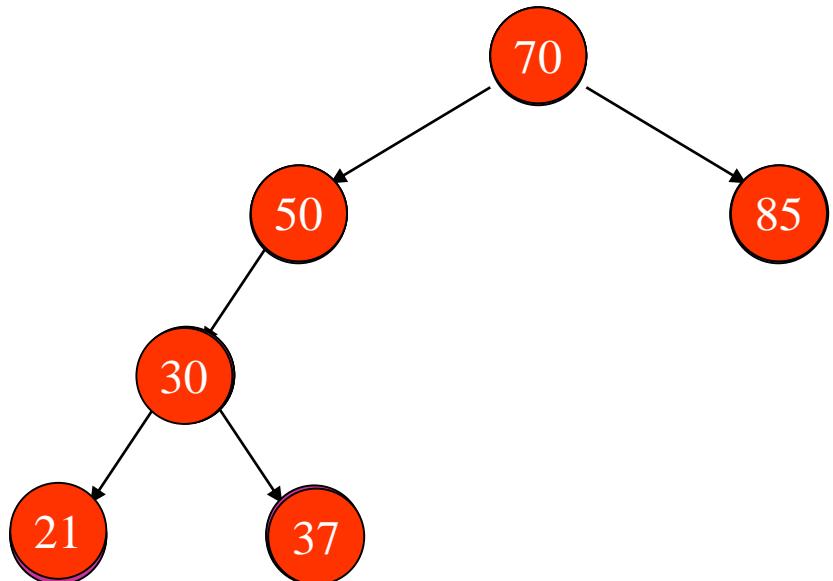


# Binary Search Tree Traversal

## In Order Traversal (LNR)



21 30 37 50 70 85

InOrder(NULL)

InOrder(21)  
InOrder(37)

InOrder(NULL)  
InOrder(30)

InOrder(85)  
InOrder(50)

InOrder(70)

```
if (t) {  
    InOrder(t→left);  
    visit(t);  
    InOrder(t→right);  
}
```

InOrder(37→left)	t=37
visit(37)	t=21
InOrder(37→right)	t=21

InOrder(30→left)	t=30
visit(30)	
InOrder(30→right)	

InOrder(85→left)	t=85
visit(85)	t=50
InOrder(85→right)	t=50

InOrder(70→left)	t=70
visit(70)	
InOrder(70→right)	

# BST Print (Inorder traversal)

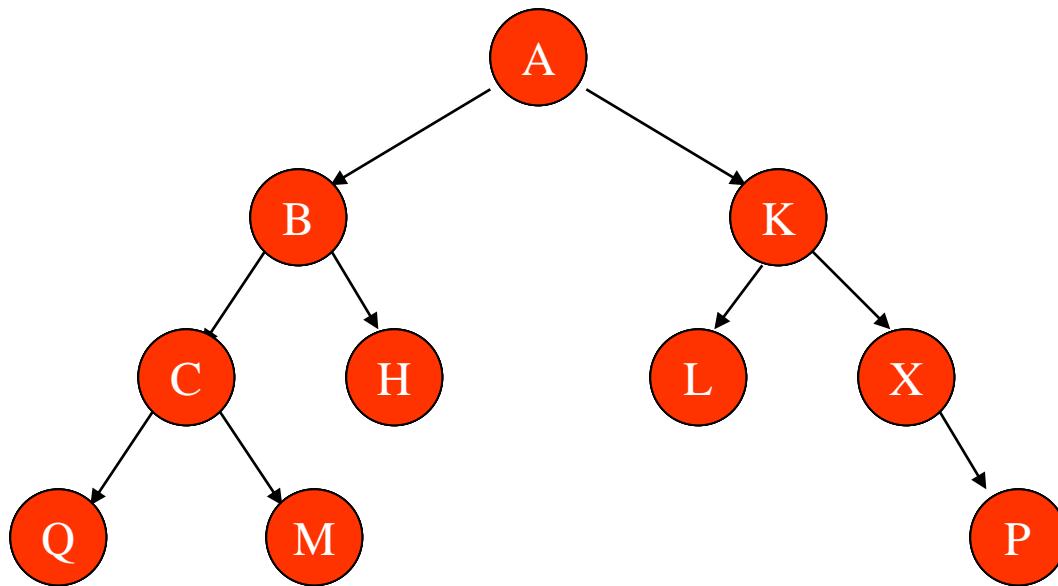
```
template <class type>
void tree<type>::Print() {
    InOrder(root);
}
```

```
template <class type>
void tree<type>::InOrder(Node<type> *t)
{
    if (t) {
        InOrder(t->left);
        visit(t);
        InOrder(t->right);
    }
}
```

```
template <class type>
void tree<type>:: : :visit(Node<type> *t){
    cout << t->data;
}
```

# Binary Tree Traversal

## In Order Traversal (LNR)



```
if (t) {
```

```
    InOrder(t→left);
```

```
    visit(t);
```

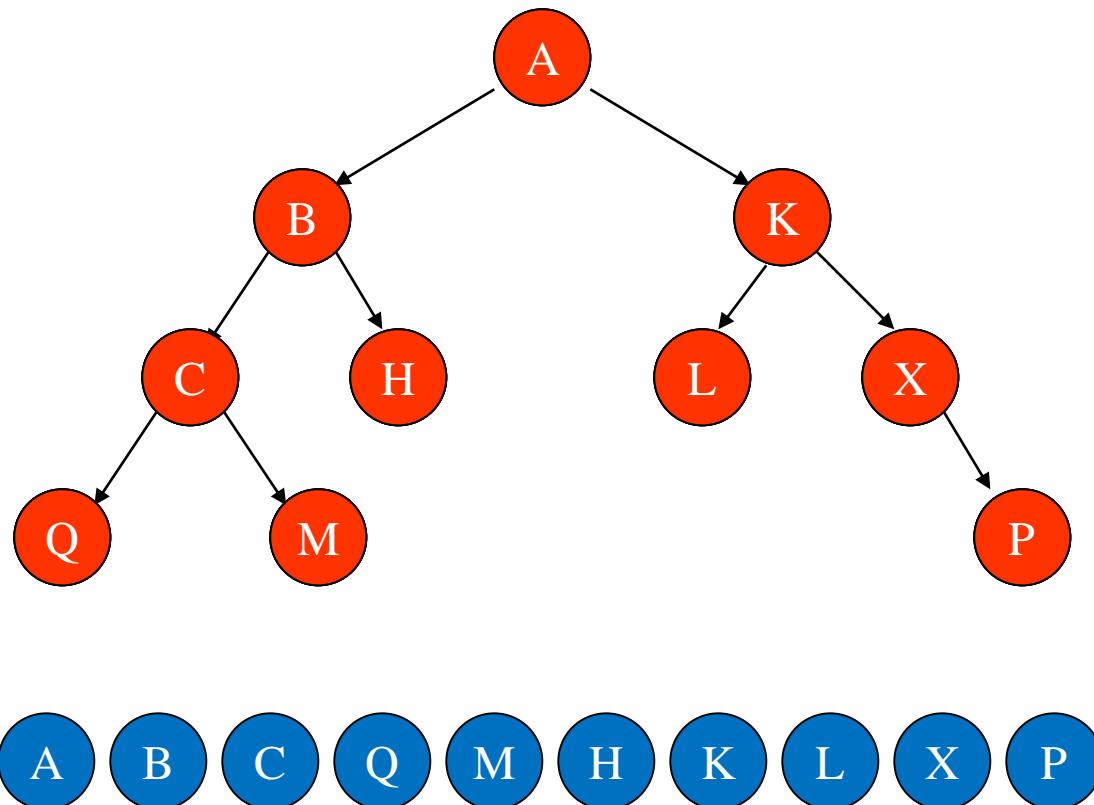
```
    InOrder(t→right);
```

```
}
```



# Binary Tree Traversal

## Pre Order Traversal (NLR)



```
if (t) {  
    visit(t);  
    PreOrder(t→left);  
    PreOrder(t→right);  
}
```

# Binary Tree Traversal

## Pre Order Traversal (NLR)

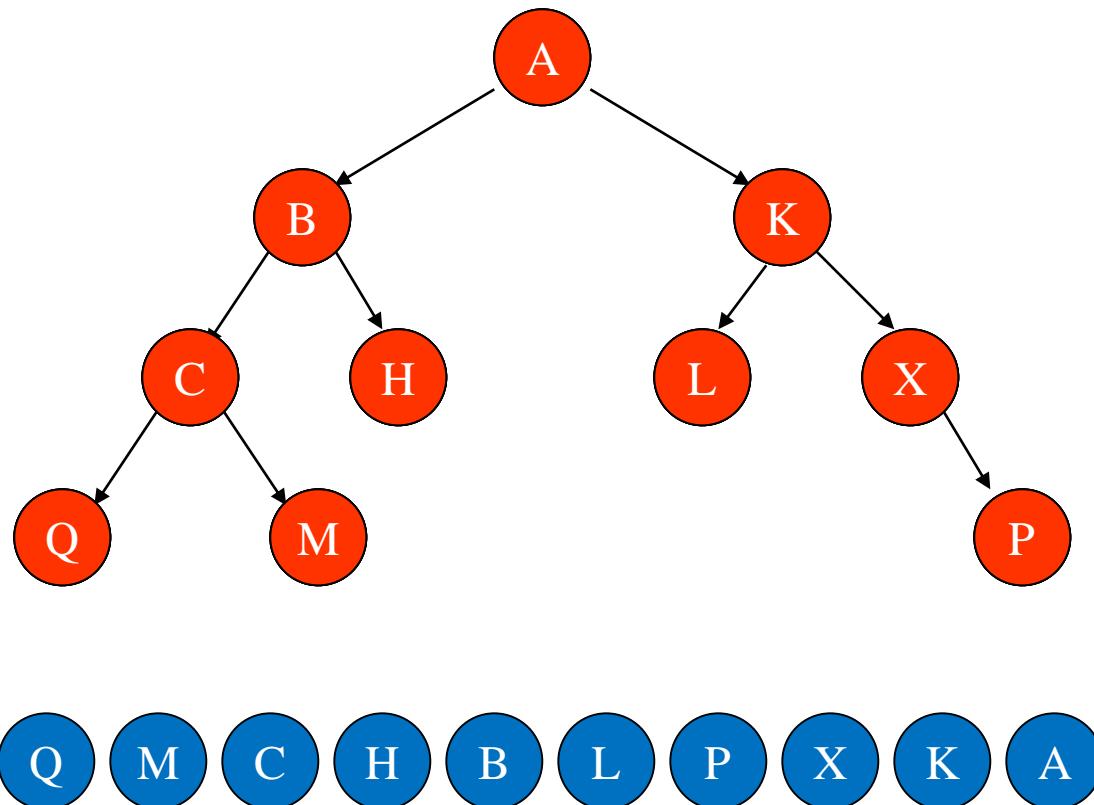
```
void BinaryTree::PreOrder()  
{  
    PreOrder(root);  
}
```

```
void BinaryTree::PreOrder(TreeNode *t)  
{  
    if (t) {  
        visit(t);  
        PreOrder(t->left);  
        PreOrder(t->right);  
    }  
}
```

```
void BinaryTree::visit(TreeNode *t) {  
    cout << t->data;  
}
```

# Binary Tree Traversal

## Post Order Traversal (LRN)



```
if (t) {
```

```
    PostOrder(t→left);
```

```
    PostOrder(t→right);
```

```
    visit(t);
```

```
}
```

# Binary Tree Traversal

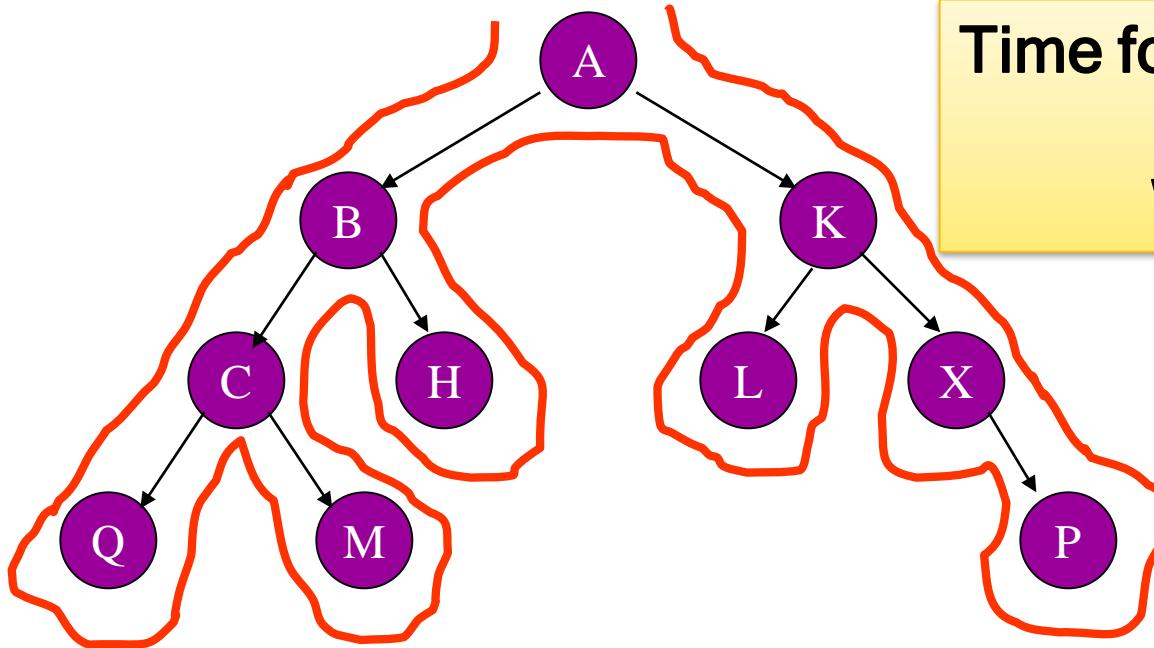
## Post Order Traversal (NLR)

```
void BinaryTree::PreOrder()
{
    PostOrder(root);
}
```

```
void BinaryTree::PostOrder(TreeNode *t)
{
    if (t) {
        PostOrder(t->left);
        PostOrder(t->right);
        visit(t);
    }
}
```

```
void BinaryTree::visit(TreeNode *t) {
    cout << t->data;
}
```

# Binary Tree Traversal



Time for Traversal  
Best case  
Worst case

NLR – visit when at the left of the Node

**A B C Q M H K L X P**

LNR – visit when under the Node

**Q C M B H A L K X P**

LRN – visit when at the right of the Node

**Q M C H B L P X K A**

# Binary Tree Destructor

Which Algorithm?

Delete both the left child and right child  
before deleting itself

LRN (post order)

# Destructor

```
void tree<type>::~tree() {  
    Destroy(root);  
}
```

POST ORDER  
traversal

```
template <class type>  
void tree<type>::Destroy(Node<type> *& node) {  
    if (node) {  
        Destroy(node→left);  
        Destroy(node→right);  
        delete node;  
    }  
}
```

# Duplicate Tree -Copy constructor

PRE ORDER  
traversal

```
template <class type>
void tree<type>::Duplicate(Node<type>*curr_tree,Node<type>*& dup_tree){
    if (curr_tree) {
        // set the value from curr_tree
        dup_tree = new Bnode(curr_tree->data);
        Duplicate(curr_tree->left, dup_tree->left);
        Duplicate(curr_tree->right, dup_tree->right);
    }
}
```

# Tree traversal

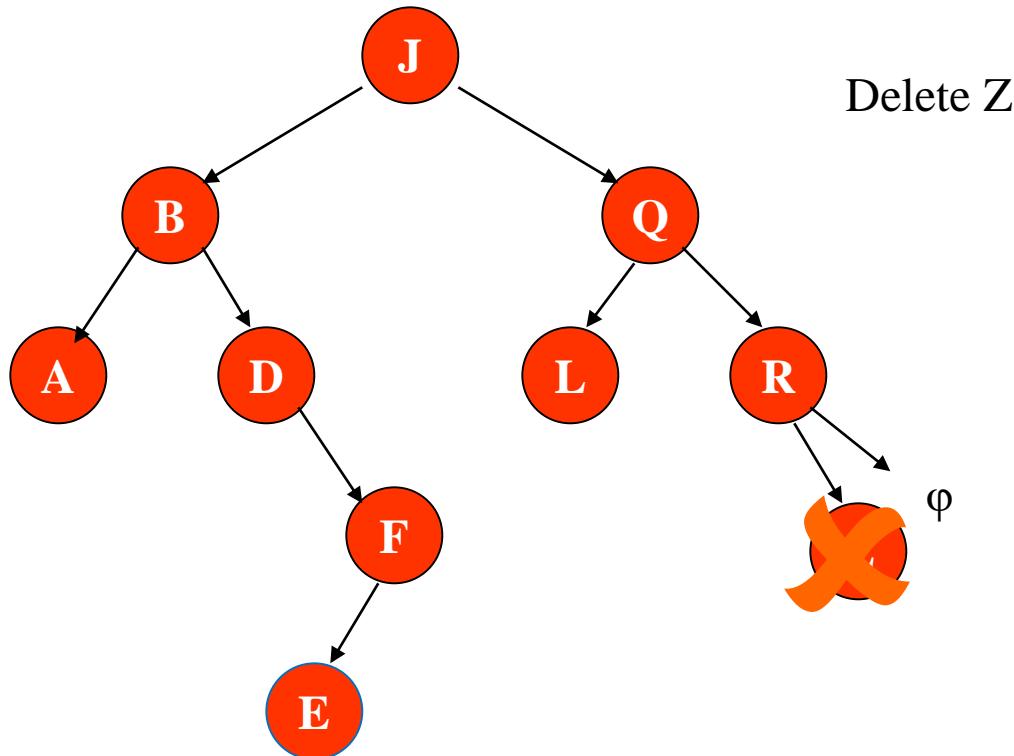
- In-order
  - Sorted data printing
- Post Order
  - Destructor
- Pre Order
  - Create a Tree copy (duplicate the current tree)

HW

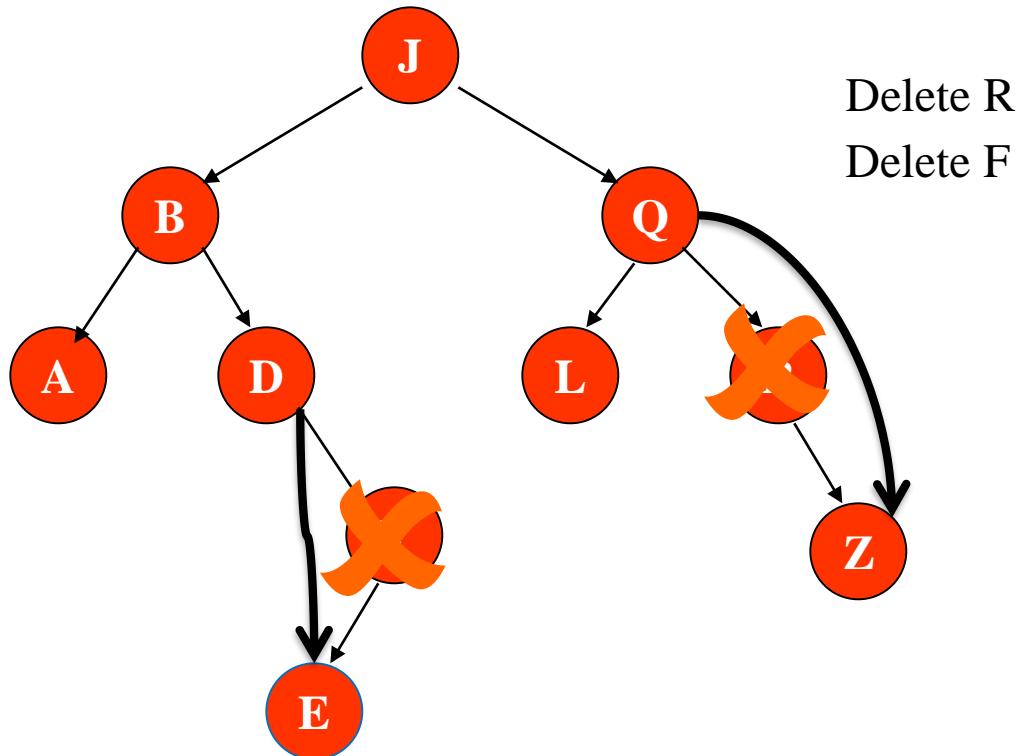
Do Iterative versions of the  
traversals

# BST DELETION

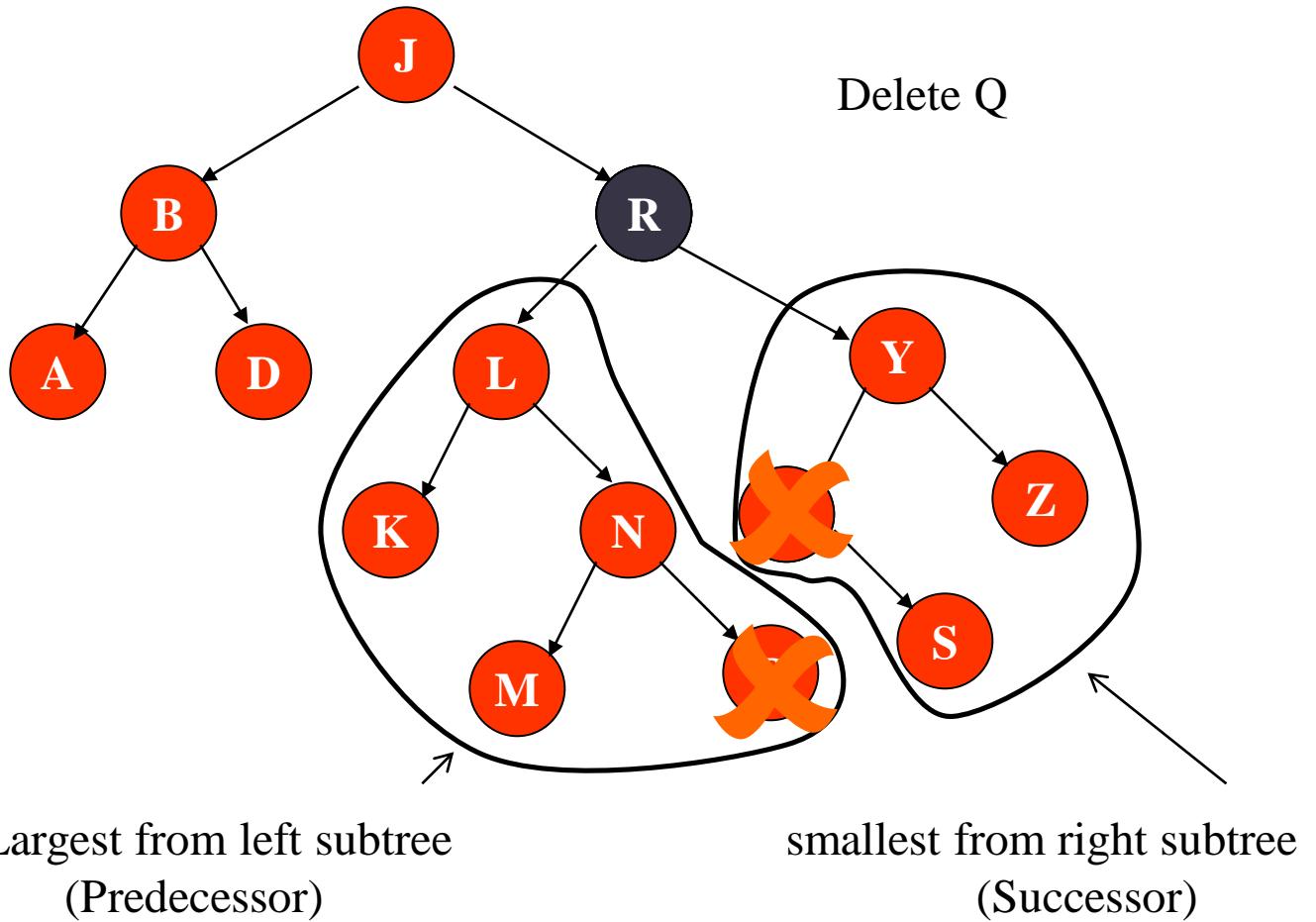
# Deleting a leaf node



# Deleting a node with only one child



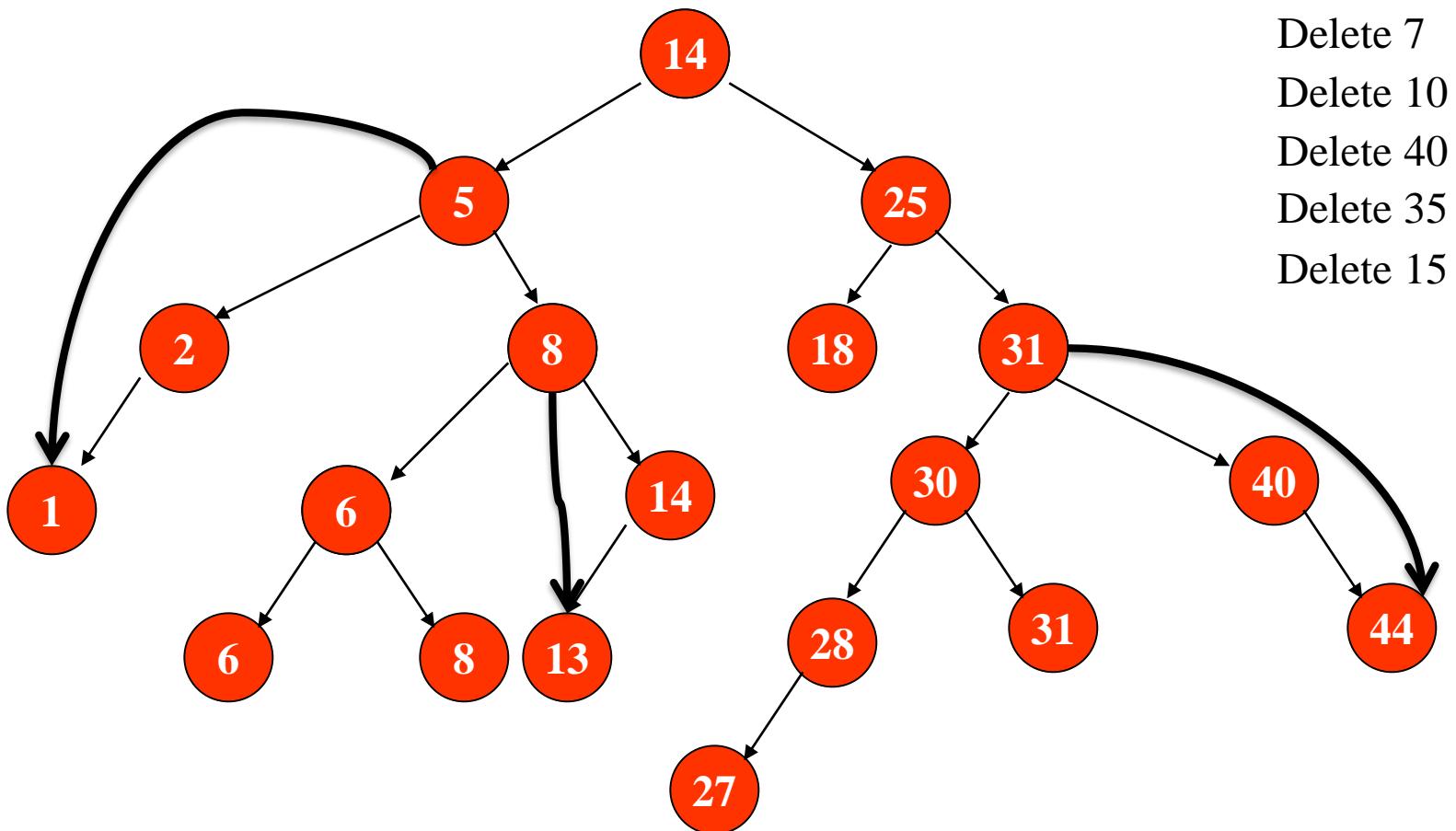
# Deleting a node with 2 children (without duplication)



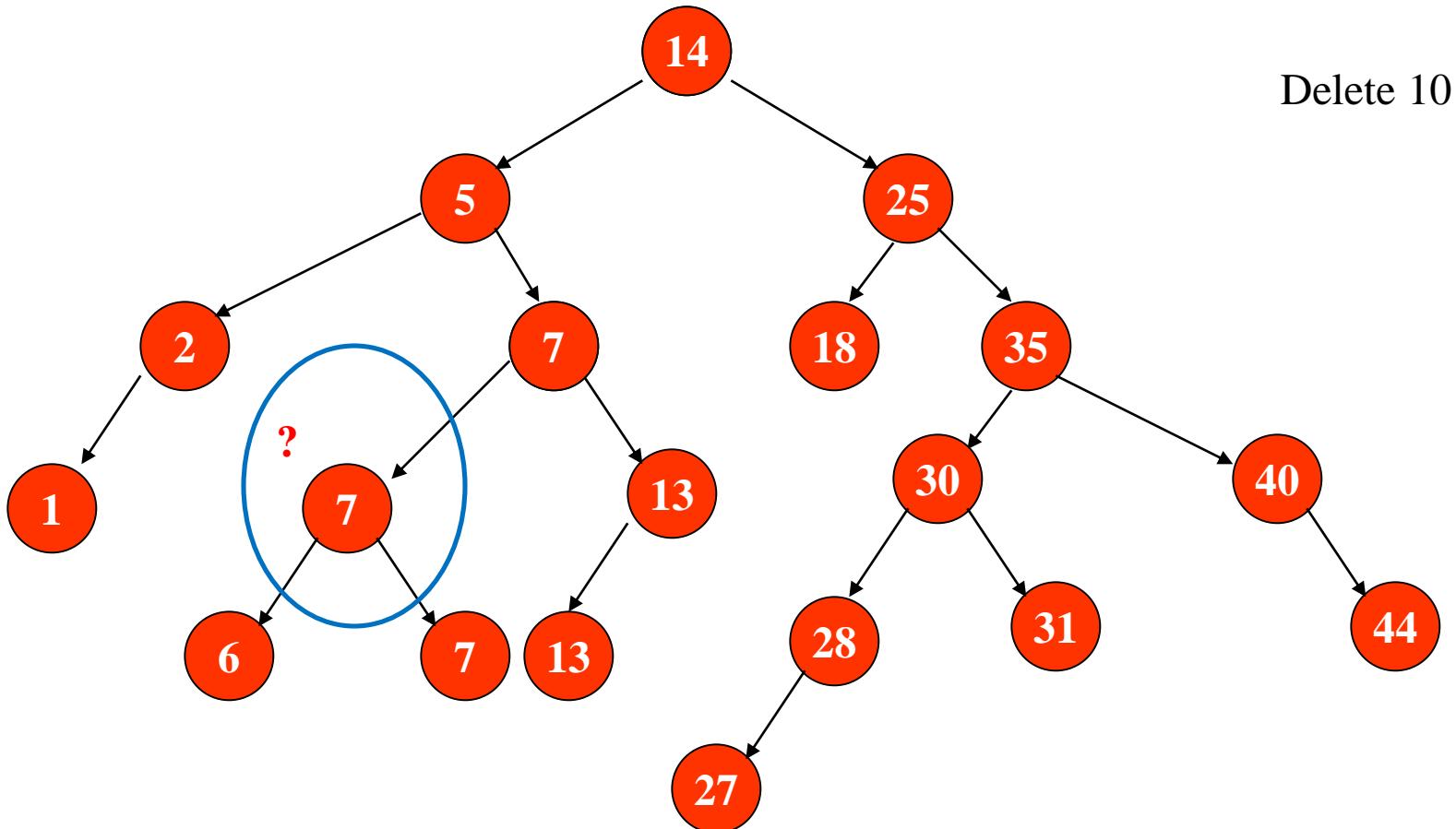
# Delete a node from a BST (without duplication)

1. Search the node to be deleted; call it  $t$
2. If  $t$  is a leaf,
  - disconnect it from its parent and set the parent pointer to NULL
3. If  $t$  has only one child,
  - remove  $t$  from the tree by making  $t$ 's parent point to its child.
4. If  $t$  has two children
  1. Find the largest/smallest among  $t$ 's LST/RST; call it  $p$ .
  2. Copy  $p$ 's information into  $t$ .
  3. Delete  $p$ .

# Delete(without duplication)

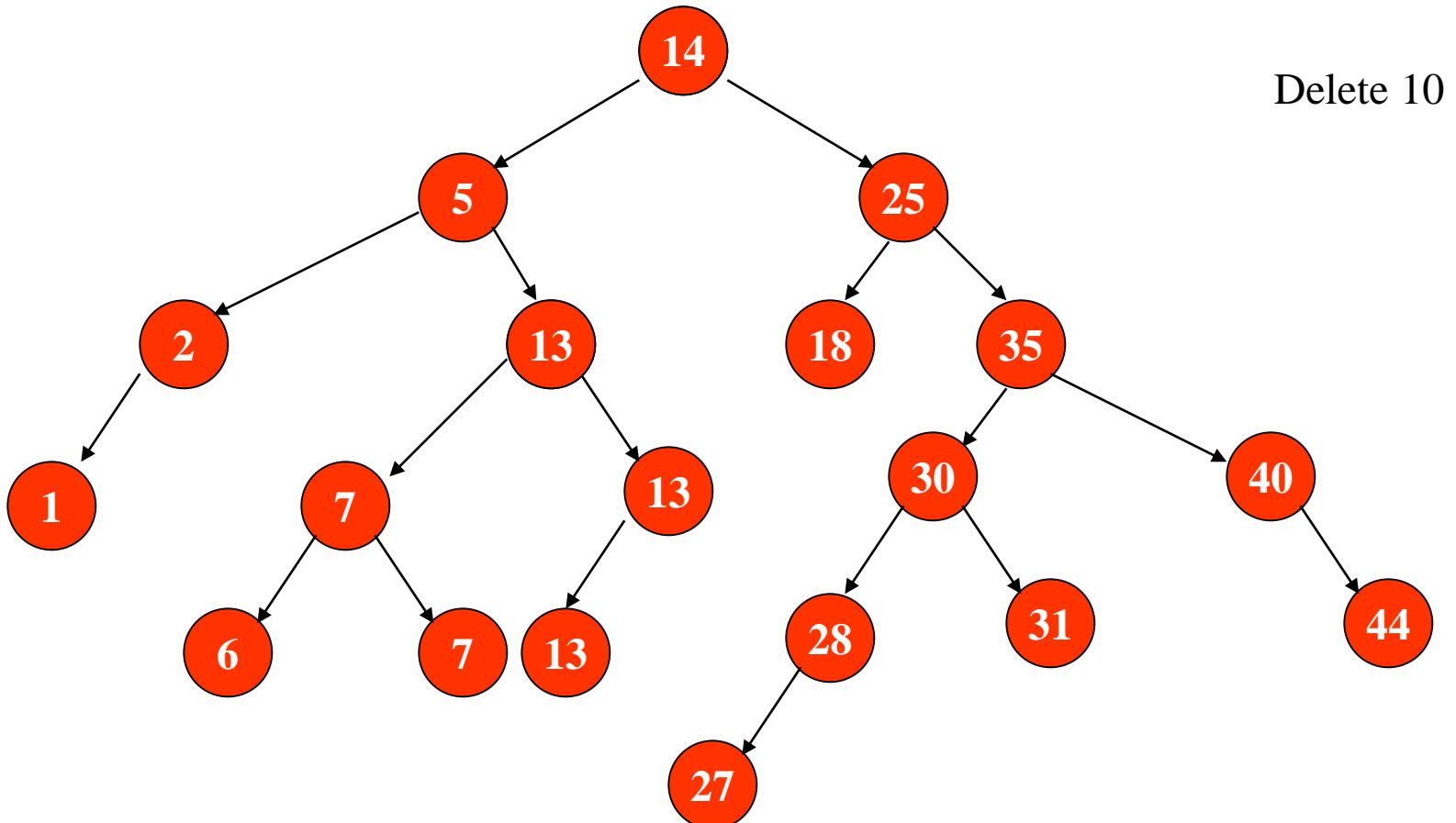


# Delete (with Duplication)



Solution : Use Successor instead of Predecessor

# Delete (with Duplication)



# Recursive Delete

```
void tree<type>::deleteR(type d)
{
    deleteR(d, root);
}
```

```
template <class type>
void tree<type>::deleteR(type d, Node<type> *& node)
{
    if (node) {
        if (d > node->data)
            deleteR(d, node->right);
        else if (d < node->data)
            deleteR(d, node->left);
        else
            deleteNode(node);
    }
}
```

# Recursive Delete

```
template <class type>
void tree<type>::deleteNode(Node <type> *& node) {

    Node <type> * temp = node;
    if (node->left == NULL) {
        node = node->right;
        delete temp;
    }
    else if(node->right == NULL) {
        node = node->left;
        delete temp;
    }
    else{
        type d = getPredecessor(node->left);
        node->data = d;
        deleteR(d, node->left);
    }
}
```

```
template <class T>
T tree<T>::getPredecessor(Node<T>*n)
{
    while (n->right != NULL)
        n = n->right;
    return n->data;
}
```

# Iterative delete

```
template <class type>
void tree<type>::deleteI(type d) {
    Node <type> * parent = root;
    Node <type> * child = root;

    while (child && child->data != d) {
        parent = child;
        if (parent->data > d)
            child = child ->left;
        else if (parent->data < d)
            child = child ->right;
    }

    if (child) { //if data is found
        if (child == root)
            deleteNode(root);
        else if (parent->left == child)
            deleteNode(parent->left);
        else
            deleteNode(parent->right);
    }
}
```

