



Image Processing (CSE281)

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Image Re-size

```
from PIL import Image #Python Imaging Library
image_path = "F:/13.jpg"
my_image = Image.open(image_path)
my_image.show()
new_size = (100, 100)
resized_image = my_image.resize(new_size)
resized_image.show()
```



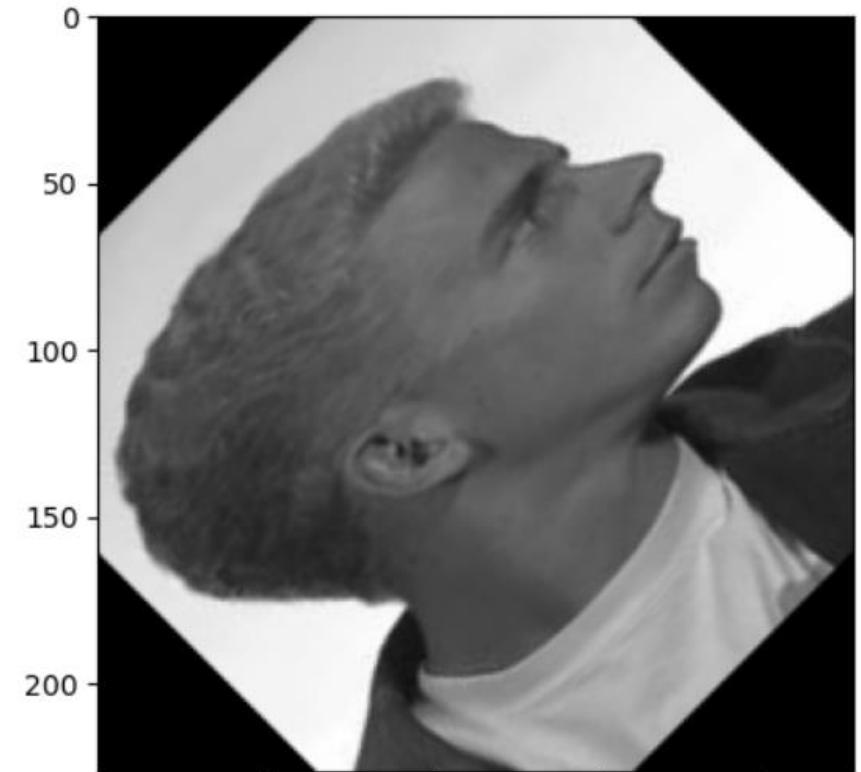
RGB to Gray

```
from PIL import Image #Python Imaging Library
image_path = "F:/13.jpg"
my_image = Image.open(image_path)
Gray_image = my_image.convert('L')
Gray_image.show()
```



Image Rotation

```
from PIL import Image #Python Imaging Library
image_path = "F:/13.jpg"
my_image = Image.open(image_path)
Rotated_image = my_image.rotate(45)
Rotated_image.show()
```



Drawing on images

```
from PIL import Image, ImageDraw  
my_image = Image.open("F:/13.jpg")  
draw = ImageDraw.Draw(my_image)  
draw.line((10, 20, 400, 20), fill = (0, 255, 0), width = 4)  
my_image.show()
```



draw.line((10, 20, 400, 20), fill = (0, 255, 0), width = 4)

Start point = (10, 20)

End point = (400, 20)

Fill = (0, 255, 0) → Green

Width = 4 → The Thickness of the Line

Drawing on images

```
from PIL import Image, ImageDraw  
my_image = Image.open("F:/13.jpg")  
draw = ImageDraw.Draw(my_image)  
draw.rectangle((10, 20, 40, 45), fill = (0, 255, 0), width = 4)  
my_image.show()
```



draw.rectangle((10, 20, 40, 45), fill = (0, 255, 0), width = 4)

Start point = (10, 20)

End point = (40, 45)

Fill = (0, 255, 0) → Green

Width = 4 → The Thickness

Drawing on images

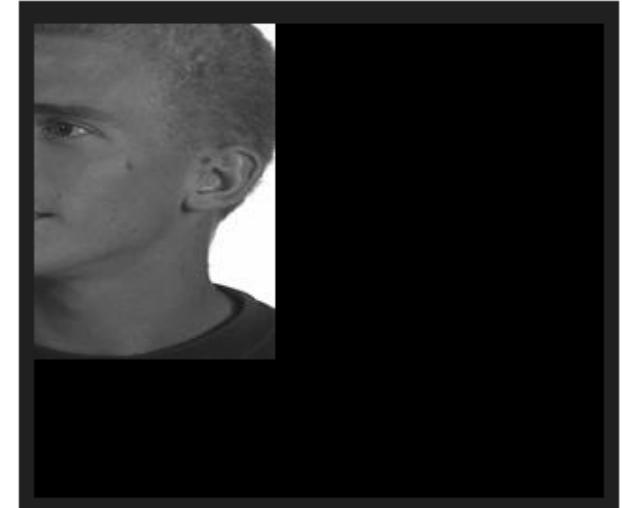
```
from PIL import Image, ImageDraw  
my_image = Image.open("F:/13.jpg")  
draw = ImageDraw.Draw(my_image)  
draw.circle((40, 80), 30, fill = (0, 255, 0), width = 4)  
my_image.show()
```



draw.circle((40, 80), 30, fill = (0, 255, 0), width = 4)
Center = (40, 80)
30 → Radius of Circle
Fill = (0, 255, 0) → Green
Width = 4 → The Thickness

Image Cropping

```
from PIL import Image  
my_image = Image.open("F:/13.jpg")  
crop_box = (100, 50, 400, 300)  
cropped_image = my_image.crop(crop_box)  
cropped_image.show()
```



Crop_box = (left, upper, right, lower)

Left = 100 → Start cropping 100 pixels from the left edge of the image.

Upper = 50 → Start cropping 50 pixels from the top edge.

Right = 400 → Stop cropping at 400 pixels from the left edge.

Lower = 300 → Stop cropping at 300 pixels from the top edge.

Image Blurring

A technique that smooths an image by reducing sharp transitions in intensity.

Purpose: Used to reduce noise, remove fine details, or prepare images for further processing such as edge detection.

Operation: Convolution with a blur kernel (such as Gaussian).

Image Blurring

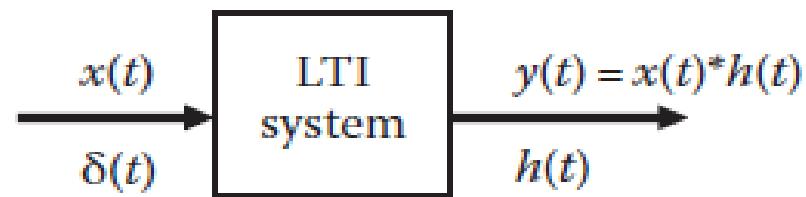
```
from PIL import Image, ImageFilter  
my_image = Image.open("F:/13.jpg")  
blurred_image = my_image.filter(ImageFilter.BLUR)  
blurred_image.show()
```



Convolution

The convolution of two signals $x(t)$ and $h(t)$ is usually written in terms of the operator $*$ as

$$y(t) = x(t) * h(t) = \int_{-\infty}^{\infty} x(\tau)h(t - \tau)d\tau$$



Convolution

Properties of the Convolution Integral

$$1. \quad x(t) * h(t) = h(t) * x(t) \quad (\text{Commutative})$$

$$2. \quad f(t) * [x(t) + y(t)] = f(t) * x(t) + f(t) * y(t) \quad (\text{Distributive})$$

$$3. \quad f(t) * [(x(t) * y(t))] = f[(t) * x(t)] * y(t) \quad (\text{Associative})$$

$$4. \quad f(t) * \delta(t) = \int_{-\infty}^{\infty} f(\tau) \delta(t - \tau) d\tau = f(t)$$

$$5. \quad f(t) * \delta(t - t_o) = f(t - t_o)$$

$$6. \quad f(t) * \delta'(t) = \int_{-\infty}^{\infty} f(\tau) \delta'(t - \tau) d\tau = f'(t)$$

$$7. \quad f(t) * u(t) = \int_{-\infty}^{\infty} f(\tau) u(t - \tau) d\tau = \int_{-\infty}^t f(\tau) d\tau$$

$$8. \quad u(t) * \delta'(t) = \int_{-\infty}^{\infty} u(\tau) \delta'(t - \tau) d\tau = u'(t) = \delta(t)$$

9. If $x_1(t) * x_2(t) = y(t)$, then

$$x_1(t + t_1) * x_2(t + t_2) = y(t + t_1 + t_2)$$

Convolution

Example

The input $x(t)$ and the impulse response $h(t)$ of an LTI system are given by $x(t) = u(t)$ and $h(t) = e^{-3t}u(t)$. Find the output response.

Solution

From Equation 2.6,

$$y(t) = \int_{-\infty}^{\infty} x(\tau)h(t - \tau)d\tau = \int_{-\infty}^{\infty} u(\tau)e^{-3(t-\tau)}u(t - \tau)d\tau$$

In this integral, t is a constant so that we can pull out the factor e^{-3t} .

By definition,

$$u(\tau) = \begin{cases} 1, & \tau > 0 \\ 0, & \tau < 0 \end{cases}$$

$$u(t - \tau) = \begin{cases} 1, & t - \tau > 0 \\ 0, & t - \tau < 0 \end{cases} = \begin{cases} 1, & \tau < t \\ 0, & \tau > t \end{cases}$$

Thus,

$$u(\tau)u(t - \tau) = \begin{cases} 1, & 0 < t < \tau \\ 0, & \text{otherwise} \end{cases}$$

Convolution

The limits on the integral now becomes $0 < \tau < t$. Therefore, Equation 2.2.1 becomes

$$\begin{aligned}y(t) &= e^{-3t} \int_0^t e^{3\tau} d\tau = \frac{e^{-3t}}{3} e^{3\tau} \Big|_0^t \\&= \frac{1}{3} (1 - e^{-3t}), \quad t > 0\end{aligned}$$

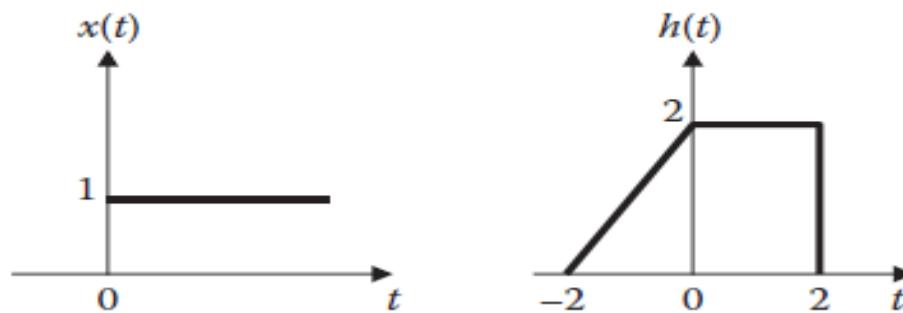
or

$$y(t) = \frac{1}{3} (1 - e^{-3t}) u(t)$$

Graphical Convolution

Example

Obtain the convolution of the two signals in Figure 2.4.



Solution

Let $y(t) = x(t)*h(t)$, where $x(t)$ is a unit step and

$$h(t) = \begin{cases} 2+t, & -2 < t < 0 \\ 1, & 0 < t < 2 \end{cases}$$

Graphical Convolution

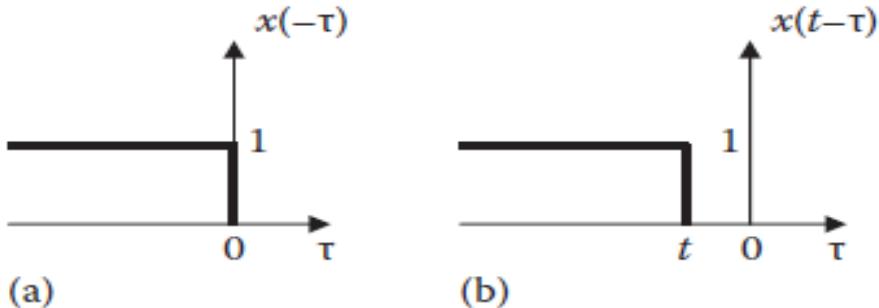
In this case, it is easy to fold $x(t)$, the unit step function. Let

$$y(t) = x(t) * h(t) = \int x(t - \tau)h(\tau)d\tau$$

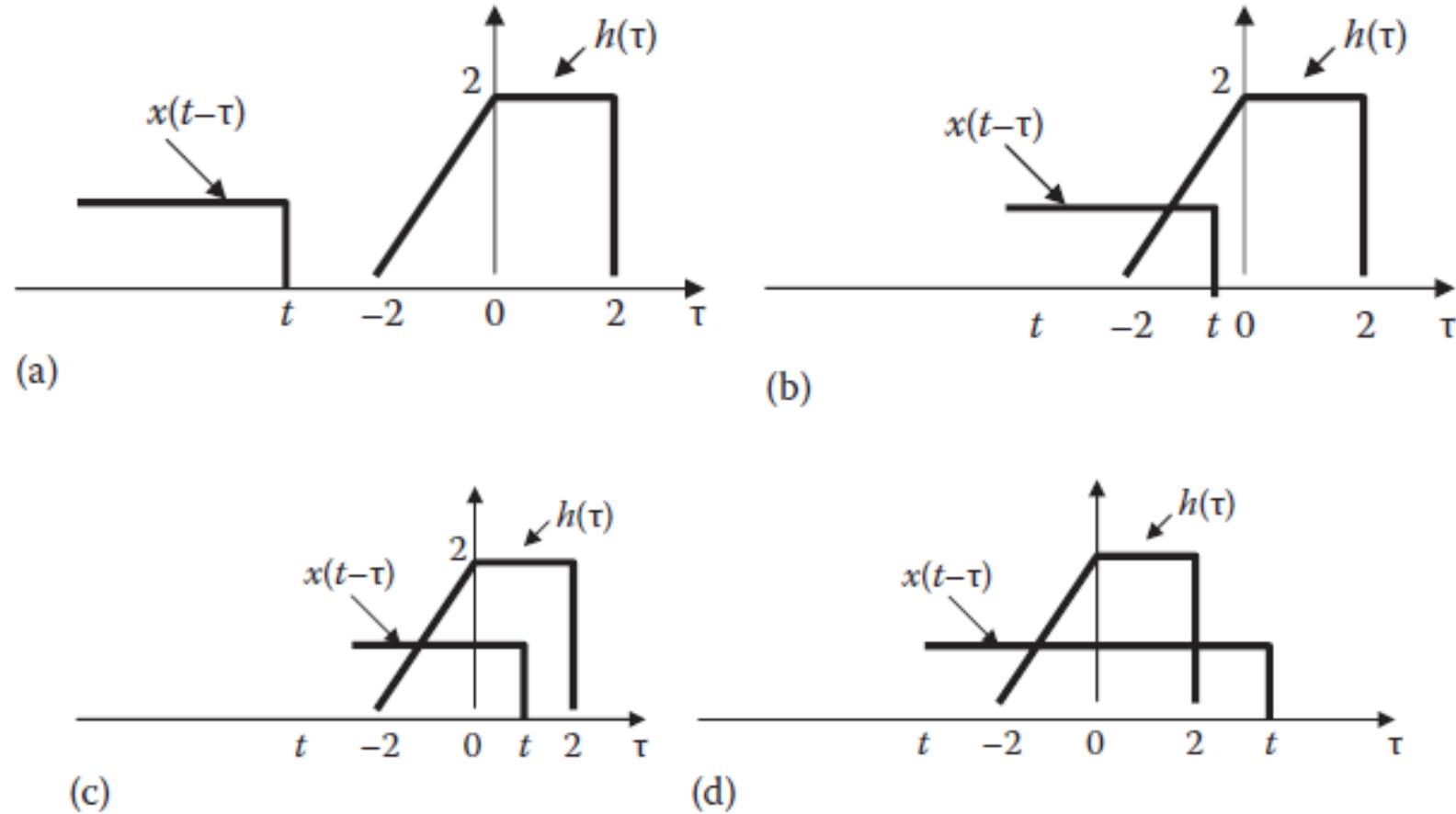
We follow the four steps to get $y(t)$. First, we fold $x(t)$ as shown in Figure 2.5a and shift it by t as shown in Figure 2.5b.

For $t < -2$, there is no overlap of the two signals, as shown in Figure 2.6a. Hence,

$$y(t) = x(t) * h(t) = 0, \quad t < -2$$



Graphical Convolution



Graphical Convolution

For $-2 < t < 0$, the two signals overlap between -2 and t , as shown in Figure 2.6b.

$$y(t) = \int_{-2}^t h(\tau)x(t-\tau)d\tau = (2+\tau)(1)d\tau \Big|_{-2}^t = 2\tau + \frac{\tau^2}{2} \Big|_{-2}^t$$
$$= 0.5t^2 + 2t + 2, \quad -2 < t < 0$$

For $0 < t < 2$, the two signals overlap between -2 and t , as shown in Figure 2.6c.

$$y(t) = \int_{-2}^0 (2+\tau)(1)d\tau + \int_0^t (2)(1)d\tau$$
$$= \left(2\tau + \frac{\tau^2}{2} \right) \Big|_{-2}^0 + 2\tau \Big|_0^t = 4 - 2 + 2t = 2(t+1), \quad 0 < t < 2$$

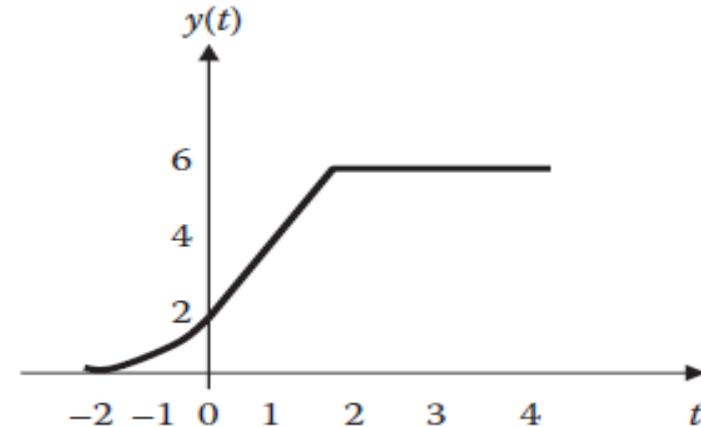
Graphical Convolution

For $t > 2$, the two signals overlap between -2 and 2 , as shown in Figure 2.6d.

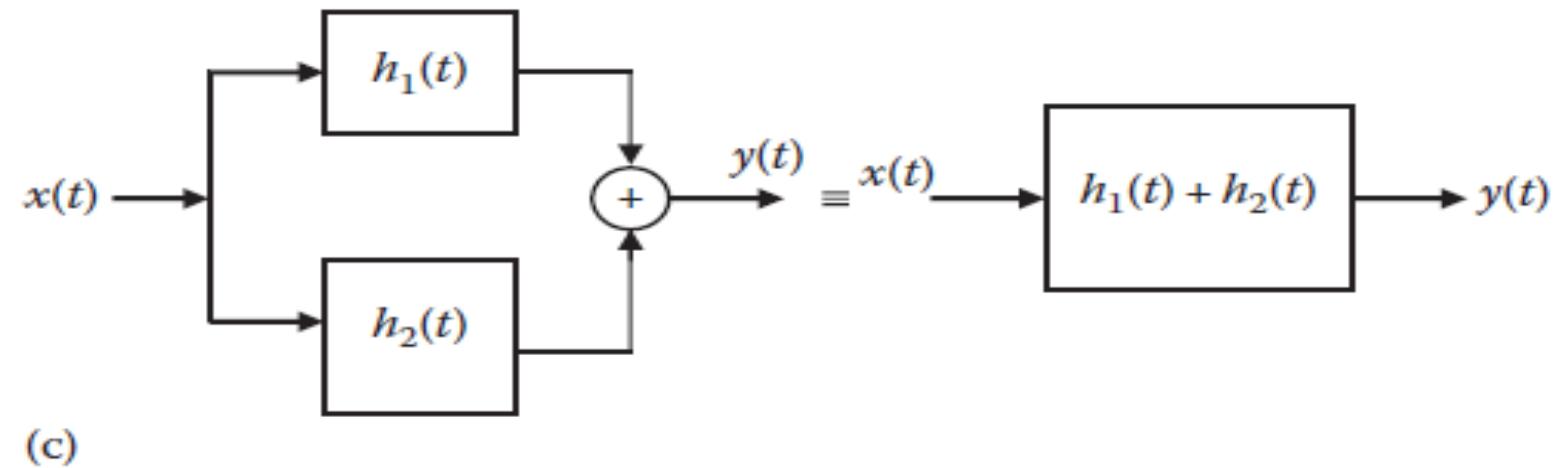
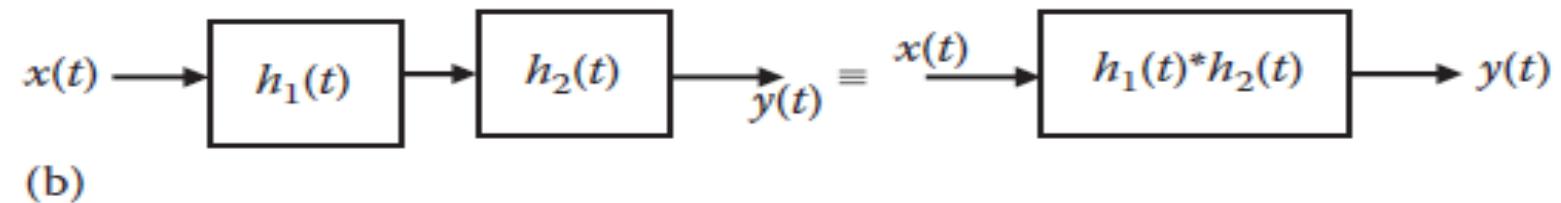
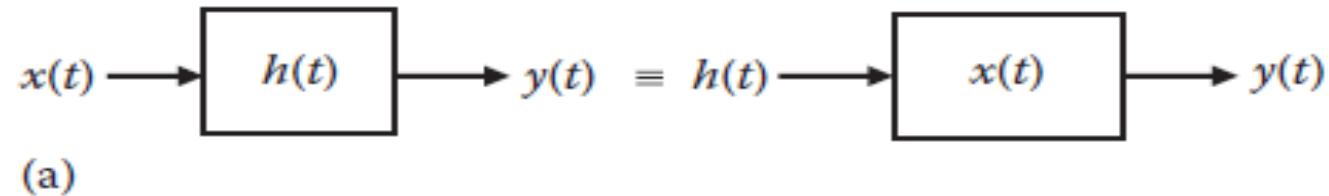
$$\begin{aligned}y(t) &= \int_{-2}^0 (2 + \tau)(1)d\tau + \int_0^2 (2)(1)d\tau \\&= \left(2\tau + \frac{\tau^2}{2} \right) \Big|_{-2}^0 + 2\tau \Big|_0^2 = 4 - 2 + 4 = 6, \quad t > 2\end{aligned}$$

Graphical Convolution

$$y(t) = \begin{cases} 0.5t^2 + 2t + 2, & -2 \leq t \leq 0 \\ 2(t+1), & 0 \leq t \leq 2 \\ 6, & t > 2 \\ 0, & \text{otherwise} \end{cases}$$



Convolution



Convolution

Example

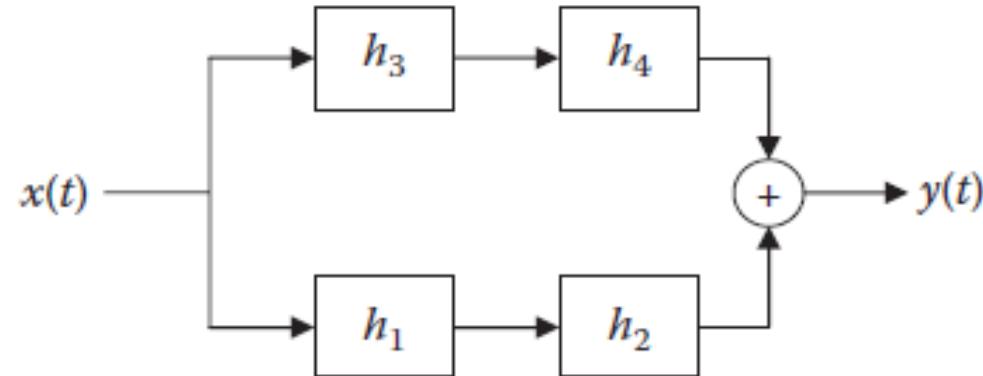
Find the impulse response of the system shown in Figure 2.13. Let

$$h_1(t) = 3\delta(t)$$

$$h_2(t) = 2e^{-t}u(t)$$

$$h_3(t) = 4e^{-2t}u(t)$$

$$h_4(t) = e^{-3t}u(t)$$



Convolution

Using the fact that $x(t) * \delta(t) = x(t)$, we obtain the first convolution on the right-hand side as

$$h_1(t) * h_2(t) = 3\delta(t) * \{2e^{-t}u(t)\} = 6e^{-t}u(t)$$

For the second convolution,

$$h_3(t) * h_4(t) = \int_{-\infty}^{\infty} 4e^{-2\tau}u(\tau)e^{-3(t-\tau)}u(t-\tau)d\tau$$

but

$$u(\tau)u(t-\tau) = \begin{cases} 1, & 0 < t < \tau \\ 0, & \text{otherwise} \end{cases}$$

Convolution

Therefore,

$$\begin{aligned} h_3(t) * h_4(t) &= \int_0^t 4e^{-2\tau} e^{-3(t-\tau)} d\tau = 4e^{-3t} \int_0^t e^{(3-2)\tau} d\tau \\ &= 4e^{-3t} e^{\tau} \Big|_0^t = 4(e^{-2t} - e^{-3t}), \quad t > 0 \\ &= 4(e^{-2t} - e^{-3t})u(t) \end{aligned}$$

Substituting Equations 2.5.2 and 2.5.3 into Equation 2.5.1 gives

$$h(t) = 6e^{-t}u(t) + 4(e^{-2t} - e^{-3t})u(t)$$

Discrete Convolution

When an input is applied to a discrete-time system, the response or output sequence can be determined in a way similar to using the impulse response and the convolution integral for continuous-time systems.

$$u[n] = \begin{cases} 0, & n < 0 \\ 1, & n \geq 0 \end{cases}$$

The unit impulse sequence is also redefined as

$$\delta[n] = \begin{cases} 0, & n \neq 0 \\ 1, & n = 0 \end{cases}$$

The signal only has value at $n = 0$. The displaced delta function is

$$\delta[n - k] = \begin{cases} 0, & n \neq k \\ 1, & n = k \end{cases}$$

Discrete Convolution

The convolution of the discrete input signal $x[n]$ and the impulse response $h[n]$ is

$$y[n] = x[n] * h[n]$$

and is defined as

$$y[n] = \sum_{k=-\infty}^{\infty} x[k]h[n-k]$$

Thus,

$$y[n] = x[n] * h[n] = \sum_{k=-\infty}^{\infty} x[k]h[n-k]$$

Discrete Convolution

Properties of the Convolution Sum

$$1. x[n] * h[n] = h[n] * x[n] \quad (\text{Commutative})$$

$$2. f[n] * [x[n] + y[n]] = f[n] * x[n] + f[n] * y[n] \quad (\text{Distributive})$$

$$3. f[n] * [x[n] * y[n]] = [f[n] * x[n]] * y[n] \quad (\text{Associative})$$

$$4. x[n-m] * h[n-k] = y[n-m-k] \quad (\text{Shifting})$$

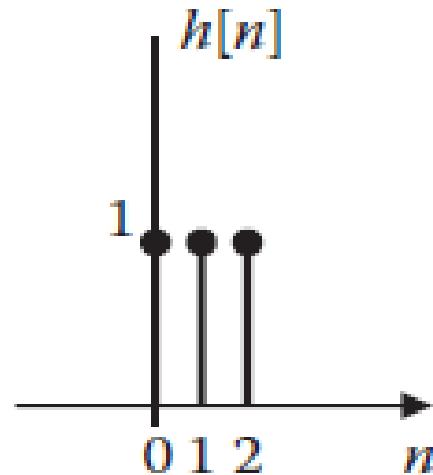
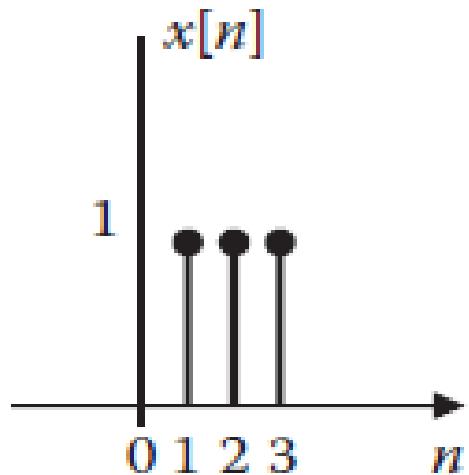
$$5. x[n] * \delta[n] = x[n]$$

Discrete Convolution

Example

Consider $x[n]$ and $h[n]$ as shown in Figure 2.17. (The signals are all zero outside the ranges indicated.) Find $y[n] = x[n]*h[n]$:

- (a) Analytically and (b) graphically.



Discrete Convolution

(a) Using Equation 2.19, we can write

$$x[n] = \delta[n-1] + \delta[n-2] + \delta[n-3]$$

$$h[n] = \delta[n] + \delta[n-1] + \delta[n-2]$$

$$y[n] = x[n] * h[n] = x[n] * \{\delta[n] + \delta[n-1] + \delta[n-2]\}$$

$$= x[n] + x[n-1] + x[n-2]$$

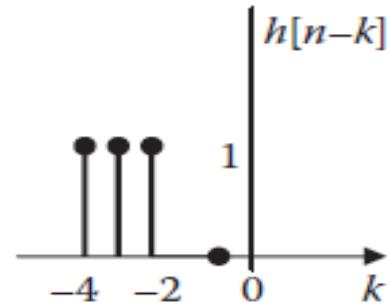
$$= \delta[n-1] + \delta[n-2] + \delta[n-3]$$

$$+ \delta[n-2] + \delta[n-3] + \delta[n-4]$$

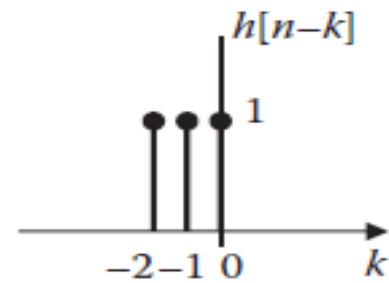
$$+ \delta[n-3] + \delta[n-4] + \delta[n-5]$$

$$= \delta[n-1] + 2\delta[n-2] + 3\delta[n-3] + 2\delta[n-4] + \delta[n-5]$$

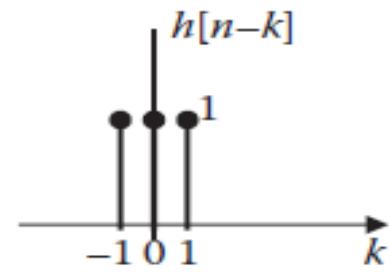
Discrete Convolution



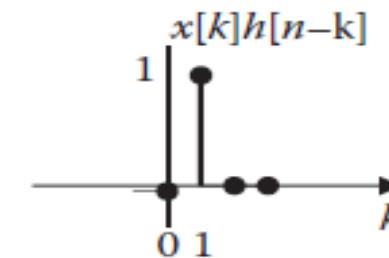
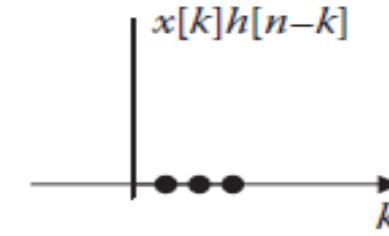
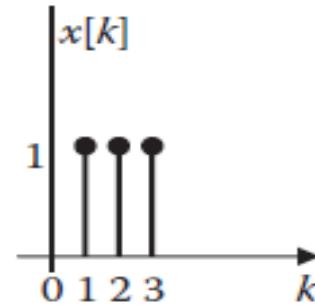
$$n < 0 \\ y = 0$$



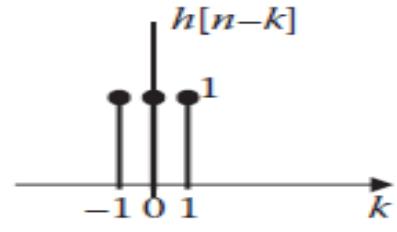
$$n < 0 \\ y = 0$$



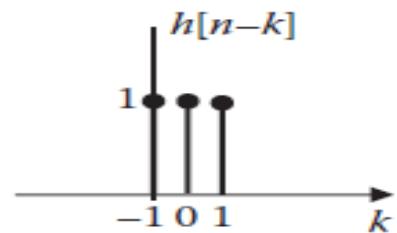
$$n = 1 \\ y = 1$$



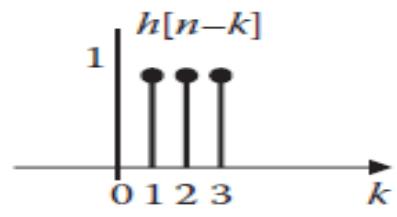
Discrete Convolution



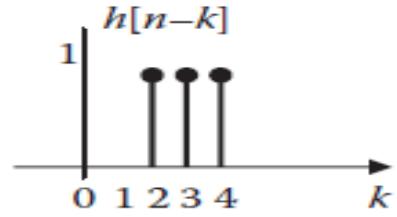
$$n = 1$$
$$y = 1$$



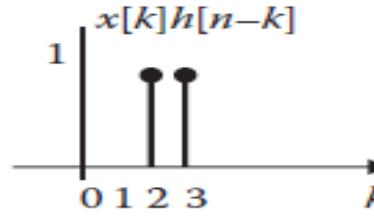
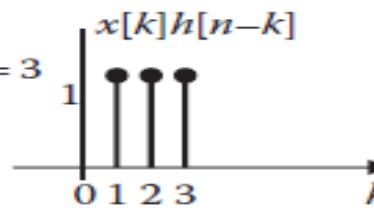
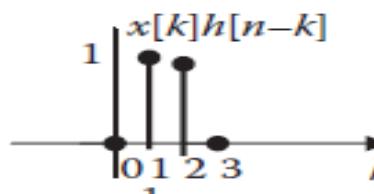
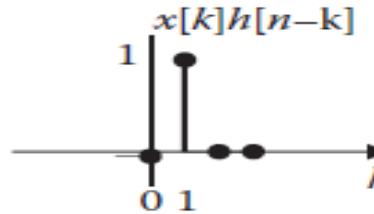
$$n = 2$$
$$y = 1 + 1 = 2$$



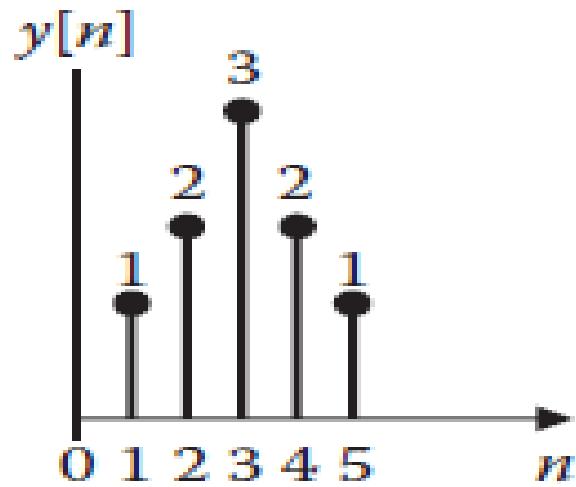
$$n = 3$$
$$y = 1 + 1 + 1 = 3$$



$$n = 4$$
$$y = 1 + 1 = 2$$



Discrete Convolution



Discrete Convolution

Example

Consider a discrete-time LTI system for which the input and impulse functions are given by

$$x[n] = (0.7)^n u[n], \quad h[n] = (0.2)^n u[n]$$

Find the response $y[n]$.

Solution

$$y[n] = x[n] * h[n] = \sum_{k=-\infty}^{\infty} x[k]h[n-k]$$

But $x[k] = (0.7)^k u[k]$ and $h[n-k] = (0.2)^{n-k} u[n-k]$

Because $x[n]$ and $h[n]$ are causal, we can use Equation 2.27.

$$\begin{aligned} y[n] &= x[n] * h[n] = \sum_{k=0}^n (0.7)^k (0.2)^{n-k}, \quad n = 0, 1, 2, \dots \\ &= (0.2)^n \sum_{k=0}^n \left(\frac{0.7}{0.2}\right)^k \end{aligned}$$