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- $\#J$
- $|v|$
- $\binom{I}{J}$
- $(a, b)$
- $[a, b]$
- $[v, w]$
- $[A, B]$
- $[\mathcal{D}, \mathcal{E}]$
- $[\theta, \zeta]$
- $[\lambda, \mu, v]$
- $[\cdot]$
- $\{F, H\}$
- $\{\mathcal{P}, \mathcal{Q}\}$
- $\langle \cdot, \cdot \rangle$
- $\langle \cdot; \cdot \rangle$
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