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Assignment - 3

Q2.) # E_1 , $P(\text{choosing Bag 1}) = 1/2$

E_2 , $P(\text{choosing Bag 2}) = 1/2$

A/E_1 , $P(\text{drawing Black ball from Bag 1}) = 6/10 = 3/5$

A/E_2 , $P(\text{drawing Black ball from Bag 2}) = 3/7$

Using Bayes's theorem,

$$\# E_1/A, P(\text{drawing Black ball, Bag 1}) = \frac{P(E_1) P(A/E_1)}{P(E_2) P(A/E_2) + P(E_1) P(A/E_1)}$$

$$\begin{aligned} P(E_1/A) &= \frac{1/2 \times 3/5}{1/2 \times 3/7 + 1/2 \times 3/5} \\ &= \frac{3/10}{3/14 + 3/10} = \frac{0.3}{0.2142 + 0.3} \end{aligned}$$

$$P(E_1/A) = \underline{\underline{0.583}}$$

Q3.)

E_1 , $P(\text{Man speaks Truth}) = 2/3$

E_2 , $P(\text{Man speaks Lie}) = 1 - 2/3 = 1/3$

A/E_1 , $P(\text{four when he speak truth}) = 1/6$

A/E_2 , $P(\text{four when he speaks lie}) = 5/6$

Using Bayes's theorem,

$$\# E_1/A, P(\text{Number is actually four}) = \frac{P(E_1) P(A/E_1)}{P(E_2) P(A/E_2) + P(E_1) P(A/E_1)}$$

$$\begin{aligned} P(E_1/A) &= \frac{2/3 \times 1/6}{1/3 \times 5/6 + 2/3 \times 1/6} \\ &= \frac{2/18}{5/18 + 2/18} = 2/7 \end{aligned}$$

$$P(E_1/A) = \underline{\underline{0.285714}}$$