

**University of Central Florida**

**Department of Computer Science**

**CDA 5106: Fall 2023**

**Machine Problem 1: Cache Design, Memory Hierarchy Design**

**by**

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Honor Pledge: "I have neither given nor received unauthorized aid on this test or assignment."

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Note: Using the GCC benchmark for all experiments, that is, use 'traces/gcc\_trace.txt' file.

## 1. L1 cache exploration: SIZE and ASSOC

### GRAPH 1: L1 Cache Miss Rate vs Log (Cache Size)

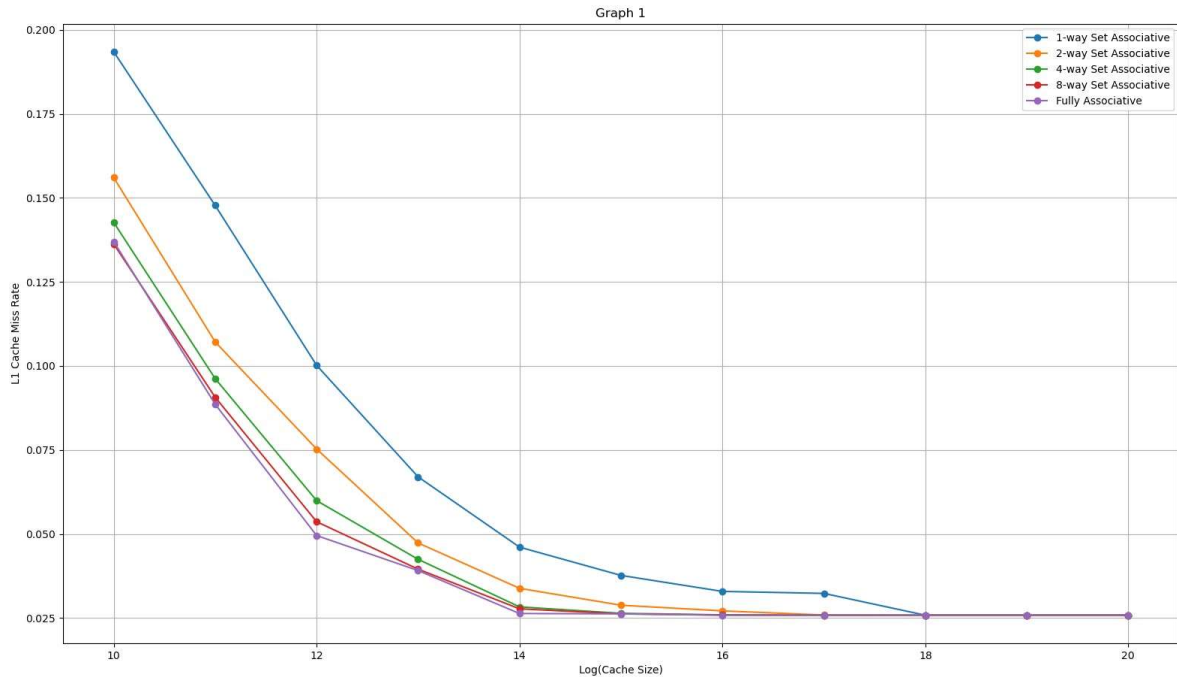
For this experiment:

- L1 cache: SIZE is varied, ASSOC is varied, BLOCKSIZE = 32.
- L2 cache: None.
- Replacement policy: LRU
- Inclusion property: non-inclusive

Graph 1: L1 Cache Miss Rate vs Log2(Cache Size)						
cache size	log (cache size)	1-way Associative	2-way Associative	4-way Associative	8-way Associative	Fully Associative
1024	10	0.19346	0.15603	0.1427	0.13627	0.13696
2048	11	0.14774	0.10714	0.09622	0.09069	0.0886
4096	12	0.10017	0.07528	0.05992	0.05365	0.04954
8192	13	0.067	0.04734	0.04247	0.03954	0.03912
16384	14	0.04609	0.03384	0.02832	0.02774	0.02634
32768	15	0.03768	0.02881	0.0264	0.02625	0.02624
65536	16	0.03292	0.02713	0.02595	0.02589	0.02583
131072	17	0.03233	0.0259	0.02582	0.02582	0.02582
262144	18	0.02584	0.02584	0.02582	0.02582	0.02582
524288	19	0.02584	0.02582	0.02582	0.02582	0.02582
1048576	20	0.02584	0.02582	0.02582	0.02582	0.02582

### Discussion:

1. We can see that the miss rates are more for lower associativity. For a given associativity, we can the miss rate decreases initially as the cache size increases, but then plateaus after a point. For a given cache size, as we increase the associativity, the miss rate decreases. This also is valid up to a point, here, after log (cache size) = 18, we see the miss rate becomes constant.
2. The compulsory miss rate represents the percentage of cache misses caused by accessing data or instructions for the first time. From the graph, we can see that compulsory miss rate can be estimated when the cache size is significantly more, and it comes around to be **0.02582**.
3. Depending on the cache size and associativity, conflict miss rates vary.  
Prior to calculating conflict miss rates, capacity misses can be determined by setting the conflict miss rate for fully associative to be 0.  
Conflict miss rates then can be computed for various associativity as the capacity miss rate and mandatory misses remain constant for associativity of the same size.



## GRAPH 2: AAT vs Log (Cache Size)

For this experiment:

- L1 cache: SIZE is varied, ASSOC is varied, BLOCKSIZE = 32.
- L2 cache: None.
- Replacement policy: LRU
- Inclusion property: non-inclusive

Miss Penalty = 100 ns

Here,

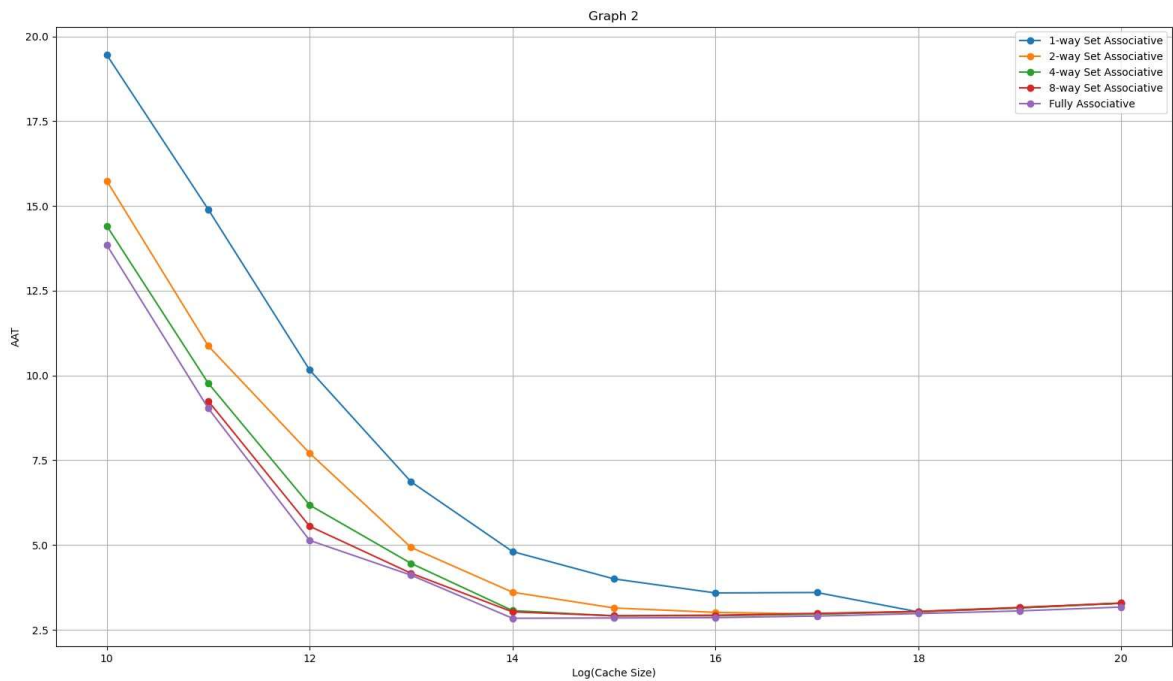
$$\text{AAT} = (\text{Miss Rate} * \text{Miss Penalty}) + \text{Hit Time}$$

Discussion:

1. For a memory hierarchy with only an L1 cache and BLOCKSIZE = 32, we can see that the configuration having full associativity and cache size = 16,384 bytes (16 KB) yields the best (i.e., lowest) AAT, that is 2.839608.

The trend is that fully associative configuration is usually better in terms of having lower AAT values, but we can see that after a certain increase in cache size, AAT values for all becomes similar.

AAT						
cache size	log (cache size)	1-way Associative	2-way Associative	4-way Associative	8-way Associative	Fully Associative
1024	10	19.460797	15.743329	14.41682		13.851484
2048	11	14.90309	10.875691	9.776496	9.249686	9.036515
4096	12	10.164005	7.709131	6.177685	5.554065	5.136948
8192	13	6.86383	4.928195	4.458173	4.166911	4.110581
16384	14	4.807417	3.607917	3.065936	3.028354	2.839608
32768	15	4.001353	3.143446	2.91125	2.913511	2.84874
65536	16	3.586627	3.013727	2.914481	2.930213	2.859281
131072	17	3.5998	2.964603	2.96228	2.983236	2.904486
262144	18	3.027812	3.029929	3.039685	3.040925	2.978009
524288	19	3.147451	3.149744	3.146418	3.160177	3.057728
1048576	20	3.28338	3.288046	3.281607	3.287819	3.170474



## 2. Replacement policy study

### GRAPH 3: AAT vs Log (Cache Size)

For this experiment:

- L1 cache: SIZE is varied, ASSOC = 4, BLOCKSIZE = 32.
- L2 cache: None.
- Replacement policy: varied
- Inclusion property: non-inclusive

Miss Penalty = 100 ns

Here,

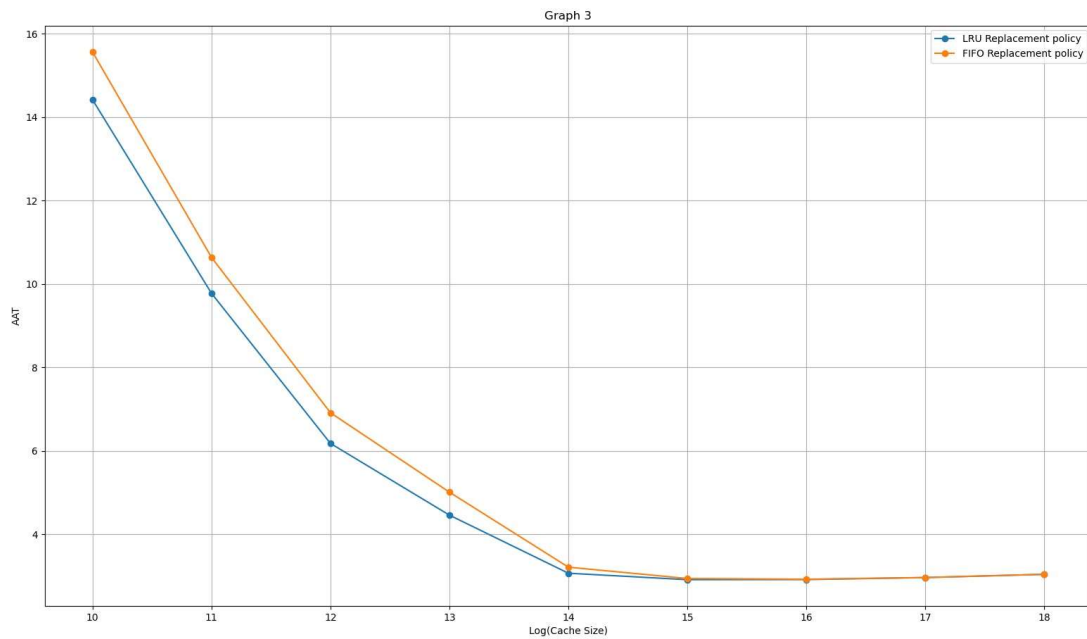
$AAT = (Miss\ Rate * Miss\ Penalty) + Hit\ Time$

Discussion:

For both LRU and FIFO, we can see that AAT decreases initially as we increase the cache size, but then plateaus. It also becomes similar for both LRU and FIFO as the cache size is more.

The replacement policy yields the best (i.e., lowest) AAT is **LRU, better than FIFO**.

AAT			
cache size	log (cache size)	LRU	FIFO
1024	10	14.41682	15.56182
2048	11	9.776496	10.637496
4096	12	6.177685	6.912685
8192	13	4.458173	5.009173
16384	14	3.065936	3.210936
32768	15	2.91125	2.93925
65536	16	2.914481	2.922481
131072	17	2.96228	2.96228
262144	18	3.039685	3.039685



### 3. Inclusion property study

GRAPH 4: AAT vs Log (Cache Size)

For this experiment:

- L1 cache: SIZE = 1KB, ASSOC = 4, BLOCKSIZE = 32.
- L2 cache: SIZE = 2KB – 64KB, ASSOC = 8, BLOCKSIZE = 32.
- Replacement policy: LRU
- Inclusion property: varied

Miss Penalty = 100 ns

$$AAT = HTL1 + MRL1 * (HTL2 + (MRL2 * \text{Miss Penalty}))$$

where HTL1 is Hit Time of the L1 cache and HTL2 is Hit Time of the L2 cache while MRL1 and MRL2 are miss rates of the respective L1 and L2 caches.

## Discussion:

For both inclusion properties, we can see that as the cache size increases, the AAT values decrease initially and then plateau around a value. For both inclusion properties, the AAT values become similar after a certain cache size value.

Initially, for smaller cache sizes, non-inclusive is giving better AAT values. However, for most of the cache sizes later on, both inclusion properties are giving similar AAT values.

AAT			
cache size	log (cache size)	non-inclusive	inclusive
2048	11	9.158608402	9.600056512
4096	12	5.541802556	5.581874007
8192	13	4.14019545	4.146223303
16384	14	2.953123096	2.953123096
32768	15	2.81298556	2.81298556
65536	16	2.784517195	2.784517195

