Magnetic Circuits & Linear DC Machine	Transformers		
$\mathfrak{F} = \phi \mathfrak{R} \qquad \mathfrak{P} = \frac{l_c}{\mu A} \qquad B = \mu H = \frac{\mu N i}{l_c}$	$\frac{\mathbf{V}_P}{\mathbf{V}_S} = a \qquad \frac{\mathbf{I}_P}{\mathbf{I}_S} = \frac{1}{a}$		
$e_{\text{ind}} = (\mathbf{v} \times \mathbf{B}) \cdot \mathbf{l} \qquad \mathbf{F} = i(\mathbf{l} \times \mathbf{B})$	$VR = \frac{V_{S,nl} - V_{S,fl}}{V_{S,fl}} \times 100\% \qquad \eta = \frac{P_{out}}{P_{out} + P_{loss}} \times 100\%$		
As Generator: $e_{ m ind} = V_B + iR$ As Motor: $e_{ m ind} = V_B - iR$	$\mathbf{V}_{P} = \mathbf{V}_{S}' + \mathbf{I}_{S}' \left(R_{eq} + jX_{eq} \right)$ $\mathbf{V}_{S}' = a\mathbf{V}_{S} \qquad \mathbf{I}_{S}' = \frac{\mathbf{I}_{S}}{a}$ $VR = \frac{V_{P} - aV_{S}}{aV_{S}} \times 100\%$ Referred to primary*		
	$\mathbf{V}_{P}^{'} = \mathbf{V}_{S} + \left(R_{EQ} + jX_{EQ}\right) \mathbf{I}_{S}$ $\mathbf{V}_{P}^{'} = \frac{\mathbf{V}_{P}}{a}$ $VR = \frac{V_{P}/a - V_{S,fl}}{V_{S,fl}} \times 100\%$ No load voltage: referred to secondary*		

Autotransformers	Three-phase Transformers		
$\frac{\mathbf{V}_L}{\mathbf{V}_H} = \frac{N_C}{N_{\text{SE}} + N_C} \qquad \frac{\mathbf{I}_L}{\mathbf{I}_H} = \frac{N_{\text{SE}} + N_C}{N_C}$	$\frac{V_{\rm LP}}{V_{\rm LS}} = \frac{\sqrt{3}V_{\phi P}}{\sqrt{3}V_{\phi S}} = a \qquad Y - Y$		
$\frac{S_{\rm IO}}{S_W} = \frac{N_{\rm SE} + N_C}{N_{\rm SE}}$	$rac{V_{ m LP}}{V_{ m LS}} = rac{V_{\phi P}}{V_{\phi S}} = a \qquad \Delta - \Delta$		
When 'transforming' (hehe) a simple transformer to a step up/down autotransformer, use the rated power of the original transformer as S_W , i.e., the power in the windings	$\frac{V_{\rm LP}}{V_{\rm LS}} = \sqrt{3}a \qquad Y - \Delta$		
The effective per-unit impedance of autotransformers is decreased by the power advantage factor, i.e., $\frac{S_{IO}}{S_W}$	$\frac{V_{\rm LP}}{V_{\rm LS}} = \frac{a}{\sqrt{3}} \qquad \Delta - Y$		
	$Z_{\text{base}} = \frac{3(V_{\phi, \text{base}})^2}{S_{\text{base}}} \qquad I_{L, \text{base}} = \frac{S_{\text{base}}}{\sqrt{3}V_{L, \text{base}}}$		

AC Machinery $\theta_{se} = \frac{P}{2}\theta_{sm} \qquad f_{se} = \frac{P}{2}f_{sm} \qquad \omega_{se} = \frac{P}{2}\omega_{sm} \qquad f_{se} = \frac{n_{sm}P}{120}$ $i_{aa'}(t) = I_{M}\sin\omega t \qquad A \qquad \qquad \mathbf{B}_{aa'}(t) = B_{M}\sin\omega t \ge 0^{\circ} \qquad \mathbf{T}$ $i_{bb'}(t) = I_{M}\sin(\omega t - 120^{\circ}) \qquad A \qquad \mathbf{B}_{bb'}(t) = B_{M}\sin(\omega t - 120^{\circ}) \ge 120^{\circ} \qquad \mathbf{T}$ $i_{cc'}(t) = I_{M}\sin(\omega t - 240^{\circ}) \qquad A \qquad \mathbf{B}_{cc'}(t) = B_{M}\sin(\omega t - 240^{\circ}) \ge 240^{\circ} \qquad \mathbf{T}$ To reverse direction of rotating magnetic field, swap any two of the three phases*

$$e_{\text{ind}} = \phi_{\text{max}} \omega \sin \omega t \qquad E_{\text{max}} = N_C \phi \omega \qquad E_A = \sqrt{2} \pi N_C \phi f$$

$$\tau_{\text{ind}} = k \mathbf{B}_R \times \mathbf{B}_S \qquad \tau_{\text{ind}} = k B_R B_{\text{net}} \sin \delta$$

$$P_{\text{out}} = 3 V_\phi I_A \cos \theta \text{ or } \sqrt{3} V_L I_L \cos \theta$$

$$VR = \frac{V_{\text{nl}} - V_{\text{fl}}}{V_{\text{fl}}} \times 100\% \qquad SR = \frac{n_{\text{nl}} - n_{\text{fl}}}{n_{\text{fl}}} \times 100\%$$

Synchronous Generator

$$E_A = \sqrt{2}\pi N_C \phi f$$
 $E_A = K\phi \omega$ $K = \frac{N_c}{\sqrt{2}}$

$$\mathbf{V}_{\phi} = \mathbf{E}_{A} - jX_{S}\mathbf{I}_{A} - R_{A}\mathbf{I}_{A} \qquad P_{\text{conv}} = \frac{3V_{\phi}E_{A}}{X_{S}}\sin\delta$$

$$P_{\max} = \frac{3V_{\phi}E_{A}}{X_{S}}$$
 $au_{\text{ind}} = \frac{3V_{\phi}E_{A}}{\omega_{m}X_{S}}\sin\delta$

Static stability limit

$$Z_S = \sqrt{R_A^2 + X_S^2} = \frac{E_A}{I_A} = \frac{V_{\phi,oc}}{I_A}$$
 $2R_A = \frac{V_{DC}}{I_{DC}}$ $\frac{2}{3}R_A = \frac{V_{DC}}{I_{DC}}$

Y-Connected Δ-Connected

Identifying synchronous generator's parameters*

$$P = s_p(f_{nl} - f_{sys}) \qquad Q = s_p(V_{T,nl} - V_{T,fl})$$

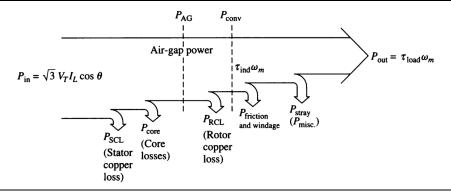
Adjusting governor set points adjusts f, and hence control the real power supplied by the generator

Adjusting field current adjusts V_T , and hence controls the reactive power supplied by the generator

Induction Motors

$$n_{\text{slip}} = n_{\text{sync}} - n_m$$
 $s = \frac{n_{\text{sync}} - n_m}{n_{\text{sync}}} (\times 100\%)$ $n_m = (1 - s)n_{\text{sync}}$

$$f_{re} = sf_{se}$$
 $f_{re} = \frac{P}{120} (n_{sync} - n_m)$



$$P_{\text{RCL}} = 3I_2^2 R_2$$
 $P_{\text{SCL}} = 3I_1^2 R_1$ $P_{\text{conv}} = 3I_2^2 R_2 \left(\frac{1-s}{s}\right)$ $P_{\text{core}} = 3E_1^2 G_C$ $P_{\text{AG}} = 3I_2^2 \frac{R_2}{s}$

$$P_{\text{RCL}} = s P_{\text{AG}}$$
 $P_{\text{conv}} = (1 - s) P_{\text{AG}}$ $\tau_{\text{ind}} = \frac{P_{\text{conv}}}{\omega_m} = \frac{P_{\text{AG}}}{\omega_{\text{sync}}}$

$$\begin{split} V_{\rm TH} &= V_{\phi} \frac{X_M}{\sqrt{R_1^2 + (X_1 + X_M)^2}} \qquad V_{\rm TH} \approx V_{\phi} \frac{X_M}{X_1 + X_M} \\ R_{\rm TH} &\approx R_1 \bigg(\frac{X_M}{X_1 + X_M} \bigg)^2 \qquad X_{\rm TH} \approx X_1 \end{split}$$

$$\tau_{\text{ind}} = \frac{3V_{\text{TH}}^2 R_2/s}{\omega_{\text{sync}} [(R_{\text{TH}} + R_2/s)^2 + (X_{\text{TH}} + X_2)^2]} \qquad s_{\text{max}} = \frac{R_2}{\sqrt{R_{\text{TH}}^2 + (X_{\text{TH}} + X_2)^2}}$$
$$\tau_{\text{max}} = \frac{3V_{\text{TH}}^2}{2\omega_{\text{sync}} [R_{\text{TH}} + \sqrt{R_{\text{TH}}^2 + (X_{\text{TH}} + X_2)^2}]}$$

Maximum torque occurs at a point (s_{max}) independent of change in V_T^* Maximum torque value is independent of change in rotor resistance R_2^*

No-Load Test
$$P_{\text{in}} = 3I_{1}^{2}R_{1} + P_{\text{rot}}$$

$$P_{\text{rot}} = P_{\text{core}} + P_{\text{F\&W}} + P_{\text{misc}}$$

$$|Z_{\text{eq}}| = \frac{V_{\phi}}{I_{1,\text{nl}}} \approx X_{1} + X_{M}$$

$$P_{\text{F}} = \cos \theta = \frac{P_{\text{in}}}{\sqrt{3}V_{T}I_{L}}$$

$$|Z_{\text{LR}}| = \frac{V_{\phi}}{I_{1}} = \frac{V_{\phi}}{I_{1}} = \frac{V_{T}}{\sqrt{3}I_{L}}$$

$$|Z_{\text{LR}}| = \frac{V_{\phi}}{I_{1}} = \frac{V_{T}}{\sqrt{3}I_{L}}$$

$$|Z_{\text{LR}}| = R_{\text{LR}} + jX'_{\text{LR}}$$

$$= |Z_{\text{LR}}|\cos \theta + j|Z_{\text{LR}}|\sin \theta$$

$$R_{\text{LR}} = R_{1} + R_{2}$$

$$X_{\text{LR}} = \frac{f_{\text{rated}}}{f_{\text{test}}}X'_{\text{LR}} = X_{1} + X_{2}$$

Locked-Rotor Test

DC Test: R_A is R_1 *

	X_1 and X_2 as functions of X_{LR}		
Rotor Design	<i>X</i> ₁	<i>X</i> ₂	
Wound rotor	0.5 X _{LR}	0.5 X _{LR}	
Design A	0.5 X _{LR}	0.5 X _{LR}	
Design B	0.4 X _{LR}	0.6 X _{LR}	
Design C	0.3 X _{LR}	0.7 X _{LR}	
Design D	0.5 X _{LR}	0.5 X _{LR}	

DC Machines

$$e_{\rm ind} = \frac{2}{\pi} \phi \omega_m \qquad \tau_{\rm ind} = \frac{2}{\pi} \phi i$$

Armature loss:
$$P_A = I_A^2 R_A$$
 $\frac{E_{A2}}{E_{A1}} = \frac{K' \phi n_{m2}}{K' \phi n_{m1}}$
Field loss: $P_F = I_F^2 R_F$

$$I_F = \frac{V_F}{R_F}$$

$$V_T = E_A + I_A R_A$$

$$I_L = I_A$$

$$I_F = \frac{V_T}{R_F}$$

$$V_T = E_A + I_A R_A$$

$$I_L = I_A + I_F$$

$$\omega_m = \frac{V_T}{K\phi} - \frac{R_A}{(K\phi)^2} \, \tau_{\text{ind}}$$

$$I_A = I_S = I_L$$

$$V_T = E_A + I_A (R_A + R_S)$$

$$\rho_m = \frac{V_T}{\sqrt{Kc}} \frac{1}{\sqrt{\tau_{ind}}} - \frac{R_A + R_S}{Kc}$$

Field loss:
$$P_F = I_F^2 R_F$$

Field loss: $P_F = I_F^2 R_F$

See characteristic curves from book*

Separately Excited DC			
Generator			

$$V_T = E_A - I_A R_A$$

$$I_F = \frac{V_F}{R_F}$$

$$I_F^* = I_F - \frac{\mathcal{F}_{AR}}{N_F}$$

$$I_A = I_F + I_L$$

$$V_T = E_A - I_A R_A$$

$$I_F = \frac{V_T}{R_F}$$

Series DC

$$I_A = I_S = I_L$$

$$V_T = E_A - I_A(R_A + R_S)$$

Compound DC

Separately Excited DC Generator

$$I_L = I_A$$
 $V_T = E_A - I_A R_A$
 $I_F = \frac{V_F}{R_F}$
 $I_F = \frac{V_F}{N_F}$

Shunt DC Generator

 $I_A = I_F + I_L$
 $I_A = I_S = I_L$
 $I_A = I_S = I_L$
 $I_A = I_L + I_F$
 $I_A = I_L + I$

See characteristic curves from book*

You made it this far! Good luck with your exams! 💗

- Arctic Monkeys makes banger songs
- KitKat >> any chocolate
- Made by me! I should go sleep ...