

Vector Space = Set of Vectors $\begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$ 3×1 Vector
(col matrix)

+ Set of Scalars
(real number)

Closed under
Vector addition
and Scalar
multiplication

Example

Set of Vector \sim All (3×1) matrix,
Set of scalars \sim All real number

$$\begin{aligned} A \quad B \quad (3 \times 1) \text{ matrix} \\ \underline{(2,3)} \quad W &= 2 \cdot A + 3 \cdot B \\ &= 2 \cdot \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix} + 3 \cdot \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} \\ &= \begin{pmatrix} 2a_1 + 3b_1 \\ 2a_2 + 3b_2 \\ 2a_3 + 3b_3 \end{pmatrix} \\ &\quad (3 \times 1) \text{ Vector} \end{aligned}$$