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# SOLUTIONS FOR 27<sup>TH</sup> OF JULY

## ABSURD TRIANGLE 5

```
for(int i = 1; i <= n-2; i++) {  
    cout << string(n-i-1, ' ') << '/' << string(2*i-2, ' ') << '\\ ' << string(n-i-1, ' ') << '\n';  
}  
cout << '/' << string(2*n-4, '_') << '\\ ' << '\n';
```

In this kind of problems, it may be convenient to use the `string` on the Standard Template Library.

## BUILDING PLAN

First, let's sort the given input so that  $x_1 < x_2 < \dots < x_n$  holds.

What should be the final distance between two adjacent buildings? It should be  $\gcd(x_2 - x_1, x_3 - x_2, \dots, x_n - x_{n-1})$ , because the final distance should be a divisor of all given distances. Also, it is a bad idea to build buildings in the left of  $x_1$  or the right of  $x_n$  (obviously)

Therefore, the answer is  $\left(\frac{x_n - x_1}{\gcd(x_2 - x_1, x_3 - x_2, \dots, x_n - x_{n-1})} + 1\right) - n$ . The former is the number of final buildings, and the latter is the number of already built buildings.

## THE INPUT IS *NOT* GUARANTEED TO BE SORTED

In the examples, the input is sorted. That *doesn't mean that the whole input is sorted!* If the statement said nothing, you should assume that the input can be in any order. This is a trick that some authors like to use.

## CALCULATOR WITH TWO BUTTONS

The key point of this problem is that it is always *not optimal* to press buttons like "--" and "+-", because they are both equal to "" (pressing no buttons) and "-", respectively. (You can check it by doing some examples)

Therefore, the optimal solution always look like this:

(Press button "-" 0 or 1 times) -> (Press button "+" 0 or more times) -> (Press button "-" 0 or 1 times)

So the algorithm goes like this: First, consider all 4 cases about the button "--": whether you press "-" at the beginning (change  $x$  to  $-x$ ) or not, and whether you press "-" at the end (change  $y$  to  $-y$ ) or not. After changing the signs, if  $x' \leq y'$  holds, we can press "+"  $y' - x'$  times and achieve the goal.

## DELIVERING

Let  $x$  as the number of 4kg package to use, and  $y$  as the number of 7kg package to use. We need to minimize the value of  $x + y$  subject to  $4x + 7y = N$ . We will find it by some observations.

- It is best to use the 7kg package as much as possible. (quite obvious?) In other words,  $y$  should be big as possible.
- If  $y$  is fixed, we can calculate  $x$  by the formula  $x = \frac{N-7y}{4}$ .
- However  $x$  should be an integer, so  $N - 7y \equiv 0 \pmod{4}$ .
- By the properties of modulo operation,  $N - 7y \equiv N + y \equiv 0 \pmod{4} \Rightarrow y \equiv -N \pmod{4}$ .
- Therefore, we can iterate  $y$  from  $\left\lfloor \frac{N}{7} \right\rfloor$  to 0, and check there exists a valid solution  $(x, y)$ . Because the necessary condition of the existence of solution is just " $y \equiv -N \pmod{4}$ ", it is guaranteed that we just need to consider at most 4 candidates of  $y$ .

## EVOLVING CREATURES

No one managed to solve this problem, so we won't reveal the solution.

## FORWARD TELEPORTERS

Let the answer for the  $i$ -th city as  $f(i)$ . We can find some recurrence relation like this:

- Base case:  $f(n) = 0$ .
- $1 \leq i \leq n - 1$ :  $f(i) = f(p_i) + 1$ .

If you calculate these values by implementing a recursive function or naive iteration, it will take  $O(n^2)$  time and will probably get TIME-LIMIT. Actually, we can improve this solution by noticing that  $p_i > i$  always holds, so we can iterate *backwards*. Starting from  $i = n$  to  $i = 1$ , we can fill out the values of  $f$ . Then, it will take  $O(n)$  time.

## GIANT BLOG

Just do what the statement says.

```
if(1 < p - k) printf("<< ");
for(int i = p-k; i <= p+k; i++) {
    if(1 <= i && i <= n) printf((i == p) ? "(%d) " : "%d ", i);
}
if(p + k < n) printf(">> ");
printf("\n");
```