



# Indian Institute of Technology Guwahati

## Department of Physics

### End-Semester Examination: Physics-I (PH101)

Total Marks: 48

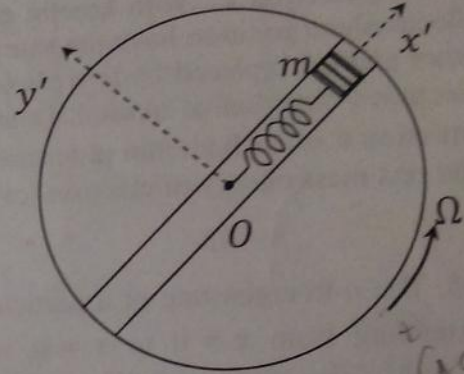
Date: 24.11.2013

Duration: 3hrs

6 × 8 = 48

Answer all six questions:

Q1. A flat, circular turntable with a straight groove passing through the center  $O$ , is rotating in a horizontal plane with a constant angular speed  $\Omega$ , as shown in the figure. A block of mass  $m$ , which is snugly fitted and constrained to move along the groove, is connected to a spring whose other end is fixed at  $O$ . Assume that the natural length of the spring is negligible, and its spring constant  $k$  is  $\leq m\Omega^2$ . The groove is of rectangular cross section having a frictionless floor but rough side walls with coefficient of kinetic friction  $\mu = 1/2$ . Consider a rotating frame  $S'$  attached to the turntable with  $x'$  axis along the groove,  $y'$  axis is on the plane of the turntable and the origin  $O' = O$ . At  $t = 0$ , the block is released from the origin  $x'(0) = 0$  with an initial velocity  $\dot{x}'(0) = v_0$  in the positive  $x'$ -direction. (Assume that the block remains on the turntable and the spring does not break.)



- (a) What are the forces (ignoring gravity) acting on the block in the rotating frame  $S'$  at any later time? (b) Write the equations of motion of the block. (c) If the spring constant  $k$  is taken to be  $m\Omega^2$ , what are the instantaneous velocity  $\dot{x}'(t)$  and position  $x'(t)$  of the block? [3+2+3=8]

Q2. A thin rectangular plate of mass  $m$  with sides  $a$  and  $2a$ , rotates with constant angular velocity  $\omega$  about an axle passing through two diagonal corners, as shown in figure. The axle is supported at the corners of the plate by bearings A and B which can exert forces only on the axle.  $xyz$  represents the body fixed frame with origin  $O$  at the center of mass of the plate,  $xy$  plane is the plane of the plate and  $x$ -axis is parallel to the side  $2a$ . (a) What is the moment of inertia tensor of the plate in the given body frame? (b) Find the torque about  $O$  required to maintain the motion. (c) Find the components of forces exerted by each bearing on the axle in the given body frame. (Ignore gravitational and frictional forces.) [2+3+3=8]

