,0,sizeof(MST));
   int vis[10005];
   for (int i=1;i<=n;i++) vis[i]=INT_MAX;
   priority_queue<pii,vector<pii>,greater<pii> > pq;
   pq.push(mp(0,1));
   vis[1]=0;
   while (!pq.empty()) {
     pii cur=pq.top();
     pq.pop();
     MST[cur.se]=1;
     for (int i=0;i<adj[cur.se].size();i++) {
       pii next=adj[cur.se][i];
       if (!MST[next.se]&&vis[next.se]>next.fi) {
        vis[next.se] = next.fi;
        pq.push(next);
   for (int i=1;i<=n;i++) cout << vis[i] << "_{\sqcup}";
```

3 Knapsack

```
int n,v[n+5],w[n+5],cap,dp[n+5];
int solve(int posi, int rem) {
  if (posi==0||rem==0) return 0;
  if (dp[posi][rem]!=-1) return dp[posi][rem];
  int ret=solve(posi-1,rem);
  if (rem>=w[posi]) ret=max(ret,solve(posi-1,rem-w[posi])+v
      → [posi]);
  dp[posi][rem]=ret;
  return ret;
int main () {
  cin >> n;
  for (int i=1;i<=n;i++) cin >> v[i];
 for (int i=1;i<=n;i++) cin >> w[i];
  memset (dp,-1,sizeof(dp));
  cout << solve(n,cap) << endl;</pre>
 return 0:
```

4 Coin Change

5 Negative Cycle Detection

```
int main () {
 int n,m;
  cin >> n >> m;
  vector<pair<int,int>,int> > edge;
 for (int i=1;i<=m;i++) {
   int u, v, w;
   cin >> u >> v >> w:
    \texttt{edge.pb(mp(mp(u,v),w));}
  int dist[35];
  for (int i=1;i<=n;i++) dist[i]=123456789;
  bool y=0;
  dist[1]=0;
  for (int i=1;i< n;i++) {
   for (int j=0; j \le m; j++) {
     \label{eq:condition} \mbox{if } (\mbox{dist[edge[j].fi.fi]+edge[j].}
       dist[edge[j].fi.se]=dist[edge[j].fi.fi]+edge[j].se;
   }
 }
 for (int i=0;i< m;i++) {
   if (dist[edge[i].fi.se]>dist[edge[i].fi.fi]+edge[i].se)
   }
```

```
if (y) cout << "ada_negative_cycle" << endl;
return 0;
}</pre>
```

6 Toposort

```
stack<int> ans;
int vis[105];
bool cycle=0;
vector<int> adj[105];
void toposort(int x) {
  vis[x]=1;
 for (int j=0; j<adj[x].size(); j++) {
   if (vis[adj[x][j]]==0) {
     vis[adj[x][j]]=1;
     toposort(adj[x][j]);
   } else if (vis[adj[x][j]]==1) cycle=1;
  ans.push(x);
  vis[x]=2;
}
int main () {
   int n,m;
    cin >> n >> m;
   for (int i=1;i<=m;i++) {
     int x,y;
     cin >> x >> y;
     adj[x].pb(y);
   memset (vis,0,sizeof(vis));
   for (int i=1;i \le n;i++) {
     if (!vis[i]) toposort(i);
   if (cycle) cout << "Ada_Cycle" << endl;</pre>
   else {
     while (!ans.empty()) {
       cout << ans.top() <<"u";
       ans.pop();
    return 0;
```

7 a/b mod m

```
LL gcd(LL a,LL b, LL &x, LL &y) {
 if (a==0) {
   x=0:
   y=1;
   return b;
 LL x1,y1;
 LL d=gcd(b\%a,a,x1,y1);
 x=y1-(b/a)*x1;
 y=x1;
 return d;
LL inverse_modulo(LL a,LL m) {
 LL x,y;
 LL ans=gcd(a,m,x,y);
 return (x%m + m)%m;
int main () {
   LL n,k,m;
   cin >> n >> k >> m;
   LL up=1;
   for (LL i=n;i>n-k;i--) {
     up*=i;
```

```
up%=m;
}
//cout << up << endl;
LL down=1;
for (LL i=1;i<=k;i++) {
    down*=i;
    down%=m;
}
//cout << down << endl;
LL im=inverse_modulo(down,m);
if (im<0) im+=m;
//cout << im << endl;
cout << ((up%m)*(im%m))%m << endl;
return 0;
}</pre>
```

8 Sieve of Erastothenes

```
bitset<10000005> prima;

void sieve(int n) {
   prima.set(); //ubah semua jadi 1
   prima[0]=0;
   prima[1]=0;
   for (int i=2;i*i<=n;i++) {
      if (prima[i]) {
        for (int j=i*i;j<=n;j+=i) {
            prima[j]=0;
        }
      }
   }
}</pre>
```

9 Modified Sieve

10 Fast Expo

11 0-1 BFS

```
int n,m;
int x[4]=\{1,0,-1,0\};
int y[4]={0,-1,0,1};
int vis[1005][1005];
char a[1005][1005];
bool inside(int a,int b) {
 if (a>=1&&a<=n&&b>=1&&b<=m) return 1;</pre>
  else return 0;
int main () {
   ios_base::sync_with_stdio(false);
   cin.tie(NULL);
   cout.tie(NULL);
   cin >> n >> m;
   for (int i=1;i \le n;i++) {
     string s;
     cin >> s;
     for (int j=1;j<=m;j++) {
       a[i][j]=s[j-1];
       vis[i][j]=INT_MAX;
   }
   deque<pii> q;
   q.push_front(mp(1,1));
   vis[1][1]=0;
   while (!q.empty()) {
     pii cur=q.front();
     q.pop_front();
     for (int p=0; p<4; p++) {
       int nx=cur.fi+x[p],ny=cur.se+y[p];
       if (inside(nx,ny)&&vis[nx][ny]>vis[cur.fi][cur.se])
         if (a[nx][ny]==a[cur.fi][cur.se]) { //cost=0
           vis[nx][ny]=vis[cur.fi][cur.se];
           q.push_front(mp(nx,ny));
         } else if (a[nx][ny]!=a[cur.fi][cur.se]){ //cost=1
           vis[nx][ny]=vis[cur.fi][cur.se]+1;
           q.push_back(mp(nx,ny));
       }
     }
   cout << vis[n][m] << endl;</pre>
   return 0:
```

12 LCS

```
int n,m,dp[5005][5005];
string a,b;
int LCS(int p,int q) {
 if (p<=0||q<=0) return 0;
 if (dp[p][q]!=-1) return dp[p][q];
 if (a[p-1]==b[q-1]) return dp[p][q]=LCS(p-1,q-1)+1;
 else return dp[p][q]=max(LCS(p-1,q),LCS(p,q-1));
int main () {
   ios_base::sync_with_stdio(false);
   cin.tie(NULL):
   cout.tie(NULL);
   cin >> n >> m;
   cin >> a >> b;
   memset (dp,-1,sizeof(dp));
   int ans=LCS(n,m);
   string answer="";
   while (n>0&&m>0) {
     if (a[n-1]==b[m-1]) {
       answer+=a[n-1];
```

13 LPS

```
LPS = LCS antara string dan reverse stringnya.
```

14 Random

```
srand(time(NULL)); //HARUS ADA
// generate random numbers between [a,b)
rand() % (b - a) + a;
// generate random numbers between [0,b)
rand() % b;
// generate random permutations
random_permutation(anArray, anArray + 10);
random_permutation(aVector, aVector + 10);
```

15 Prime number < 100

```
2, 3, 5, 7, 11,
13, 17, 19, 23, 29,
31, 37,41, 43, 47,
53, 59, 61, 67, 71,
73, 79, 83, 89, 97
```

16 Leap Year

```
bool isLeap(int n)
{
   if (n%100==0)
      if (n%400==0) return true;
      else return false;
   if (n%4==0) return true;
   else return false;
}
```

17 Generate Combinations

```
// n>=m, choose M numbers from 1 to N.
void combination(int n, int m)
{
    if (n<m) return;
    int a[50]={0};
    int k=0;
    for (int i=1;i<=m;i++) a[i]=i;
    while (true) {
        for (int i=1;i<=m;i++)
            cout << a[i] << "\ldot";
        cout << endl;
        k=m;
        while ((k>0) && (n-a[k]==m-k)) k--;
        if (k==0) break;
        a[k]++;
        for (int i=k+1;i<=m;i++)</pre>
```

```
a[i]=a[i-1]+1;
}
}
```

18 Binomial Coefficient

```
#define MAXN 100 // largest n or m
long long bc[MAXN] [MAXN]; //bc[n][r]=nCr
void binomial_coefficient(int n) {
   for (int i=0; i<=n; i++) bc[i][0] = 1;
   for (int j=0; j<=n; j++) bc[j][j] = 1;
   for (int i=1; i<=n; i++)
   for (int j=1; j<i; j++)
       bc[i][j] = bc[i-1][j-1] + bc[i-1][j];
}</pre>
```

19 Bignum Multiplication - JAVA

```
// fast algorithm to find multiplication of two big numbers
import java.math.BigInteger;
import java.util.Random;
class Karatsuba {
       private final static BigInteger ZERO = new
            → BigInteger("0");
       public static BigInteger karatsuba(BigInteger x,
            → BigInteger y)
              int N = Math.max(x.bitLength(), y.bitLength
              if (N <= 2000) return x.multiply(y);</pre>
              N=(N/2)+(N %2);
              BigInteger b = x.shiftRight(N);
              BigInteger a = x.subtract(b.shiftLeft(N));
              BigInteger d = y.shiftRight(N);
              BigInteger c = y.subtract(d.shiftLeft(N));
              BigInteger ac = karatsuba(a, c);
              BigInteger bd = karatsuba(b, d);
              BigInteger abcd = karatsuba(a.add(b), c.add(
                   \hookrightarrow d));
              return ac.add(abcd.subtract(ac).subtract(bd)
                   → .shiftLeft(N)).add(bd.shiftLeft(2*N)
                   \hookrightarrow );
       public static void main(String[] args)
              long start, stop, elapsed;
              Random random = new Random();
              int N = Integer.parseInt(args[0]);
              BigInteger a = new BigInteger(N, random);
              BigInteger b = new BigInteger(N, random);
              start = System.currentTimeMillis();
              BigInteger c = karatsuba(a, b);
              stop = System.currentTimeMillis();
              System.out.println(stop - start);
              start = System.currentTimeMillis();
              BigInteger d = a.multiply(b);
              stop = System.currentTimeMillis();
              System.out.println(stop - start);
              System.out.println((c.equals(d)));
       }
```

20 Euler totient function

Application: $a^{\varphi(n)} \equiv 1 \pmod{n}$ kalau a dan m koprima

21 Longest increasing common sequence (LICS)

```
int a[100];
int b[100]:
int f[100];
int n=0, m=0;
int main() {
       cin >> n;
       for (int i=1;i<=n;i++) cin >> a[i];
       cin >> m:
       for (int i=1;i<=m;i++) cin >> b[i];
       for (int i=1;i<=n;i++) {
               int k=0;
               for (int j=1;j<=m;j++) {
                       if (a[i]>b[j] && f[j]>k) k=f[j];
                       else if (a[i]==b[j] \&\& k+1>f[j]) f[j]
                            \hookrightarrow ]=k+1;
       int ans=0:
       for (int i=1;i<=m;i++)
               if (f[i]>ans) ans=f[i];
       cout << ans << endl:
       return 0;
```

22 LIS

```
int n=0:
int a[100], f[100], x[100];
int main() {
       cin >> n;
        for (int i=1;i<=n;i++) {
               cin >> a[i];
               x[i]=INT_MAX;
       f[0]=0;
       int ans=0;
       for(int i=1;i<=n;i++) {
               int 1=0, r=i;
               while (l+1<r) {
                       int m=(1+r)/2;
                       if (x[m]<a[i]) l=m; else r=m;
                       // change to x[m] \le a[i] for non-
                            \hookrightarrow decreasing case
               f[i]=1+1;
               x[1+1]=a[i];
               if (f[i]>ans) ans=f[i];
        cout << ans << endl;
       return 0;
```

23 Max sum rectangle

```
int a[150][150]={0};
int c[200]={0};
int maxarray(int n) {
       int b=0, sum=-100000000;
       for (int i=1;i<=n;i++) {
               if (b>0) b+=c[i];
               else b=c[i];
               if (b>sum) sum=b;
       }
       return sum;
int maxmatrix(int n) {
       int sum=-100000000, max=0;
       for (int i=1;i<=n;i++) {
               for (int j=1; j <=n; j++)
                       c[j]=0;
               for (int j=i;j \le n;j++) {
                       for (int k=1; k \le n; k++)
                              c[k] += a[j][k];
                       max=maxarray(n);
                       if (max>sum) sum=max;
       return sum;
int main() {
       int n=0;
       cin >> n:
       for (int i=1;i<=n;i++)
               for (int j=1; j<=n; j++)
                       cin >> a[i][j];
       cout << maxmatrix(n);</pre>
       return 0;
}
```

24 Floyd Warshall

25 LCA+RMQ

A weighted tree is given. You must find the distance between two given nodes. Input The first line contains the number of nodes of the tree n (1 n 50000). The nodes are numbered from 0 to n 1. Each of the next n 1 lines contains three integers u, v, w, which correspond to an edge with weight w (0 w 1000) connecting nodes u and v. The next line contains the number of queries m (1 m 75000). In each of the next m lines there are two integers. Output For each range minimum query, output the distance between the nodes with the given numbers.

```
struct Graph {
    struct Edge {
        int to;
        int len;
    };

    const static int MAXNODE = 1 * 1e5 + 2;

    vector<int> g[MAXNODE];
    vector<Edge> edge;
```

```
int n;
int root = 0;
void init(int nn, int m=0) {
   n = nn:
   for (int i = 0; i <= n; i++)
       g[i].clear();
   edge.clear();
   m *= 2;
   edge.reserve(m); // may speedup // add_e too slow
void add_e(int x, int y, int len) {
   g[x].push_back(edge.size());
   edge.push_back((Edge){y, len});
   g[y].push_back(edge.size());
   edge.push_back((Edge){x, len});
void show() {
   for (int i = 0; i \le n; i++) {
       printf("%d:", i);
       for (int ie : g[i])
           printf("\"\d", edge[ie].to);
       printf("\n");
   printf("\n");
// --- start of LCA ---
vector<int> dis_to_root;
vector<int> first_visit_time; // max possible number of
    → visits to all nodes == 2 * number of nodes - 1
vector<int> visit;
int visit_counter;
vector<vector<int>> rmq;
int range_minimum_query(int 1, int r) { // query [l, r]  
   if (1 > r)
       swap(1, r);
   int interval_len = r - 1; // (r - l + 1) - 1
   int first_half = 1;
   while ((1 << first_half) <= interval_len)
       first_half++;
   first_half--;
   int second_half = r - (1 << first_half) + 1;</pre>
   if (first_visit_time[rmq[l][first_half]] <</pre>
        → first_visit_time[rmq[second_half][
        → first_half]])
       return rmq[l][first_half];
   return rmq[second_half][first_half];
int get_lca(int x, int y) {
   return range_minimum_query(first_visit_time[x],

    first_visit_time[y]);
int dist(int x, int y) {
   int lca = get_lca(x, y);
   return dis_to_root[x] + dis_to_root[y] - 2 *

    dis_to_root[lca];

void euler_tour(int cur) {
   visit[++visit_counter] = cur; // v_t[node] = time
         \hookrightarrow // needed in case don't have two child
   if (first_visit_time[cur] == 0) // if first time
       first_visit_time[cur] = visit_counter; // record
            \hookrightarrow time f_v_t[node] = time
   for (int ie : g[cur]) {
       const Edge& e = edge[ie];
```

```
int nx = e.to;
           int len = e.len;
           if (first_visit_time[nx] == 0) {
               dis_to_root[nx] = dis_to_root[cur] + len;
               euler_tour(nx);
               visit[++visit_counter] = cur; // every two
                    \hookrightarrow child_visit_time have one
                    → parent_visit_time inserted between
       }
   }
   void build_lca() { // O(Nlog(N))
       int one_n = n + 1;
       int two_n = 2 * one_n;
       vector<int>(one_n, 0).swap(dis_to_root);
       vector<int>(one_n, 0).swap(first_visit_time);
       vector<int>(two_n, 0).swap(visit);
       int LOG_MAXLENGTH = log2(two_n) + 2;
       vector<vector<int>>(two_n, vector<int>(
            → LOG_MAXLENGTH)).swap(rmq);
       visit_counter = 0;
       euler_tour(root);
       for (int i = 0; i < visit_counter; i++)</pre>
           rmq[i][0] = visit[i];
       for (int j = 1; j < LOG_MAXLENGTH; j++)</pre>
           for (int i = 0; i < visit_counter; i++) {</pre>
               if (i + (1 << j) > visit_counter)
                   break:
               rmq[i][j] = rmq[i][j - 1];
               if (first_visit_time[rmq[i][j - 1]] >
                    → first_visit_time[rmq[i + (1 << (j -</pre>
                    → 1))][j - 1]])
                   rmq[i][j] = rmq[i + (1 << (j - 1))][j

→ -1];
           }
    // --- end of LCA ---
};
int n, m;
Graph g;
int main(int argc, char const *argv[]) {
   scanf("%d", &n);
   g.init(n, n);
   for (int i = 1; i < n; i++) {
       int x, y, d;
       scanf("%d_{\sqcup}%d_{\sqcup}%d", &x, &y, &d);
       g.add_e(x, y, d);
   g.build_lca();
   scanf("%d", &m);
   for (int i = 0; i < m; i++) \{
       int x, y;
       scanf("%d_{\sqcup}%d", &x, &y);
       printf("%d\n", g.dist(x, y));
   }
}
```

26 Segtree

1=Update (add Z to elements indexed X to Y), 2=max and min per query

```
const 11 sz = 4e5+5;
11 seg[2][sz], lazy[sz], a[sz];
11 N, M, X, L, R, Y, Z;
```

```
void check(ll p, ll s, ll e) {
       if (lazy[p] != 0) {
               seg[0][p] += lazy[p];
               seg[1][p] += lazy[p];
               if (s != e) {
                      lazy[2*p] += lazy[p];
                      lazy[2*p+1] += lazy[p];
               lazy[p] = 0;
       }
}
void build(ll p,ll s,ll e) {
       check(p,s,e);
       if (s == e) {
               seg[0][p] = a[s];
               seg[1][p] = a[s];
               return;
       build(2*p,s,(s+e)/2);
       build(2*p+1,(s+e)/2+1,e);
       seg[0][p] = min(seg[0][2*p], seg[0][2*p+1]);
       seg[1][p] = max(seg[1][2*p], seg[1][2*p+1]);
void update(ll p,ll s,ll e,ll a,ll b,ll v) {
       check(p,s,e);
       if(s >= a && e <= b) {
               seg[0][p] += v;
               seg[1][p] += v;
               if (s != e) {
                      lazy[2*p] += v;
                      lazy[2*p+1] += v;
               }
               return;
       }
       if(s > b || e < a) {
               return;
       update(2*p,s,(s+e)/2,a,b,v);
       update(2*p+1,(s+e)/2+1,e,a,b,v);
       seg[0][p] = min(seg[0][2*p], seg[0][2*p+1]);
       seg[1][p] = max(seg[1][2*p], seg[1][2*p+1]);
ll getMin(ll p, ll s, ll e, ll a, ll b) {
       check(p,s,e);
       if (s >= a && e <= b) {
              return seg[0][p];
       }
       if (s > b || e < a) {
               return INT_MAX;
       return min(getMin(2*p,s,(s+e)/2,a,b),getMin(2*p+1,(
            \hookrightarrow s+e)/2+1,e,a,b));
11 getMax(11 p, 11 s, 11 e, 11 a, 11 b) {
       check(p,s,e);
       if (s \ge a \&\& e \le b) {
               return seg[1][p];
       if (s > b || e < a) {
               return INT_MIN;
       return max(getMax(2*p,s,(s+e)/2,a,b),getMax(2*p+1,(
            \hookrightarrow s+e)/2+1,e,a,b));
int main() {
       ios_base::sync_with_stdio(false);
```

```
cin.tie(NULL);
       memset(seg,0,sizeof(seg));
       cin >> N ;
       for (ll i = 0; i < N; i++) cin >> a[i];
       cin >> M;
       build(1,0,N-1);
       while (M--) {
              int p;
              cin >> p >> X >> Y;
              X--, Y--;
              if (p==1) {
                      cin >> Z;
                      update(1,0,N-1,X,Y,Z);
                      continue:
              cout << getMax(1,0,N-1,X,Y)-getMin(1,0,N-1,X</pre>
                    → ,Y) << '\n';
       return 0;
}
```

27 KMP

```
#define HHH 10003
int ne[HHH]; // next[], if par[i] not matched, jump to i =
    → ne[i]
int kmp(string& par, string& ori) {
   ne[0] = -1;
   for (int p = ne[0], i = 1; i < par.length(); i++) {</pre>
       while (p >= 0 && par[p+1] != par[i])
          p = ne[p];
       if (par[p+1] == par[i])
          p++;
       ne[i] = p;
   7
   int match = 0:
   for (int p = -1, q = 0; q < ori.length(); q++) {
       while (p \ge 0 \&\& par[p+1] != ori[q])
          p = ne[p];
       if (par[p+1] == ori[q])
       if (p + 1 == par.length()) { // match!
          p = ne[p];
          match++:
       }
   }
   return match; // return number of occurance
int main () {
  int n;
   cin >> n;
   string par, ori;
   while (cin >> par >> ori)
       cout << kmp(par, ori) << endl;</pre>
   return 0;
```

28 Kruskal MST

```
//Pseudocode:
// Initialize result
mst_weight = 0

// Create V single item sets
for each vertex v
    parent[v] = v;
    rank[v] = 0;

Sort all edges into non decreasing
```

```
order by weight w
for each (u, v) taken from the sorted list E
   do if FIND-SET(u) != FIND-SET(v)
       print edge(u, v)
       mst_weight += weight of edge(u, v)
       UNION(u, v)
//-- END OF PSEUDOCODE --
// \mathit{C++} program for Kruskal's algorithm to find Minimum
// Spanning Tree of a given connected, undirected and
// weighted graph
#include<bits/stdc++.h>
using namespace std;
// Creating shortcut for an integer pair
typedef pair<int, int> iPair;
// Structure to represent a graph
struct Graph
   int V, E;
   vector< pair<int, iPair> > edges;
   // Constructor
   Graph(int V, int E)
       this->V = V;
       this->E = E;
   // Utility function to add an edge
   void addEdge(int u, int v, int w)
       edges.push_back({w, {u, v}});
   // Function to find MST using Kruskal's
   // MST algorithm
   int kruskalMST();
// To represent Disjoint Sets
struct DisjointSets
   int *parent, *rnk;
   int n;
    // Constructor.
   DisjointSets(int n)
       // Allocate memory
       this->n = n;
       parent = new int[n+1];
       rnk = new int[n+1];
       // Initially, all vertices are in
       // different sets and have rank 0.
       for (int i = 0; i <= n; i++)
       {
           rnk[i] = 0;
           //every element is parent of itself
          parent[i] = i;
       }
   }
   // Find the parent of a node 'u'
   // Path Compression
   int find(int u)
       /* Make the parent of the nodes in the path
          from u--> parent[u] point to parent[u] */
       if (u != parent[u])
           parent[u] = find(parent[u]);
       return parent[u];
   }
   // Union by rank
```

```
void merge(int x, int y)
        x = find(x), y = find(y);
        /* Make tree with smaller height
           a subtree of the other tree */
        if (rnk[x] > rnk[y])
            parent[y] = x;
        else // If rnk[x] <= rnk[y]
            parent[x] = y;
        if (rnk[x] == rnk[y])
            rnk[y]++;
};
 /* Functions returns weight of the MST*/
int Graph::kruskalMST()
    int mst\_wt = 0; // Initialize result
    // Sort edges in increasing order on basis of cost
    sort(edges.begin(), edges.end());
    // Create disjoint sets
    DisjointSets ds(V);
    // Iterate through all sorted edges
    vector< pair<int, iPair> >::iterator it;
    for (it=edges.begin(); it!=edges.end(); it++)
        int u = it->second.first;
        int v = it->second.second:
        int set_u = ds.find(u);
        int set_v = ds.find(v);
        // Check if the selected edge is creating
        // a cycle or not (Cycle is created if u
        // and v belong to same set)
        if (set_u != set_v)
            // Current edge will be in the MST
            // so print it
            cout << u << "_{\sqcup}" << v << endl;
            // Update MST weight
            mst_wt += it->first;
            // Merge two sets
            ds.merge(set_u, set_v);
        }
    }
    return mst_wt;
// Driver program to test above functions
int main()
    /* Let us create above shown weighted
      and unidrected graph */
    int V,E;
    cin >> V >> E;
    Graph g(V, E);
    // making above shown graph
    for (int i=1;i<=E;i++) {
        int u,v,w;
        cin >> u >> v >> w;
        g.addEdge(u,v,w);
    \texttt{cout} << \texttt{"Edges}_{\sqcup} \texttt{of}_{\sqcup} \texttt{MST}_{\sqcup} \texttt{are}_{\sqcup} \backslash \texttt{n"};
    int mst_wt = g.kruskalMST();
    \verb|cout| << "\nWeight_\of_\MST_\ois_\"| << mst_wt;
    return 0;
```

29 NIM Game

```
Rules of the Game of Nim: There are n piles of coins. When

it is a players turn he chooses one pile and takes

at least one coin from it. If someone is unable to

move he loses (so the one who removes the last

coin is the winner).

Let n1, n2, ..., nk, be the sizes of the piles. It is a

losing position for the player whose turn it is if

and only if n1 xor n2 xor ... xor nk = 0.
```

30 Convex Hull - Graham Scan

```
struct Point {
   long x;
   long y;
   bool at_right_of(Point& that, Point& base) {
       Point vec_self = {this->x - base.x, this->y - base.
       Point vec_that = {that.x - base.x, that.y - base.y
           \hookrightarrow }:
       long product = vec_self * vec_that;
       if (product > 0)
           return true; // "this" is at right of "that"
       if (product == 0 && vec_self.length() > vec_that.
            → length())
           return true; // "this" is at right of "that"
       return false; // "this" is NOT at right of "that"
   };
   long operator* (Point& that) {
       return this->x * that.y - this->y * that.x;
   double distance_to(Point& that) {
       long x_diff = this->x - that.x;
       long y_diff = this->y - that.y;
       return sqrt(x_diff * x_diff + y_diff * y_diff);
   }:
   double length() {
       return sqrt(this->x * this->x + this->y * this->y);
   }
};
Point p[1005];
int my_stack[1005];
int n, 1, my_stack_top = -1;
bool compare(Point p1, Point p2) {
   return p1.at_right_of(p2, p[0]);
void push(int index) {
   my_stack[++my_stack_top] = index;
int pop() {
   int temp = my_stack[my_stack_top--];
   return temp;
void graham_scan() {
   push(0);
   push(1);
   int pre;
   int prepre;
   for (int i = 2; i < n; i++) {
       pre = my_stack_top;
       prepre = my_stack_top - 1;
```

```
while (p[i].at_right_of(p[my_stack[pre]], p[
            → my_stack[prepre]])) {
           pop();
           if (my_stack_top == 0)
              break;
           pre = my_stack_top;
           prepre = my_stack_top - 1;
       push(i);
   }
   int last = my_stack_top;
   if (p[0].at_right_of(p[my_stack[last]], p[my_stack[pre
       pop();
}
int main(int argc, char const *argv[]) {
   cin >> n >> 1;
   int minimun = 0;
   for (int i = 0; i < n; ++i) {
       int temp_x, temp_y;
       cin >> temp_x >> temp_y;
       p[i] = {temp_x, temp_y};
       if ((p[i].y < p[minimun].y) \mid | (p[i].y == p[minimun])
            → ].y && p[i].x < p[minimun].x))</pre>
           minimun = i;
   Point temp = {p[minimun].x, p[minimun].y}; // swap
         \hookrightarrow lowest and most left point to p[0]
   p[minimun] = p[0];
   p[0] = temp;
   sort(p + 1, p + n, compare); // use p[0] as base, sort
         \hookrightarrow according to polar angle
   graham_scan();
   // now all points in the stack is on Convex Hull //
         → size of stack = 1 + stack_top
   for (int i = 0; i <= my_stack_top; i++)</pre>
       cout << "point_" << my_stack[i] << "_is_on_Convex_
            → Hull" << endl;</pre>
```

31 LOG

```
Built-in log(double) is not accurate for integer.
Should (int)(log(double)+0.000....001)
```

32 Square Root

```
long long sq(long long a) {
  long long l = 1;
  long long r = a + 1;
  while (l + 1 < r) {
    long long m = (l + r) / 2;
    if (a / m < m)
        r = m;
    else
        l = m;
  }
  return l;
}</pre>
```

33 Weighted Activity Selection

```
// \mathit{C++} program for weighted job scheduling using Dynamic
// Programming and Binary Search
#include <iostream>
#include <algorithm>
using namespace std;
// A job has start time, finish time and profit.
    int start, finish, profit;
// A utility function that is used for sorting events
// according to finish time
bool myfunction(Job s1, Job s2)
    return (s1.finish < s2.finish);
// A Binary Search based function to find the latest job
// (before current job) that doesn't conflict with current
// job. "index" is index of the current job. This function
// returns -1 if all jobs before index conflict with it.
// The array jobs[] is sorted in increasing order of finish
// time.
int binarySearch(Job jobs[], int index)
    // Initialize 'lo' and 'hi' for Binary Search
    int lo = 0, hi = index - 1;
    // Perform binary Search iteratively
    while (lo <= hi)
        int mid = (lo + hi) / 2;
       if (jobs[mid].finish < jobs[index].start)</pre>
           if (jobs[mid + 1].finish < jobs[index].start)</pre>
               lo = mid + 1:
           else
               return mid:
       }
        else
           hi = mid - 1;
    }
    return -1:
// The main function that returns the maximum possible
// profit from given array of jobs
int findMaxProfit(Job arr[], int n)
    // Sort jobs according to finish time
    sort(arr, arr+n, myfunction);
    // Create an array to store solutions of subproblems.
        \hookrightarrow table[i]
    // stores the profit for jobs till arr[i] (including
         \hookrightarrow arr[i]
    int *table = new int[n];
    table[0] = arr[0].profit;
    // Fill entries in table[] using recursive property
    for (int i=1; i<n; i++)
        // Find profit including the current job
       int inclProf = arr[i].profit;
       int 1 = binarySearch(arr, i);
       if (1 != -1)
           inclProf += table[1];
        // Store maximum of including and excluding
       table[i] = max(inclProf, table[i-1]);
    // Store result and free dynamic memory allocated for
         \hookrightarrow table[]
    int result = table[n-1];
    delete[] table;
```

34 Template

```
#include <bits/stdc++.h>
#define fi first
#define se second
#define pb push_back
#define mp make_pair
#define MOD 1000000007
#define pii pair<int,int>
#define LL long long

using namespace std;
int main () {
   ios_base::sync_with_stdio(false);
   cin.tie(NULL);
   cout.tie(NULL);
   return 0;
}
```