$$\chi^{2} = \frac{\left(\times \text{pred} - \times \text{res} \right)^{2}}{6i^{2}}$$

$$\chi^2 = \frac{2}{2} \left(\frac{\alpha x_i + b - y_i}{6i^2} \right)^2$$

$$\frac{\partial x^2}{\partial a} = \frac{2(ax_i + b - y_i) \cdot x_i}{6i^2} = 0$$

$$\frac{\partial x^2}{\partial b} = \frac{2(ax_1 + b - g_1)}{6x_2^2} = 0$$

$$a(x^2) + b(x) - (xy) = 0$$

$$N_{\alpha}(x^{2}) + 5 < x > N - (xy) N = 0$$

$$\alpha(x^{2}) + 5 < x > N - (x) < y > = 0$$

$$\alpha((x^{2}) - (x)^{2}) = (xy) - (x) < y >$$

$$\alpha = \frac{N(xy) - (x)^{2}}{N(x^{2}) - (x)^{2}}$$

$$a (x^{2})(x) + b (x)^{2} - (xy)(x) = 0$$

$$a (x) (x^{2}) + b N (x^{2}) - (y)(x^{2}) = 0$$

$$b (N(x^{2}) - (x)^{2}) = (x^{2}) (x) - (xy)(x)$$

$$b = (y)(x^{2}) - (xy)(x)$$

$$b = (y)(x^{2}) - (x^{2})$$

Central Limit Theorem:

- 1) We derived an example:
 Poisson Distribution -> Gaussin Distribution
 for large N.
- 2) In scipy, we saw that

 many rinder nowbers in CO, 23 lead

 to Gaussia distributur
- Generally CLT says pritherize non of independent randon variables with friete verince converses to a Grussian distribution in limit at large of.
- In cose of Poisson we san tris consequence on se very fast (Wall)
- In practice: this rems the most likely distribution or will encounter to the Grussian distribution.
- Therefore; when we know no -better
 we assume our PDF is Gaussian...

X2 Tests

Want to unlorstand how likely a set of data;

 $\{X_1 \pm 6_1, X_2 \pm 6_2, X_3 \pm 6_3, \dots\} \equiv X_1 \pm 6_1$ is the result of a corresponding theoretical prediction;

{ 9, , 92, ---, 9, } = 9;

Assume Gaussian uncertainties on X tren probability of one recourement

 $P_{i} = \frac{1}{\sqrt{2\pi} 6i} \exp \left(-\frac{1}{2} \frac{(y_{i} - x_{i})^{2}}{6i^{2}}\right)$

The probability for the complete set of a measurements is called the Likelih...)

 $\mathcal{L} = \prod_{i} P_{i} = \prod_{j \in \mathbb{Z} \cap G_{i}} \exp\left(-\frac{1}{2} \frac{(y_{i} - x_{i})^{2}}{g_{i}^{2}}\right)$

(In fact likelihoo) (and mitent follows) is quite a sit were severy, we could have another PDF in some circumstances, and a different Likelihood Fractural)

Best Estimates for X:

Suppose re make a menurements
"drawn from a Gaussin distribution"

x, x, x3, --- , x,

What is our best estimate for the

For a "true value" of X and an uncertainty of each rensurement B, the probability of rensureing within Dx of X; is

$$P(x_1) = \frac{1}{\sqrt{2\pi} 6} \exp\left(-\frac{(x_1 - \hat{X})^2}{2 6^2}\right) \Delta x$$

The combined probability of our while series is

$$P = P(x_1) \cdot P(x_2) \cdot P(x_3) \cdot P(x_n)$$

$$= \left(\frac{\partial x}{\partial x}\right)^{N} e^{x} P\left(-\frac{(x_1 - x)^2}{26^2}\right) \cdot e^{x} P\left(-\frac{(x_2 - x)^2}{26^2}\right) \cdot e^{x}$$

$$= \left(\frac{\partial x}{\partial x}\right)^{N} \left(\frac{\partial x}{\partial x}\right)^{N} \cdot \left(\frac{\partial x}{\partial x$$

$$= \left(\frac{\Delta x}{2\pi 6}\right)^{N} exp\left(-\frac{Z_{0}(x_{0}-x)^{2}}{Z_{0}^{2}}\right)$$

- Since suns are enythin products, and los to monotarionly thereising 109 2 Since we physicists trink about minimization (as opposed to mexica entire) - log 2 Since there is an anaring factor of to in exponent, scale - 2 109 2 Lets calculate it; Z (y: -x:) Does not depend on = x2 X' or y, only a constant dependending on precion or apperiment (= -2 log 2 + cont) $\chi^{2} = \frac{1}{2} \frac{(y_{1}^{2} - x_{1}^{2})^{2}}{6!^{2}}$ SMALL X2 => Large Probability Jitz and predicting (*)

FUT LUNDATING @ PD

Xi ~> N! G: 2 -7 N!

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Chapters 1-3

Uncertainties

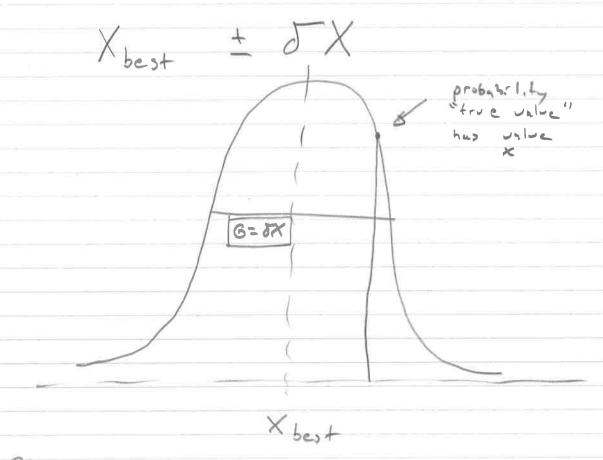
or scientist believe (or inspire) they are parfect (

Error # mintile

Error = Uncertainty

- -> Why are uncertainties useful?
 - -> Report the pracision of the
 - to other presourcesty
 - -> Measurement can be compared to tracery predictions

Gaussin Uncertainties:



Converting

Kbest I JX meins POF

Why?

- 1) CLT. 2) Simple: 2 parameters: men and styres.
 - 3) Math is easy... as we will see, extracting best willy of

- rons

Error Function

Suppose me nevore tre speed of light

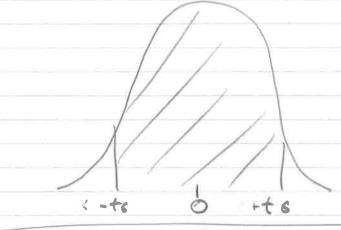
3.3 ± 0.2 × 10 8 m/s

How consistent is this with the generally accepted whe

3,0 × 10 4 ~/s

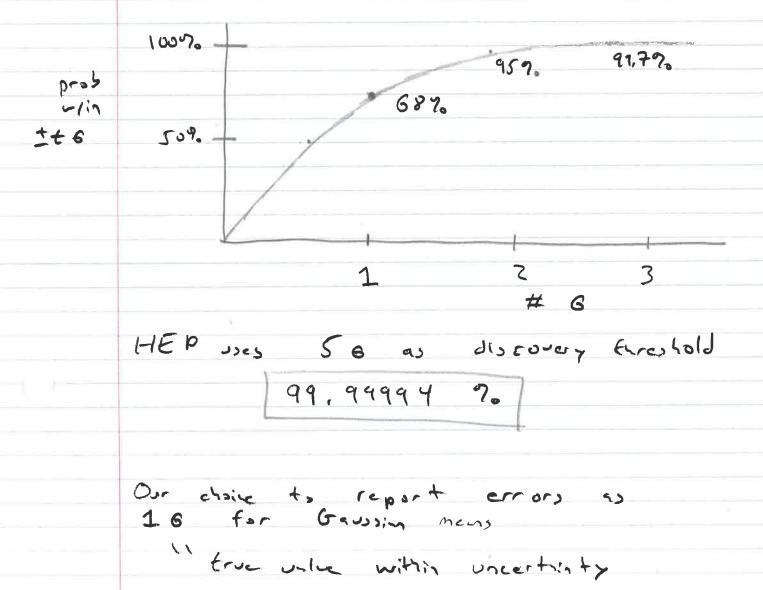
First asser : 3.3 - 3.0 = [1.5 5imn]

But whit if we want to know probility racioned within ± t.6.



$$erf(t) = \frac{1}{\sqrt{2\pi}} \left(-\frac{x^2}{2} \right)$$

No maly the solution, so we just define the function and topshiple it.



6890 OF time "