

Q1] find first 4 Raw moments for the following data

x	-1	0	1	2	3	4
f	2	4	3	7	3	1

Q2] for the following ungrouped data find Karl Pearson's coefficient of skewness.

12, 18, 25, 15, 16, 10, 18, 8, 15, 27, 14.

Q3] The avg income of 100 men in a city is ₹15,000 with S.D ₹8500 and the avg income of 100 women is ₹12,000 and S.D. ₹9000 <sup>can</sup> it be said at 5% level of confidence that there is a significant difference between the avg income of men & women.

Q4] A manufacturer claims that 10% of his products are defective. A sample of 300 is selected at random and has 32 defective product. Test his claim at 1% level of significance.

### SOLUTION

Q3]	men	women
	n = 100	n = 100
	S.D = 8500	SD = 9000
	$\bar{x}_1 = 15000$	$\bar{x}_2 = 12000$

$$SE = \sqrt{\frac{(\sigma_1)^2}{n_1} + \frac{(\sigma_2)^2}{n_2}} = \sqrt{\frac{(8500)^2}{100} + \frac{(9000)^2}{100}}$$

$$= 875.36 \quad \boxed{875.36} =$$

<u>Q.1.</u>	$x$	$f$	$f \cdot x$	$f \cdot x^2$	$f \cdot x^3$	$f \cdot x^4$
	-1	2	-2	2	-2	2
	0	4	0	0	0	0
	1	3	3	3	3	3
	2	7	14	28	56	112
	3	3	9	27	81	243
	4	1	4	16	64	256
		$N=20$	28	76	202	616

$$\mu_r = \frac{\sum f(x_i)^r}{N}$$

$$\mu_1 = \frac{\sum fx}{N} = \frac{28}{20} = 1.4$$

$$\mu_2 = \frac{\sum f x^2}{N} = \frac{76}{20} = 3.8$$

$$\mu_3 = \frac{\sum f x^3}{N} = \frac{202}{20} = 10.1$$

$$\mu_4 = \frac{\sum f x^4}{N} = \frac{616}{20} = 30.8$$

Q.2. Mem:

$$\sum x = 12 + 18 + 25 + 15 + 16 + 10 + 8 + 15 + 27 + 14 = 160$$

$$\bar{x} = \frac{\sum x}{n} = \frac{160}{10} = 16$$

Mode : 15 repeated 2 times.

$$\therefore \text{Mode} = 15$$



For Standard Deviation ( $\sigma$ ).

$$\begin{aligned}\sum x^2 &= (12)^2 + (18)^2 + (25)^2 + (15)^2 + (16)^2 \\ &\quad + (10)^2 + (8)^2 + (15)^2 + (27)^2 + (14)^2 \\ &= 144 + 324 + 625 + 225 + 256 + 100 \\ &\quad + 64 + 225 + 729 + 196 \\ &= \boxed{2888}\end{aligned}$$

$$\sigma = \sqrt{\frac{\sum x^2}{n} - (\bar{x})^2}$$

$$= \sqrt{\frac{2888}{10} - (16)^2} = \sqrt{\frac{2888}{10} - 256}$$

$$= \sqrt{32.8}$$

$$\sigma = \boxed{5.727}$$

Karl Pearson's Coefficient of Skewness

$$S_k = \frac{\text{Mean} - \text{Mode}}{\sigma}$$

$$= \frac{16 - 15}{5.727} = \frac{1}{5.727}$$

$$= 0.1746$$

$$0.1746 > 0$$

$$\therefore S_k = \boxed{0.1746}$$

Q.3. Mean

$$n = 100$$

$$\bar{x} = 15000$$

$$SD = 8500$$

$$S.E. = \sqrt{\frac{\sigma_1^2}{n} + \frac{\sigma_2^2}{n}}$$

$$= \sqrt{\frac{(8500)^2}{100} + \frac{(8000)^2}{100}}$$

$$= 1237.94$$

$$|Z| = \left| \frac{\bar{x}_1 - \bar{x}_2}{S.E.} \right|$$

$$= \frac{15000 - 12000}{1237.94}$$

$$= 2.42 > 1.96$$

$H_0$  is Rejected.

$$\begin{aligned}
 &= 4.2071 \\
 (z) &= \left| \frac{x_1 - x_2}{s.e} \right| \\
 &= \frac{120 - 90}{4.2071} \\
 &= 7.130 \\
 &\rightarrow
 \end{aligned}$$

Q7. A manufacturer claims that 10% of his is defective. A sample of 300 items select random had 32 defective items. Test his at 1% level of significance (At 1% significance the value of 2.58)

$$\Rightarrow H_0 = \pi = 10\% = \frac{10}{100} = 0.1$$

$$H_1 = \pi \neq 10\% = 0.1$$

$$n = 300, \quad p = \frac{32}{300} = 0.1067$$

$$q = 1 - 0.1067 = 0.8933$$

$$Z_{\alpha} = 1\% = 2.58$$

$$\begin{aligned}
 SE &= \sqrt{\frac{pq}{n}} \\
 &= \sqrt{\frac{0.1067 \times 0.8933}{300}} \\
 &= 0.0178
 \end{aligned}$$

$$z_{cal} = \frac{n - p}{S.E}$$

$$= \frac{0.1 - 0.1067}{0.0178}$$

$$= -0.3764 < 2.58$$

$H_0$  is accepted.

Q. An old machine produced 10  
batch of 300. After the servi