

## DSA

- Arrays are contiguous in memory
  - ↳ not a variable ; just a name of a collection
  - ↳ not an lvalue that can be written on LHS of =
  - $x[n]$  →  $x[1] = 2$ ; // valid  
→  $x = 2$ ; // invalid  
→ + base addr
  - array address = elem size \* (i - first index)
    - ↳ constant access time

### • 2D Array

- ↳ in memory , 2D arrays are also contiguous

row major	$[i_1, j_1   i_1, j_2   i_2, j_1   \dots]$
col. major	$[i_1, j_1   i_2, j_1   i_1, j_2   \dots]$

$$\rightarrow \text{row major} = \text{base addr} + \text{elem size} ((i - \text{first index})N + (j - \text{first index}))$$

$$\rightarrow \text{col. major} = \text{base addr} + \text{elem size} ((i - \text{first index}) + (j - \text{first index})M)$$

M : row length  
 N : col. length } Example : arr [1 ... 10][1 ... 15]  
 base = 100 size = 1  
 Find arr [8][6]

Answer

row major → 210

- 3D Array

↳ (width, row, col.)

$$\rightarrow \text{row major} = \text{base addr} + \text{elem size} (\text{MN}(i - \text{first elem})) \\ \dots + N(j - \text{first elem}) + (k - \text{first elem}))$$

Example } arr [1:9, -4:1, 5:10] size = 2

base = 400 sign is considered

- Find arr [5][-1][8]

Answer

row major  $\rightarrow \underline{\underline{730}}$

$$\rightarrow \text{lcm(rows / cols / width)} = \text{Upper} - \text{lower} + 1$$

$$\rightarrow \text{col major} = \text{base addr} + \text{elem size} (\text{MN}(i - \text{first elem})) \\ \dots + (j - \text{first elem}) + M(k - \text{first elem}))$$

Example } arr [1:8, -5:5, -10:-5] size = 4

base = 400

- Find arr [3][3][3]

Answer

col major  $\rightarrow \underline{\underline{2412}}$

Dry Run

$\xrightarrow{\text{slides}}$

1	2
3	4

output

DSAstructure  
class

C specific / in C++, functionality is same  
 ↗ public vs. private  
 scope, polymorphism is not applicable  
 to structs ; unlike classes

pointers contain address of a variable

const & pointers

1. pointer to a constant [pointer value cannot be changed but location can]

- └ const int \* px = &x;
- └ \*px = 1; => invalid ] example
- └ px = &y; => valid

2. constant pointer [location can't be changed but value can]

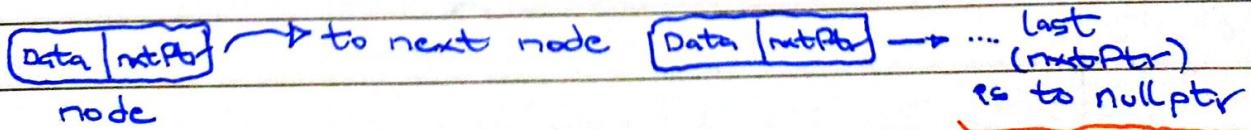
- └ int \* const ptr = &a;
- └ \*ptr = 32; => valid
- └ ptr = &b; => invalid

3. constant pointer to a constant [neither can change]

- └ const int \* const ptr = &a;

→ int \* const r = &n; ≡ int dr = n;

linked list



to grow linked list in size ; change nullptr to next (new) node

## Advantages

- └ dynamic
- └ easy insertion and deletion

## Disadvantages

- └ efficient search not possible
- └  $O(n)$  complexity for random access  
worst case

## • Creating a Linked list

- └ pointers to NULL
- └ inserting
- └ deleting
- └ traversing

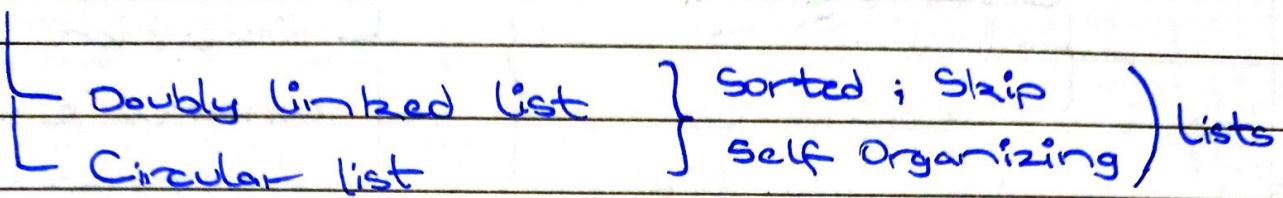
see implementations

from slides (easy stuff :))

→ important : reversing a linked list

# DSA

## • Linked List Variants



## • Doubly linked list



- [ add to tail ()      { Read from slides }  
delete from tail () ]

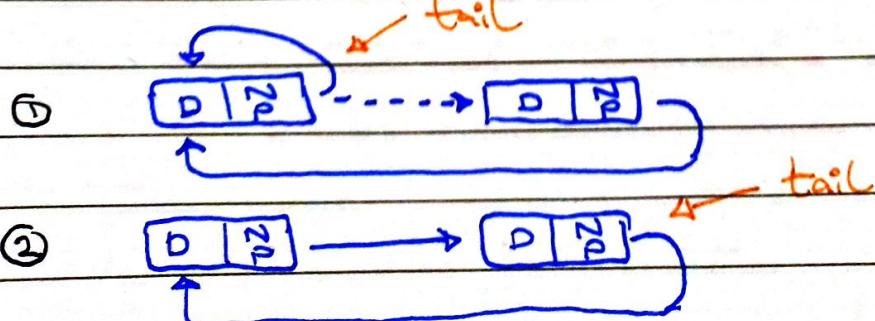
## • Circularly linked list

- [ for compute processes ; current pointer  
points to the executing process  
only one permanent pointer ; "tail"



initial case (only one node)

add to tail()



## DSA

- Arrays of Linked Lists

↳ can manage a collection of linked lists using arrays

- see practical implementation from slides

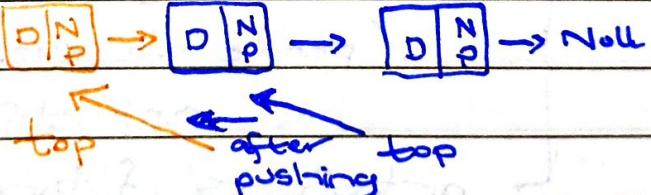
- Stack {LIFO / FILO}

↳ Top : Pointer to the first (top) element  
Stack under/over flow ⇒ adding to a full stack results in overflow ; removing from empty stack results in underflow

→ [array based] } easy

→ [linked list based]

↳ push()



↳ Stacks for Validating Expression

i.e.  $(A + B)$

$[C + (A * B)]$

from slides

DSA• Operands & Operators

└  $(*) = (/) \Rightarrow (+) = (-)$  DMAS

└ if same prio. operators are used, precedence is towards the left

infix {normal "x+y, a\*b"}  
etc.

prefix  $\equiv * + xyz \rightarrow * (x+y)z \rightarrow (x+y)*z$  etc.

postfix  $\equiv xyz^*+$  etc.

→ Algo.

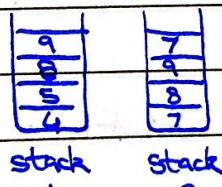
•  $(A+B)/C + D \rightarrow \text{out} = AB + C/D +$

• Adding large numbers

num 1: 4589

+  
num 2: 7897

carry = 0



Pop from each stack ; add ; push unit part to the result stack ; continue

if carry is non-zero after both stacks are empty ; append carry result to result stack

→ Recursion | Divide & conquer

# DSA

- Queue

- when  $\text{front} == \text{rear}$ ; queue is empty
  - if  $\text{rear} == \text{size} - 1$ ; queue is full (!?)
  - not true; check slides
  - solution (circular queue)  $\approx$
  - maintain a counter

## Read from slides

- Real World : Data Structures

- Tree is non-linear {unlike arrays, etc}
  - special node  $\equiv$  root
  - other nodes are partitioned into disjoint sets

- Trees & Leaves : {leaves do not have any outgoing arcs/links}

- depth of a node  $\sqcap$  links from the root of the tree

- root := only outwards
  - inner := both inwards & outwards
  - leaf := only inwards

- Binary Trees {left & right}

- read from slides

DSA• Trees {Binary}

## └ Traversal

└ Pre order (RLR<sup>i</sup>)└ In order (LRR<sup>i</sup>)└ Post order (LR<sup>i</sup>R)

correspond to  
 prefix, infix & postfix  
 when evaluating expressions

∴ R<sup>i</sup> : right

R : root

L : left

• Binary Search Tree

└ value in left child < <sup>current value</sup> < value in right child  
 └ in order → ascending order

• Huffman Coding {compression}

└ occurrence probabilities → variable length codes  
 └ lossless  
 prefix of one cannot be another code

$$N_{avg} = \sum_k N_k P(k)$$

$$\therefore P(k) = f(k)/\tau$$

↳ frequency ↳ total

~ Deletion of BST

DSA• Big-O Notation

↳ analysis of algorithm's efficiency

- complexity in terms of input size
- machine independent
- instruction dependent

→ worst / best / avg case

e.g.  $O(n)$  implies size increases linearly  
 $O(n^2) \rightarrow$  quadratic

Rules

↳ ignore constants

↳ terms dominate one - another { lower ones are ignored } | dropped }

• AVL Trees → Search:  $O(\log n)$ 

↳ self-balancing binary search tree (BST)

↳ difference b/w left and right subtrees for any node is the "balance factor"

$$BF(x) = \text{height}(x \rightarrow \text{right}) \dots$$

$$- \text{height}(x \rightarrow \text{left})$$

↓  
balanced when  $BF < 2$

DSA• Left - Left (LL) case

- └ node as well as its child is left-heavy
- └ make
- └ root → left = left child's right
- └ left child's right = root
- └ ↗ theoretical / not-algorithmic

• Right - Right (RR) case

- └ → same operations but  
replace left with right  
and vice versa

• Left - Right (LR) case

- └ when node is left-heavy but its  
left child is right-heavy

• Right - Left (RL) case

- └ inverse of LR case

Heap (As almost complete binary tree)

Implemented through arrays

$$\left. \begin{array}{l} \text{Parent}(i) \rightarrow i/2 \\ \text{Left}(i) \rightarrow 2i \\ \text{Right}(i) \rightarrow 2i + 1 \end{array} \right\} \text{indexing}$$

→ max-heap } root of sub-tree holds max

→ min-heap } " " " min

- read operations from slides
- ↑ ↑

- when heapifying

└ redundant to call `heapify()` on leaf nodes

→  $n/2$  to 1

$$\hookrightarrow O\left(\frac{n \log n}{2}\right) \sim O(n \log n)$$

Average is  $\Omega(n)$

- heapsort

└ given array A

└ build maxheap (A)

└ exchange  $A[1] \leftrightarrow A[i]$

└ decrease size [detach element]

└ call max-heap again

repeat

priority queue

Each element has a property that defines its priority

day/date

24<sup>th</sup> April / 2024 , 1

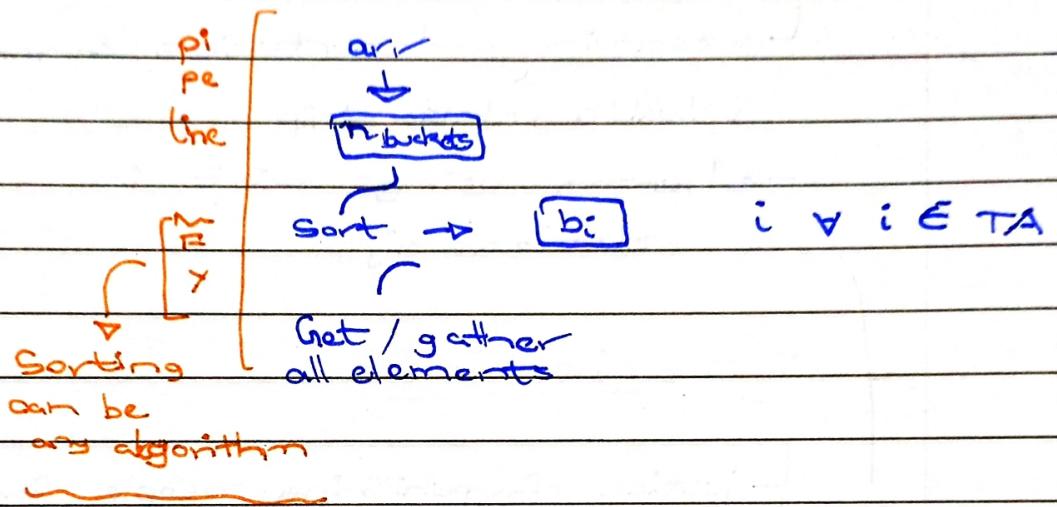
## DSA

### Sorting Algos.

- Bubble Sort → for small arrays
  - └ 1<sup>st</sup> loop →  $(n-1)$  comparisons
  - └ 2<sup>nd</sup> loop →  $(n-2)$ ; so on
    - ↳ check iterative & recursive implementation from slides
- Insertion Sort
  - └ efficient for small - arrays
  - └ rest from slides ~~
- Selection Sort
  - └ search (min/max) elements and put in selected position
    - └  $O(n^2)$  ; again, does not work on large datasets
- Merge Sort
  - └ Divide and Conquer
  - └ solve multiple subproblems
  - └ base case ⇒ p == r (array of size 1)
- Bucket Sort
  - └ create n empty buckets & loop
  - └ find bucket index and insert into buckets

DSA

## → continued Bucket Sort



## • Quicksort

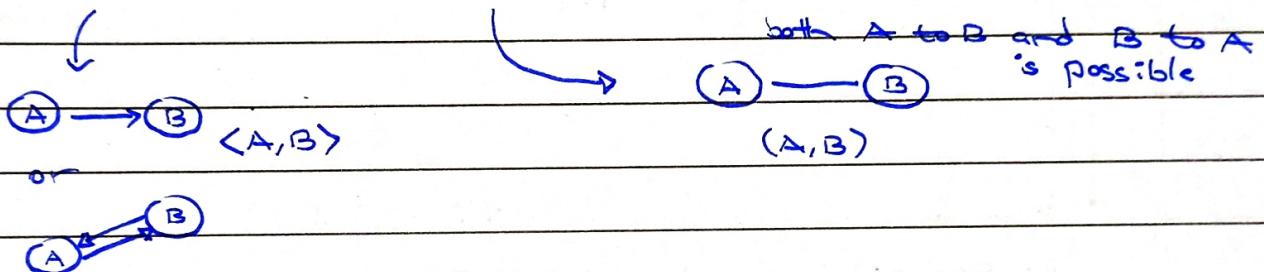
- └ select pivot element (i.e. rightmost)
- └ make larger/smaller pointers for elements > or < pivot
- └ swap until pivot is in correct position
- └ Rest from slides

## Data Structures & Algos.

### Graphs

$G = (V, E)$  where  $V$  is set of vertex  
 $E$  is set of edges b/w  
the vertices

### Directed & undirected graphs



Also expressed as nodes and paths  
→ read slides for classifications

Adjacency Matrix  $\rightarrow$  where 1 denotes existence of edge

$\begin{bmatrix} A \\ B \\ C \\ D \\ E \end{bmatrix}$	$\begin{bmatrix} A & B & C & D & E \\ B & " & " & " & " \\ C & " & " & " & " \\ D & " & " & " & " \\ E & " & " & " & " \end{bmatrix}$	$\rightarrow$ for undirected graph, symmetry about diagonal exists
$N$ vertex	diagonal edges can exist	

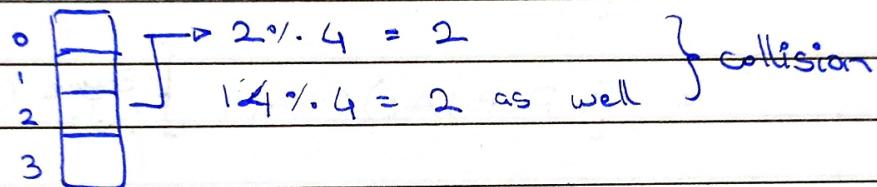
### Adjacency List

L can be implemented using Linked Lists

{ See C++ implementations from slides }

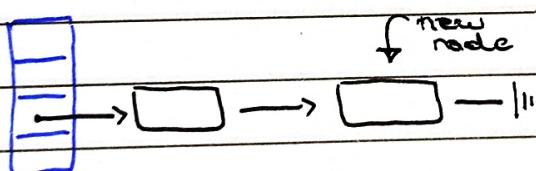
DSAGraph Traversal

- Depth-first  $\rightsquigarrow$  Stack
- Breadth-first  $\rightsquigarrow$  Queue

Hash Table {key: value} pairs

② [ Open Chaining (Separate)  
 Hashing ]

Same index start chaining



	best	worst
insert	$O(1)$	$O(n)$
find	$O(1)$	$O(n)$
delete	$O(1)$	$O(n)$

} at ends of  
linked list

Load factor  $\lambda = n/c$

③ [ Closed } open  
 Hashing } Addressing

L Linear Probing [Add 1 if index is occupied]