Example A1-3 KCL (Supernode)

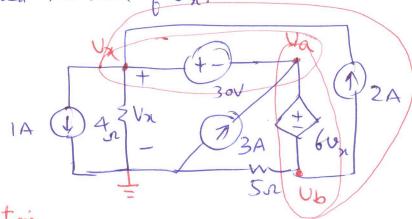
[PD 796 8th Ed Hel))

Find the value of Un. 14 30 V 1A D V 24 1 2 3A Solution: Applying KCL at Vx? $7 - 1 - \frac{U_{x}}{4} + 3 + \frac{-U_{x} - V_{A}}{5} = 0$ Now VA = -30-6Ux $-1 - \frac{Ux}{4} + 3 + \frac{-Ux}{5} + \frac{30 + 60x}{5} = 0$ $-20 - 50x + 60 + \frac{200x}{120} + 120 = 0$ $V_{H} = -\frac{160}{183}$ $V_{n=-\frac{32}{3}}$ Volts

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Example A 1-3 KCL (Supernode) (Different Reference) (PD 796 8th Ed HKD)

Find the Value of Un.



Solution

$$\frac{\text{kcl}}{\text{Suprude}} = \frac{1 + \frac{Un}{4} - 3 + \frac{Ub}{5} = 0}{4} = \frac{0}{4} + \frac{\frac{Ub}{5}}{5} = \frac{2}{3} \times \frac{20}{3}$$

$$\frac{5 u_{x} + 4 u_{b}}{4} = \frac{40}{5} = \frac{1}{4} = \frac{1}{5}$$

Constraint = NS

$$U_{n}-U_{a}=30 \qquad \text{or} \quad U_{a}=U_{n}-30$$

$$U_{a}-U_{b}=6U_{n}$$

So
$$u_{n}-30-0b=6u_{n}$$

 $5u_{n}+0b=-30$ — ② $\times 4$
 $5u_{n}+40b=-120$

$$-150_{\pi} = 160$$

$$0_{\pi} = -\frac{32}{3} \text{ Volts}.$$

as before