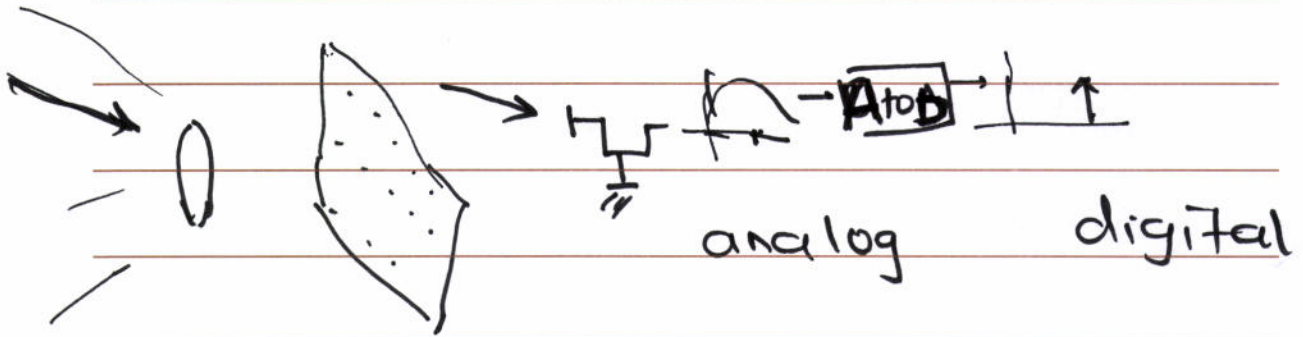
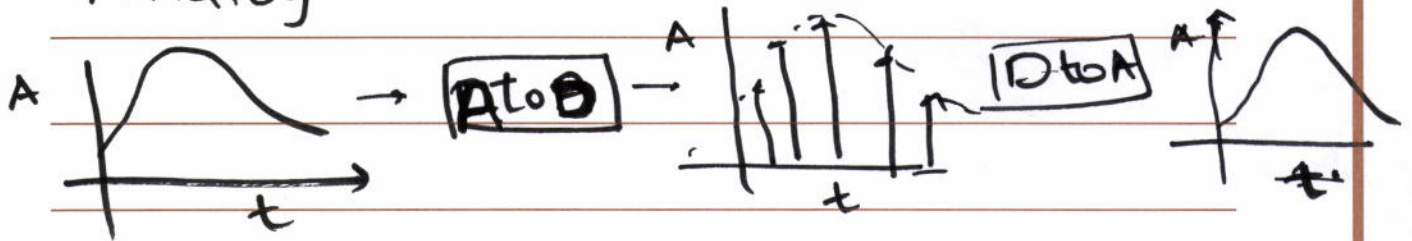


camera



Analog



continuous

discrete

analog

A to D

sampling

Quantization

## Sampling

$$y = x(t)$$

$$x_s[n] = x(nT)$$

$T$  is sampling period

$$x_s[1] = x(T)$$

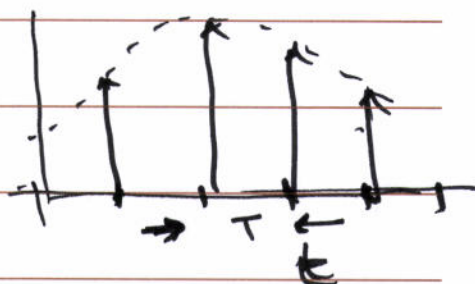
$$x_s[2] = x(2T)$$

$$x_s[3] = x(3T)$$

$\vdots$

$$f = \frac{1}{T}$$

sampling frequency



$$T \uparrow \uparrow \rightarrow f \downarrow \downarrow$$

data decreases

$$T \downarrow \downarrow \rightarrow f \uparrow \uparrow$$

data increases

## Quantization

$$x_q[n] = Q[x_s[n]]$$

range  $R$

each sample  $\rightarrow b$  bits



$$\frac{1}{2} \left( \frac{R}{2^b - 1} \right) \Rightarrow \text{max error}$$

Bitrate

$$= \text{bits/second}$$

$$= \frac{\text{samples}}{\text{second}} \times \frac{\text{bits}}{\text{sample}}$$

$$= F \times b$$

$$\text{sampling freq} \times \text{bits/sample}$$

~~What should T be?~~

LTI - Linear Time Invariant

$$y = x(t)$$

$$x_1 \rightarrow y_1 \quad x_2 \rightarrow y_2$$

$$c_1 x_1 + c_2 x_2 \rightarrow c_1 y_1 + c_2 y_2$$

$$y_1 = x(t_1) \quad y_2 = x(t_2)$$

$$x(c_1 t_1 + c_2 t_2) = c_1 y_1 + c_2 y_2$$

$$y = kx \quad \text{linear?}$$

$$x_1 \quad y_1 = kx_1$$

$$x_2 \quad y_2 = kx_2$$

$$x_1 + x_2 \quad y = k(x_1 + x_2) = kx_1 + kx_2 \\ = y_1 + y_2$$

$$y = x^2 \quad \text{linear?} \quad \text{No}$$

$$y = \frac{dx}{dt}$$

$$y = x + a$$

$$x_1: y_1 = x_1 + a$$

$$x_2: y_2 = x_2 + a$$

$$x_1 + x_2: y = x_1 + x_2 + a \neq y_1 + y_2$$



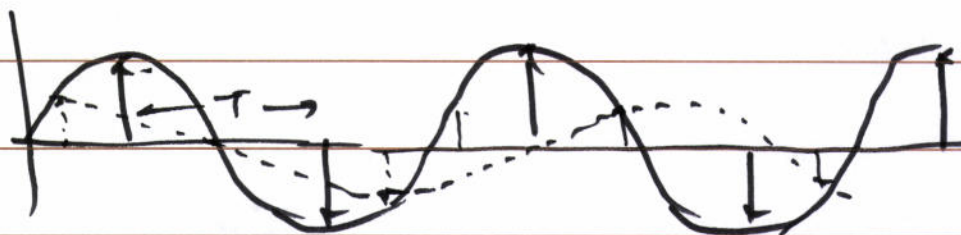
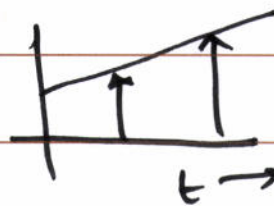
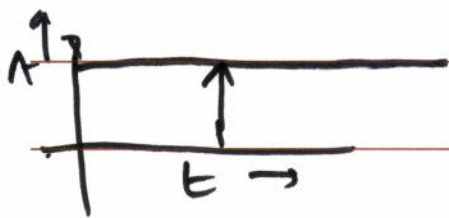
Time domain view:

If your system is LTI, & you know how it responds to a delta function  $\rightarrow$

$$x(t) \rightarrow \boxed{h(t)} \rightarrow y(t)$$

$$y(t) = h(t) \otimes x(t)$$

What should  $T$  be?

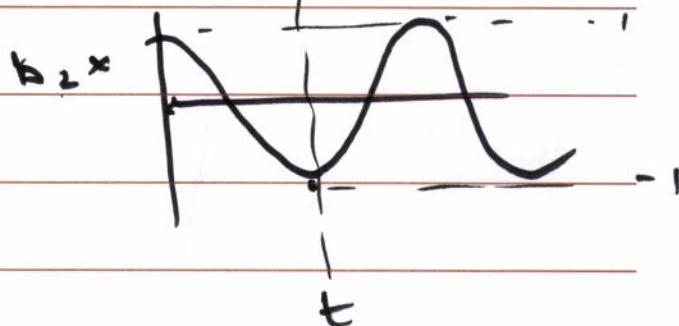
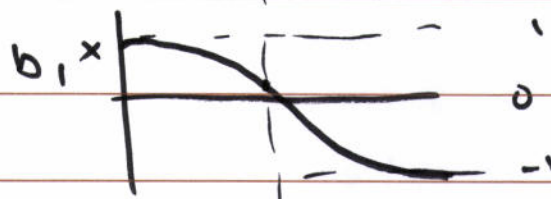
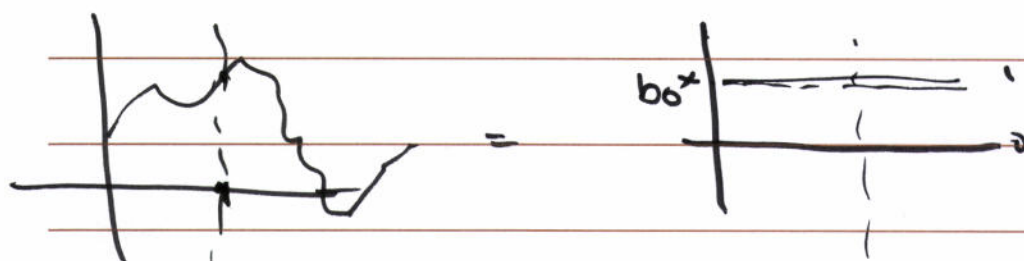


$F > 2 \times \text{max freq. in signal}$

$$f(t) = \sum a_i \sin i\omega t + \sum b_i \cos i\omega t$$

$$f(t) = \sum b_i \cos i\omega t$$

$$f(t) = b_0 + b_1 \cos \omega t + b_2 \cos 2\omega t + \dots$$



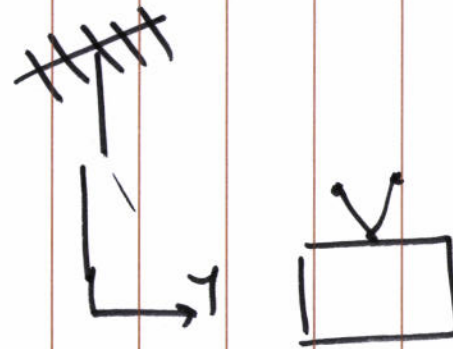
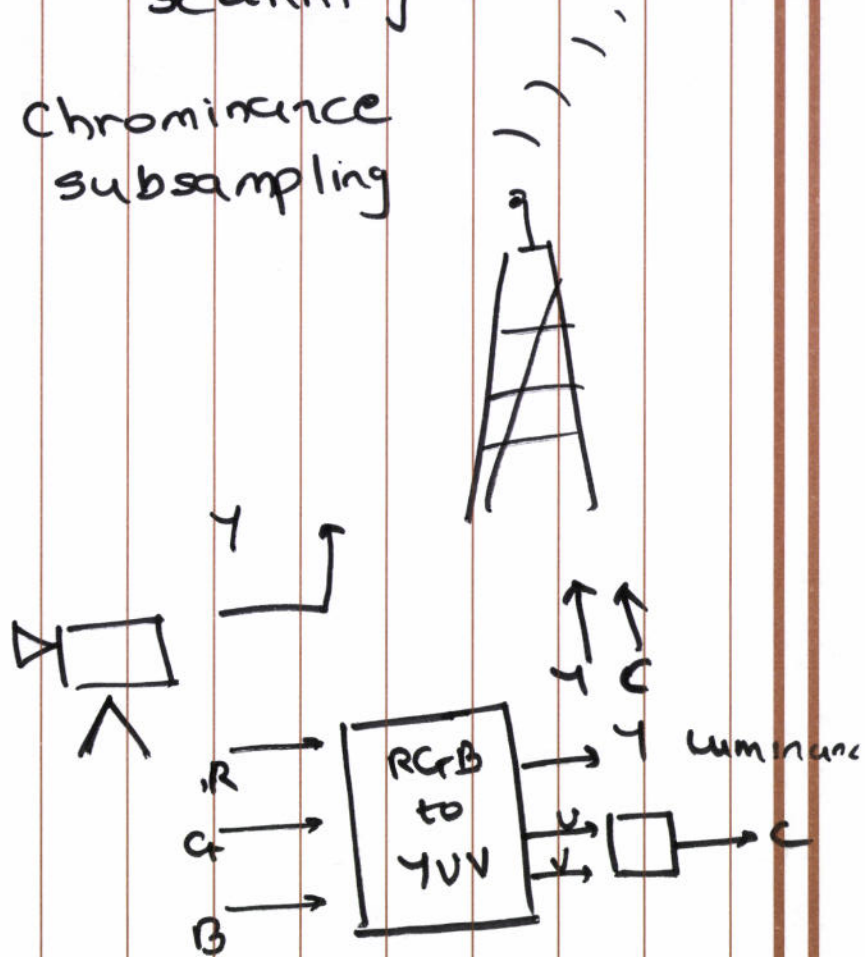
$f(t)$

$t$

$$b_i = \int_{-\infty}^{\infty} f(t) \cos i\omega t dt$$

synchronization  
interlaced  
scanning

chrominance  
subsampling



RGB  $\rightarrow$  YUV

YUV 4:4:4

for every four pixels

$$\text{keep all Y } 4 \times 8 = 32$$

$$\text{keep all U } 4 \times 8 = 32$$

$$\text{keep all V } 4 \times 8 = \underline{32}$$
$$96$$

$$\text{avg bits/pixel} = \frac{96}{4}$$
$$= 24$$

YUV 4:2:2

for every four pixels

$$\text{keep all Y } 4 \times 8 = 32$$

$$\text{keep only 2 U } 2 \times 8 = 16$$

$$\text{keep only 2 V } 2 \times 8 = \underline{16}$$
$$64$$

$$\text{avg bits/pixel} = \frac{64}{4}$$
$$= 16$$



YUV 4:2:0 4:1:1

for every four pixels

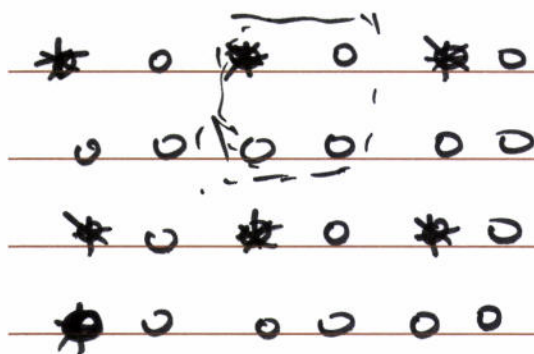
keep all Y  $\rightarrow 4 \times 8 = 32$

keep 1 U  $\rightarrow 1 \times 8 = 8$

keep 1 V  $\rightarrow 1 \times 8 = 8$   
48

$$\begin{aligned} \text{avg bits} / \text{pixel} &= \frac{48}{4} \\ &= 12 \end{aligned}$$

4:2:0



4:1:1

