### Genetic algorithms

#### **Evolutionary Computing**

- · Natural systems as guiding metaphors
- · Charles Darwinian Evolution 1859
- Theory of natural selection
- It proposes that the plants and animals that exist today are the result of millions of years of adaptation to the demands of the environment
- Over time, the entire population of the ecosystem is said to evolve
  - to contain organisms that, on average, are fitter than those of previous generations of the population

#### **Evolutionary Computing**

- Humans have evolved (and continue to evolve) over time....
- We presume that prehistoric species of man were less intelligent than we are.
- As conditions on earth change, species become extinct (e.g. the dinosaurs) and other species emerge
- Can we model this process and "evolve" new programs and even hardware?

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#### **Evolutionary Computing**

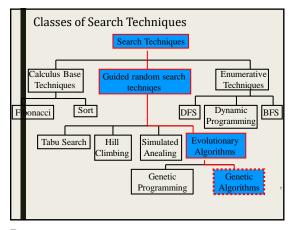
- Evolutionary computation(EC) techniques abstract these evolutionary principles into algorithms to search for optimal solutions to a problem.
- In a search algorithm
- A number of possible solutions to a problem are available
- Task is to find the best solution possible in a fixed amount of time
- For a search space with only a small number of possible solutions, all the solutions can be examined in a reasonable amount of time and the optimal one found.
- This exhaustive search, however, quickly becomes impractical as the search space grows in size.

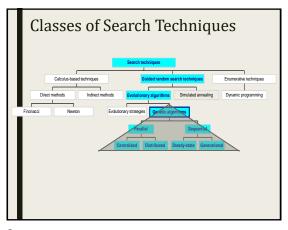
#### **Evolutionary Computing**

- \* Traditional search algorithms randomly or heuristically sample the search space (one solution at a time) in the hopes of finding the optimal solution
- The key aspect distinguishing an evolutionary search algorithm from such traditional algorithms is that it is population-based.

- heuristic method based on 'survival of the fittest'
- useful when search space very large or too complex for analytic treatment
- in each iteration (generation) possible solutions or individuals represented as strings of numbers

4 5





#### Genetic Algorithms

- The science that deals with the mechanisms responsible for similarities and differences in a species is called **Genetics**.
- The concepts of Genetic Algorithms are directly derived from natural evolution.
- In the early 70's a person named John Holland introduced the concept of genetic algorithms (Holland, 1975).

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#### The Genetic Algorithm

- Directed search algorithms based on the mechanics of biological evolution
- Developed by John Holland, University of Michigan (1970's)
  - To understand the adaptive processes of natural systems
  - To design artificial systems software that retains the robustness of natural systems
- Provide efficient, effective techniques for optimization and machine learning applications
- Widely-used today in business, scientific and engineering circles

A genetic algorithm maintains a population of candidate solutions for the problem at hand, and makes it evolve by iteratively applying a set of stochastic operators

Genetic Algorithms

- The Cell
- Every animal/human cell is a complex of many "small" factories that work together.
- The center of all this is the cell nucleus.
- The genetic information is contained in the cell nucleus

10 11 12

#### Genetic Algorithms

#### Chromosomes

END

- · All the genetic information gets stored in the chromosomes.
- The chromosomes are divided into several parts called genes.
- Genes code the properties of species i.e., the characteristics of an individual.
- The possibilities of the genes for one property are called allele and a gene can take different alleles.
- For example, there is a gene for eye color, and all the different possible alleles are black, brown, blue and green

#### Genetic Algorithms

- Another biological based method.
- Based on the Darwin's theory. (Evolution of
- Based on: survival of the most fittest individual
- Key steps: reproduction, survive
- Try to simulate life.
- Individual = solution
- Environment = problem

#### The Main Stages of GA

The main stages of GA are:

- 1. Creation of a **population** of individuals
- 2. Evaluation of individual's performance in the given environment
- 3. Selection of best individuals
- 4. Genetic **manipulation** on the selected individuals
- At stage 1, a population of individuals is created, and then the population is modified through a cycle of stages 2,..., 4

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# START Create initial, random population of organisms (potential solutions) Evaluate fitness for each Reproduce and kill Mutate organisms

#### Representation

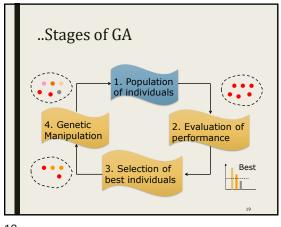
- Like in real life, the process is not done on the solution (individual), but on its representation (chromosome).
- Therefore we don't use knowledge we have about the problem.
- Very often, based on strings. (but not always), like biological

#### **Breeding Ground**

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- The idea is that you represent the solution to your problem in a structured way
- the simplest is a string
- this is not necessarily the best representation, but it is simple to explain
- We then build a population of random solutions and
- let them "breed" using genetic operators

  at each generation we apply "Survival of the fittest" and hopefully better and better solutions evolve
- the best solutions are more likely to survive and more likely to produce even better solutions



...Stages of GA

Each cycle of GA produces a new population of individuals with better performance
In the example of selecting red roses, this means that the proportion of red roses becomes greater and grey less (because the grey roses are not selected for the next seed)

Termination of GA

The cycles run while the performance is improved
Once the performance becomes stable (e.g., all roses became red), the GA terminates

Termination
point

Cycles

21

19

Definitions for GA

A population is often named *generation*A new population of individuals, created as a result of the genetic manipulation, is often called *offspring*The performance of individuals in the given environment are also called *fitness*For example, if our aim is select horses for racing, the performance (fitness) can be evaluated in terms of speed

..Definitions for GA

Individuals can be coded into bit-strings which are also named chromosomes
The bits are often named genes
An example of string (chromosome) consisting of 5 bits (genes):

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Types of Genetic Manipulation

Typically, genetic manipulation on selection of individuals consists of 2 operators: *crossover* and *mutation*The crossover operator recombines bits of two selected strings at the *crossover* point

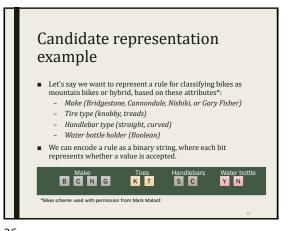
The crossover points are assigned randomly among the bits of strings

One or more crossover points can be given

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# Candidate representation We want to encode candidates in a way that makes mutation and crossover easy. The typical candidate representation is a binary string. This string can be thought of as the genetic code of a candidate – thus the term "genetic algorithm"! Other representations are possible, but they make crossover and mutation harder.



Candidate representation example

The candidate will be a bit string of length 10, because we have 10 possible attribute values.

Let's say we want a rule that will match any bike that is made by Bridgestone or Cannondale, has treaded tires, and has straight handlebars. This rule could be represented as 1100011011:

Make Tires Handlebars Water bottle B C N G K T S C Y N

25 26 27

...Crossover

An example of the recombination of 2 parent strings into 2 offspring when the crossover point is given after the 3<sup>rd</sup> bit;

So that the 4th and 5th bits are recombined

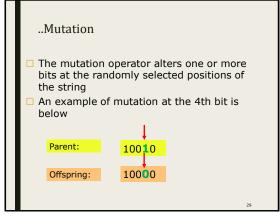
Crossover point

Parents:

100 10 010 00

Offspring:

100 00 010 10



An Example of Using GA
 Assume a function f(x) = x² which should be maximised in the interval 0 ≤ x ≤ 31
 In this example the fitness function is function f(x) itself - the larger its values, the better its fitness
 The number of bits in strings must be equal to 5 because x varies between 0 and 31

28 29 30

#### ..An Example

- Then the number of combinations of bits is 2<sup>5</sup> = 32
- To maximise function *f*(*x*), let us define 4 strings with the random values of *x* shown on the next slide

Table 1: Fitness of strings in initial population 1

# String	String	х	f(x)
1	01101	13	169
2	11000	24	576
3	01000	8	64
4	10011	19	361
Sum			1170

..An Example

- ☐ To create the first generation of individuals, let us clone string 2 whose fitness is maximal, 576
- ☐ Select the other 2 strings, #4 and #1, whose fitness values are equal to 361 and 169, respectively
- Let these 4 strings form the selection to make a genetic manipulation as shown on the next slide

31 32 33

#### ..An Example

- To make genetic manipulation on the selection, let us randomly assign a partner-string to each string as follows:
- #1 and #2
- #2 and #1
- #3 and #4
- #4 and #3
- ☐ The crossover points are randomly assigned at points 5, 5, 3, 3, respectively, as depicted in Table on the next slide

#### Table 2: Strings in population 2

#	String	Partner string #	Crossing	New population
1	01101	2	0110[1]	01100
2	11000	1	1100[0]	11001
3	*1100 0	4	11[000]	11011
4	10011	3	10[011]	10000

..An Example

- Now we can calculate the fitness for each string in population 2 as shown in Table 3 on the next slide
- From this Table we see that the sum of the new fitness values is now equal to 1754
- As the sum in population 1 is 1170, we can conclude that the individuals in population 2 fit better than those in population 1

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### Table 3: Fitness of strings in population 2

# String	String	Х	f(x)
1	01100	12	144
2	11001	25	625
3	01011	27	729
4	10000	16	256
Sum			1754

..An Example

- In the same manner we can run new cycles while the fitness increases
- When the fitness becomes stable, the GA terminates, and an individual with the best fitness is assigned as the resultant solution

Why Genetic Algorithms Work?

- To understand how genetic algorithms work, Holland has introduced *schemata* (plural of *schema*)
- A schema is a string in which the sign \* represents any value of bits
- For example, schema 1011\*001\*0 matches the following (2\*2 = 4) string variants:
  - 1011000100
  - 1011000110
  - 1011100100
  - 1011100110

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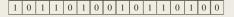
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#### **Definitions of Schemata**

- The length of a schema is the distance between the first and last defined bits in the schema
- For example, the length of the following schemata is 4:
  - \*\*10111\*
  - 1\*0\*1\*\*
  - 11111
  - 1\*\*\*1

#### Genetic Algorithms

 Holland was concerned with manipulating strings of binary digits using natural selection and genetic- inspired techniques.



A 16-bit binary string of an artificial chromosome

#### Genetic Operators

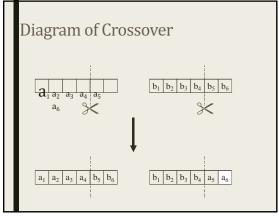
Crossover

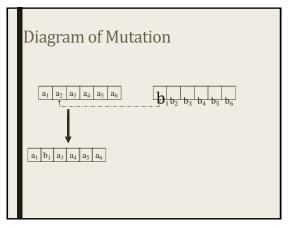
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- we cut two solutions at a random point and switch the respective parts
- Typically a value of 0.7 for crossover probability gives good results.
- Mutation
  - we randomly change a bit in the solution
- occasional mutation makes the method much less sensitive to the original population and also allows "new" solutions to emerge
  - Typically, a value between 0.001 and 0.01 for mutation robability is used.

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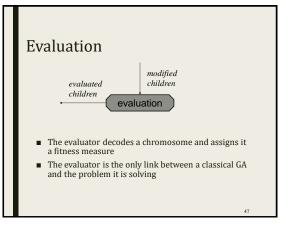


Stochastic operators Selection replicates the most successful solutions found in a population at a rate proportional to their relative quality Recombination decomposes two distinct solutions and then randomly mixes their parts to form novel solutions Mutation randomly perturbs a candidate solution

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The GA Cycle of Reproduction modification reproduction modified parents children evaluation population evaluated children deleted members discard



**Evaluation of Individuals** ■ Adaptability – "fitness" Relates to the objective function value for a DOP Fitness is maximized ■ Used in selection ("Survival of the fittest") ■ Often normalized  $f: S \rightarrow [0,1]$ 

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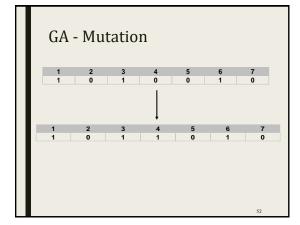
#### **Genetic Operators**

- Manipulates chromosomes/solutions
- Mutation: Unary operator
  - Inversions
- Crossover: Binary operator

GA - Evolution

- N generations of populations
- For every step in the evolution
  - Selection of individuals for genetic operations
  - Creation of new individuals (reproduction)
  - Mutation
  - Selection of individuals to survive
- Fixed population size M

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Mutation: Local Modification

Before: (1 0 1 1 0 1 1 0)

After: (1 0 1 0 0 1 1 0)

Before: (1.38 -69.4 326.44 0.1)

After: (1.38 -67.5 326.44 0.1)

Causes movement in the search space (local or global)

Restores lost information to the population

Crossover: Recombination

P1 (011 01000) (011 11010) c1

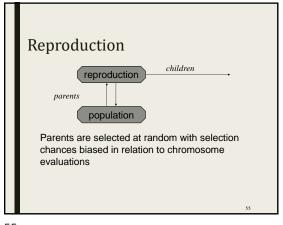
P2 (110 11010) (110 01000) c2

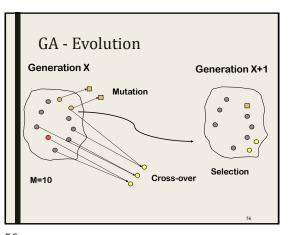
Crossover is a critical feature of genetic algorithms:

- It greatly accelerates search early in evolution of a population

- It leads to effective combination of schemata (subsolutions on different chromosomes)

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Population

Chromosomes could be:

- Bit strings (0101 ... 1100)

- Real numbers (43.2 - 33.1 ... 0.0 89.2)

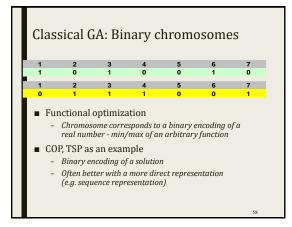
- Permutations of element (E11 E3 E7 ... E1 E15)

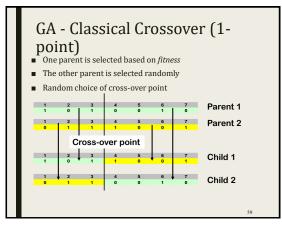
- Lists of rules (R1 R2 R3 ... R22 R23)

- Program elements (genetic programming)

- ... any data structure ...

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GA – Classical Crossover

Arbitrary (or worst) individual in the population is changed with one of the two offspring (e.g. the best)

Reproduce as long as you want

Can be regarded as a sequence of almost equal populations

Alternatively:

One parent selected according to fitness

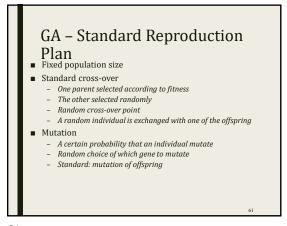
Crossover until (at least) M offspring are created

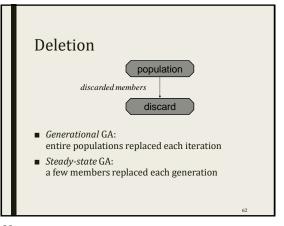
The new population consists of the offspring

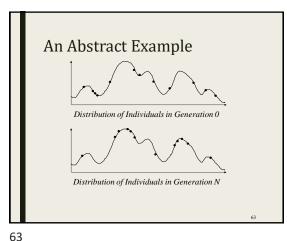
Lots of other possibilities ...

Basic GA with classical crossover and mutation often works well

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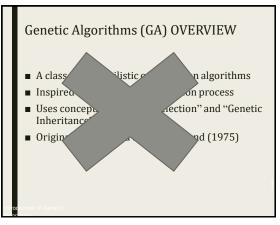




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Simple Genetic Algorithm
 initialize population;
 evaluate population;
 while TerminationCriteriaNotSatisfied
    select parents for reproduction;
    perform recombination and mutation;
    evaluate population;
```

```
Genetic Algorithm
1: Choose an initial population of chromosomes
2: while stopping criterion not met do
     while sufficient offspring has not been created do
       if condition for crossover is satisfied then
         Select parent chromosomes
         Choose crossover parameters
         Perform crossover
       if condition for mutation is satisfied then
10:
         Choose mutation points
11:
         Perform mutation
12:
       end if
       Evaluate fitness of offspring
13:
     end while
15: end while
```



GA overview (cont)

Particularly well suited for and problems where rlying search space

Wide ce and engineering

# Evaluation and Selection • We then see how good the solutions are, using an evaluation function • often this is a heuristic, especially if it is computationally expensive to do a complete evaluation • the final population can then be evaluated more deeply to decide on the best solution

Survival of the Fittest

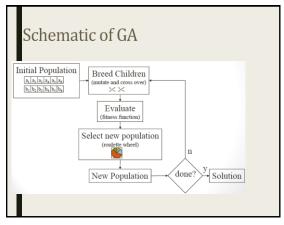
• We then select the surviving population

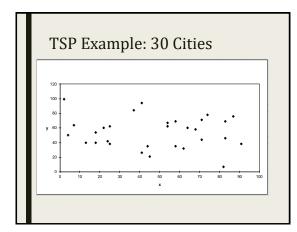
• Likelihood of survival is related in some way to your score on the fitness function

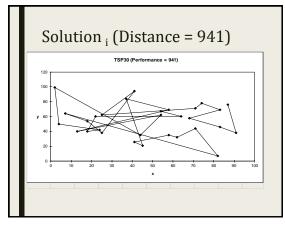
• the most common technique is roulette wheel selection

• Note we always keep the best solution so far (maybe this is the best we can do, so we don't want to lose this solution)

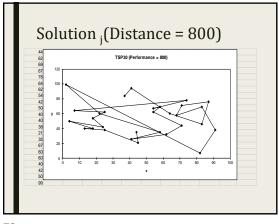
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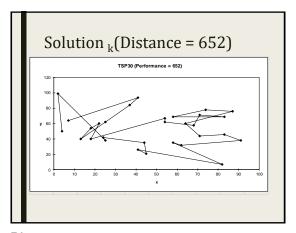


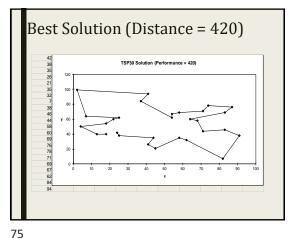




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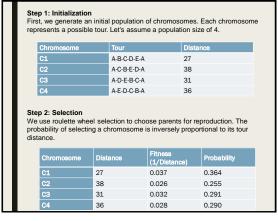






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f 0	Problem Definition The Traveling Salesman Problem involves finding the shortest possible route that visits each city exactly once and returns to the origin city. Let's consider a small example with 5 cities. Cities and Distances We'll define 5 cities (A, B, C, D, E) and their distances in a matrix form:						
		A	В	С	D	E	
	A	0	2	9	10	7	
	В	2	0	6	4	3	
	C	9	6	0	8	5	
	D	10	4	8	0	6	
	E	7	3	5	6	0	



Step 3: Crossover
We perform crossover between selected parents to create offspring. Assume C1 and C3 are selected as parents, and C2 and C4 are selected as another pair of parents. We'll use partially matched crossover (PMX).

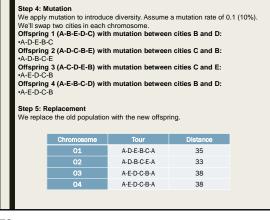
Crossover between C1 (A-B-C-D-E) and C3 (A-D-E-B-C):
Assume the crossover points are between the second and fourth cities:
+Parent 1: A-B-C-D-E
+Parent 2: A-D-E-B-C

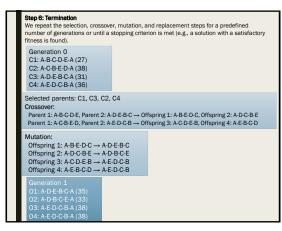
Offspring 2: A-D-C-B-E

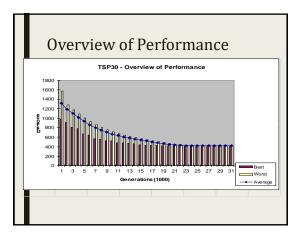
Crossover between C2 (A-C-B-E-D) and C4 (A-E-D-C-B):
Assume the crossover points are between the first and third cities:
+Parent 1: A-C-B-E-D
+Parent 2: A-E-D-C-B

Offspring 3: A-C-D-E-B
Offspring 3: A-C-D-E-B
-Offspring 3: A-C-D-E-B
-Offspring 4: A-E-B-C-D

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#### Example (Negnevitsky, 2002)

 To find the maximum value of the function (15x-x²), where parameter x varies between 0 and 15.
 Assumption: x takes only integer values.

Integer	Binary code
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

Example (Contd.)

\* Suppose that the size of the chromosome population N is 6, the crossover probability  $p_{\rm n}$  equals 0.7 and the mutation probability  $p_{\rm m}$  equals 0.001, the fitness function in our example is defined by

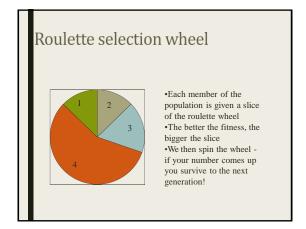
 $f(x)=(15x-x^2)$ 

E	Example (Contd.)  • The GA creates an initial population of chromosomes by filling six 4-bit strings with randomly generated ones and zeros.				
	Chromosome label	Chromosome string	Decoded integer	Chromosome fitness	Fitness ratio %
	X1	1100	12	36	16.5
	X2	0100	4	44	20.2
	Х3	0001	1	14	6.4
	X4	1110	14	14	6.4
	X5	0111	7	56	25.7
	Х6	1001	9	54	24.8

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#### Example (Contd.)

- Last column in the previous table shows the ratio of the individual chromosome fitness to the populations total fitness.
- According to the example, chromosomes X5 and X6 have a pretty good chance of being selected for mating, while X3 and X4 have a poor chance.
- Roulette selection wheel is the most commonly used chromosome selection technique.



#### Example (Contd.)

- To select a chromosome for mating, a random number (between 0 and 100) is generated.
- The roulette wheel is spun and when the arrow comes to rest on one of the segments, the corresponding chromosome is selected.
- In the current case, the wheel is spun six times.
  - The first two spins might select, X6 and X2;
- Second two spins might select X1 and X5;
- The last two spins might select X2 and X5.

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#### Example (Contd.)

- Genetic algorithms assure the continous improvement of the average fitness of the population, and after many generations (typically several hundreds), the population evolves to a near optimal solution.
- In the current case, 0111 and 1000.

# GA: Hybridization and Parallelization

- GAs strengths and weaknesses:
- Domain independence
- Hybridization
  - Seed good individuals in the initial population
  - Combine with other Metaheuristics to improve some solutions
- Parallelization
  - Fitness-evaluation
  - Sub-populations
  - The Island Model

#### **Issues for GA Practitioners**

- Basic implementation issues:
  - Representation
  - $-\quad Population\ size,\ mutation\ rate, \dots$
  - Selection, deletion policies
  - Crossover, mutation operators
- Termination Criteria
- Performance, scalability
- Solution is only as good as the evaluation function (often hardest part)

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#### Benefits of Genetic Algorithms

- Concept is easy to understand
- Modular, separate from application
- Supports multi-objective optimization
- Good for "noisy" environments
- Always an answer; answer gets better with time
- Inherently parallel; easily distributed

## Benefits of Genetic Algorithms (cont.)

- Many ways to speed up and improve a GAbased application as knowledge about the problem domain is gained
- Easy to exploit previous or alternate solutions
- Flexible building blocks for hybrid applications
- Substantial history and range of use

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#### When to Use a GA

- Alternate methods are too slow or overly complicated
- Need an exploratory tool to examine new approaches
- Problem is similar to one that has already been successfully solved by using a GA
- Want to hybridize with an existing method
- Benefits of the GA technology meet key problem requirements

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Some GA Application Types				
Domain	Application Types			
Control	gas pipeline, pole balancing, missile evasion, pursuit			
Design	semiconductor layout, aircraft design, keyboard configuration, communication networks			
Scheduling	manufacturing, facility scheduling, resource allocation			
Robotics	trajectory planning			
Machine Learning	designing neural networks, improving classification algorithms, classifier systems			
Signal Processing	filter design			
Game Playing	poker, checkers, prisoner's dilemma			
Combinatorial Optimization	set covering, travelling salesman, routing, bin packing, graph colouring and partitioning			
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#### GA: Overview

- Important characteristics:
  - Population av solutions
  - Domain independence encoding
  - Structure is not exploited
  - Inherent parallell schema, vocabulary
  - Robust
  - Good mechanisms for intensification
  - Lacking in diversification

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#### Genetic Algorithms

- Bit-string encoding is inappropriate for many combinatorial problems. In particular, crossover may lead to infeasible or meaningless solutions.
- Pure GAs are usually not powerful enough to solve hard combinatorial problems.
- Hybrid GAs use some form of local search as mutation operator to overcome this.

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#### Memetic Algorithms (1)

- Basically, a Memetic Algorithm is a GA with Local Search as
  - Also known under different names
  - An example of hybridization
- A meme is a unit of cultural information transferable from one mind to another
  - Sounds like gene: the unit carrying inherited information

#### Memetic Algorithms (2)

- The experience is that GAs do not necessarily perform well in
- Using Local Search in addition to the population mechanisms proves to be an improvement
- In a sense this elevates the population search to a search among locally optimal solutions, rather than among any solution in the solution space

#### **Summary of Lecture**

- Local Search
  - Short summary
- Genetic Algorithms
  - Population based Metaheuristic
  - Based on genetics:
    - Mutation
    - Combination of chromosomes from parents
  - Hybridization: Memetic Algorithm

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#### Advantages of GA's

- Interesting idea, parallelism
- Very easy to use
- Need no knowledge about the solution
- Could be efficient

#### Disadvantages of GA's

- Slow (blind search).
- No proof (or hints) about the quality of the solution.
- Sometimes difficult to use them efficiently.
- Tradeoff between mutation and crossover?
- Tradeoff between speed and quality?
- How important is each parameter?

#### Summary

- It's a big family, with a lot of possibilities
- Easy to use
- Efficiency?
- Areas: Graph problems (Graph coloring), optimization (Networks, schedulings etc)

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