

## MAT217 OLASILIK

### FORMÜL KAĞIDI

$$F(X_0) = P(X \leq x_0)$$

$$\mu = E(X) = \sum_x x \cdot P(X = x)$$

$$\mu = E(X) = \int x \cdot f(x) dx$$

$$E(a) = a$$

$$E(aX + b) = a \cdot E(X) + b$$

$$Var(X) = V(X) = \sigma^2 = \sum_x (x - \mu)^2 P(X = x)$$

$$Var(X) = V(X) = \sigma^2 = \int (x - \mu)^2 P(X = x)$$

$$Var(X) = V(X) = \sigma^2 = E(X^2) - [E(X)]^2$$

$$Var(aX + b) = a^2 Var(X)$$

$$g(x) = \sum_y f(x, y)$$

$$g(x) = \int_y f(x, y) dy$$

$$h(y) = \sum_x f(x, y)$$

$$h(y) = \int_x f(x, y) dx$$

$$f(x|y) = \frac{f(x, y)}{h(y)}$$

$$f(y|x) = \frac{f(x, y)}{g(x)}$$

$$\mu_{g(x, y)} = E[g(x, y)] = \sum_x \sum_y g(x, y) f(x, y)$$

$$\mu_{g(x, y)} = E[g(x, y)] = \int_x \int_y g(x, y) f(x, y) dy dx$$

$$Cov(X, Y) = E[(X - \mu_x)(Y - \mu_y)] = E(XY) - \mu_x \mu_y$$

$$Cov(X, Y) = E[(X - \mu_x)(Y - \mu_y)] = \sum_x \sum_y (x - \mu_x)(y - \mu_y) f(x, y)$$

$$Cov(X, Y) = E[(X - \mu_x)(Y - \mu_y)] = \int_y \int_x (x - \mu_x)(y - \mu_y) f(x, y) dx dy$$

$$\rho_{XY} = Corr(X, Y) = \frac{Cov(X, Y)}{\sqrt{Var(X) \cdot Var(Y)}} = \frac{Cov(X, Y)}{\sigma_X \sigma_Y}$$

### Kesikli Uniform Dağılım

$$P(X = x) = \begin{cases} \frac{1}{k} & x = 1, 2, 3, \dots, k \\ 0 & \text{d.d.} \end{cases} \quad E(x) = \frac{k(k+1)}{2}, \quad Var(x) = \frac{(k-1)(k+1)}{12}$$

### Bernoulli Dağılımı

$$P(X=x)=\begin{cases} p^x \cdot (1-p)^{1-x} & x=0,1 \\ 0 & d.d. \end{cases} \quad E(x)=p, \quad Var(x)=p(1-p)$$

### Binom Dağılımı

$$P(X=x)=\begin{cases} \binom{n}{x} p^x (1-p)^{n-x} & x=0,1,2,\dots,n \\ 0 & d.d. \end{cases} \quad E(x)=n.p, \quad Var(x)=n.p(1-p)=n.p.q$$

### Negatif Binom Dağılımı

$$P(X=x)=\begin{cases} \binom{x-1}{k-1} p^k (1-p)^{x-k} & x=k, k+1, k+2, \dots \\ 0 & d.d. \end{cases} \quad E(x)=\frac{k}{p}, \quad Var(x)=\frac{k(1-p)}{p^2}=\frac{k.q}{p^2}$$

### Geometrik Dağılım

$$P(X=x)=\begin{cases} p(1-p)^{x-1} & x=1,2,3,\dots \\ 0 & d.d. \end{cases} \quad E(x)=\frac{1}{p}, \quad Var(x)=\frac{(1-p)}{p^2}=\frac{q}{p^2}$$

### Hipergeometrik Dağılım

$$P(X=x)=\begin{cases} \frac{\binom{M}{x} \binom{N-M}{n-x}}{\binom{N}{n}} & x=0,1,2,\dots,n, \quad x \leq M, \quad n-x \leq N-M \\ 0 & d.d. \end{cases}$$

$$E(x)=n \frac{M}{N}, \quad Var(x)=\left(\frac{N-n}{N-1}\right) n \left(\frac{M}{N}\right) \left(1-\frac{M}{N}\right)$$

### Poisson Dağılımı

$$P(X=x)=\begin{cases} \frac{e^{-\lambda} \lambda^x}{x!} & x=0,1,2,\dots \quad \lambda > 0 \\ 0 & d.d. \end{cases} \quad E(x)=\lambda, \quad Var(x)=\lambda$$

### Süreklî Uniform Dağılım

$$f(x)=\begin{cases} \frac{1}{b-a} & a < x < b \\ 0 & d.d. \end{cases} \quad E(x)=\frac{(a+b)}{2}, \quad Var(x)=\frac{(b-a)^2}{12}$$

### Üstel Dağılım

$$f(x)=\begin{cases} \frac{1}{\beta} e^{-\frac{x}{\beta}} & x > 0 \\ 0 & d.d. \end{cases} \quad E(x)=\beta, \quad Var(x)=\beta^2 \quad P(X \geq a)=e^{-\frac{a}{\beta}}$$

## Normal Dağılım

$$f(x) = \begin{cases} \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2} & -\infty < x < \infty, \quad -\infty < \mu < \infty, \quad \sigma^2 > 0 \\ 0 & \text{d.d.} \end{cases} \quad E(x) = \mu, \quad Var(x) = \sigma^2$$

## Standart Normal Dağılım

$$Z = \frac{x - \mu}{\sigma}$$

$$f(z) = \begin{cases} \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}z^2} & -\infty < x < \infty, \quad \mu = 0, \quad \sigma^2 = 1 \\ 0 & \text{d.d.} \end{cases}$$