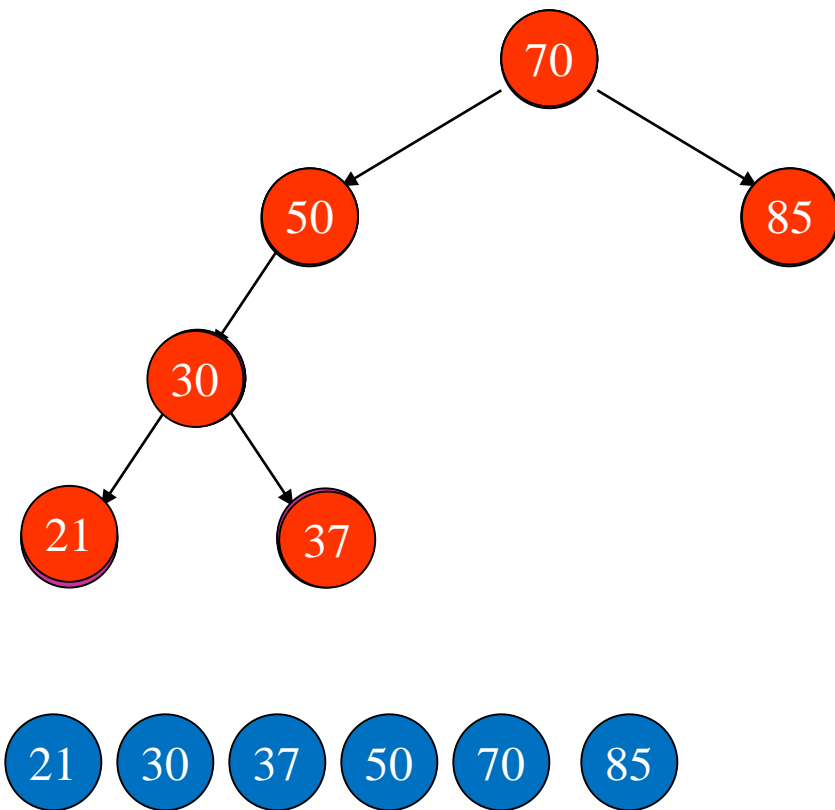


Binary Search Tree

Traversal

In Order Traversal (LNR)



```
if (t) {
```

```
    InOrder(t→left);
```

```
    visit(t);
```

```
    InOrder(t→right);
```

```
}
```

InOrder(NULL)

InOrder(21)
InOrder(37)

InOrder(NULL)
InOrder(30)

InOrder(85)
InOrder(50)

InOrder(70)

```
InOrder(37→left)
```

```
visit(37)
```

```
InOrder(37→right)
```

t=37
t=21

```
InOrder(30→left)
```

```
visit(30)
```

```
InOrder(30→right)
```

t=30

```
InOrder(85→left)
```

```
visit(85)
```

```
InOrder(85→right)
```

t=85
t=50

```
InOrder(70→left)
```

```
visit(70)
```

```
InOrder(70→right)
```

t=70

BST Print (Inorder traversal)

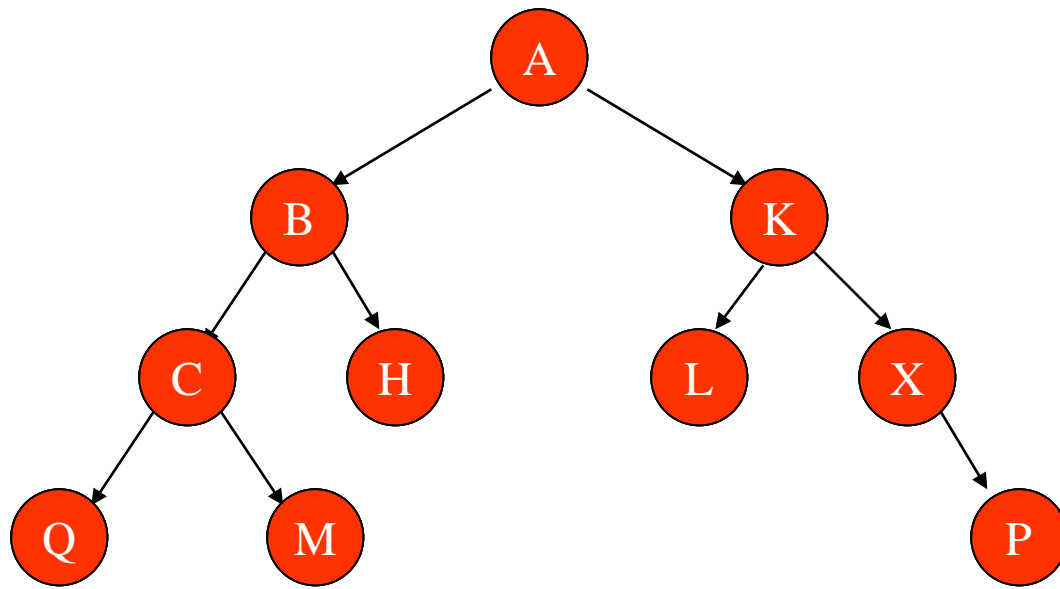
```
template <class type>
void tree<type>::Print() {
    InOrder(root);
}
```

```
template <class type>
void tree<type>::InOrder(Node<type> *t)
{
    if (t) {
        InOrder(t->left);
        visit(t);
        InOrder(t->right);
    }
}
```

```
template <class type>
void tree<type>::visit(Node<type> *t){
    cout << t->data;
}
```

Binary Tree Traversal

In Order Traversal (LNR)



Q C M B H A L K X P

```
if (t) {
```

```
  InOrder(t→left);
```

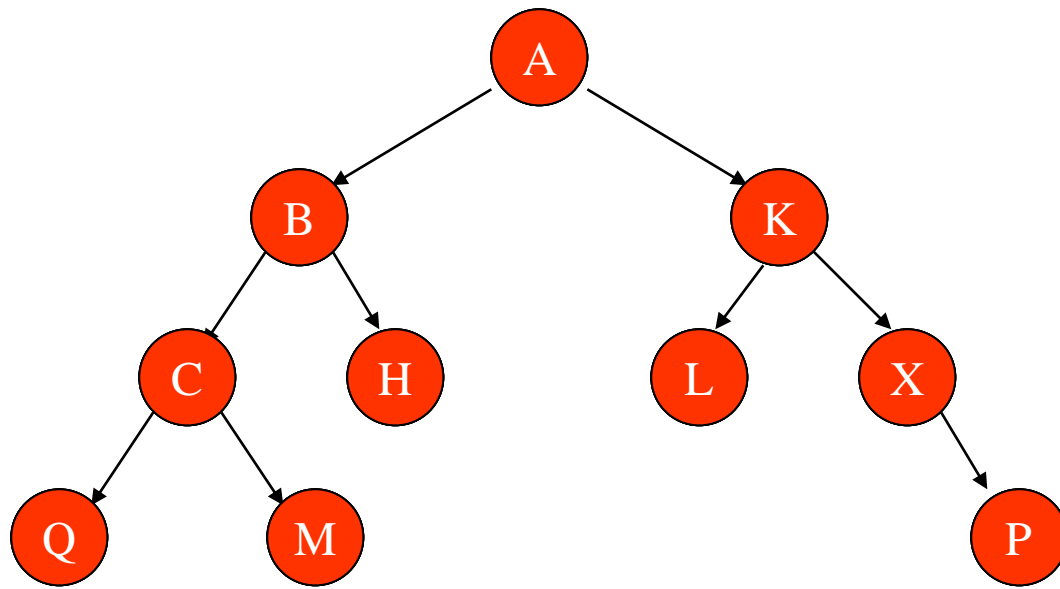
```
  visit(t);
```

```
  InOrder(t→right);
```

```
}
```

Binary Tree Traversal

Pre Order Traversal (NLR)



A B C Q M H K L X P

```
if (t) {
```

```
    visit(t);
```

```
    PreOrder(t→left);
```

```
    PreOrder(t→right);
```

```
}
```

Binary Tree Traversal

Pre Order Traversal (NLR)

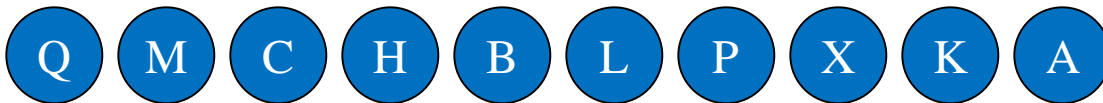
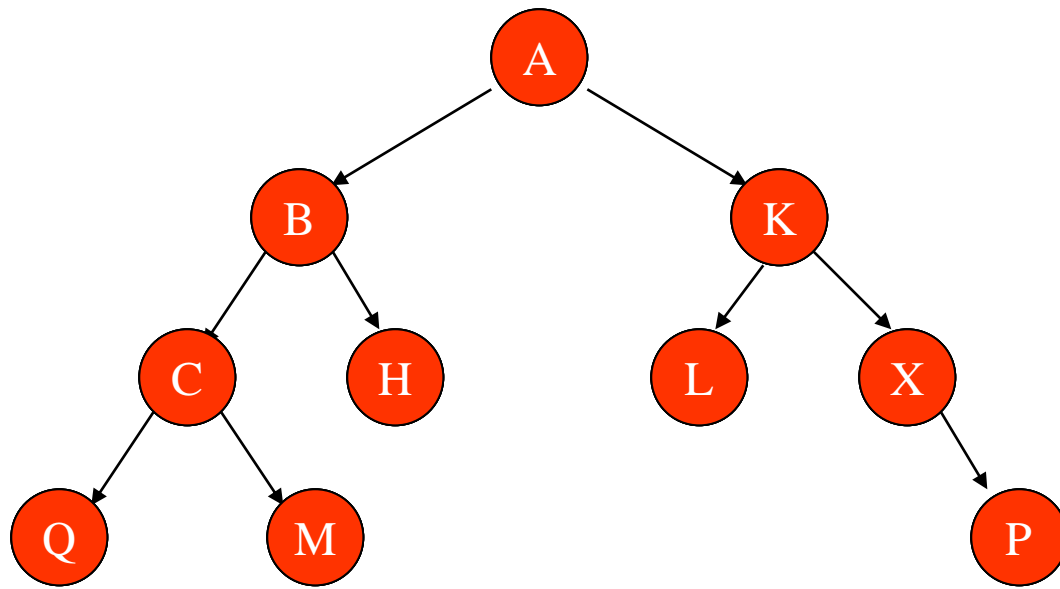
```
void BinaryTree::PreOrder()  
{  
    PreOrder(root);  
}
```

```
void BinaryTree::PreOrder(TreeNode *t)  
{  
    if (t) {  
        visit(t);  
        PreOrder(t->left);  
        PreOrder(t->right);  
    }  
}
```

```
void BinaryTree::visit(TreeNode *t) {  
    cout << t->data;  
}
```

Binary Tree Traversal

Post Order Traversal (LRN)



```
if (t) {
```

```
    PostOrder(t→left);
```

```
    PostOrder(t→right);
```

```
    visit(t);
```

```
}
```

Binary Tree Traversal

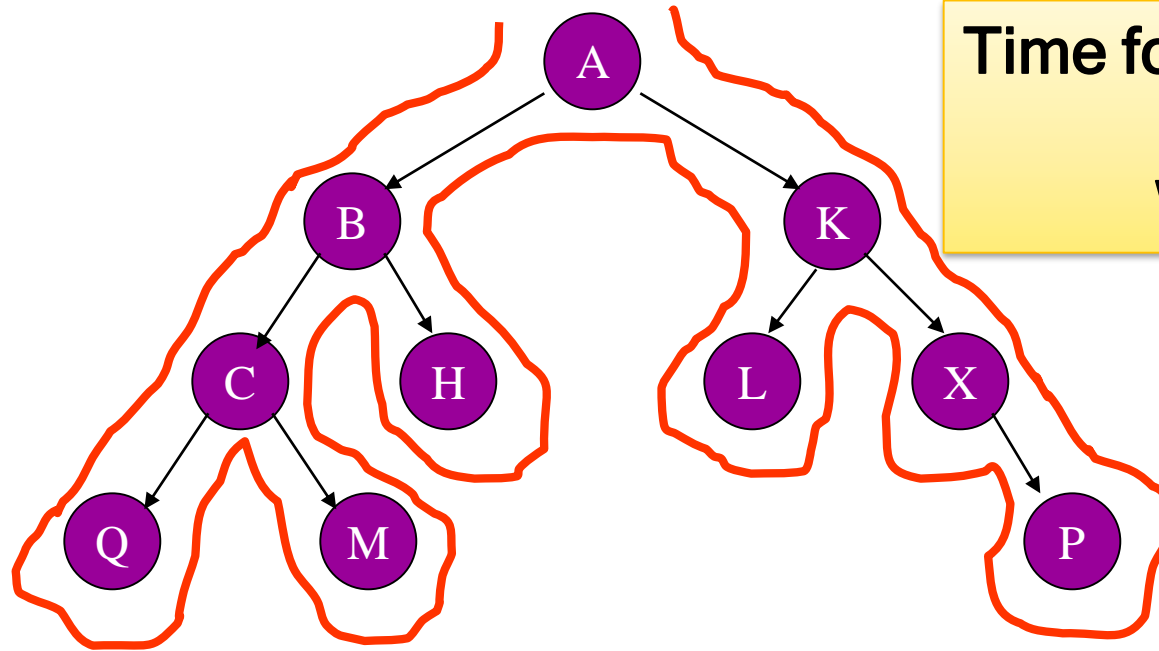
Post Order Traversal (NLR)

```
void BinaryTree::PreOrder()  
{  
    PostOrder(root);  
}
```

```
void BinaryTree::PostOrder(TreeNode *t)  
{  
    if (t) {  
        PostOrder(t->left);  
        PostOrder(t->right);  
        visit(t);  
    }  
}
```

```
void BinaryTree::visit(TreeNode *t) {  
    cout << t->data;  
}
```

Binary Tree Traversal



Time for Traversal
Best case
Worst case

NLR – visit when at the left of the Node

A B C Q M H K L X P

LNR – visit when under the Node

Q C M B H A L K X P

LRN – visit when at the right of the Node

Q M C H B L P X K A

Binary Tree Destructor

Which Algorithm?

Delete both the left child and right child
before deleting itself

LRN (post order)

Destructor

POST ORDER traversal

```
void tree<type>::~~tree() {  
    Destroy(root);  
}
```

```
template <class type>  
void tree<type>::Destroy(Node<type> *& node) {  
    if (node) {  
        Destroy(node->left);  
        Destroy(node->right);  
        delete node;  
    }  
}
```

Duplicate Tree -Copy constructor

PRE ORDER traversal

```
template <class type>
void tree<type>::Duplicate(Node<type>*curr_tree,Node<type>*& dup_tree){
    if (curr_tree) {
        // set the value from curr_tree
        dup_tree = new Bnode(curr_tree->data);
        Duplicate(curr_tree->left, dup_tree->left);
        Duplicate(curr_tree->right, dup_tree->right);
    }
}
```

Tree traversal

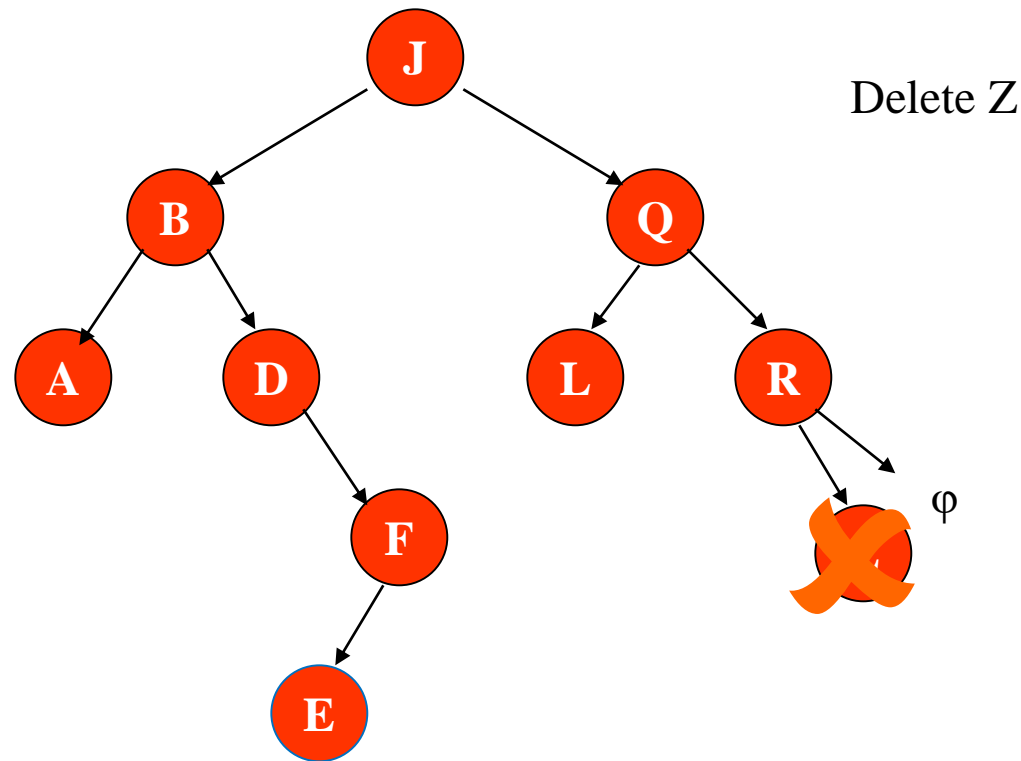
- In-order
 - Sorted data printing
- Post Order
 - Destructor
- Pre Order
 - Create a Tree copy (duplicate the current tree)

HW

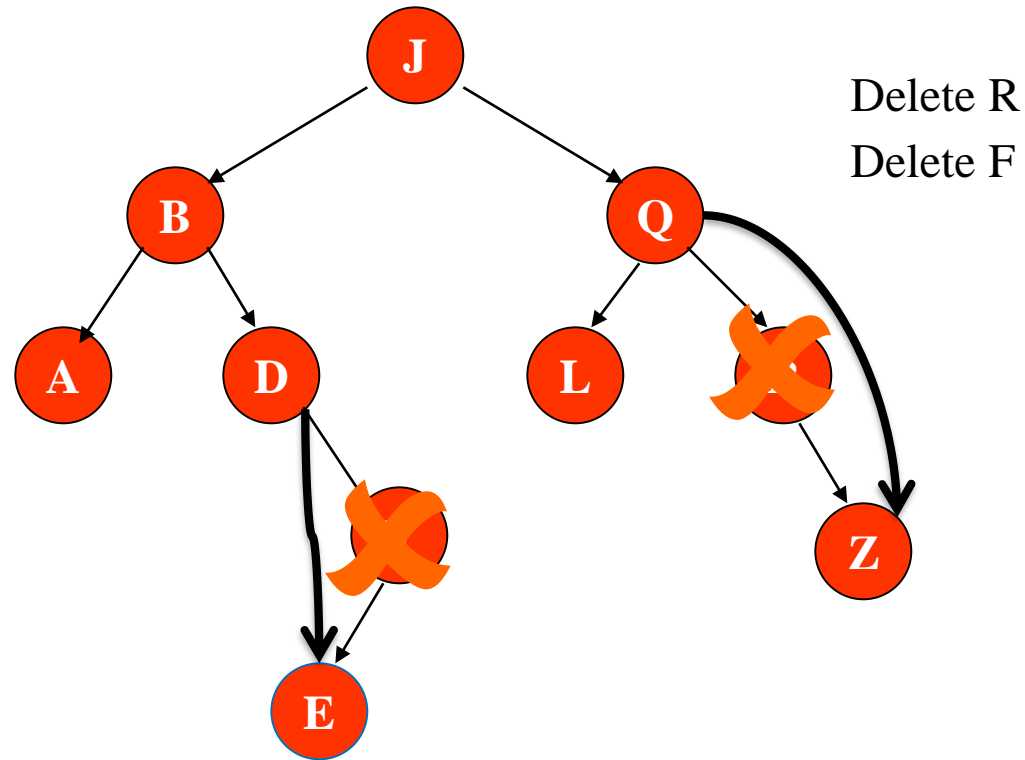
**Do Iterative versions of the
traversals**

BST DELETION

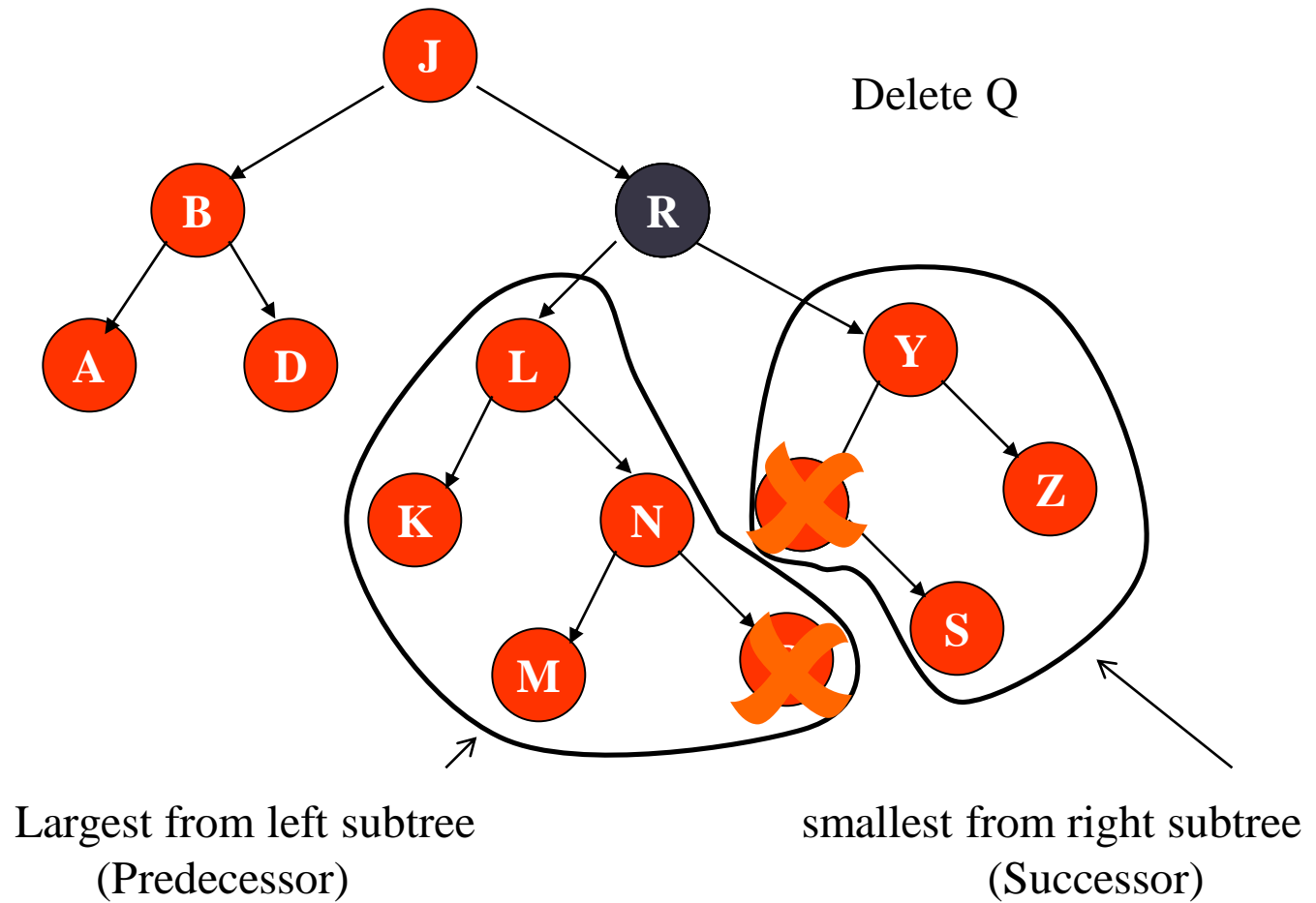
Deleting a leaf node



Deleting a node with only one child



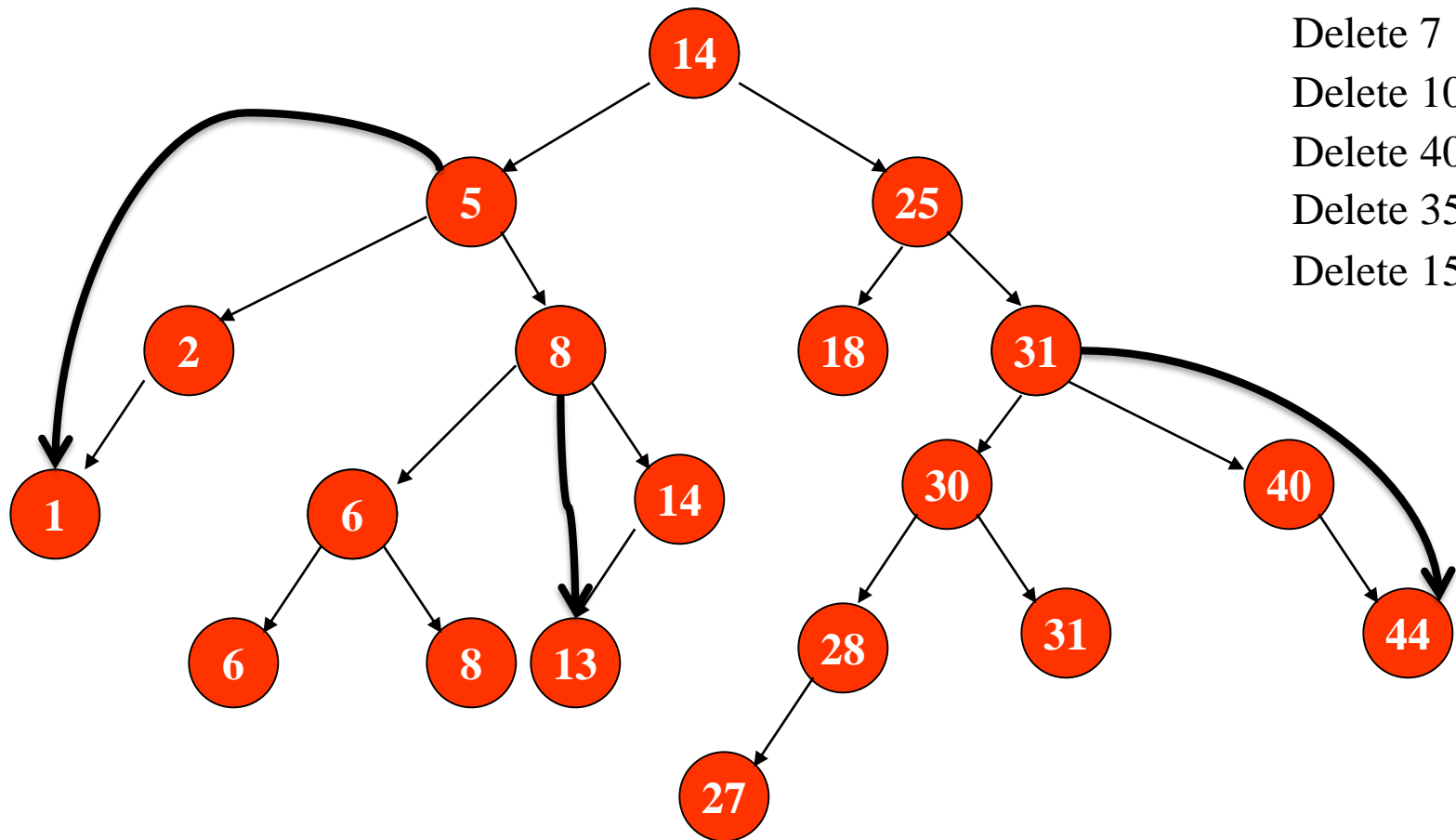
Deleting a node with 2 children (without duplication)



Delete a node from a BST (without duplication)

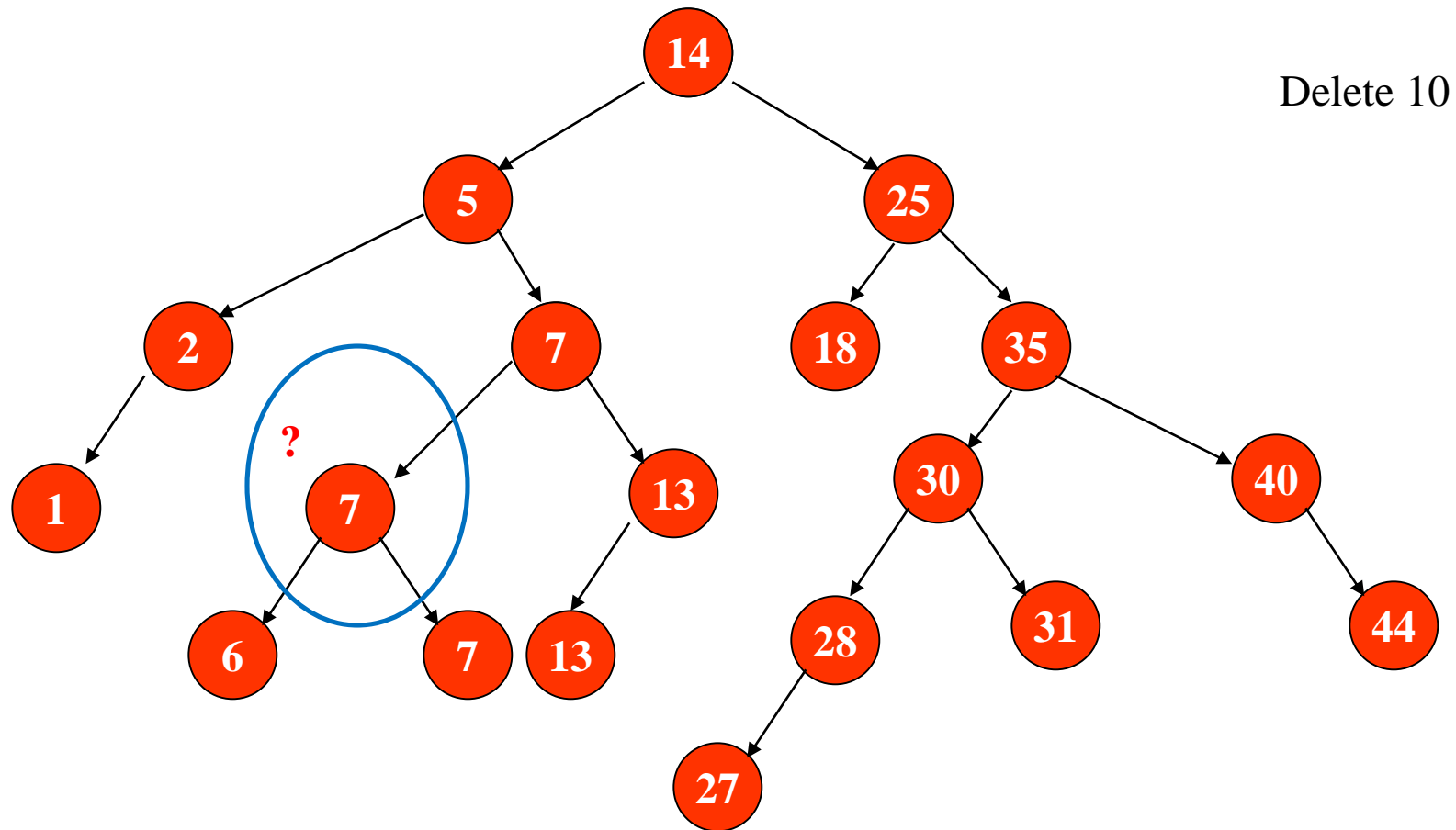
1. Search the node to be deleted; call it t
2. If t is a leaf,
 - disconnect it from its parent and set the parent pointer to NULL
3. If t has only one child,
 - remove t from the tree by making t 's parent point to its child.
4. If t has two children
 1. Find the largest/smallest among t 's LST/RST; call it p .
 2. Copy p 's information into t .
 3. Delete p .

Delete(without duplication)



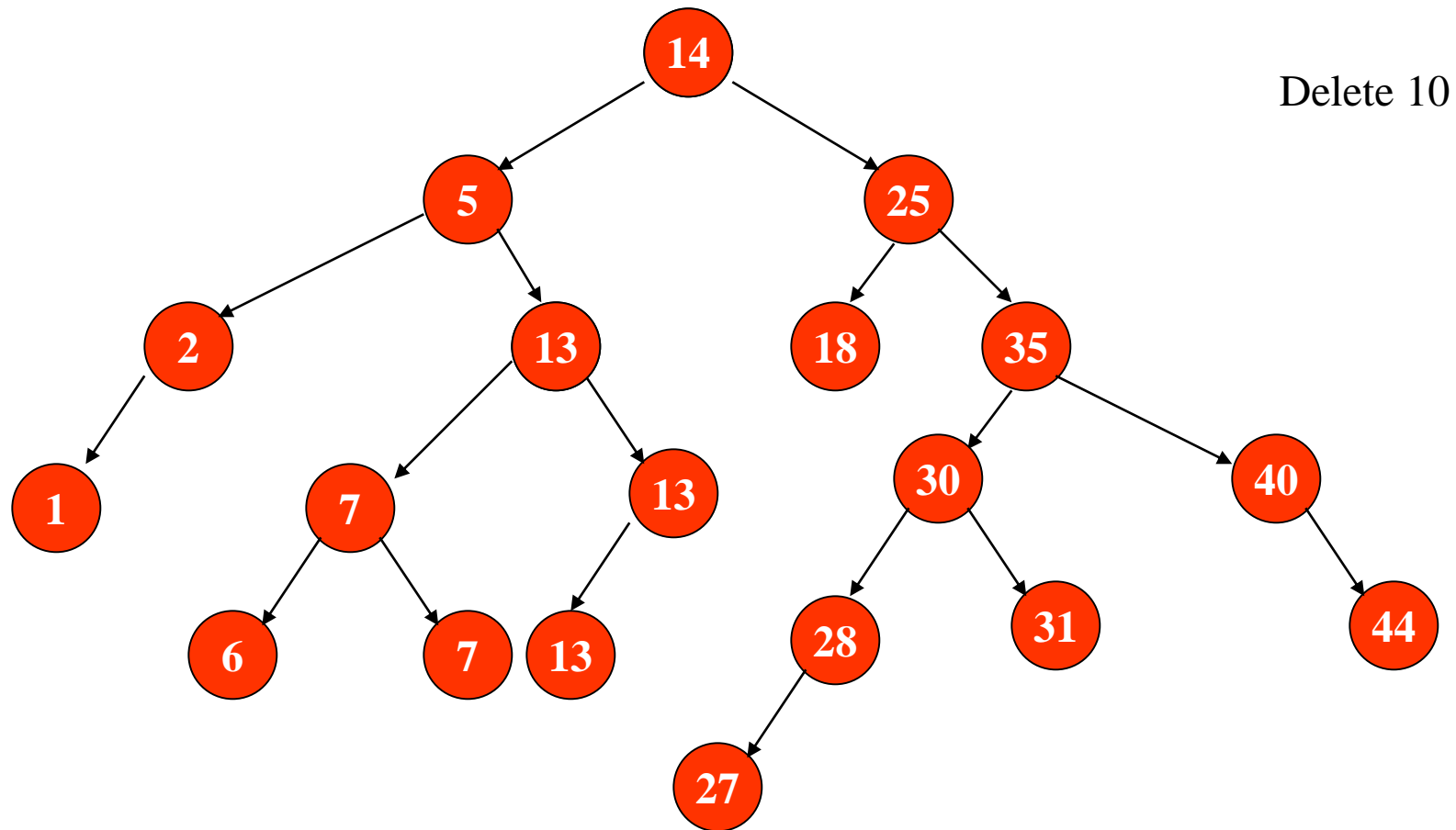
Delete 2
Delete 7
Delete 10
Delete 40
Delete 35
Delete 15

Delete (with Duplication)



Solution :Use Successor instead of Predecessor

Delete (with Duplication)



Recursive Delete

```
void tree<type>::deleteR(type d)
{
    deleteR(d, root);
}
```

```
template <class type>
void tree<type>::deleteR(type d, Node<type> *& node)
{
    if (node) {
        if (d > node->data)
            deleteR(d, node->right);
        else if (d < node->data)
            deleteR(d, node->left);
        else
            deleteNode(node);
    }
}
```

Recursive Delete

```
template <class type>
void tree<type>::deleteNode(Node <type> *& node) {
```

```
    Node <type> * temp = node;
    if (node->left == NULL) {
        node = node->right;
        delete temp;
    }
    else if (node->right == NULL) {
        node = node->left;
        delete temp;
    }
    else{
        type d = getPredecessor(node->left);
        node->data = d;
        deleteR(d, node->left);
    }
}
```

```
template <class T>
T tree<T>::getPredecessor(Node<T>*n)
{
    while (n->right != NULL)
        n = n->right;
    return n->data;
}
```

Iterative delete

```
template <class type>
void tree<type>::deleteI(type d) {
    Node <type> * parent = root;
    Node <type> * child = root;

    while (child && child->data != d) {
        parent = child;
        if (parent->data > d)
            child = child->left;
        else if (parent->data < d)
            child = child->right;
    }

    if (child) { //if data is found
        if (child == root)
            deleteNode(root);
        else if (parent->left == child)
            deleteNode(parent->left);
        else
            deleteNode(parent->right);
    }
}
```

