

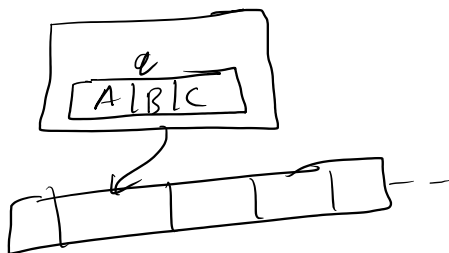
1. storage in state ✓
2. Multiple tracks
3. subroutines →  $m \times n \Rightarrow 0^m 1 0^n 1 0^{mn} \Rightarrow 0^3 1 0^6$

Note:-

Here none of these techniques are  
extending the functionality of TM

### 1) Storage in state :-

Finite control not only to represent a position  
in the program of TM, but also to  
hold a finite amount of data



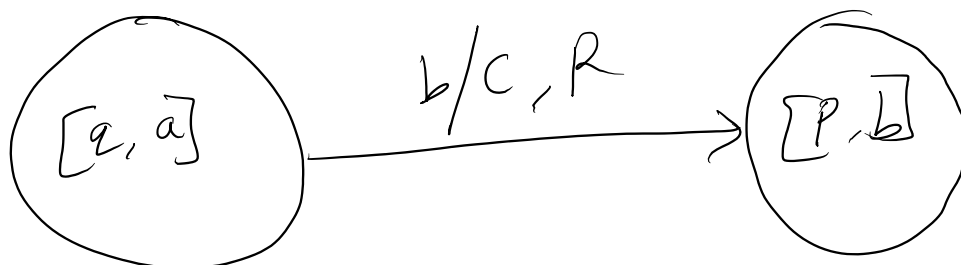
$(Q, \Sigma, \Gamma, \delta, q_0, B, F)$

$Q$  is of the form  $[q, a]$   $q \in Q$   
 $a \in \Gamma$

$\delta$  is defined as  $\Rightarrow (Q \times \Gamma) \times \Gamma \rightarrow [Q \times \Gamma] \times T \times [L, R]$

$$\delta([q, a], b) = ([p, b], c, R)$$

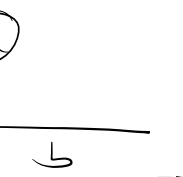
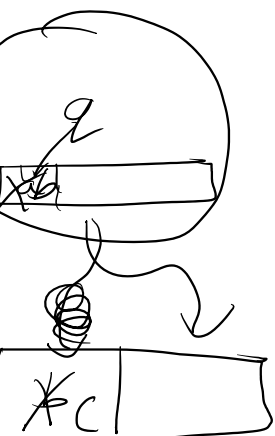
$q$  with a  $a$  symbol replaces  $a$  by  $b$  on seeing  $b$  on the  
changing state from  $q$  to  $p$

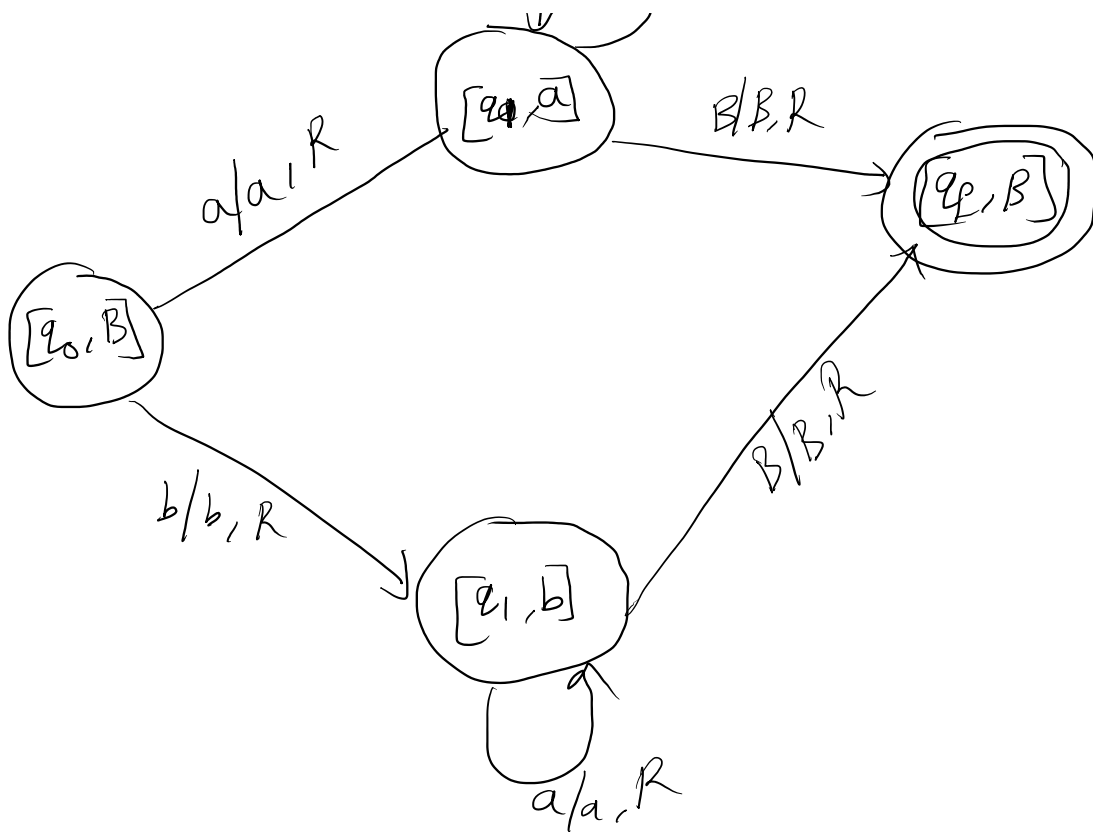


Construct TM that accepts the language  $\{a b^* \cup b a^*\}$



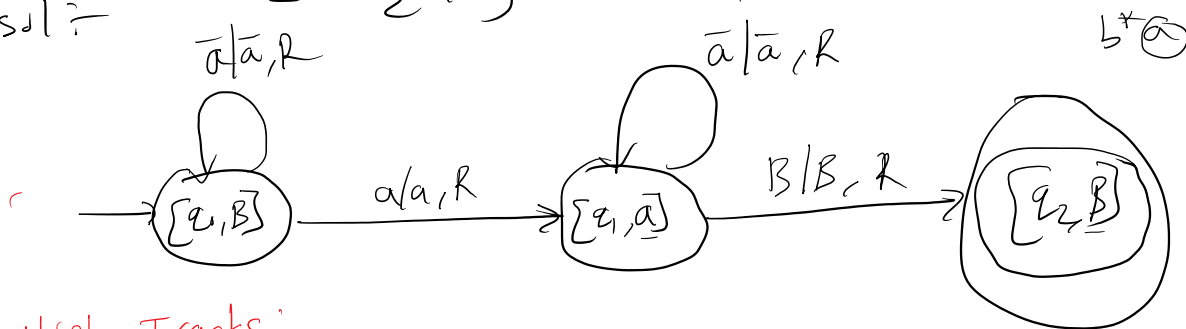
tape &





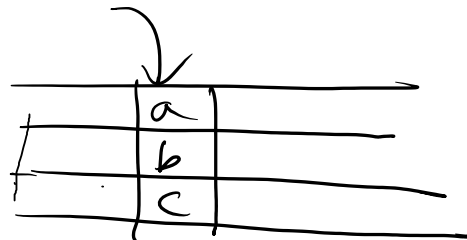
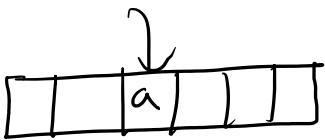
Ex: 2: Design TM & check that 'a' should not be repeated for strings of a's & b's

sol:  $\Sigma = \{a, b\}$   $ab^* \Rightarrow a\bar{a}$

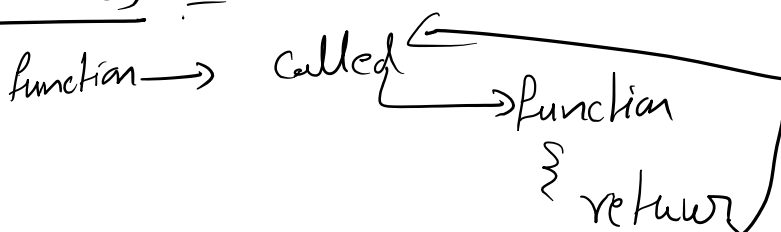


### Multiple Tracks:-

In this a single tape is assumed to be divided into tracks.



### 3) Sub routines :-



a + L



} return  
}

Ex:- Multiplication  $\Rightarrow$  language  $\Rightarrow$   $\begin{matrix} m & n & mn \\ 0 & 1 & 0 \\ \downarrow & \downarrow & \downarrow \\ I_1 & I_2 & \text{output} \end{matrix}$

Informal:-

B 0 0 1 0 0 0 1 B B B  
↑  
→ x 0 0 1 0

x x 0 1 0 0

x x x 1 0 0 0 0 0 0 0

← copy → subtractive

00 x 000 = 0000000

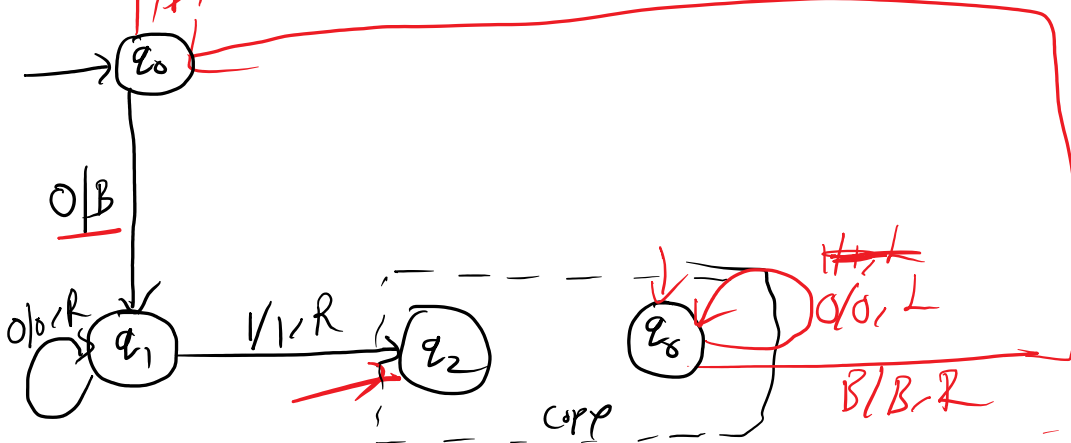
Method 1:- 00 00 00

Method 2:- 000 000

C

0/B, R → q<sub>1</sub> 1/B, R → q<sub>2</sub>

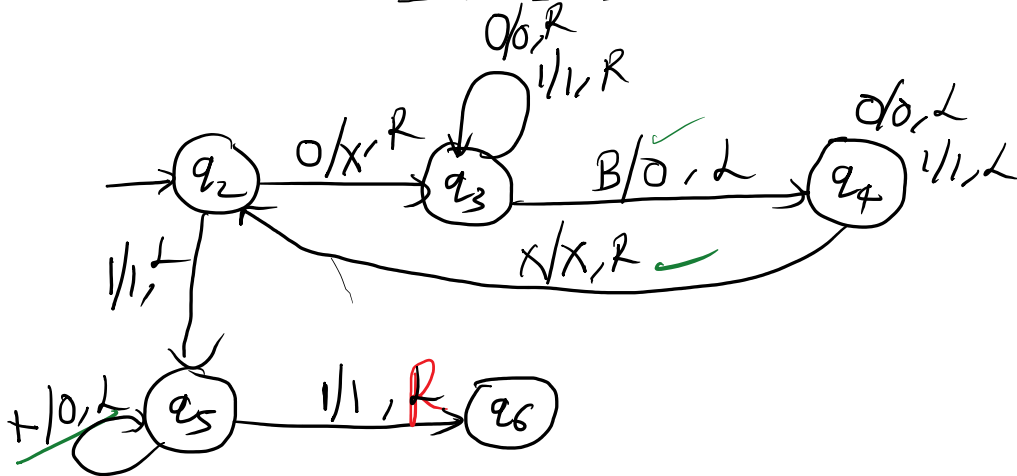
0/B, R



I/P

B 0<sup>3</sup> 1 0<sup>2</sup> 1

B 0 0  
↓  
B B 0



1<sup>st</sup>

2<sup>nd</sup> group

} etc.

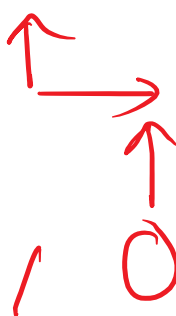
B B B

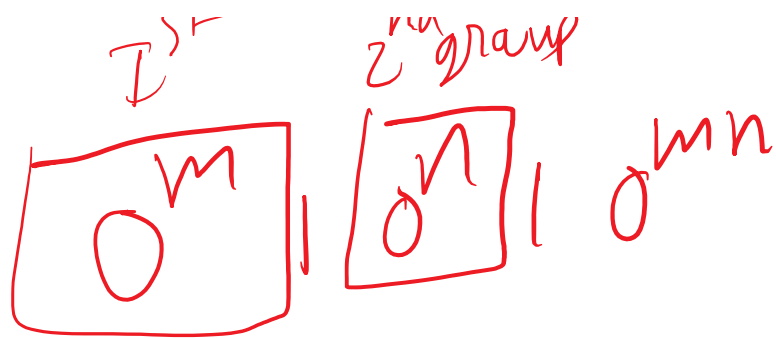
00100 | B B B

00 | X X 1 0 0

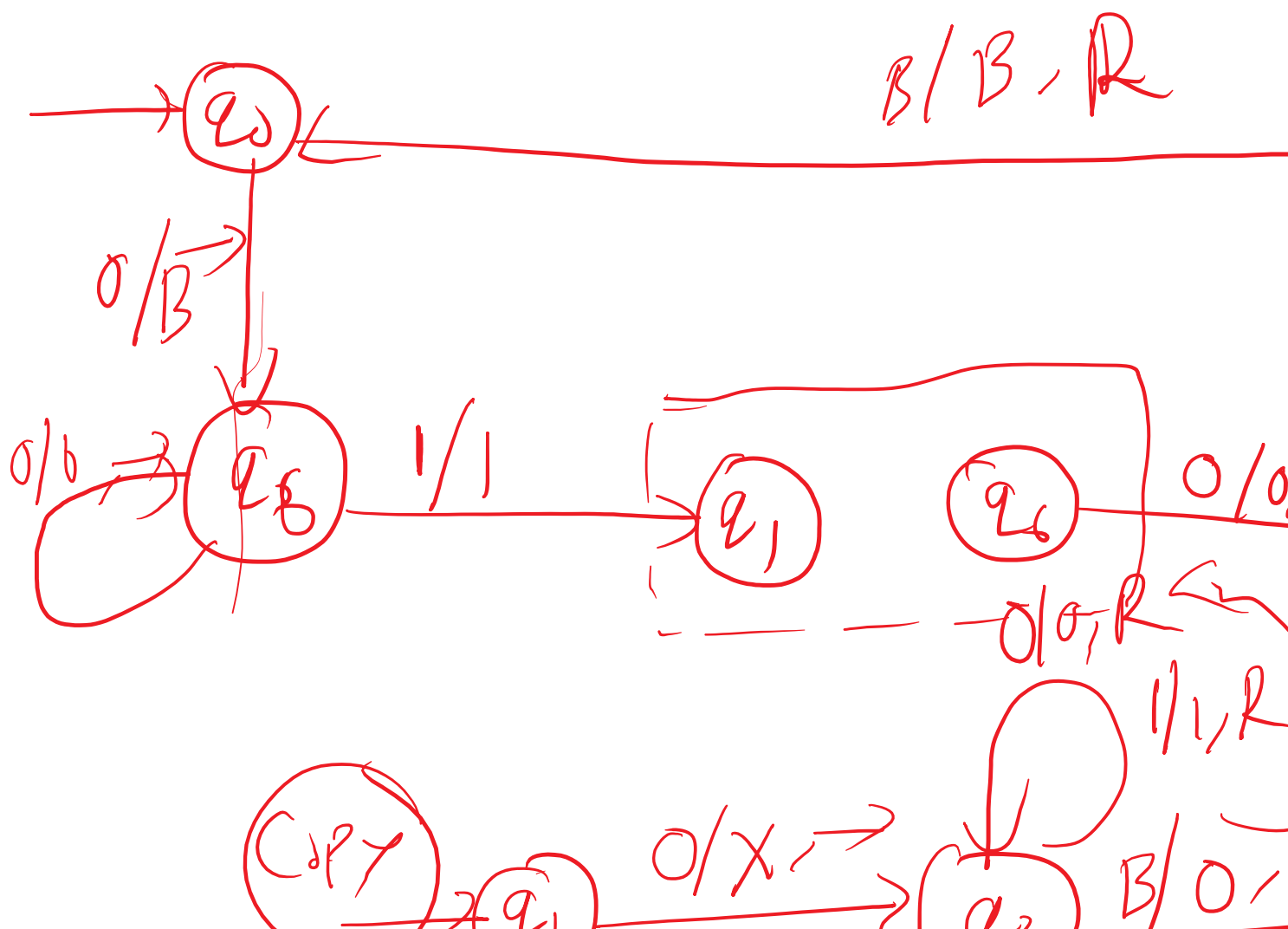


1 0 0





- 1) Reading  $mn$
- 2) Marking first group first zero to



B

Copy  
B B 0 0 0 1 0 0 1 B B B  
B 0 0 1 x 0 1 0

1 x x 1 0 0  
0 0 1 0 0

