Práctico 6 - Dispersión: Se deberá entregar el ejercicio número 1.a y 1.c.

## Ejercicio 1.

a) Suponga una estructura de hash cerrada con técnica de resolución lineal con una sola ranura por balde y  $h(x)=x \mod 13$  y  $h^{'}(x)=(h(x)+i) \mod 13$  Para las siguientes claves dibuje la estructura paso a paso y calcule el Rho (una vez cargada la estructura) . Claves : 11, 3, 27, 99, 8, 50, 77, 22, 12, 31, 33, 40, 53

|                             |   |          |   |   |   |   |   |     |    |          |     |     | -  |
|-----------------------------|---|----------|---|---|---|---|---|-----|----|----------|-----|-----|----|
|                             |   |          |   |   |   |   |   |     |    |          |     |     |    |
|                             | 0 | 1        | 2 | 3 | 4 | 5 | 6 | 7   | 8  | 9        | 10  | 11  | 12 |
|                             |   |          |   |   |   |   |   |     |    |          |     |     |    |
|                             |   |          |   |   |   |   |   |     |    |          |     | 11  |    |
|                             |   | <u> </u> | I |   | I |   |   | I   | I  |          |     | 11  |    |
| h(11) = 11 mod 13 = 11      | 0 | 1        | 2 | 3 | 4 | 5 | 6 | 7   | 8  | 9        | 10  | 11  | 12 |
| 11(11) - 11 11100 13 - 11   |   | _ '      |   |   |   |   |   |     |    | <u> </u> | 10  | 11  | 12 |
|                             |   |          |   | 3 | _ | - | - |     |    |          |     |     |    |
|                             |   |          |   | 3 |   |   |   |     |    |          |     | 11  |    |
| $h(3) = 3 \mod 13 = 3$      | 0 | 1        | 2 | 3 | 4 | 5 | 6 | 7   | 8  | 9        | 10  | 11  | 12 |
|                             |   | 07       |   |   |   |   |   |     |    |          |     |     |    |
|                             |   | 27<br>27 |   | 2 |   |   |   | I   |    |          |     | 11  |    |
| h(27) = 27 mod 13 = 1       | 0 | 1        | 2 | 3 | 4 | 5 | 6 | 7   | 8  | 9        | 10  | 11  | 12 |
| 11(27) - 27 11100 13 - 1    | U | l        |   | J | 4 | ာ | 0 | _ / | 0  | 9        | 10  | 11  | 12 |
|                             |   |          |   |   |   |   |   |     | 99 |          |     |     |    |
|                             |   | 27       |   | 3 |   |   |   |     | 99 |          |     | 11  |    |
| h(99) = 99 mod 13 = 8       | 0 | 1        | 2 | 3 | 4 | 5 | 6 | 7   | 8  | 9        | 10  | 11  | 12 |
|                             |   |          |   |   |   |   |   |     |    |          |     |     |    |
|                             |   |          | ı |   | 1 |   |   | 1   | 8  |          |     | 4.4 |    |
| h(0) 0 m d 40 0             |   | 27       |   | 3 |   | _ |   | _   | 99 | _        | 40  | 11  | 40 |
| $h(8) = 8 \mod 13 = 8$      | 0 | 1        | 2 | 3 | 4 | 5 | 6 | 7   | 8  | 9        | 10  | 11  | 12 |
|                             |   |          |   |   |   |   |   |     |    | 8        |     |     |    |
|                             |   | 27       |   | 3 |   |   |   |     | 99 | 8        |     | 11  |    |
| h'(8) = (8+1) mod 13 = 9    | 0 | 1        | 2 | 3 | 4 | 5 | 6 | 7   | 8  | 9        | 10  | 11  | 12 |
|                             |   | •        |   |   |   | • | • |     |    |          | •   |     |    |
|                             |   | l        |   |   |   |   |   |     |    | _        |     | 50  |    |
|                             |   | 27       |   | 3 |   | _ |   | _   | 99 | 8        | 4.0 | 11  | 10 |
| h(50) = 50 mod 13 = 11      | 0 | 1        | 2 | 3 | 4 | 5 | 6 | 7   | 8  | 9        | 10  | 11  | 12 |
|                             |   |          |   |   |   |   |   |     |    |          |     |     | 50 |
|                             |   | 27       |   | 3 |   |   |   |     | 99 | 8        |     | 11  | 50 |
| h'(50) = (50+1) mod 13 = 12 | 0 | 1        | 2 | 3 | 4 | 5 | 6 | 7   | 8  | 9        | 10  | 11  | 12 |
|                             |   |          |   |   |   |   |   |     |    |          |     |     |    |
|                             |   | 1        |   |   |   |   |   |     |    |          |     |     | 77 |
|                             |   | 27       |   | 3 |   |   |   |     | 99 | 8        |     | 11  | 50 |
| h(77) = 77 mod 13 = 12      | 0 | 1        | 2 | 3 | 4 | 5 | 6 | 7   | 8  | 9        | 10  | 11  | 12 |

|                              | 77 | 27 |    | 3  |   |    |   |    | 99 | 8  |    | 11 | 50 |
|------------------------------|----|----|----|----|---|----|---|----|----|----|----|----|----|
| h'(77) = (77+1) mod 13 = 0   | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              |    | •  |    |    |   |    |   |    |    | 22 |    |    |    |
|                              | 77 | 27 |    | 3  |   |    |   |    | 99 | 8  |    | 11 | 50 |
| h(22) = 22 mod 13 = 9        | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              |    | •  |    |    |   |    |   |    |    |    | 22 |    |    |
|                              | 77 | 27 |    | 3  |   |    |   |    | 99 | 8  | 22 | 11 | 50 |
| h'(22) = (22+1) mod 13 = 10  | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              |    |    |    |    |   |    |   |    |    |    |    |    | 12 |
|                              | 77 | 27 |    | 3  |   |    |   |    | 99 | 8  | 22 | 11 | 50 |
| h(12) = 12 mod 13 = 12       | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              | 12 |    |    |    |   |    |   |    |    |    |    |    |    |
|                              | 77 | 27 |    | 3  |   |    |   |    | 99 | 8  | 22 | 11 | 50 |
| h'(12) = (12+1) mod 13 = 0   | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              |    | 12 |    |    |   | _  |   | _  |    |    | -  |    |    |
|                              | 77 | 27 |    | 3  |   |    |   |    | 99 | 8  | 22 | 11 | 50 |
| h"(12) = (12+2) mod 13 = 1   | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              |    |    | 12 |    |   |    |   |    |    |    | -  |    |    |
|                              | 77 | 27 | 12 | 3  |   |    |   |    | 99 | 8  | 22 | 11 | 50 |
| h'''(12) = (12+3) mod 13 = 2 | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              |    |    |    |    |   | 31 |   |    |    |    |    |    |    |
|                              | 77 | 27 | 12 | 3  |   | 31 |   |    | 99 | 8  | 22 | 11 | 50 |
| h(31) = 31 mod 13 = 5        | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              |    |    |    |    |   |    |   | 33 |    |    |    |    |    |
|                              | 77 | 27 | 12 | 3  |   | 31 |   | 33 | 99 | 8  | 22 | 11 | 50 |
| h(33) = 33 mod 13 = 7        | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              |    | 40 |    |    |   | •  |   | •  | •  |    |    |    |    |
|                              | 77 | 27 | 12 | 3  |   | 31 |   | 33 | 99 | 8  | 22 | 11 | 50 |
| h(40) = 40 mod 13 = 1        | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              |    |    | 40 |    |   |    |   |    | •  |    | •  |    |    |
|                              | 77 | 27 | 12 | 3  |   | 31 |   | 33 | 99 | 8  | 22 | 11 | 50 |
| h'(40) = (1+1) mod 13 = 2    | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              |    |    |    | 40 |   |    |   |    |    |    |    |    |    |
|                              | 77 | 27 | 12 | 3  |   | 31 |   | 33 | 99 | 8  | 22 | 11 | 50 |
| h"(40) = (1+2) mod 13 = 3    | 0  | 1  | 2  | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
|                              |    |    |    |    |   |    |   |    |    |    |    |    |    |

Realice lo mismo utilizando técnica de resolución:

c) seudoazar  $h'(x) = [h(x) + Zi] \mod M Z = (1,5,2,4,3,6)$ 

|                        | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|------------------------|---|---|---|---|---|---|---|---|---|---|----|----|----|
|                        |   |   |   |   |   |   |   |   |   |   |    |    |    |
|                        |   |   |   |   |   |   |   |   |   |   |    | 11 |    |
|                        |   |   |   |   |   |   |   |   |   |   |    | 11 |    |
| h(11) = 11 mod 13 = 11 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|                        |   |   |   |   |   |   |   |   |   |   |    |    |    |
|                        |   |   |   | 3 |   |   |   |   |   |   |    |    |    |
|                        |   |   |   | 3 |   |   |   |   |   |   |    | 11 |    |
| h(3) = 3 mod 13 = 3    | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |

|                             |    | 21 |   |   |   |   |   |   |    |    |    |    |     |
|-----------------------------|----|----|---|---|---|---|---|---|----|----|----|----|-----|
|                             |    | 27 |   | 3 |   | _ |   |   |    |    |    | 11 |     |
| h(27) = 27 mod 13 = 1       | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |
|                             |    |    |   |   |   | 1 |   |   | 99 | T  |    |    |     |
|                             |    | 27 |   | 3 |   | _ |   | _ | 99 |    | 40 | 11 | 4.0 |
| h(99) = 99 mod 13 = 8       | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |
|                             |    |    |   |   |   |   |   |   | 8  |    |    |    |     |
|                             |    | 27 |   | 3 |   | _ |   | _ | 99 |    | 40 | 11 | 4.0 |
| h(8) = 8 mod 13 = 8         | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |
|                             |    |    |   |   |   |   |   |   |    | 8  |    |    |     |
|                             | _  | 27 | _ | 3 |   | _ | _ | _ | 99 | 8  |    | 11 |     |
| h'(8) = (8+1) mod 13 = 9    | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |
|                             |    |    |   |   |   |   |   |   |    |    |    | 50 |     |
|                             |    | 27 |   | 3 |   |   |   |   | 99 | 8  |    | 11 |     |
| h(50) = 50 mod 13 = 11      | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |
|                             |    |    |   |   |   |   |   |   |    |    |    |    | 50  |
|                             |    | 27 |   | 3 |   |   |   |   | 99 | 8  |    | 11 | 50  |
| h'(50) = (50+1) mod 13 = 12 | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |
|                             |    |    |   |   |   |   |   |   |    |    |    |    | 77  |
|                             |    | 27 |   | 3 |   |   |   |   | 99 | 8  |    | 11 | 50  |
| h(77) = 77 mod 13 = 12      | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |
|                             | 77 |    |   |   |   |   |   |   |    |    |    |    |     |
|                             | 77 | 27 |   | 3 |   |   |   |   | 99 | 8  |    | 11 | 50  |
| h'(77) = (77+1) mod 13 = 0  | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |
|                             |    |    |   |   |   |   |   |   |    | 22 |    |    |     |
|                             | 77 | 27 |   | 3 |   |   |   |   | 99 | 8  |    | 11 | 50  |
| h(22) = 22 mod 13 = 9       | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |
|                             |    |    |   |   |   |   |   |   |    |    | 22 |    |     |
|                             | 77 | 27 |   | 3 |   |   |   |   | 99 | 8  | 22 | 11 | 50  |
| h'(22) = (22+1) mod 13 = 10 | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |
|                             |    |    |   |   |   |   |   |   |    |    |    |    | 12  |
|                             | 77 | 27 |   | 3 |   |   |   |   | 99 | 8  | 22 | 11 | 50  |
| h(12) = 12 mod 13 = 12      | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |
|                             | 12 |    |   |   |   |   |   |   |    |    |    |    |     |
|                             | 77 | 27 |   | 3 |   |   |   |   | 99 | 8  | 22 | 11 | 50  |
| h'(12) = (12+1) mod 13 = 0  | 0  | 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8  | 9  | 10 | 11 | 12  |

|                            |    |    |    |   | 12 |    |    |    |    |   |    |    |    |
|----------------------------|----|----|----|---|----|----|----|----|----|---|----|----|----|
|                            | 77 | 27 |    | 3 | 12 |    |    |    | 99 | 8 | 22 | 11 | 50 |
| h"(12) = (12+5) mod 13 = 1 | 0  | 1  | 2  | 3 | 4  | 5  | 6  | 7  | 8  | 9 | 10 | 11 | 12 |
|                            |    |    |    |   |    | 31 |    |    |    |   |    |    |    |
|                            | 77 | 27 |    | 3 | 12 | 31 |    |    | 99 | 8 | 22 | 11 | 50 |
| h(31) = 31 mod 13 = 5      | 0  | 1  | 2  | 3 | 4  | 5  | 6  | 7  | 8  | 9 | 10 | 11 | 12 |
|                            |    |    |    |   |    |    |    | 33 |    |   |    |    |    |
|                            | 77 | 27 |    | 3 | 12 | 31 |    | 33 | 99 | 8 | 22 | 11 | 50 |
| h(33) = 33 mod 13 = 7      | 0  | 1  | 2  | 3 | 4  | 5  | 6  | 7  | 8  | 9 | 10 | 11 | 12 |
|                            |    | 40 |    |   |    |    |    |    |    |   |    | Į. |    |
|                            | 77 | 27 |    | 3 | 12 | 31 |    | 33 | 99 | 8 | 22 | 11 | 50 |
| h(40) = 40 mod 13 = 1      | 0  | 1  | 2  | 3 | 4  | 5  | 6  | 7  | 8  | 9 | 10 | 11 | 12 |
|                            | _  |    |    |   |    |    |    |    | _  |   |    |    |    |
|                            |    |    | 40 |   |    |    |    |    |    |   |    |    |    |
|                            | 77 | 27 | 40 | 3 | 12 | 31 |    | 33 | 99 | 8 | 22 | 11 | 50 |
| h'(40) = (1+1) mod 13 = 2  | 0  | 1  | 2  | 3 | 4  | 5  | 6  | 7  | 8  | 9 | 10 | 11 | 12 |
|                            |    | 53 |    |   |    |    |    |    |    |   |    |    |    |
|                            | 77 | 27 | 40 | 3 | 12 | 31 |    | 33 | 99 | 8 | 22 | 11 | 50 |
| h(53) = 53 mod 13 = 1      | 0  | 1  | 2  | 3 | 4  | 5  | 6  | 7  | 8  | 9 | 10 | 11 | 12 |
|                            |    | •  | 53 |   |    |    |    | •  |    |   |    |    |    |
|                            | 77 | 27 | 40 | 3 | 12 | 31 |    | 33 | 99 | 8 | 22 | 11 | 50 |
| h'(53) = (1+1) mod 13 = 2  | 0  | 1  | 2  | 3 | 4  | 5  | 6  | 7  | 8  | 9 | 10 | 11 | 12 |
|                            |    |    |    |   |    | ı  | 53 | ı  |    |   |    |    |    |
|                            | 77 | 27 | 40 | 3 | 12 | 31 | 53 | 33 | 99 | 8 | 22 | 11 | 50 |
| h"(53) = (1+5) mod 13 = 6  | 0  | 1  | 2  | 3 | 4  | 5  | 6  | 7  | 8  | 9 | 10 |    | 12 |
| ( ), ( ), ( )              |    |    | _  |   |    |    |    |    | -  |   |    |    |    |
| Rho = 13/13 = 1            | 77 | 27 | 40 | 3 | 12 | 31 | 53 | 33 | 99 | 8 | 22 | 11 | 50 |
|                            | 0  | 1  | 2  | 3 | 4  | 5  | 6  | 7  | 8  | 9 | 10 | 11 | 12 |
|                            |    |    |    |   |    |    |    |    |    |   |    |    |    |