

# Step 1 – Convolution

# Step 1 - Convolution

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$$(f * g)(t) \stackrel{\text{def}}{=} \int_{-\infty}^{\infty} f(\tau) g(t - \tau) d\tau$$

# Step 1 - Convolution

## Additional Reading:

*Introduction to Convolutional  
Neural Networks*

By Jianxin Wu (2017)

Link:

<http://cs.nju.edu.cn/wujx/paper/CNN.pdf>

$$\begin{aligned}\frac{\partial z}{\partial (\text{vec}(\mathbf{y})^T)} (\mathbf{F}^T \otimes \mathbf{I}) &= \left( (\mathbf{F} \otimes \mathbf{I}) \frac{\partial z}{\partial \text{vec}(\mathbf{y})} \right)^T \\ &= \left( (\mathbf{F} \otimes \mathbf{I}) \text{vec} \left( \frac{\partial z}{\partial \mathbf{Y}} \right) \right)^T \\ &= \text{vec} \left( \mathbf{I} \frac{\partial z}{\partial \mathbf{Y}} \mathbf{F}^T \right)^T \\ &= \text{vec} \left( \frac{\partial z}{\partial \mathbf{Y}} \mathbf{F}^T \right)^T,\end{aligned}$$

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image

0	0	1
1	0	0
0	1	1

Feature Detector

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0				

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1			

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0		

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	

Feature Map



# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0				

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1			

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1		

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1				

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0			

Feature Map



# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1		

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1				

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4			

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2		

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0

Feature Map



# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0				

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0	0			

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0	0	1		

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0	0	1	2	

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

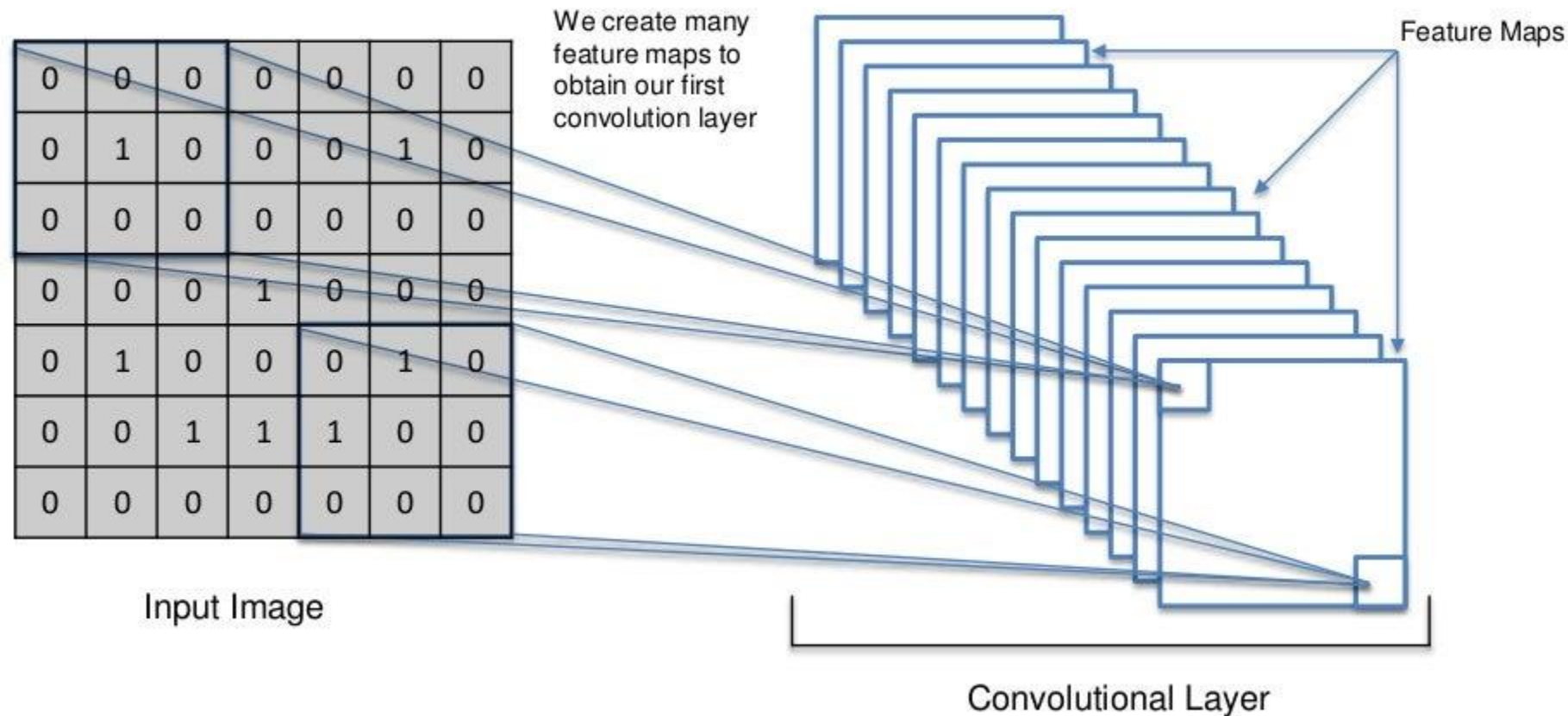
Feature Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0	0	1	2	1

Feature Map

# Step 1 - Convolution



# Step 1 - Convolution

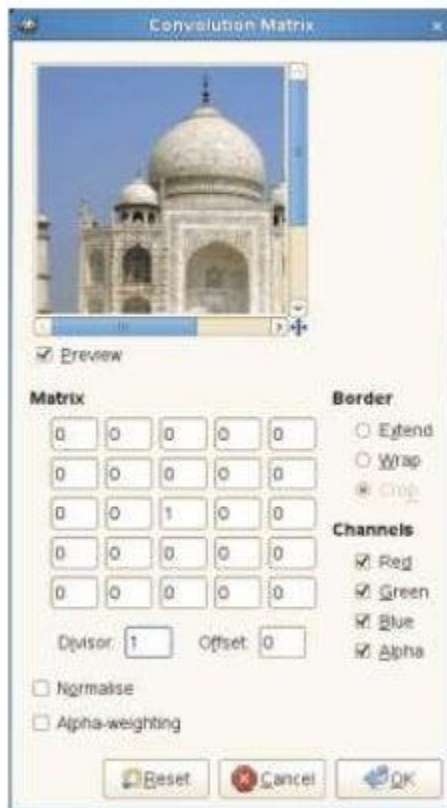


Image Source: [docs.gimp.org/en/plugin-in-convmatrix.html](https://docs.gimp.org/en/plugin-in-convmatrix.html)



# Step 1 - Convolution

Sharpen:

0	0	0	0	0
0	0	-1	0	0
0	-1	5	-1	0
0	0	-1	0	0
0	0	0	0	0

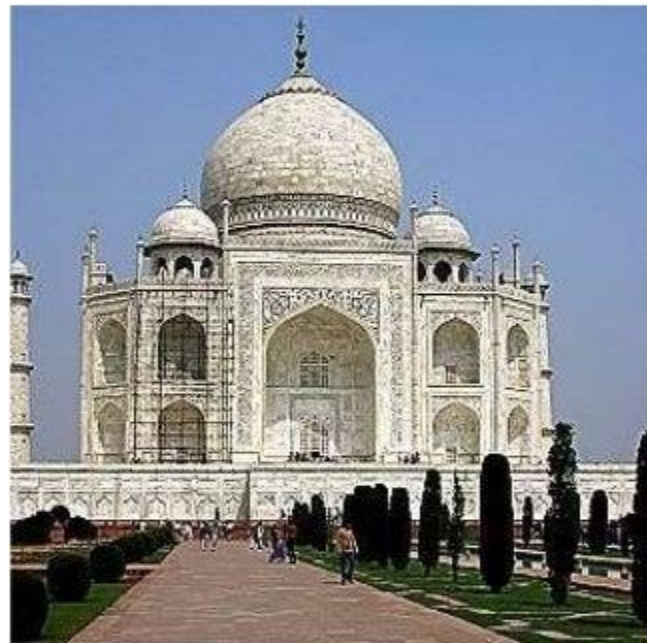


Image Source: [docs.gimp.org/en/plugin-in-convmatrix.html](https://docs.gimp.org/en/plugin-in-convmatrix.html)



# Step 1 - Convolution

Blur:

0	0	0	0	0
0	1	1	1	0
0	1	1	1	0
0	1	1	1	0
0	0	0	0	0



Image Source: [docs.gimp.org/en/plugin-in-convmatrix.html](https://docs.gimp.org/en/plugin-in-convmatrix.html)

# Step 1 - Convolution

Edge Enhance:

	0	0	0	
	-1	1	0	
	0	0	0	



*Image Source: [docs.gimp.org/en/plugin-in-convmatrix.html](https://docs.gimp.org/en/plugin-in-convmatrix.html)*

# Step 1 - Convolution

Edge Detect:

	0	1	0	
	1	-4	1	
	0	1	0	



Image Source: [docs.gimp.org/en/plugin-in-convmatrix.html](https://docs.gimp.org/en/plugin-in-convmatrix.html)

# Step 1 - Convolution

Emboss:

	-2	-1	0	
	-1	1	1	
	0	1	2	



Image Source: [docs.gimp.org/en/plugin-in-convmatrix.html](https://docs.gimp.org/en/plugin-in-convmatrix.html)

# Step 1 - Convolution



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1	0	-1
2	0	-2
1	0	-1



*Image Source: eonardoaraujosantos.gitbooks.io*