

Solution
Quiz 3 Mobile Communication

- a) Suppose that a non-line-of-sight wireless channel at 1.9 GHz has an rms delay spread of 100 ns. Further, suppose the mobile terminal is moving with a speed of 70 miles/hr. If a BPSK signal is transmitted with a bit rate of 22 Mbps, then give a complete description of the small-scale fading that this signal will undergo. (Flat or frequency selective and slow or fast)?
- b) If the speed of the mobile is increased to 100 km/hr, whether the channel will be frequency selective or flat? Explain.

$$f_c = 1.9 \times 10^9 \text{ Hz} ; \sigma_{\tau} = 100 \text{ ns} ; V = 70 \text{ miles/hr}$$

$$R_b = 22 \text{ Mbps} \quad V = 31.29 \text{ m/s}$$

(a) $R_b = R_s \Rightarrow T_s = 1/R_s$

$$T_s = 1/22 \times 10^6 = \boxed{45 \text{ ns}}$$

$\therefore \sigma_{\tau} > 0.2 T_s$ } Frequency Selective.

$100 \text{ ns} > 0.2 (45 \text{ ns})$

$$\lambda = c/f \Rightarrow \lambda = 3 \times 10^8 / 1.9 \times 10^9 = \boxed{0.1579 \text{ m}}$$

$$f_m = V/\lambda = 31.29 / 0.1579 = \boxed{198.661 \text{ Hz}}$$

$$T_c = \frac{0.423}{f_m} = \frac{0.423}{198.661} = \boxed{2.12 \text{ ms}}$$

$\therefore T_c \gg T_s$ } slow fading.

$2.12 \text{ ms} \gg 45 \text{ ns}$

- b) increasing speed doesn't effect the doppler frequency & T_c , channel will remain freq selective.
- Coherence bandwidth.

Quiz 4 Mobile Communication

Consider the following digital wireless systems,

System	Data Rate (kbps)	Modulation	
USDC	48.6	$\pi/4$ DQPSK	a)
GSM	270.833	GMSK	b)
DECT	1152	GMSK	c)
			d)

- a) Estimate the maximum rms delay spread for each system for which no equalizer is required at the receiver (neglect channel coding). Note that GMSK has one bit per symbol and DQPSK has 2 bits per symbol.
- b) If GSM at 900MHz has a non line-of-sight communication with a level crossing rate of 3 crossing per second at a threshold $p = -20\text{dB}$, what can be predicted about the time-varying nature of the channel (fast or slow)?

part a:

(a) USDC: $K=2$, $T_s = \frac{2}{48.6} \Rightarrow T_s = 41.15 \mu\text{s}$

$$\frac{\sigma_{\epsilon}}{T_s} \leq 0.1 \Rightarrow \sigma_{\epsilon \text{ max}} = 4.1 \mu\text{s}$$

(b) GSM: $K=1$, $T_s = \frac{1}{270.833} \Rightarrow T_s = 3.69 \mu\text{s}$

$$\frac{\sigma_{\epsilon}}{T_s} \leq 0.1 \Rightarrow \sigma_{\epsilon \text{ max}} = 369 \text{ ns}$$

(c) DECT: $K=1$, $T_s = \frac{1}{1152} \Rightarrow T_s = 868 \text{ ns}$

$$\frac{\sigma_{\epsilon}}{T_s} \leq 0.1 \Rightarrow \sigma_{\epsilon \text{ max}} = 86.8 \text{ ns}$$

part b: $f_c = 900 \text{ MHz}$, $N_k = 3/\text{sec}$, $P = -20 \text{ dB} = 0.1 \text{ W}$

$$NR = \sqrt{2\pi} f_m (0.1) e^{-(0.1)^2}$$

$$f_m = 12.08 \text{ Hz}$$

$$T_s = 1/R_b$$

$$T_s = 1/270.833$$

$$T_s = 3.69 \mu\text{s}$$

$$T_c = \frac{0.423}{f_m}$$

$$T_c = \frac{0.423}{12.08}$$

$$T_c = 0.035 \text{ s}$$

$$T_c \gg T_s \text{ (slow fading)}$$