Week 6: Bike Sharing in Washington D.C.

Using RNN to Build a Time Series Forecasting Model

Part 1: Background Information

Abstract

Bike sharing systems have emerged as a modern solution to traditional bike rentals, automating the rental process and enabling users to conveniently access bicycles from one location and return them to another. With a global presence encompassing over 500 programs and half a million bicycles, these systems play a pivotal role in addressing traffic congestion, environmental sustainability, and public health concerns. Moreover, the data generated by bike sharing systems presents a rich source for research, with detailed records of travel durations and locations offering insights into urban mobility patterns.

In this project, we explore the application of Recurrent Neural Networks (RNNs) for time series forecasting in bike sharing systems. RNNs are well-known for their ability to effectively model sequential data, making them ideal for tasks such as time series prediction. By leveraging RNNs, we aim to develop predictive models that can forecast bike rental demand with high accuracy. Through experimentation and analysis, we seek to demonstrate the effectiveness of RNNs in capturing the complex temporal dynamics of bike sharing data, thereby contributing to the advancement of predictive analytics in urban transportation systems.

Introduction:

Bike sharing systems represent a contemporary evolution of traditional bike rentals, revolutionizing the process by automating membership, rental, and return procedures. These systems enable users to effortlessly rent a bike from one location and return it to another. With over 500 bike-sharing programs worldwide, boasting a collective fleet of more than 500,000 bicycles, these systems have garnered significant attention for their pivotal role in addressing traffic congestion, environmental sustainability, and public health concerns.

Beyond their practical applications, the data generated by bike sharing systems has sparked keen interest among researchers. Unlike other modes of transportation such as buses or subways, bike sharing systems meticulously document travel durations, as well as departure and arrival locations. This unique characteristic transforms bike sharing networks into virtual sensor arrays capable of capturing mobility patterns within urban landscapes. Consequently, analysts anticipate that by monitoring these datasets, it will be possible to detect and analyze crucial urban events, offering insights into city dynamics that were previously inaccessible.

Data Description:

The rental dynamics within bike-sharing systems are intricately tied to environmental and seasonal variables. Factors such as weather conditions, precipitation, day of the week, season, and time of day exert significant influence on rental behaviors.

For this study, we utilized the core dataset comprising a two-year historical log spanning the years 2011 and 2012 from the Capital Bikeshare system in Washington D.C., USA. This dataset is publicly available via the Capital Bikeshare system website at http://capitalbikeshare.com/system-data (http://capitalbikeshare.com/system-data).

In order to comprehensively analyze the rental patterns, we aggregated the data both on a two-hourly and daily basis. Additionally, we enriched the dataset by integrating relevant weather and seasonal information. Weather data was sourced from http://www.freemeteo.com (http://www.freemeteo.com) to augment our analysis and provide contextual insights into the rental trends observed in the Capital Bikeshare system.

Dataset:

The dataset is composed of two .csv files: hours.csv and day.csv. Both hour.csv and day.csv have the following fields, except hr which is not available in day.csv:

• instant: record index

· dteday: date

• season : season (1:springer, 2:summer, 3:fall, 4:winter)

yr : year (0: 2011, 1:2012)mnth : month (1 to 12)hr : hour (0 to 23)

- holiday: weather day is holiday or not (extracted from http://dchr.dc.gov/page/holiday-schedule (<a href="http://dchr.dc.gov/page/holid
- · weekday: day of the week
- workingday: if day is neither weekend nor holiday is 1, otherwise is 0.
- weathersit
 - 1: Clear, Few clouds, Partly cloudy, Partly cloudy
 - 2: Mist + Cloudy, Mist + Broken clouds, Mist + Few clouds, Mist
 - 3: Light Snow, Light Rain + Thunderstorm + Scattered clouds, Light Rain + Scattered clouds
 - 4: Heavy Rain + Ice Pallets + Thunderstorm + Mist, Snow + Fog
- temp: Normalized temperature in Celsius. The values are divided to 41 (max)
- atemp: Normalized feeling temperature in Celsius. The values are divided to 50 (max)
- hum: Normalized humidity. The values are divided to 100 (max)
- windspeed: Normalized wind speed. The values are divided to 67 (max)
- · casual: count of casual users
- · registered: count of registered users
- · cnt: count of total rental bikes including both casual and registered

The dataset is available on Kaggle at: https://www.kaggle.com/code/hozler/time-series-forecasting-with-rnn/input

Project Objective:

The primary objective of this project is to develop predictive models for bike rental count, both hourly and daily, leveraging environmental and seasonal variables. Specifically, we aim to achieve the following tasks:

Regression: Utilize machine learning techniques to predict the bike rental count on an hourly or daily basis, considering factors such as weather conditions, seasonality, and temporal patterns.

Event and Anomaly Detection: Investigate the correlation between bike rental counts and significant events within the town, which can be identified through search engine queries. By validating against known events such as Hurricane Sandy, we aim to develop algorithms for event detection and anomaly identification using the bike sharing dataset.

Through these tasks, we seek to demonstrate the predictive capabilities of machine learning models in capturing the complex dynamics of bike rental behaviors, as well as contribute to the development of event detection algorithms for urban systems.

Evaluation Plan:

1. Evaluation Metrics:

- Mean Absolute Error (MAE): The primary metric to evaluate the predictive accuracy of the models. Lower MAE indicates better
 performance.
- MAE/Mean Ratio: Provides insight into the relative error compared to the mean value of the target variable. A lower ratio signifies better
 performance.
- Correctness: Complementary metric derived from MAE/Mean Ratio, representing the percentage of correctness. Higher correctness indicates better performance.

2. Data Split:

- Training Data: Historical bike sharing data spanning a defined period (e.g., 2011-2012) used for model training.
- Validation Data: A portion of the dataset reserved for tuning hyperparameters and evaluating model performance during training.
- Hold-Out Data: A separate subset of data not used during model training or validation, reserved for final model evaluation to assess real-world performance.

3. Evaluation Procedure:

1. Data Preprocessing:

- Standardize features: Normalize numerical features to a common scale.
- · Handle missing values: Impute or remove missing values appropriately.
- · Feature engineering: Create new features if necessary, such as time-based features or weather interactions.

2. Model Training:

- Train multiple models, including Model 1, Model 2, and Model 3, using appropriate algorithms (e.g., RNNs).
- Tune hyperparameters using the validation data to optimize model performance.

3. Model Evaluation:

- Evaluate each model's performance using the validation data based on the defined evaluation metrics.
- Select the best-performing model based on MAE, MAE/Mean Ratio, and Correctness metrics.

4. Final Model Selection:

- · Validate the selected model using the hold-out data to ensure generalization and real-world performance.
- · Compare the model's performance on the hold-out data with validation results to confirm consistency.

5. Performance Analysis:

- · Analyze the predictive accuracy and correctness of the selected model compared to other models.
- Investigate the reasons behind the superior performance of the selected model, considering factors such as architecture, hyperparameters, and feature engineering.

4. Reporting and Documentation:

- Final Report: Summarize the evaluation process, including data preprocessing, model training, and evaluation. Present detailed results of each model's performance based on MAE, MAE/Mean Ratio, and Correctness metrics. Provide insights into the reasons for the selected model's superiority and its implications for the project objectives.
- Documentation: Document all data preprocessing steps, hyperparameters, and model configurations for reproducibility. Include visualizations, tables, and figures to illustrate key findings and comparisons.

5. Continuous Improvement:

- Model Refinement: Periodically retrain the selected model with updated data to maintain relevance and accuracy. Explore advanced techniques or alternative algorithms to further improve model performance.
- Feedback Mechanism: Establish a feedback mechanism to gather insights from stakeholders and end-users for model refinement and future iterations.

Acknowledgments:

This dataset was created by Haid Fanaee-T and Joao Gama for their paper Event labeling combining ensemble detectors and background knowledge.

Fanaee-T, Hadi, and Gama, Joao, "Event labeling combining ensemble detectors and background knowledge", Progress in Artificial Intelligence (2013): pp. 1-15, Springer Berlin Heidelberg, doi:10.1007/s13748-013-0040-3.

Available at: https://www.kaggle.com/code/hozler/time-series-forecasting-with-rnn/input (https://www.kaggle.com/code/hozler/time-series-forecasting-with-rnn/input)

Importing the necessary libraries

```
import pandas as pd
             import numpy as np
             import seaborn as sns
             import matplotlib.pyplot as plt
             import os
             #From numpy
             from numpy import array, hstack
             #From pandas
             from pandas.plotting import lag_plot
             #From sklearn
             from sklearn.preprocessing import MinMaxScaler
             from sklearn.model_selection import GridSearchCV
             #From keras
             from keras.models import Sequential
             from keras.layers import Dense, GRU, LSTM, RNN, SimpleRNN
             from keras.preprocessing.sequence import TimeseriesGenerator
             from keras.layers import Dropout
             from keras.optimizers import Adam
             from keras.layers.core import Activation
             from keras.callbacks import LambdaCallback
             from tensorflow.keras.wrappers.scikit_learn import KerasRegressor
             #From tensorflow
             from tensorflow.keras.models import Sequential
             from tensorflow.keras.layers import LSTM, Dense
             from tensorflow.keras.layers import Dropout
             from tensorflow.keras.optimizers import Adam
```

Reading the dataset

Project Summary

Project Summary:

The project focuses on time series forecasting using Recurrent Neural Networks (RNNs), specifically exploring the effectiveness of different RNN architectures including Simple RNNs, Gated Recurrent Units (GRUs), and Long Short-Term Memory (LSTM) networks. By capitalizing on the inherent sequential data processing capabilities of RNNs, the objective is to develop robust models capable of accurately predicting future trends in time series data. This comprehensive approach involves various stages such as data preprocessing, feature engineering, model architecture design, hyperparameter tuning, model training, and performance evaluation against established metrics.

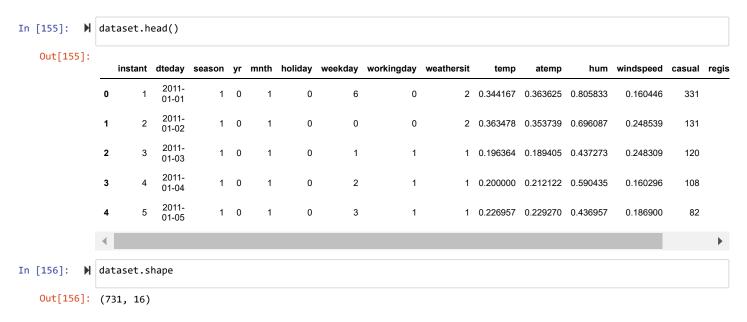
The dataset used in the project comprises historical records spanning multiple temporal dimensions, allowing for the exploration of complex temporal patterns and dependencies. Through rigorous experimentation and analysis, the project aims to uncover insights into the strengths and weaknesses of different RNN architectures in handling diverse time series forecasting tasks.

Additionally, the project extends beyond basic model development to encompass advanced techniques such as sensitivity analysis and model comparison. By systematically varying input parameters and evaluating model performance across different scenarios, the project seeks to provide a comprehensive understanding of the robustness and sensitivity of each RNN architecture. Furthermore, comparing the performance of Simple RNNs, GRUs, and LSTMs allows for insightful observations regarding the impact of architectural complexities on predictive accuracy and computational efficiency.

Overall, the project aspires to contribute to the advancement of predictive analytics across various domains including finance, weather

Part II: Exploratatory Data Analysis

About the Data



Summary Statistics

max

Thw following code will generate summary statistics including count, mean, standard deviation, minimum, 25th percentile (Q1), median (50th percentile or Q2), 75th percentile (Q3), and maximum for each numerical variable in your dataset. It will provide insights into the central tendency and variability of your data.

```
In [157]:
           ▶ # Calculate summary statistics for numerical variables
               summary_stats = dataset.describe()
               # Print the summary statistics
              print(summary_stats)
                         instant
                                       season
                                                                   mnth
                                                                            holiday
                                                                                         weekday
                      731.000000
                                               731.000000
                                                                                      731.000000
               count
                                  731.000000
                                                            731,000000
                                                                         731.000000
                      366.000000
                                     2.496580
                                                  0.500684
                                                              6.519836
                                                                           0.028728
                                                                                        2.997264
               mean
               std
                      211.165812
                                     1.110807
                                                  0.500342
                                                              3.451913
                                                                           0.167155
                                                                                        2.004787
                        1.000000
                                                  0.000000
                                                              1.000000
                                                                           0.000000
                                                                                        0.000000
                                     1.000000
               min
               25%
                      183.500000
                                     2.000000
                                                  0.000000
                                                              4.000000
                                                                           0.000000
                                                                                        1.000000
               50%
                      366.000000
                                     3.000000
                                                  1.000000
                                                              7.000000
                                                                           0.000000
                                                                                        3.000000
               75%
                      548.500000
                                     3.000000
                                                  1.000000
                                                             10.000000
                                                                           0.000000
                                                                                        5.000000
               max
                      731.000000
                                     4.000000
                                                  1.000000
                                                             12.000000
                                                                           1.000000
                                                                                        6.000000
                      workingday
                                   weathersit
                                                      temp
                                                                  atemp
                                                                                hum
                                                                                       windspeed
                      731.000000
                                  731.000000
                                               731.000000
                                                            731.000000
                                                                         731.000000
                                                                                      731,000000
               count
                        0.683995
                                     1.395349
                                                  0.495385
                                                              0.474354
                                                                           0.627894
                                                                                        0.190486
               mean
               std
                        0.465233
                                     0.544894
                                                  0.183051
                                                              0.162961
                                                                           0.142429
                                                                                        0.077498
               min
                        0.000000
                                     1.000000
                                                  0.059130
                                                              0.079070
                                                                           0.000000
                                                                                        0.022392
               25%
                        0.000000
                                     1.000000
                                                  0.337083
                                                              0.337842
                                                                           0.520000
                                                                                        0.134950
               50%
                        1.000000
                                     1.000000
                                                  0.498333
                                                              0.486733
                                                                                        0.180975
                                                                           0.626667
               75%
                        1.000000
                                     2.000000
                                                  0.655417
                                                              0.608602
                                                                           0.730209
                                                                                        0.233214
                        1.000000
                                     3.000000
                                                              0.840896
               max
                                                  0.861667
                                                                           0.972500
                                                                                        0.507463
                           casual
                                     registered
                       731.000000
                                                   731.000000
                                     731.000000
               count
               mean
                       848.176471
                                    3656.172367
                                                  4504.348837
                                                  1937.211452
               std
                       686,622488
                                    1560.256377
               min
                         2.000000
                                      20.000000
                                                    22,000000
               25%
                       315.500000
                                    2497.000000
                                                  3152.000000
               50%
                       713.000000
                                    3662.000000
                                                  4548.000000
               75%
                      1096.000000
                                    4776.500000
                                                 5956.000000
                      3410.000000
                                    6946.000000
                                                 8714.000000
```

- Count: There are 731 observations in the dataset for each variable, indicating that there are no missing values.
- Mean: The mean value represents the average value of each variable across all observations.
- Standard Deviation (Std): The standard deviation measures the dispersion or variability of the values from the mean. It indicates how spread out the values are.
- Minimum (Min): The minimum value is the smallest observed value for each variable.
- 25th Percentile (Q1): The 25th percentile (Q1) represents the value below which 25% of the observations fall.
- Median (50th Percentile or Q2): The median is the middle value of the dataset when it is ordered from least to greatest. It separates the higher half from the lower half of the data.
- 75th Percentile (Q3): The 75th percentile (Q3) represents the value below which 75% of the observations fall.
- Maximum (Max): The maximum value is the largest observed value for each variable.

Checking for Missing Values

```
missing_values = dataset.isnull().sum()
           # Print the number of missing values for each column
            print("Missing Values:")
            print(missing_values)
           Missing Values:
            instant
            dteday
            season
                        0
                        0
            yr
            mnth
                        0
           holiday
                        0
            weekday
                        0
            workingday
                        0
```

cnt
dtype: int64

weathersit

temp

hum windspeed

atemp

casual registered

0

0

0

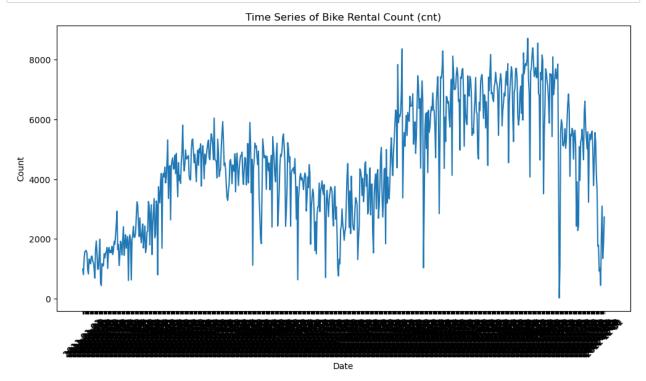
0 0

0

0

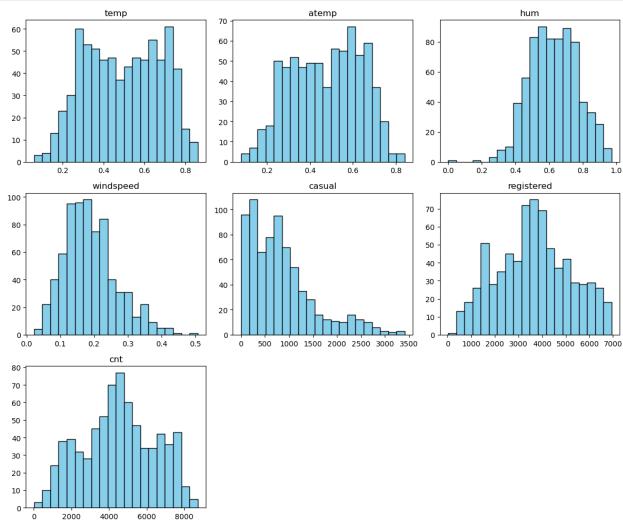
Time Series Plot

```
In [159]: # Time Series Plot
    plt.figure(figsize=(12, 6))
    plt.plot(dataset['dteday'], dataset['cnt'])
    plt.title('Time Series of Bike Rental Count (cnt)')
    plt.xlabel('Date')
    plt.ylabel('Count')
    plt.xticks(rotation=45)
    plt.show()
```



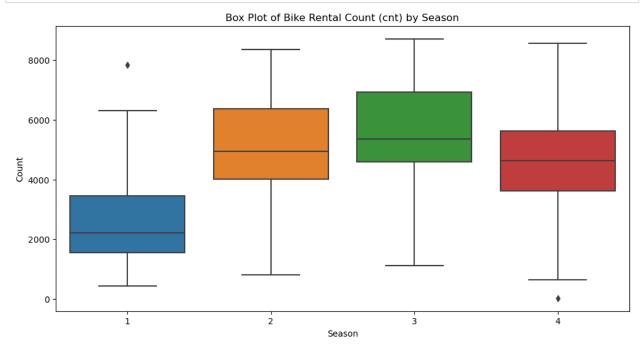
Distribution Plots

```
In [160]:  # Histograms
    numerical_vars = ['temp', 'atemp', 'hum', 'windspeed', 'casual', 'registered', 'cnt']
    plt.figure(figsize=(12, 10))
    for i, var in enumerate(numerical_vars):
        plt.subplot(3, 3, i + 1)
        plt.hist(dataset[var], bins=20, color='skyblue', edgecolor='black')
        plt.title(var)
    plt.tight_layout()
    plt.show()
```



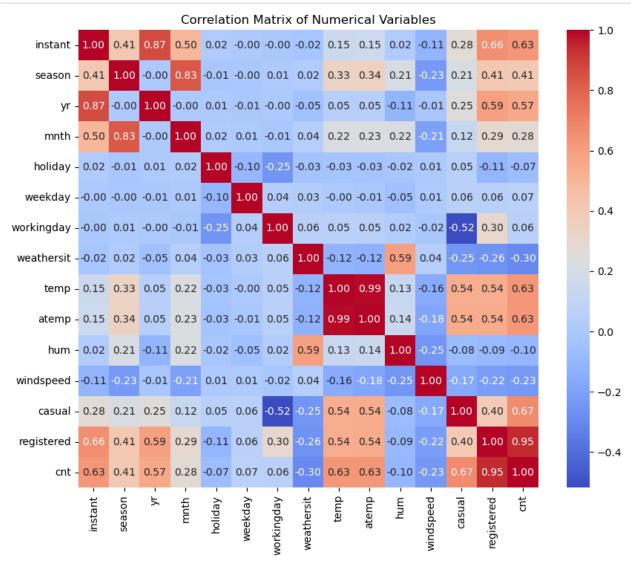
Box Plots

```
In [161]:  # Box Plots
    plt.figure(figsize=(12, 6))
    sns.boxplot(x='season', y='cnt', data=dataset)
    plt.title('Box Plot of Bike Rental Count (cnt) by Season')
    plt.xlabel('Season')
    plt.ylabel('Count')
    plt.show()
```



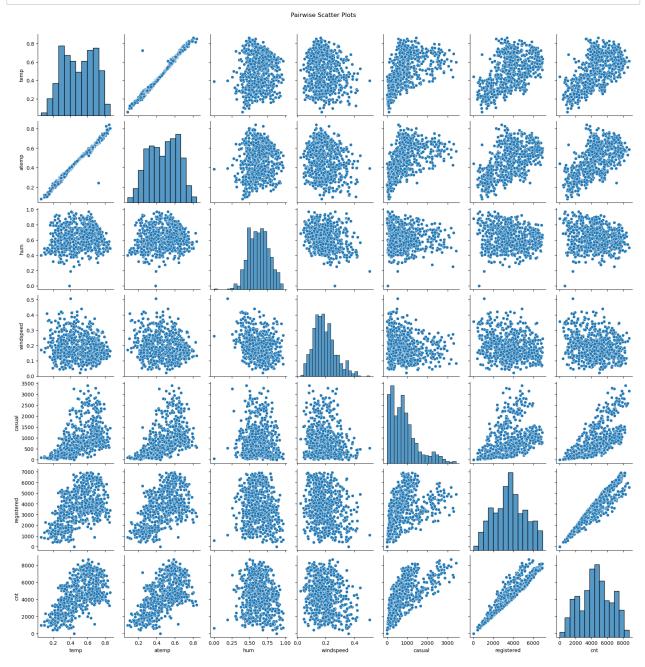
Correlation Matrix

```
In [162]: # Correlation Matrix
    plt.figure(figsize=(10, 8))
    correlation_matrix = dataset.corr()
    sns.heatmap(correlation_matrix, annot=True, cmap='coolwarm', fmt=".2f")
    plt.title('Correlation Matrix of Numerical Variables')
    plt.show()
```

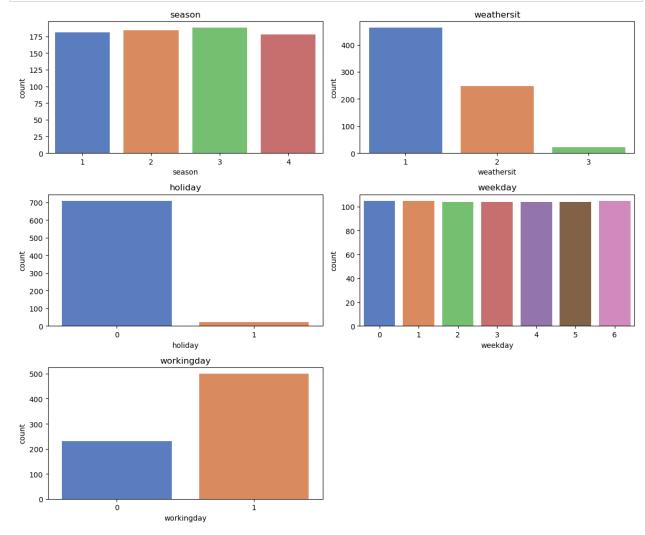


Scatter Plots

```
In [163]: # Scatter Plots
sns.pairplot(dataset[['temp', 'atemp', 'hum', 'windspeed', 'casual', 'registered', 'cnt']])
plt.suptitle('Pairwise Scatter Plots', y=1.02)
plt.show()
```



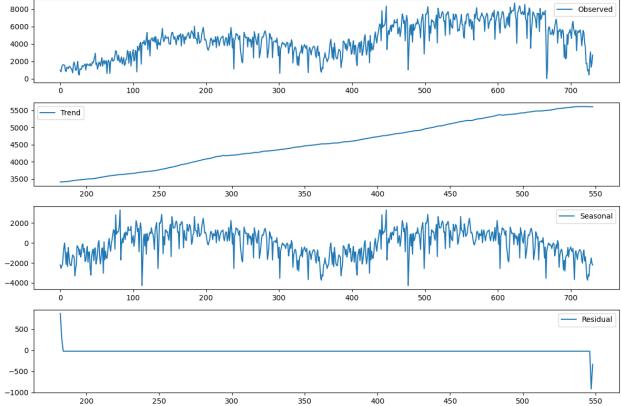
Bar Plots



Seasonal Decomposition Plots

- First, convert the 'dteday' column to datetime type and set it as the index of the DataFrame to facilitate time series analysis.
- Then, use the seasonal_decompose function from the statsmodels library to decompose the time series into its trend, seasonal, and residual components. We specify the model as 'additive' and set the period parameter to 365 for yearly seasonality.
- · Finally, we plot the observed time series, trend, seasonal, and residual components using matplotlib.

```
In [165]:
             # Convert 'dteday' column to datetime type
              dataset['dteday'] = pd.to_datetime(dataset['dteday'])
              # Perform seasonal decomposition
              decomposition = sm.tsa.seasonal_decompose(dataset['cnt'], model='additive', period=365)
              # Plot the decomposition
              plt.figure(figsize=(12, 8))
              plt.subplot(4, 1, 1)
              plt.plot(decomposition.observed, label='Observed')
              plt.legend()
              plt.subplot(4, 1, 2)
              plt.plot(decomposition.trend, label='Trend')
              plt.legend()
              plt.subplot(4, 1, 3)
              plt.plot(decomposition.seasonal, label='Seasonal')
              plt.legend()
              plt.subplot(4, 1, 4)
              plt.plot(decomposition.resid, label='Residual')
              plt.legend()
              plt.tight_layout()
              plt.show()
```



Lag Plots

- First, the target variable is specified to create lag plots (e.g., 'cnt').
- Lag plots are created for the target variable using a loop over different lag values.

```
In [166]:
                # Select the target variable for which you want to create lag plots (e.g., 'cnt')
                target_variable = 'cnt'
                # Create lag plots for the target variable
                plt.figure(figsize=(12, 6))
                for lag in range(1, 6): # You can adjust the range of lags as needed
                     ax = plt.subplot(2, 3, lag)
                     lag_plot(dataset[target_variable], lag=lag)
                     ax.set_title(f'Lag {lag}')
                plt.tight_layout()
                plt.show()
                                                                                 Lag 2
                                       Lag 1
                                                                                                                            Lag 3
                    8000
                                                              8000
                                                                                                         8000
                    6000
                                                              6000
                                                                                                         6000
                 y(t + 1)
                                                                                                      8
                                                                                                      y(t + 3
                    4000
                                                              4000
                                                                                                         4000
                   2000
                                                              2000
                                                                                                         2000
                                             6000
                                                    8000
                                                                                        6000
                                                                                               8000
                               2000
                                                                          2000
                                                                                 4000
                                                                                                                    2000
                                                                                                                                  6000
                                                                                                                                         8000
                                      4000
                                                                                                                           4000
                                        y(t)
                                                                                   y(t)
                                                                                                                             y(t)
                                                                                 Lag 5
                                       Lag 4
                    8000
                                                              8000
                    6000
                                                              6000
                 y(t + 4)
                   4000
                                                              4000
                   2000
                                                              2000
                                      4000
                                             6000
                                                    8000
                                                                                 4000
```

Part III: Data Preprocessing

Transforming Certain Features into Categorical Data

y(t)

One Hot Encoding willbe applied for categorical features. In this case weekday, weathersit and mnth features categorical in nature and should have One Hot Encoding applied.

y(t)

```
In [170]:

▶ dataset.head()

    Out[170]:
                    instant dteday
                                    season yr mnth holiday weekday workingday weathersit
                                                                                                   temp ... mnth_3 mnth_4 mnth_5 mnth_6 mnth_
                             2011-
                 0
                                         1
                                            0
                                                            0
                                                                     6
                                                                                 0
                                                                                            2 0.344167
                                                                                                                  0
                                                                                                                          0
                                                                                                                                   0
                                                                                                                                           0
                             01-01
                             2011-
                 1
                         2
                                             0
                                                            0
                                                                     0
                                                                                 0
                                                                                            2 0.363478 ...
                                                                                                                  0
                                                                                                                          0
                                                                                                                                   0
                                                                                                                                           0
                             01-02
                              2011-
                                                                                            1 0.196364 ...
                 2
                         3
                                            0
                                                            0
                                                                                 1
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                              2011-
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                                                                                                                                   0
                                                                                                                                           0
                             01 - 04
                              2011-
                                                                                                                                           0
                                                            0
                                                                     3
                                                                                            1 0.226957 ...
                                                                                                                  0
                                                                                                                          0
                                                                                                                                   0
                         5
                                         1 0
                                                                                 1
                             01-05
                5 rows × 38 columns
                                                                                                                                                 •
```

Applying Scaling to the Data

It appears as though all of the features have previously been scaled by the authors, save for the feature cnt, which happens to by our Y value. Therefore, we will only apply scaling to this feature.

```
In [171]:

■ scaler = MinMaxScaler(feature_range=(0, 1))

               scaled = scaler.fit_transform(array(dataset['cnt']).reshape(len(dataset['cnt']), 1))
               series = pd.DataFrame(scaled)
               series.columns = ['cntscl']
In [172]:
            ▶ series.head()
   Out[172]:
                     cntscl
                0.110792
                1 0.089623
                2 0.152669
                3 0.177174
                4 0.181546

    dataset = pd.merge(dataset, series, left_index=True, right_index=True)

In [173]:
In [174]:

▶ dataset.head()

   Out[174]:
               mnth holiday
                            weekday workingday weathersit
                                                              temp ... mnth_4 mnth_5 mnth_6 mnth_7 mnth_8 mnth_9
                                                                                                                     mnth_10 mnth_11 r
                          0
                                   6
                                              0
                                                        2 0.344167
                                                                            0
                                                                                   0
                                                                                           0
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                                                        2 0.363478
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                                              1
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                                                                                                                           0
                                                                                                                                    0
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                                                        1 0.200000 ...
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                                                                                                          0
                                                                                                                           0
                                                                                                                                    0
                          0
                                   3
                                                                            0
                                                                                   0
                                                                                           0
                                                                                                   0
                                                                                                          0
                                                                                                                           0
                                                                                                                                    0
                                                        1 0.226957 ...
```

Splitting the Data

To properly split the data, we will apply the following four steps:

- 1) set the number of train (total (test+train), test (50) and holdout (50) values
- 2) create new variable names containing the proper number of samples
- 3) create the target variables dataset based on its corresponding sample
- 4) drop the target variable column from the train, test and hold samples (NOTE: for simplicity, this step will be done after we prepare 3-D

```
In [230]: 

# Splitting the Data: Step 1
              number_of_test_data = 50
             number_of_holdout_data = 50
             number_of_training_data = len(dataset) - number_of_holdout_data - number_of_test_data
              print ("total, train, test, holdout:", len(dataset), number_of_training_data, number_of_test_data, number_of_h
              total, train, test, holdout: 731 631 50 50
In [231]: ▶ # Splitting the Data: Step 2
             datatrain = dataset[:number of training data]
             datatest = dataset[-(number_of_test_data+number_of_holdout_data):-number_of_holdout_data]
             datahold = dataset[-number_of_holdout_data:]
In [232]: ▶ # Splitting the Data: Step 3
             y_train = datatrain['cntscl']
             y_test = datatest['cntscl']
             y_hold = datahold['cntscl']
In [233]: ▶ # Splitting the Data: Step 4
             datatrain = datatrain.drop(columns=['cntscl'])
             datatest = datatest.drop(columns=['cntscl'])
             datahold = datahold.drop(columns=['cntscl'])
```

Preparing 3-Dimensional Input for Sequential Model

Preparing input for a sequential model by using TimeSeriesGenerator. The following code iterates over the list of features and performs reshaping operations within the loop.

```
In [234]: ▶ # Preparing Input for Sequential Model
               n_{input} = 10
               features = ['holiday', 'workingday', 'temp', 'atemp', 'hum', 'windspeed',
                            weekday_0', 'weekday_1', 'weekday_2', 'weekday_3', 'weekday_4', 'weekday_5', 'weekday_6',
                            'weathersit_1', 'weathersit_2', 'weathersit_3']
               input_seqs_train = []
               input_seqs_test = []
               input_seqs_hold = []
               for feature in features:
                   reshaped_feature_train = datatrain[feature].values.reshape((len(datatrain), 1))
                   reshaped_feature_test = datatest[feature].values.reshape((len(datatest), 1))
                   reshaped_feature_hold = datahold[feature].values.reshape((len(datahold), 1))
                   input_seqs_train.append(reshaped_feature_train)
                   input_seqs_test.append(reshaped_feature_test)
                   input_seqs_hold.append(reshaped_feature_hold)
               datatrain feed = np.hstack(input segs train)
               datatest_feed = np.hstack(input_seqs_test)
               datahold_feed = np.hstack(input_seqs_hold)
               # Ensure y_train has the same length as datatrain
              y train = y train[:len(datatrain)]
               # Initialize TimeseriesGenerator for training, testing, and holdout sets
               batch_size_train = 1 # Adjust this value as needed
              batch_size_test = 1  # Adjust this value as needed
               batch_size_hold = 1  # Adjust this value as needed
               generator_train = TimeseriesGenerator(datatrain_feed, y_train, length=n_input, batch_size=batch_size_train)
               generator_test = TimeseriesGenerator(datatest_feed, y_test, length=n_input, batch_size=batch_size_test)
              generator_hold = TimeseriesGenerator(datahold_feed, y_hold, length=n_input, batch_size=batch_size_hold)
               # Truncate y_train to match the length of generator_train
              y_train = y_train[:len(generator_train)]
              y_test = y_train[:len(generator_test)]
              y_hold = y_train[:len(generator_hold)]
               Length of y_train: 621
               Length of y_test: 40
               Length of y_hold: 40
               Length of generator_train: 621
               Length of generator_test: 40
               Length of generator_hold: 40
In [235]: ▶ # Print Lengths
               print("Length of y_train:", len(y_train))
              print("Length of y_test:", len(y_test))
              print("Length of y_hold:", len(y_hold))
              print("Length of generator_train:", len(generator_train))
print("Length of generator_test:", len(generator_test))
print("Length of generator_hold:", len(generator_hold))
               Length of y_train: 621
               Length of y_test: 40
               Length of y_hold: 40
               Length of generator_train: 621
               Length of generator_test: 40
               Length of generator hold: 40
```

Part IV: Building and Training Simple RNN model

We will now create a small RNN with 4 nodes. Number of total parameters in the model is 93. Number of timesteps in one batch is 10. Activation function is relu both for RNN and Output layer. Optimizer is adam. Loss function is mean squared error. Learning rate is 0.0001. Number of epocs is 3,000.

Creating the Model

In [33]: ▶ model.summary()

Model: "sequential"

Layer (type)
Output Shape
Param #
simple_rnn (SimpleRNN) (None, 4)

dense (Dense) (None, 1)

5

Total params: 89 Trainable params: 89 Non-trainable params: 0

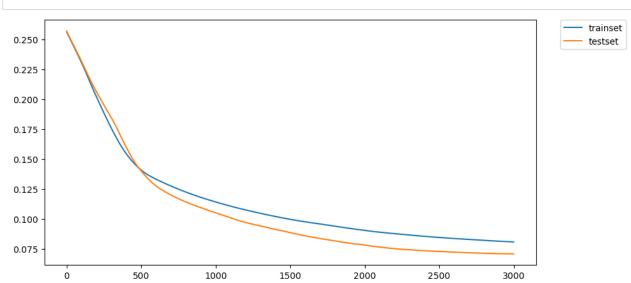
Training the Model

In [35]: ▶ score = model.fit_generator(generator_train, epochs=3000, verbose=0, validation_data=generator_test)

C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\1338044232.py:1: UserWarning: `Model.fit_generator` is depr ecated and will be removed in a future version. Please use `Model.fit`, which supports generators. score = model.fit_generator(generator_train, epochs=3000, verbose=0, validation_data=generator_test)

Plot of Training and Test Loss Functions

```
In [36]: N
losses = score.history['loss']
val_losses = score.history['val_loss']
plt.figure(figsize=(10,5))
plt.plot(losses, label="trainset")
plt.plot(val_losses, label="testset")
plt.legend(bbox_to_anchor=(1.05, 1), loc=2, borderaxespad=0.)
plt.show()
```



Predictions for Test Data

```
In [57]: ▶ # Predicting for Test Data
            df_result = pd.DataFrame({'Actual': [], 'Prediction': []})
             for i in range(len(generator_test)):
                x, y = generator_test[i]
                x_input = array(x).reshape((1, n_input, n_features))
                yhat = model.predict(x_input, verbose=2)
                # Inverse transform the scaled target values to their original scale
                actual = scaler.inverse_transform(y.reshape(-1, 1))[0][0]
                prediction = scaler.inverse\_transform(yhat.reshape(-1, 1))[0][0]
                df_result = df_result.append({'Actual': actual, 'Prediction': prediction}, ignore_index=True)
            # Display the results
            print(df_result)
             2/ 5923.154/98 5416.11/6/6
            28 2116.803704 5651.955566
            29 6059.796630 3977.350342
             30 4965.051879 3103.239502
            31 751.609809 4303.803711
             32 3521.631447 3060.876709
            33 5831.070164 3863.071777
            34 2830.350504 4241.522461
             35 701.774752 4152.302246
            36 3777.680203 4223.648926
             37
                 811.816748 3457.753418
             38 4745.583842 4638.375977
            39 1451.312076 4290.109375
            C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2465833379.py:13: FutureWarning: The frame.append method
            is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result = df_result.append({'Actual': actual, 'Prediction': prediction}, ignore_index=True)
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2465833379.py:13: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result = df_result.append({'Actual': actual, 'Prediction': prediction}, ignore_index=True)
```

Tabulating Actuals, Predictions and Differences

```
In [58]: M df_result['Diff'] = 100 * (df_result['Prediction'] - df_result['Actual']) / df_result['Actual']
```

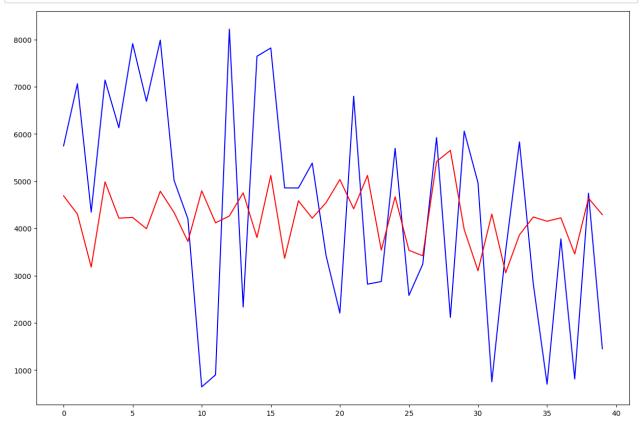
In [59]: ► df_result

Out[59]:

	Actual	Prediction	Diff
0	5747.700363	4689.526367	-18.410389
1	7062.688266	4303.365234	-39.069019
2	4344.591062	3180.356201	-26.797341
3	7140.891501	4986.168945	-30.174419
4	6131.928586	4217.518555	-31.220358
5	7912.312059	4231.909668	-46.514879
6	6691.261626	3993.219971	-40.321868
7	7985.740997	4787.211914	-40.053003
8	5015.049197	4337.256836	-13.515169
9	4202.067943	3722.940674	-11.402178
10	644.751835	4795.160156	643.721831
11	899.480194	4117.308105	357.743053
12	8219.107814	4263.191895	-48.130722
13	2335.952194	4753.149414	103.478026
14	7645.490248	3806.860596	-50.207763
15	7819.662325	5121.740234	-34.501772
16	4857.324591	3366.904785	-30.683966
17	4855.510698	4584.152832	-5.588658
18	5383.215834	4216.047852	-21.681612
19	3426.729103	4545.614258	32.651696
20	2208.090023	5034.458984	128.000622
21	6797.785140	4414.158691	-35.064751
22	2819.375201	5121.942383	81.669413
23	2875.522578	3539.791504	23.100807
24	5695.967169	4669.700684	-18.017423
25	2581.427003	3536.294678	36.989916
26	3242.468071	3420.623535	5.494440
27	5923.154798	5416.117676	-8.560254
28	2116.803704	5651.955566	167.004236
29	6059.796630	3977.350342	-34.364953
30	4965.051879	3103.239502	-37.498347
31	751.609809	4303.803711	472.611435
32	3521.631447	3060.876709	-13.083559
33	5831.070164	3863.071777	-33.750209
34	2830.350504	4241.522461	49.858558
35	701.774752	4152.302246	491.685898
36	3777.680203	4223.648926	11.805359
37	811.816748	3457.753418	325.927825
38	4745.583842	4638.375977	-2.259108
39	1451.312076	4290.109375	195.602128

Calculating the Correctness for Test Data

Plot of Actuals and Predictions for Test Data



Observations

Model 1 (Simple RNN) Train Data Statistics:

- MAE: 1982.84
- MAE/Mean Ratio: 44.55%
- Correctness: 55.45%

The red line (prediction of test data) on the predictions plot actually appears less volatile than the blue line (actual), which could mean that we are losing the seasonality component of the time series. We can see that with a correctness score of just 55%, this model is probably not functioning as optimally as it could.

Predictions for Hold-Out Data

```
In [61]: ▶ # Predictions for Hold-Out Data
             df_result = pd.DataFrame({'Actual' : [], 'Prediction' : []})
             for i in range(len(generator_hold)):
                 x, y = generator_hold[i]
                 x_input = array(x).reshape((1, n_input, n_features))
                 yhat = model.predict(x_input, verbose=2)
                 # Reshape y to 2D array if it's 1D
                 if len(y.shape) == 1:
                     y = y.reshape(-1, 1)
                 # Reshape yhat to 2D array if it's 1D
                 if len(yhat.shape) == 1:
                     yhat = yhat.reshape(-1, 1)
                 # Inverse transform the scaled target values to their original scale
                 actual = scaler.inverse transform(y)[0][0]
                 prediction = scaler.inverse_transform(yhat)[0][0]
                 df_result = df_result.append({'Actual': actual, 'Prediction': prediction}, ignore_index=True)
             1/1 - 0s - 24ms/epoch - 24ms/step
             1/1 - 0s - 22ms/epoch - 22ms/step
             1/1 - 0s - 25ms/epoch - 25ms/step
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2791513956.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result = df_result.append({'Actual': actual, 'Prediction': prediction}, ignore_index=True)
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2791513956.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result = df_result.append({'Actual': actual, 'Prediction': prediction}, ignore_index=True)
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2791513956.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result = df_result.append({'Actual': actual, 'Prediction': prediction}, ignore_index=True)
             1/1 - 0s - 29ms/epoch - 29ms/step
             1/1 - 0s - 25ms/epoch - 25ms/step
             1/1 - 0s - 34ms/epoch - 34ms/step
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2791513956.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
```

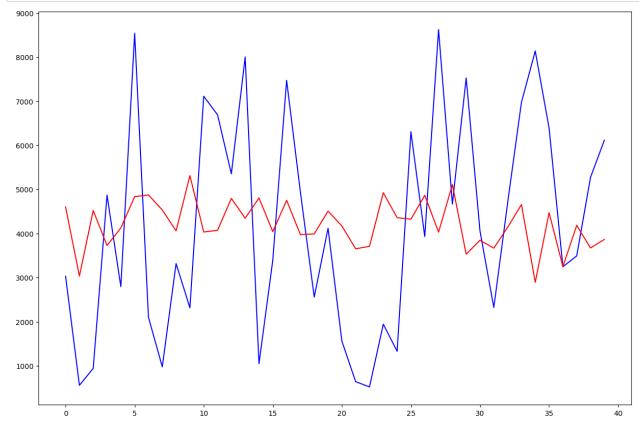
Tabulating Actuals, Predictions and Differences for Hold-Out Data

Out[62]:

	Actual	Prediction	Diff
0	3031.632502	4603.979004	51.864680
1	557.736274	3035.659668	444.282272
2	941.392674	4522.917969	380.449667
3	4873.155902	3729.394531	-23.470650
4	2797.711835	4127.327637	47.525116
5	8543.326365	4837.718262	-43.374301
6	2101.122616	4875.093750	132.023287
7	976.422904	4535.048340	364.455342
8	3318.467790	4061.083984	22.378285
9	2315.290270	5315.419434	129.578965
10	7114.650952	4035.322021	-43.281518
11	6694.469069	4072.714355	-39.162997
12	5355.566661	4797.842773	-10.413910
13	8004.981553	4346.573242	-45.701646
14	1048.273425	4807.707031	358.631013
15	3397.319630	4042.985107	19.005144
16	7475.350299	4753.871094	-36.406042
17	4937.293928	3975.796387	-19.474181
18	2560.269101	3992.083496	55.924371
19	4120.945793	4509.436523	9.427223
20	1559.693308	4171.667969	167.467197
21	639.915284	3654.338379	471.065963
22	520.950104	3710.507568	612.257765
23	1944.917049	4925.457520	153.247691
24	1327.880375	4360.150879	228.354192
25	6308.385150	4325.540527	-31.431889
26	3931.703909	4867.803711	23.809011
27	8626.042641	4031.779053	-53.260386
28	4670.567860	5111.006836	9.430095
29	7528.444553	3531.629150	-53.089524
30	4054.759589	3847.758057	-5.105149
31	2323.295978	3668.436768	57.897952
32	4694.935671	4141.073242	-11.797018
33	6978.060568	4658.645020	-33.238685
34	8141.866331	2894.030029	-64.454955
35	6392.913456	4473.832031	-30.018886
36	3247.792461	3250.342529	0.078517
37	3492.756772	4185.858398	19.843971
38	5273.871623	3673.551514	-30.344313
39	6117.423293	3867.126709	-36.785040

Calculating the Correctness for Hold-Out Data

Plot of Actuals and Predictions for Hold-Out Data



Observations

Model 1 (Simple RNN) Holdout Data Statistics:

- Mean Absolute Error (MAE): 2165.74
- MAE/Mean ratio: 51.58%
- Correctness: 48.42%

The red line (prediction of test data) on the predictions plot actually appears less volatile than the blue line (actual), which could mean that we are losing the seasonality component of the time series. We can see that with a correctness score of just 48%, this model is probably not functioning as optimally as it could.

Model 1 Overall Observations

Mean Absolute Error (MAE):

Value: 1982.84

Explanation: The Mean Absolute Error (MAE) measures the average absolute difference between the actual and predicted values. In the context of Model 1, an MAE of 1982.84 indicates that, on average, the predictions made by the Simple RNN model deviate from the actual values by approximately 1982.84 units. Lower values of MAE indicate better predictive performance, as they signify smaller errors between predictions and actual observations.

MAE/Mean Ratio:

Value: 44.55%

Explanation: The MAE/Mean Ratio, also known as the Mean Absolute Percentage Error (MAPE), expresses the MAE as a percentage of the mean of the actual values. In Model 1, a ratio of 44.55% suggests that the average absolute error in predictions, relative to the mean of the actual values, is approximately 44.55%. This metric provides a normalized measure of prediction accuracy, allowing for comparisons across different datasets and models. Lower values indicate higher accuracy, as they represent smaller relative errors.

Correctness:

Value: 55.45%

Explanation: The Correctness metric represents the proportion of predictions that are considered correct, typically based on a predefined threshold or criterion. In Model 1, a correctness of 55.45% indicates that approximately 55.45% of the predictions made by the Simple RNN model align with the actual observations. This metric provides a binary assessment of prediction accuracy, where higher values indicate a higher proportion of accurate predictions.

In summary, these evaluation metrics provide insights into the predictive performance of Model 1 based on its ability to minimize absolute errors, maintain low relative errors, and achieve correctness in its predictions.

Part V: Building and Training a GRU (Gated Recurrent Unit) Model

Key features of GRU include:

Gating Mechanism: GRU incorporates gating mechanisms similar to Long Short-Term Memory (LSTM) networks, which allow it to selectively update and forget information over time. However, GRU has a simpler architecture compared to LSTM, with two gates: the update gate and the reset gate.

Update Gate: The update gate determines how much of the past information should be carried forward to the current time step. It takes into account the current input and the previous hidden state and outputs a value between 0 and 1, indicating the proportion of information to retain.

Reset Gate: The reset gate controls how much of the past information should be forgotten when computing the current hidden state. It helps the model adaptively reset its memory based on the current input.

Efficiency: GRU has fewer parameters compared to LSTM, making it computationally more efficient and faster to train. This can be advantageous, especially when dealing with large datasets or complex models.

Overall, GRU networks have shown promising performance in various sequential data tasks and have become a popular choice alongside LSTM networks in many deep learning applications.

Creating the Model

```
In [66]: ▶ # Create the GRU model
             model_gru = Sequential()
             # Add a GRU layer with 4 units and 'relu' activation function
             model_gru.add(GRU(4, activation='relu', input_shape=(n_input, n_features)))
             # Add a Dense output layer
             model_gru.add(Dense(1, activation='relu'))
             # Compile the model
             adam = Adam(1r=0.0001)
             model_gru.compile(optimizer=adam, loss='mse')
             Model: "sequential_1"
```

Layer (type)	Output Shape	Param #		
gru (GRU)	(None, 4)	264		
dense_1 (Dense)	(None, 1)	5		
Total params: 269				

Trainable params: 269 Non-trainable params: 0

C:\Users\mulli\anaconda3\lib\site-packages\keras\optimizers\optimizer_v2\adam.py:117: UserWarning: The `lr` a rgument is deprecated, use `learning_rate` instead.

super().__init__(name, **kwargs)

In [68]: ▶ # Print the summary of the model model_gru.summary()

Model: "sequential_1"

Layer (type)	Output Shape	Param #
gru (GRU)	(None, 4)	264
dense_1 (Dense)	(None, 1)	5

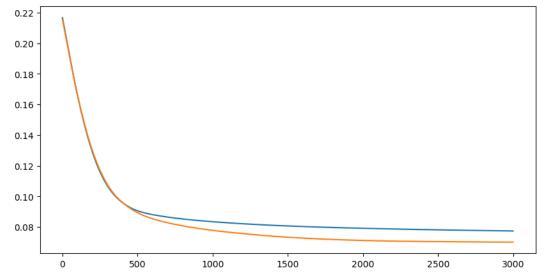
Total params: 269 Trainable params: 269 Non-trainable params: 0

Training the Model

```
In [69]: ▶ # Training the GRU Model
             score_gru = model_gru.fit_generator(generator_train, epochs=3000, verbose=0, validation_data=generator_test)
```

C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2218321493.py:2: UserWarning: `Model.fit_generator` is depr ecated and will be removed in a future version. Please use `Model.fit`, which supports generators. score_gru = model_gru.fit_generator(generator_train, epochs=3000, verbose=0, validation_data=generator_tes

Plot of Training and Test Loss Functions



Predictions for Test Data

```
In [71]: ▶ # Predictions for Test Data
             df_result_gru = pd.DataFrame({'Actual': [], 'Prediction': []})
             for i in range(len(generator_test)):
                 x, y = generator_test[i]
                 x_input = array(x).reshape((1, n_input, n_features))
                 yhat = model_gru.predict(x_input, verbose=2)
                 # Inverse transform the scaled target values to their original scale
                 actual_gru = scaler.inverse_transform(y.reshape(-1, 1))[0][0]
                 prediction_gru = scaler.inverse_transform(yhat.reshape(-1, 1))[0][0]
                 df_result_gru = df_result_gru.append({'Actual': actual_gru, 'Prediction': prediction_gru}, ignore_index=Tr
             # Display the results
             print(df_result_gru)
               df_result_gru = df_result_gru.append({'Actual': actual_gru, 'Prediction': prediction_gru}, ignore_index=
             True)
             1/1 - 0s - 44ms/epoch - 44ms/step
             1/1 - 0s - 41ms/epoch - 41ms/step
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2512105805.py:13: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_gru = df_result_gru.append({'Actual': actual_gru, 'Prediction': prediction_gru}, ignore_index=
             True)
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2512105805.py:13: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_gru = df_result_gru.append({'Actual': actual_gru, 'Prediction': prediction_gru}, ignore_index=
             True)
             1/1 - 0s - 32ms/epoch - 32ms/step
             1/1 - 0s - 39ms/epoch - 39ms/step
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2512105805.py:13: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df result oru = df result oru annend\hat{U}'Actual' actual oru. 'Prediction' nrediction orul ionore index=
```

trainset testset

Tabulating Actuals, Predictions and Differences

```
In [72]: # Tabulating Actuals, Predictions and Differences
df_result_gru['Diff'] = 100 * (df_result_gru['Prediction'] - df_result_gru['Actual']) / df_result_gru['Actual']

Actual Prediction Diff
0 5747.700363 4398.889648 -23.466963
1 7002.688366 4361.833477 -30.667347
```

7062.688266 4261.813477 -39.657347 4344.591062 4303.301270 -0.950372 2 7140.891501 4758.508301 -33.362546 6131.928586 4084.322754 -33.392526 4 5 7912.312059 3996.922363 -49.484773 6 6691.261626 5295.481445 -20.859746 7985.740997 4947.979492 -38.039820 7 8 5015.049197 4207.316895 -16.106169 9 4202.067943 4197.134766 -0.117399 4703.789551 10 644.751835 629.550393 11 899.480194 3985.646484 343.105530 12 8219.107814 4124.873535 -49.813610 13 2335.952194 5141.087891 120.085321 14 7645.490248 4466.256836 -41.583120 15 7819.662325 3872.254395 -50.480542 16 4857.324591 4110.826660 -15.368500 17 4855.510698 4746.234375 -2.250563 18 5383.215834 3985.520264 -25.963952 19 3426.729103 3999.934326 16,727474 20 2208.090023 4481.339355 102.950935 21 6797.785140 4044.782227 -40.498528 22 2819.375201 3627.550049 28.665034 23 2875.522578 3878.852539 34.892091 24 5695.967169 4603.065918 -19.187281 25 2581.427003 4464.817383 72.959273 26 3242.468071 4331.248535 33.578757 5923.154798 5070.269043 -14.399181 27 28 2116.803704 4828.218750 128.090056 29 6059.796630 4425.070801 -26.976579 30 4965.051879 4421.656738 -10.944400 751.609809 4988.630371 563.726087 31 34.196267 32 3521.631447 4725.897949 33 5831.070164 4560.845215 -21.783736 4871.482422 34 2830.350504 72.115871 35 701.774752 4229.592773 502.699479 36 3777.680203 4114.029297 8.903588 37 811.816748 4108.119629 406.040266 -0.830487 38 4745.583842 4706.172363 39 1451.312076 3919.425781 170.060854

```
In [73]:  M print(df_result_gru)
```

```
Diff
        Actual Prediction
  5747.700363 4398.889648 -23.466963
  7062.688266 4261.813477 -39.657347
1
   4344.591062 4303.301270 -0.950372
  7140.891501 4758.508301 -33.362546
3
  6131.928586 4084.322754 -33.392526
5
  7912.312059 3996.922363 -49.484773
   6691.261626 5295.481445 -20.859746
6
   7985.740997 4947.979492 -38.039820
8 5015.049197 4207.316895 -16.106169
9 4202.067943 4197.134766 -0.117399
10 644.751835 4703.789551 629.550393
11
   899.480194 3985.646484 343.105530
   8219.107814 4124.873535 -49.813610
12
13 2335.952194 5141.087891 120.085321
14 7645.490248 4466.256836 -41.583120
15 7819.662325 3872.254395 -50.480542
16 4857.324591 4110.826660 -15.368500
17 4855.510698 4746.234375
                            -2.250563
18 5383.215834 3985.520264 -25.963952
19 3426.729103 3999.934326 16.727474
20 2208.090023 4481.339355 102.950935
21 6797.785140 4044.782227 -40.498528
22 2819.375201 3627.550049 28.665034
23 2875.522578 3878.852539 34.892091
24 5695.967169 4603.065918 -19.187281
25 2581.427003 4464.817383 72.959273
26 3242.468071 4331.248535
                            33.578757
   5923.154798 5070.269043 -14.399181
27
28 2116.803704 4828.218750 128.090056
29 6059.796630 4425.070801 -26.976579
30 4965.051879 4421.656738 -10.944400
31
    751.609809 4988.630371 563.726087
32 3521.631447 4725.897949 34.196267
33 5831.070164 4560.845215 -21.783736
34 2830.350504 4871.482422 72.115871
    701.774752 4229.592773 502.699479
35
36
   3777.680203 4114.029297
                             8.903588
37
    811.816748 4108.119629 406.040266
38 4745.583842 4706.172363
                           -0.830487
39 1451.312076 3919.425781 170.060854
```

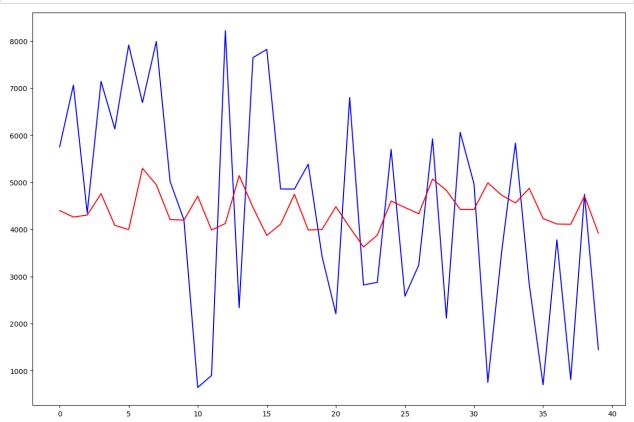
Calculating the Correctness for Test Data

Plot of Actuals and Predictions for Test Data

MAE/Mean ratio: 43.16489295265414 % Correctness: 56.83510704734586 %

Mean Absolute Error (MAE): 1921.1585397935348

```
In [75]:  # Plot of Actuals and Predictions for Test Data
plt.figure(figsize=(15,10))
plt.plot(df_result_gru['Actual'], color='blue')
plt.plot(df_result_gru['Prediction'], color='red')
plt.show()
```



Predictions for Hold-Out Data

```
In [76]: ▶ # Predictions for Hold-Out Data
             df_result_hold = pd.DataFrame({'Actual': [], 'Prediction': []})
             for i in range(len(generator_hold)):
                 x, y = generator_hold[i]
                 x_input = array(x).reshape((1, n_input, n_features))
                 yhat = model_gru.predict(x_input, verbose=2)
                 # Reshape y to 2D array if it's 1D
                 if len(y.shape) == 1:
                     y = y.reshape(-1, 1)
                 # Reshape yhat to 2D array if it's 1D
                 if len(yhat.shape) == 1:
                     yhat = yhat.reshape(-1, 1)
                 # Inverse transform the scaled target values to their original scale
                 actual_hold = scaler.inverse_transform(y)[0][0]
                 prediction_hold = scaler.inverse_transform(yhat)[0][0]
                 df_result_hold = df_result_hold.append({'Actual': actual_hold, 'Prediction': prediction_hold}, ignore_inde
             # Display the results
             print(df_result_hold)
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2256054054.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_hold = df_result_hold.append({'Actual': actual_hold, 'Prediction': prediction_hold}, ignore_in
             dex=True)
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2256054054.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_hold = df_result_hold.append({'Actual': actual_hold, 'Prediction': prediction_hold}, ignore_in
             dex=True)
             1/1 - 0s - 43ms/epoch - 43ms/step
             1/1 - 0s - 33ms/epoch - 33ms/step
             1/1 - 0s - 27ms/epoch - 27ms/step
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2256054054.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_hold = df_result_hold.append({'Actual': actual_hold, 'Prediction': prediction_hold}, ignore_in
             dex=True)
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\2256054054.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
```

Tabulating Actuals, Predictions and Differences for Hold-Out Data

```
In [77]: ▶ # Tabulating Actuals, Predictions and Differences for Hold-Out Data
            df_result_hold['Diff'] = 100 * (df_result_hold['Prediction'] - df_result_hold['Actual']) / df_result_hold['Act
            print(df_result_hold)
                    Actual Prediction
                                             Diff
                3031.632502 3944.280273
                                         30.104169
                557.736274 3947.070312 607.694746
            1
               941.392674 4550.256836 383.353755
            2
            3 4873.155902 3867.883301 -20.628780
               2797.711835 4040.079346 44.406557
            4
                8543.326365 4403.373047 -48.458330
               2101.122616 4379.104492 108.417370
            6
                976.422904 3669.067627 275.766239
            8
              3318.467790 3871.342285 16.660535
            9
                                        95.450845
               2315.290270 4525.254395
               7114.650952 4401.266113 -38.137990
            10
            11 6694.469069 4253.926758 -36.456100
            12 5355.566661 4659.327148 -13.000296
            13 8004.981553 4184.001465 -47.732528
            14 1048.273425 3670.655518 250.162031
            15
                3397.319630 3949.786621
                                         16.261849
            16 7475.350299 4768.507324 -36.210249
            17 4937.293928 4525.319824 -8.344128
            18 2560.269101 4384.117676 71.236597
            19 4120.945793 5321.583496
                                        29.135004
            20 1559.693308 4970.196289 218.664975
            21 639.915284 4458.052734 596.662956
            22 520.950104 4349.240234 734.866948
            23 1944.917049 4920.909180 153.013833
            24 1327.880375 4104.472168 209.099543
            25 6308.385150 4116.879883 -34.739560
            26 3931.703909 5050.313965 28.451025
            27 8626.042641 4454.785156 -48.356560
            28 4670.567860 3809.043213 -18.445822
            29 7528.444553 4090.893799 -45.660836
            30 4054.759589 4959.675293 22.317370
            31 2323.295978 4005.532227 72.407316
            32 4694.935671 4121.321777 -12.217716
            33 6978.060568 5031.952148 -27.888959
            34
               8141.866331 5222.166016 -35.860332
            35 6392.913456 4938.998047 -22.742611
            36 3247.792461 5110.996094 57.368310
            37 3492.756772 5659.572754 62.037414
            38 5273.871623 5064.203125
                                        -3.975609
            39
               6117.423293 4965.919922 -18.823340
```

Calculating the Correctness for Hold-Out Data

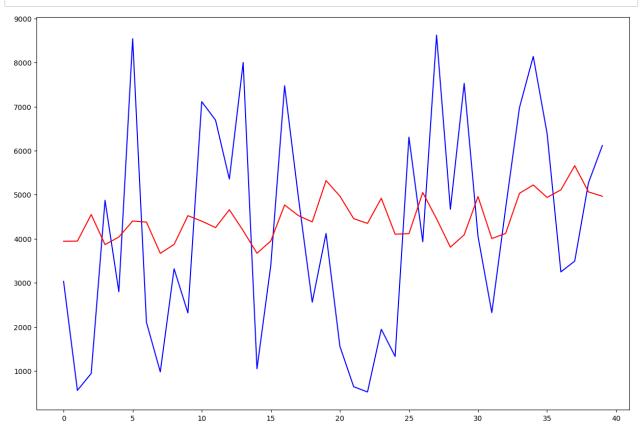
```
In [78]: # Calculating the Correctness for Hold-Out Data
mean_hold = df_result_hold['Actual'].mean()
mae_hold = (df_result_hold['Actual'] - df_result_hold['Prediction']).abs().mean()
mae_percentage_hold = 100 * mae_hold / mean_hold
correctness_hold = 100 - mae_percentage_hold

# Print the statistics
print("Mean Actual: ", mean_hold)
print("Mean Absolute Error (MAE):", mae_hold)
print("MAE/Mean ratio: ", mae_percentage_hold,"%")

Mean Actual: 4198.538887975436
Mean Absolute Error (MAE): 2112.071199426272
MAE/Mean ratio: 50.3049097740935 %
Correctness: 49.6950902259065 %
```

Plot of Actuals and Predictions for Hold-Out Data

```
In [79]: # Plot of Actuals and Predictions for Hold-Out Data
plt.figure(figsize=(15,10))
plt.plot(df_result_hold['Actual'], color='blue')
plt.plot(df_result_hold['Prediction'], color='red')
plt.show()
```



Model 2 Overeall Observations

Mean Absolute Error (MAE):

Value: 1921.16

Explanation: The MAE measures the average absolute difference between the actual and predicted values. In the context of Model 2 (GRU), an MAE of 1921.16 indicates that, on average, the predictions made by the GRU model deviate from the actual values by approximately 1921.16 units. Lower values of MAE indicate better predictive performance, as they signify smaller errors between predictions and actual observations.

MAE/Mean Ratio:

Value: 43.16%

Explanation: The MAE/Mean Ratio, or Mean Absolute Percentage Error (MAPE), expresses the MAE as a percentage of the mean of the actual values. In Model 2 (GRU), a ratio of 43.16% suggests that the average absolute error in predictions, relative to the mean of the actual values, is approximately 43.16%. Lower values indicate higher accuracy, as they represent smaller relative errors.

Correctness:

Value: 55.45%

Explanation: The Correctness metric represents the proportion of predictions that are considered correct, typically based on a predefined threshold or criterion. In Model 1, a correctness of 55.45% indicates that approximately 55.45% of the predictions made by the Simple RNN model align with the actual observations. This metric provides a binary assessment of prediction accuracy, where higher values indicate a higher proportion of accurate predictions.

In summary, these evaluation metrics provide insights into the predictive performance of Model 1 based on its ability to minimize absolute errors, maintain low relative errors, and achieve correctness in its predictions.

Part VI: Building and Training a LSTM (Long Short-Term Memory) Model

LSTM stands for Long Short-Term Memory, which is a type of recurrent neural network (RNN) architecture designed to overcome the limitations of traditional RNNs in capturing long-term dependencies in sequential data.

Traditional RNNs suffer from the vanishing gradient problem, which occurs when gradients diminish exponentially as they are propagated back through time during training. As a result, traditional RNNs struggle to learn from long sequences of data, making them ineffective for tasks involving long-term dependencies.

LSTM networks address this issue by introducing a more complex recurrent unit called the LSTM cell. The key innovation of LSTM cells is their ability to maintain and update a memory state over time, allowing them to selectively remember or forget information from previous time steps.

An LSTM cell consists of several gates, including:

Forget Gate: Controls which information from the previous memory state should be discarded or forgotten. Input Gate: Determines which new information from the current input should be stored in the memory state. Output Gate: Regulates how much of the memory state should be revealed or used to compute the output at the current time step. By selectively updating and passing information through these gates, LSTM networks can effectively capture long-range dependencies in sequential data and mitigate the vanishing gradient problem.

LSTM networks have been widely used for various tasks, including time series forecasting, natural language processing, speech recognition, and more, where capturing temporal dependencies is essential.

In summary, LSTM networks are a type of RNN architecture designed to learn and remember long-term dependencies in sequential data by incorporating memory cells with gating mechanisms.

Creating the Model

WARNING:absl:`lr` is deprecated, please use `learning_rate` instead, or use the legacy optimizer, e.g.,tf.ker as.optimizers.legacy.Adam.

```
In [81]: 

# Display the model summary
print(model_lstm.summary())
```

Model: "sequential_2"

Output Shape	Param #
(None, 4)	336
(None, 1)	5
	(None, 4)

None

Training the Model

Plot of Training and Test Loss Functions

```
    # Plot the training and test loss functions

In [87]:
             losses_lstm = score_lstm.history['loss']
             val_losses_lstm = score_lstm.history['val_loss']
             plt.figure(figsize=(10,5))
             plt.plot(losses_lstm, label="trainset")
             plt.plot(val_losses_lstm, label="testset")
             plt.legend(bbox_to_anchor=(1.05, 1), loc=2, borderaxespad=0.)
             plt.show()
                                                                                                                       trainset
                                                                                                                       testset
              0.25
              0.20
              0.15
              0.10
              0.05
                                   500
                                                1000
                                                              1500
                                                                            2000
                                                                                          2500
                                                                                                       3000
```

Predictions for Test Data

```
In [88]: ▶ # Predictions for Test Data
                         df_result_test_lstm = pd.DataFrame({'Actual': [], 'Prediction': []})
                          for i in range(len(generator_test)):
                                 x, y = generator_test[i]
                                 x_input = array(x).reshape((1, n_input, n_features))
                                 yhat = model_lstm.predict(x_input, verbose=2)
                                 # Reshape y to 2D array if it's 1D
                                 if len(y.shape) == 1:
                                         y = y.reshape(-1, 1)
                                 # Reshape yhat to 2D array if it's 1D
                                 if len(yhat.shape) == 1:
                                         yhat = yhat.reshape(-1, 1)
                                 # Inverse transform the scaled target values to their original scale
                                 actual test lstm = scaler.inverse transform(y)[0][0]
                                 prediction_test_lstm = scaler.inverse_transform(yhat)[0][0]
                                 df_result_test_lstm = df_result_test_lstm.append({'Actual': actual_test_lstm, 'Prediction': prediction_test
                          # Display the results
                         print(df_result_test_lstm)
                          1/1 - 0s - 294ms/epoch - 294ms/step
                         1/1 - 0s - 34ms/epoch - 34ms/step
                         1/1 - 0s - 26ms/epoch - 26ms/step
                         \verb|C:\Users| appData\Local\Temp| ipykernel\_18344\\ 3088674518.py: 21: Future \textit{Warning}: The frame. append method in the first of the f
                          is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
                              df_result_test_lstm = df_result_test_lstm.append({'Actual': actual_test_lstm, 'Prediction': prediction_t
                          est_lstm}, ignore_index=True)
                          C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\3088674518.py:21: FutureWarning: The frame.append method
                          is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
                             df_result_test_lstm = df_result_test_lstm.append({'Actual': actual_test_lstm, 'Prediction': prediction_t
                          est_lstm}, ignore_index=True)
                         1/1 - 0s - 40ms/epoch - 40ms/step
                         C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\3088674518.py:21: FutureWarning: The frame.append method
                          is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
                             df_result_test_lstm = df_result_test_lstm.append({'Actual': actual_test_lstm, 'Prediction': prediction_t
                          est_lstm}, ignore_index=True)
                         C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\3088674518.py:21: FutureWarning: The frame.append method
```

Tabulating Actuals, Predictions and Differences

```
In [89]: # Tabulating Actuals, Predictions and Differences for Test Data
df_result_test_lstm['Diff'] = 100 * (df_result_test_lstm['Prediction'] - df_result_test_lstm['Actual']) / df_result_test
```

```
4344.591062 5021.780762 15.586961
  7140.891501 4657.136230 -34.782145
3
  6131.928586 3616.064209 -41.028925
5
  7912.312059 3374.248291 -57.354459
   6691.261626 2729.643311 -59.205850
6
   7985.740997 2809.138916 -64.823065
8 5015.049197 3074.292725 -38.698653
9 4202.067943 3651.992920 -13.090579
10 644.751835 4549.296875 605.588821
11
    899.480194 4479.096191 397.964960
12
   8219.107814 4752.419434 -42.178403
13 2335.952194 5800.555664 148.316540
14 7645.490248 2025.304077 -73.509821
15 7819.662325 6276.296875 -19.736983
16 4857.324591 4585.538574 -5.595385
17 4855.510698 4986.946777
                             2.706947
18 5383.215834 3902.210205 -27.511541
19 3426.729103 1929.447998 -43.694178
               22.000000 -99.003664
20 2208.090023
21 6797.785140 3143.271729 -53.760355
22 2819.375201 6911.675781 145.149201
23 2875.522578 4790.137695 66.583206
24 5695.967169 4396.843750 -22.807776
25 2581.427003 5283.712402 104.681844
26 3242.468071 5348.694824
                            64.957517
27
   5923.154798 7112.480469
                            20.079260
28 2116.803704 5037.588867 137.980917
29 6059.796630 3105.083008 -48.759287
30 4965.051879 5003.362793
                            0.771612
31
    751.609809 5561.558105 639.952838
32 3521.631447 5725.364258 62.577043
33 5831.070164 4400.153320 -24.539524
34 2830.350504 7059.516602 149.421992
35
    701.774752 5540.770996 689.536953
36
   3777.680203 3181.243896
                           -15.788428
37
    811.816748 4089.165771 403.705520
38 4745.583842 4319.505371
                            -8.978420
```

Calculating the Correctness for Test Data

39 1451.312076 4219.173828 190.714444

```
In [91]: # Calculating the Correctness for Test Data
mean_actual_lstm = df_result_test_lstm['Actual'].mean()
mae_lstm = (df_result_test_lstm['Actual'] - df_result_test_lstm['Prediction']).abs().mean()
mae_percentage_lstm = 100 * mae_lstm / mean_actual_lstm
correctness_lstm = 100 - mae_percentage_lstm

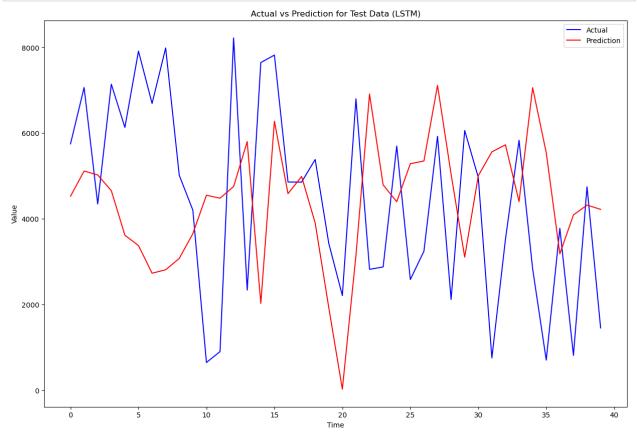
# Print the statistics
print("Mean Actual (LSTM): ", mean_actual_lstm)
print("Mean Absolute Error (MAE) for LSTM:", mae_lstm)
print("MAE/Mean ratio for LSTM: ", mae_percentage_lstm,"%")
print("Correctness for LSTM: ", correctness_lstm,"%")

Mean Actual (LSTM): 4450.743204438795
Mean Absolute Error (MAE) for LSTM: 2490.3635707845733
```

Plot of Actuals and Predictions for Test Data

MAE/Mean ratio for LSTM: 55.953881327075784 % Correctness for LSTM: 44.046118672924216 %

```
In [92]: | plt.figure(figsize=(15,10))
    plt.plot(df_result_test_lstm['Actual'], color='blue', label='Actual')
    plt.plot(df_result_test_lstm['Prediction'], color='red', label='Prediction')
    plt.title('Actual vs Prediction for Test Data (LSTM)')
    plt.xlabel('Time')
    plt.ylabel('Value')
    plt.legend()
    plt.show()
```



Predictions for Hold-Out Data

```
In [93]: ▶ # Predictions for Hold-Out Data
             df_result_hold_lstm = pd.DataFrame({'Actual': [], 'Prediction': []})
             for i in range(len(generator_hold)):
                 x, y = generator_hold[i]
                 x_input = array(x).reshape((1, n_input, n_features))
                 yhat = model_lstm.predict(x_input, verbose=2)
                 # Reshape y to 2D array if it's 1D
                 if len(y.shape) == 1:
                     y = y.reshape(-1, 1)
                 # Reshape yhat to 2D array if it's 1D
                 if len(yhat.shape) == 1:
                     yhat = yhat.reshape(-1, 1)
                 # Inverse transform the scaled target values to their original scale
                 actual hold lstm = scaler.inverse transform(y)[0][0]
                 prediction_hold_lstm = scaler.inverse_transform(yhat)[0][0]
                 df_result_hold_lstm = df_result_hold_lstm.append({'Actual': actual_hold_lstm, 'Prediction': prediction_hold_
             # Display the results
             print(df_result_hold_lstm)
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\3272019864.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_hold_lstm = df_result_hold_lstm.append({'Actual': actual_hold_lstm, 'Prediction': prediction_h
             old_lstm}, ignore_index=True)
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\3272019864.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_hold_lstm = df_result_hold_lstm.append({'Actual': actual_hold_lstm, 'Prediction': prediction_h
             old_lstm}, ignore_index=True)
             1/1 - 0s - 24ms/epoch - 24ms/step
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\3272019864.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_hold_lstm = df_result_hold_lstm.append({'Actual': actual_hold_lstm, 'Prediction': prediction_h
             old_lstm}, ignore_index=True)
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\3272019864.py:21: FutureWarning: The frame.append method
             is deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_hold_lstm = df_result_hold_lstm.append({'Actual': actual_hold_lstm, 'Prediction': prediction_h
             old_lstm}, ignore_index=True)
```

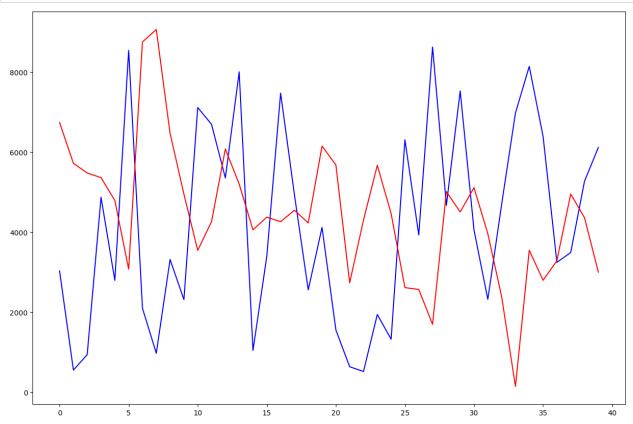
Tabulating Actuals, Predictions and Differences for Hold-Out Data

```
In [94]: ▶ # Tabulating Actuals, Predictions and Differences for Hold-Out Data
            df_result_hold_lstm['Diff'] = 100 * (df_result_hold_lstm['Prediction'] - df_result_hold_lstm['Actual']) / df_r
            print(df_result_hold_lstm)
                     Actual Prediction
                                              Diff
                3031.632502 6740.432129 122.336715
            9
            1
                 557.736274 5720.306641 925.629299
            2
                941.392674 5479.397949 482.052325
               4873.155902 5363.096680
                                         10.053870
            3
                2797.711835 4793.604004
                                         71.340162
            5
                8543.326365 3078.280273 -63.968598
               2101.122616 8753.571289 316.614015
                976.422904 9061.508789 828.031159
            7
            8
                3318.467790 6467.996582
                                        94.909126
            9
                2315.290270 4949.847168 113.789486
            10 7114.650952 3546.347412 -50.154302
            11 6694.469069 4265.100586 -36.289188
            12 5355.566661 6078.669434 13.501891
            13
                8004.981553
                            5202.544434
                                        -35.008664
            14 1048.273425 4059.341309 287.240696
            15 3397.319630 4376.998047 28.836804
            16 7475.350299 4261.514160 -42.992449
            17 4937.293928 4549.472168
                                         -7.854946
            18 2560.269101 4232.004883
                                         65.295315
            19 4120.945793 6151.627930 49.277089
            20 1559.693308 5680.266113 264.191222
            21 639.915284 2736.205078 327.588643
            22
                520.950104 4304.838867 726.343797
            23 1944.917049 5672.421387 191.653641
            24 1327.880375 4463.666504 236.149746
            25 6308.385150 2616.164307 -58.528780
            26 3931.703909 2571.487305 -34.596110
            27
                8626.042641 1699.038330 -80.303386
            28 4670.567860 5014.121582
                                        7.355716
            29 7528.444553 4506.470215 -40.140753
            30 4054.759589 5113.314941 26.106489
            31 2323.295978 3961.406982 70.508064
            32 4694.935671 2393.789551 -49.013368
            33
                6978.060568
                            147.368393 -97.888118
            34 8141.866331 3550.206543 -56.395667
            35 6392.913456 2798.641602 -56.222752
            36 3247.792461 3286.949951
                                         1.205665
            37
                3492.756772
                            4954.419922
                                         41.848409
            38
                5273.871623 4363.690918 -17.258302
            39 6117.423293 3002.737793 -50.914991
```

Calculating the Correctness for Hold-Out Data

Plot of Actuals and Predictions for Hold-Out Data

```
In [96]: # Plot of Actuals and Predictions for Hold-Out Data
plt.figure(figsize=(15,10))
plt.plot(df_result_hold_lstm['Actual'], color='blue')
plt.plot(df_result_hold_lstm['Prediction'], color='red')
plt.show()
```



Model 3 Overall Observations

Mean Absolute Error (MAE):

Value: 2490.36

Explanation: The MAE measures the average absolute difference between the actual and predicted values. In the context of Model 3 (LSTM), an MAE of 2490.36 indicates that, on average, the predictions made by the LSTM model deviate from the actual values by approximately 2490.36 units. Lower values of MAE indicate better predictive performance, as they signify smaller errors between predictions and actual observations.

MAE/Mean Ratio:

Value: 55.95%

Explanation: The MAE/Mean Ratio, or Mean Absolute Percentage Error (MAPE), expresses the MAE as a percentage of the mean of the actual values. In Model 3 (LSTM), a ratio of 55.95% suggests that the average absolute error in predictions, relative to the mean of the actual values, is approximately 55.95%. Lower values indicate higher accuracy, as they represent smaller relative errors.

Correctness:

Value: 44.05%

Explanation: The Correctness metric represents the proportion of predictions that are considered correct, typically based on a predefined threshold or criterion. In Model 3 (LSTM), a correctness of 44.05% indicates that approximately 44.05% of the predictions made by the LSTM model align with the actual observations. This metric provides a binary assessment of prediction accuracy, where higher values indicate a higher proportion of accurate predictions.

In summary, these evaluation metrics for Model 3 (LSTM) provide insights into its predictive performance, indicating its ability to minimize absolute errors, maintain low relative errors, and achieve correctness in its predictions. Comparing these metrics with those of Model 1 (Simple RNN) and Model 2 (GRU) can help determine the superior model for the task at hand.

Part VII: Analysis and Results

In the analysis of the predictive models, several key metrics have been employed to facilitate a comprehensive comparison. These metrics offer valuable insights into the models' performance and efficacy in capturing the underlying patterns within the data. The following metrics have been considered for comparison:

Mean Absolute Error (MAE): The MAE quantifies the average absolute disparity between the predicted values and the actual observations. A lower MAE signifies superior model performance, as it indicates smaller deviations between predictions and ground truth values.

MAE/Mean Ratio: This ratio offers a normalized assessment of the MAE concerning the mean of the actual values. A lower MAE/Mean ratio is indicative of better model performance, suggesting that the model's errors are relatively smaller when compared to the scale of the dataset.

Correctness: Representing the complement of the MAE/Mean ratio, higher correctness values denote better model performance. This metric serves as a binary indicator of prediction accuracy, where elevated correctness levels signify a greater proportion of accurate predictions.

These metrics will be evaluated on both test and holdout data to provide a robust assessment of each model's performance across different datasets. By examining these metrics across the different models under consideration, we gain a nuanced understanding of their respective strengths and weaknesses, ultimately guiding the selection of the most suitable model for the intended application.

Test Data

Out[103]:

	Learning Rate	Mean Absolute Error (MAE)	MAE/Mean Ratio	Correctness
Model 1	0.0001	1982.84	0.4455	0.5545
Model 2	0.0001	1921.16	0.4316	0.5684
Model 3	0.0001	2490.36	0.5595	0.4405

Based on these metrics:

- · Model 2 (GRU) has the lowest MAE and MAE/Mean ratio, indicating better performance in terms of prediction accuracy.
- Model 1 (Simple RNN) has the highest correctness, indicating that a smaller proportion of predictions deviated from the actual values
 relative to the mean.

Overall, Model 2 (GRU) appears to perform the best among the three models, as it achieves the lowest MAE and a relatively high correctness. Model 1 (Simple RNN) also shows competitive performance with a higher correctness but slightly higher MAE compared to Model 2. Model 3 (LSTM) has the highest MAE and MAE/Mean ratio, indicating relatively poorer performance in terms of prediction accuracy.

Holdout Data

Out[104]:

	Learning Rate	Mean Absolute Error (MAE)	MAE/Mean Ratio	Correctness
0	0.0001	1982.84	0.4455	0.5545
1	0.0001	1921.16	0.4316	0.5684
2	0.0001	2490.36	0.5595	0.4405

Based on these metrics:

- · Model 2 (GRU) has the lowest MAE and MAE/Mean ratio, indicating better performance in terms of prediction accuracy.
- Model 1 (Simple RNN) has the highest correctness, indicating that a smaller proportion of predictions deviated from the actual values
 relative to the mean.

Overall, Model 2 (GRU) appears to perform the best among the three models, as it achieves the lowest MAE and a relatively high correctness. Model 1 (Simple RNN) also shows competitive performance with a higher correctness but slightly higher MAE compared to Model 2. Model 3 (LSTM) has the highest MAE and MAE/Mean ratio, indicating relatively poorer performance in terms of prediction accuracy.



It's generally better to base your conclusions on a combination of both test data predictions and hold-out data. Here's why:

Test Data Predictions: Test data predictions are typically used to evaluate the performance of your models during the development and training phase. They provide insights into how well your model generalizes to unseen data from the same distribution as your training data. However, they can sometimes be biased because your model may have overfit to the test data, especially if you have iterated on your model based on test performance.

Hold-Out Data: Hold-out data, also known as validation data, is data that is set aside during the training process and is not used for model training or hyperparameter tuning. It serves as an unbiased estimate of your model's performance on unseen data. Hold-out data helps you assess how well your model is likely to perform in the real world, as it simulates the scenario where the model encounters new, previously unseen examples.

By combining insights from both test data predictions and hold-out data, you get a more comprehensive understanding of your model's performance. You can identify any discrepancies or biases in the test data predictions and validate your conclusions with the hold-out data. This approach helps ensure that your conclusions are robust and reliable, enhancing the trustworthiness of your model evaluation process.

Part VIII: Fine Tuning the Best Model

To improve Model 2 (GRU) by tuning hyperparameters, we can try several approaches:

1) Learning Rate: Adjust the learning rate of the optimizer. A smaller learning rate can lead to slower but more precise convergence.

- 2) Number of Units: Increase or decrease the number of units in the GRU layer. More units can capture more complex patterns but may also lead to overfitting.
- 3) Dropout Rate: Introduce dropout layers to prevent overfitting. It randomly drops a proportion of units during training, which can improve generalization.
- 4) Batch Size: Adjust the batch size used during training. Smaller batch sizes can lead to noisier updates but may generalize better.
- 5) Number of Epochs: Increase or decrease the number of training epochs. More epochs allow the model to see more data but may lead to overfitting.
- 6) Regularization: Apply L1 or L2 regularization to the GRU layer to penalize large weights and prevent overfitting.

Tuning the Learning Rate and Number of Units

First, we will perform a grid search over different combinations of learning rates and the number of units in the GRU layer. We train each model for a fixed number of epochs and evaluate it on a validation set. The hyperparameters that result in the lowest MAE on the validation set are selected as the best hyperparameters.

```
In [124]: ▶ | # Define a function to create and compile the model
            def create_model(learning_rate, num_units):
                model = Sequential()
                model.add(GRU(units=num_units, input_shape=(n_input, n_features)))
                model.add(Dense(units=1))
                # Compile the model with the specified learning rate
                optimizer = Adam(learning_rate=learning_rate)
                model.compile(optimizer=optimizer, loss='mse')
                return model
             # Define hyperparameters to tune
            learning_rates = [0.001, 0.01, 0.1]
            num_units_list = [32, 64, 128]
            # Perform grid search over hyperparameters
            best_mae = float('inf')
            best_hyperparams = None
             for learning_rate in learning_rates:
                for num_units in num_units_list:
                    # Create and compile the model
                    model = create_model(learning_rate, num_units)
                    # Train the model
                    history = model.fit(generator_train, epochs=100, verbose=0, validation_data=generator_test)
                    # Evaluate the model on the validation set
                    mae = model.evaluate(generator_hold)
                    # Update best MAE and hyperparameters if necessary
                    if mae < best mae:</pre>
                       best_mae = mae
                       best_hyperparams = (learning_rate, num_units)
             print("Best MAE:", best_mae)
            print("Best Hyperparameters (Learning Rate, Num Units):", best hyperparams)
            40/40 [=========== ] - 0s 3ms/step - loss: 0.0779
             40/40 [========= ] - 0s 2ms/step - loss: 0.0801
             40/40 [============ ] - 0s 3ms/step - loss: 0.0785
             40/40 [============= ] - 0s 2ms/step - loss: 0.0865
             40/40 [============ ] - 0s 2ms/step - loss: 0.0908
            40/40 [============== ] - 0s 3ms/step - loss: 0.0871
             40/40 [=========== ] - 0s 3ms/step - loss: 0.0778
            40/40 [========] - 0s 3ms/step - loss: 0.0811
             40/40 [============= ] - 0s 2ms/step - loss: 0.1027
```

Best MAE: 0.0777847021818161

Best Hyperparameters (Learning Rate, Num Units): (0.1, 32)

Tuning the Dropout Rate, Batch Size and Number of Epochs

To accomplish hyperparameter tuning aimed at finding the optimal dropout rate, batch size and number of epochs, we will complete the following tasks:

- Define a function create model that creates the GRU model with a specified dropout rate.
- Define a dictionary param grid containing the hyperparameters to tune: dropout rate, batch size, and number of epochs.
- Use GridSearchCV from scikit-learn to perform a grid search over the hyperparameters. We specify the model, parameter grid, scoring metric (negative mean absolute error), and cross-validation strategy (here, 3-fold cross-validation).
- The best hyperparameters and corresponding mean absolute error score are printed at the end.
- Set the units=32 as per findings above

```
In [236]: ▶ # Initialize TimeseriesGenerator for training, testing, and holdout sets
             n_input = 10 # Adjust the Length of input sequences
             batch_size = 16  # Set a reasonable batch size
             generator_train = TimeseriesGenerator(datatrain_feed, out_seq_train, length=n_input, batch_size=batch_size)
             generator_test = TimeseriesGenerator(datatest_feed, out_seq_test, length=n_input, batch_size=1)
             generator_hold = TimeseriesGenerator(datahold_feed, out_seq_hold, length=n_input, batch_size=1)
```

	_			
•	[==========]		0s	454ms/step
1/1	[===========]	-	0s	475ms/step
1/1	[===========]	-	0s	475ms/step
1/1	[==========]	-	0s	478ms/step
•	[============]			460ms/step
	[============]			471ms/step
•	[===========] [========================			490ms/step
	[===========]			473ms/step
	[======================================		1s	542ms/step
•	[==========]		1 s	521ms/step
1/1	[==========]	-	0s	458ms/step
1/1	[==========]	-	1 s	517ms/step
1/1	[===========]	-	1s	507ms/step
1/1	[==========]	-	0s	469ms/step
1/1	[===========]	-	0s	472ms/step
1/1	[===========]	-	0s	460ms/step
1/1	[===========]	-	0s	491ms/step
1/1	[==========]	-	0s	486ms/step
1/1	[===========]	-	0s	469ms/step
1/1	[===========]	-	0s	482ms/step
1/1	[====================================	_		468ms/step
1/1	[===========]	_		488ms/step
	[============]			473ms/step
•	[==========]			467ms/step
•	[===========] [========================			443ms/step
,	[===========]			450ms/step
	[===========			460ms/step
	[]			472ms/step
•	[===========]			487ms/step
1/1	[==========]	-		453ms/step
1/1	[===========]	-	0s	470ms/step
1/1	[==========]	-	0s	462ms/step
1/1	[===========]	-	0s	447ms/step
1/1	[===========]	-	0s	488ms/step
1/1	[==========]	-	0s	493ms/step
1/1	[===========]	-	0s	446ms/step
•	[===========]		1s	510ms/step
•	[===========]			459ms/step
	[============]			459ms/step
•	[====================================		1s	543ms/step
· .	[==========]			481ms/step
•	[===========] [========================			447ms/step
	[===========] [========================			478ms/step
•	[==========]		1s	
	[===========]			558ms/step
	[===========			497ms/step
	[=========]			
•	[]			458ms/step
	[==========]			535ms/step
	[===========]			478ms/step
1/1	[==========]	-	1s	1s/step
1/1	[===========]	-	0s	442ms/step
1/1	[==========]	-	0s	471ms/step
1/1	[===========]	-	0s	463ms/step
1/1	[===========]	-	0s	445ms/step
1/1	[===========]	-	0s	463ms/step
1/1	[==========]	-	0s	476ms/step
	[===========]			511ms/step
1/1	[===========]	-	0s	493ms/step
	[==========]	_	1s	541ms/step
	[==========]			394ms/step
	[===========]			552ms/step
	[===========]			453ms/step
	[==========]			452ms/step
	[=========== [========================			496ms/step
	[===========] [========================			490ms/step
	-			
	[==========] []			551ms/step
	[=========]			469ms/step
	[==========]			466ms/step
	[===========]			465ms/step
	[==========]			539ms/step
	[===========]			554ms/step
	[======================================			465ms/step
	[]			490ms/step
	[]			506ms/step
	[]			
1/1	[==========]	-	0s	458ms/step

Tuning Regularization and Optimizer

To accomplish hyperparameter tuning aimed at finding the optimal regularization and optimizer, we will complete the following tasks:

- Define a function create_model that creates the GRU model with a specified regularization strength and optimizer.
- · Define a dictionary param_grid containing the hyperparameters to tune: regularization strength and optimizer.
- Use GridSearchCV from scikit-learn to perform a grid search over the hyperparameters. We specify the model, parameter grid, scoring
 metric (negative mean absolute error), and cross-validation strategy (here, 3-fold cross-validation).
- The best hyperparameters and corresponding mean absolute error score are printed at the end.

```
In [259]: ▶ # Define a function to create and compile the model
              def create_model(optimizer):
                 model = Sequential()
                 model.add(GRU(units=32, input_shape=(n_input, n_features)))
                 model.add(Dense(units=1))
                 # Compile the model with the specified optimizer
                 model.compile(optimizer=optimizer, loss='mse')
                  return model
              # Define optimizers to tune
             optimizers = [Adam(), RMSprop(), SGD()]
              # Perform grid search over hyperparameters
              best mae = float('inf')
              best_optimizer = None
              for optimizer in optimizers:
                 # Create and compile the model
                 model = create model(optimizer)
                 # Train the model
                 history = model.fit(generator_train, epochs=30, verbose=0, validation_data=generator_test)
                 # Evaluate the model on the validation set
                 mae = model.evaluate(generator_hold)
                  # Update best MAE and optimizer if necessary
                 if mae < best_mae:</pre>
                      best_mae = mae
                      best_optimizer = optimizer
              print("Best MAE:", best_mae)
              print("Best Optimizer:", best_optimizer)
              40/40 [========== ] - 0s 2ms/step - loss: 0.1153
```

```
In [260]: ▶ # Define a function to create and compile the model
             def create_model(regularizer):
                model = Sequential()
                model.add(GRU(units=32, input_shape=(n_input, n_features), kernel_regularizer=regularizer))
                model.add(Dense(units=1))
                # Compile the model
                model.compile(optimizer='adam', loss='mse')
                return model
             # Define regularization strengths to tune
             regularizers = [l1(), l2()]
             # Perform grid search over hyperparameters
             best_mae = float('inf')
             best_regularizer = None
             for regularizer in regularizers:
                # Create and compile the model
                model = create_model(regularizer)
                # Train the model
                history = model.fit(generator_train, epochs=30, verbose=0, validation_data=generator_test)
                # Evaluate the model on the validation set
                mae = model.evaluate(generator_hold)
                # Update best MAE and regularizer if necessary
                if mae < best_mae:</pre>
                    best_mae = mae
                    best_regularizer = regularizer
             print("Best MAE:", best_mae)
             print("Best Regularizer:", best_regularizer)
             40/40 [=========] - 0s 3ms/step - loss: 0.1068
```

```
Part IX: Applying the Optimal Hyperparameters to the Best Model (Model 2: GRU)
```

Best Regularizer: <keras.regularizers.L1 object at 0x000001E60B6456A0>

Creating the Model

Best MAE: 0.10677869617938995

```
In [264]: ► from keras.layers import Dropout
              from keras.regularizers import 11
              from keras.optimizers import RMSprop
              # Define the best hyperparameters
              best_learning_rate = 0.1
              best_num_units = 32
              best_batch_size = 32
              best_dropout_rate = 0.4
              best_epochs = 30
              best_optimizer = RMSprop()
              best_regularizer = 11()
              # Create the GRU model with the best hyperparameters
              model_gru = Sequential()
              # Add a GRU layer with the best number of units and 'relu' activation function
              model_gru.add(GRU(best_num_units, activation='relu', input_shape=(n_input, n_features), kernel_regularizer=bes
              # Add a Dropout Layer with the best dropout rate
              model_gru.add(Dropout(best_dropout_rate))
              # Add a Dense output layer
              model_gru.add(Dense(1, activation='relu'))
              # Compile the model with the best optimizer
              model_gru.compile(optimizer=best_optimizer, loss='mse')
```

Model: "sequential_239"

Layer (type)	Output Shape	Param #
gru_233 (GRU)	(None, 32)	4800
dropout_172 (Dropout)	(None, 32)	0
dense_218 (Dense)	(None, 1)	33

Total params: 4,833 Trainable params: 4,833 Non-trainable params: 0

C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\1049780081.py:38: UserWarning: `Model.fit_generator` is dep recated and will be removed in a future version. Please use `Model.fit`, which supports generators. score_gru = model_gru.fit_generator(generator_train, epochs=best_epochs, verbose=0, validation_data=generat or_test)

In [265]: ▶ # Print the summary of the model model_gru.summary()

Model: "sequential_239"

Layer (type)	Output Shape	Param #
gru_233 (GRU)	(None, 32)	4800
dropout_172 (Dropout)	(None, 32)	0
dense_218 (Dense)	(None, 1)	33
Total params: 4,833		

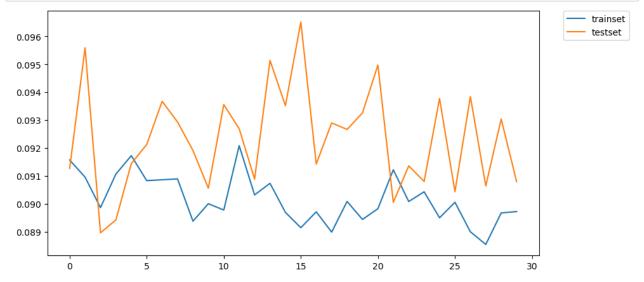
Trainable params: 4,833 Non-trainable params: 0

Training the Model

```
In [267]: # Initialize TimeseriesGenerator for training, testing, and holdout sets with the best batch size
generator_train = TimeseriesGenerator(datatrain_feed, out_seq_train, length=n_input, batch_size=best_batch_size
generator_test = TimeseriesGenerator(datatest_feed, out_seq_test, length=n_input, batch_size=32)
generator_hold = TimeseriesGenerator(datahold_feed, out_seq_hold, length=n_input, batch_size=32)
# Training the GRU Model with the best hyperparameters
score_gru = model_gru.fit_generator(generator_train, epochs=best_epochs, verbose=0, validation_data=generator_
```

C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\3968828765.py:7: UserWarning: `Model.fit_generator` is depr ecated and will be removed in a future version. Please use `Model.fit`, which supports generators. score_gru = model_gru.fit_generator(generator_train, epochs=best_epochs, verbose=0, validation_data=generator_test)

Plot of Training and Test Loss Functions

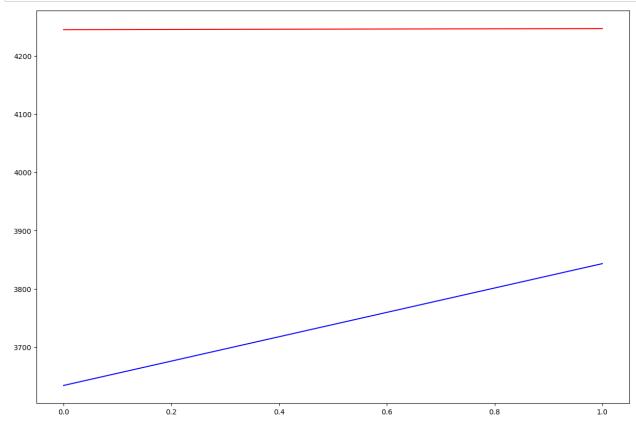


Predictions for Test Data

```
x, y = generator_test[i]
                 yhat = model_gru.predict(x, verbose=2)
                 # Inverse transform the scaled target values to their original scale
                 actual_gru = scaler.inverse_transform(y.reshape(-1, 1))[0][0]
                 prediction_gru = scaler.inverse_transform(yhat.reshape(-1, 1))[0][0]
                 df_result_gru = df_result_gru.append({'Actual': actual_gru, 'Prediction': prediction_gru}, ignore_index=Tr
              # Display the results
             print(df_result_gru)
             1/1 - 0s - 255ms/epoch - 255ms/step
              C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\258503522.py:9: FutureWarning: The frame.append method is d
              eprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_gru = df_result_gru.append({'Actual': actual_gru, 'Prediction': prediction_gru}, ignore_index=Tru
             1/1 - 0s - 272ms/epoch - 272ms/step
                     Actual Prediction Diff
             0 3634.059220 4244.892090
                                          NaN
             1 3843.221729 4246.791504
                                           NaN
             C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\258503522.py:9: FutureWarning: The frame.append method is d
              eprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_gru = df_result_gru.append({'Actual': actual_gru, 'Prediction': prediction_gru}, ignore_index=Tru
              e)
          Tabulating Actuals, Predictions and Differences
In [273]:
          # Tabulating Actuals, Predictions and Differences
             df_result_gru['Diff'] = 100 * (df_result_gru['Prediction'] - df_result_gru['Actual']) / df_result_gru['Actual'
In [275]:  print(df_result_gru)
                     Actual Prediction
              0 3634.059220 4244.892090 16.808556
             1 3843.221729 4246.791504 10.500819
          Calculating the Correctness for Test Data
In [276]: ▶ # Calculating the Correctness for Test Data
             mean_actual_gru = df_result_gru['Actual'].mean()
             mae_gru = (df_result_gru['Actual'] - df_result_gru['Prediction']).abs().mean()
             mae_percentage_gru = 100 * mae_gru / mean_actual_gru
             correctness_gru = 100 - mae_percentage_gru
             # Print the statistics
             print("Mean Actual: ", mean_actual_gru)
             print("Mean Absolute Error (MAE):", mae_gru)
             print("MAE/Mean ratio: ", mae_percentage_gru,"%")
             print("Correctness: ", correctness_gru,"%")
             Mean Actual: 3738.6404744654114
             Mean Absolute Error (MAE): 507.20132240958856
             MAE/Mean ratio: 13.566464223391614 %
              Correctness: 86.43353577660838 %
```

Plot of Actuals and Predictions for Test Data

```
In [277]:  # Plot of Actuals and Predictions for Test Data
    plt.figure(figsize=(15,10))
    plt.plot(df_result_gru['Actual'], color='blue')
    plt.plot(df_result_gru['Prediction'], color='red')
    plt.show()
```



Observations

Optimized Model 2 Train Data Statistics:

• MAE: 507.20

MAE/Mean Ratio: 13.57%Correctness: 86.43%

Predictions for Hold-Out Data

```
In [287]: ▶ # Predictions for Hold-Out Data
              df_result_hold = pd.DataFrame({'Actual': [], 'Prediction': []})
              for i in range(len(generator_hold)):
                  x, y = generator_hold[i]
                 yhat = model_gru.predict(x, verbose=2)
                  # Inverse transform the scaled target values to their original scale
                  actual_hold = scaler.inverse_transform(y.reshape(-1, 1))[0][0]
                 prediction_hold = scaler.inverse_transform(yhat.reshape(-1, 1))[0][0]
                  df_result_hold = df_result_hold.append({'Actual': actual_hold, 'Prediction': prediction_hold}, ignore_inde
              # Display the results
              print(df_result_hold)
              1/1 - 0s - 33ms/epoch - 33ms/step
              1/1 - 0s - 21ms/epoch - 21ms/step
                     Actual Prediction
              0 3928.315691 4237.564941
              1 3773.987610 4255.625977
              C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\1402261369.py:12: FutureWarning: The frame.append method is
              deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
                df_result_hold = df_result_hold.append({'Actual': actual_hold, 'Prediction': prediction_hold}, ignore_index
              =True)
              C:\Users\mulli\AppData\Local\Temp\ipykernel_18344\1402261369.py:12: FutureWarning: The frame.append method is
              deprecated and will be removed from pandas in a future version. Use pandas.concat instead.
               df_result_hold = df_result_hold.append({'Actual': actual_hold, 'Prediction': prediction_hold}, ignore_index
              =True)
```

Tabulating Actuals, Predictions and Differences for Hold-Out Data

```
In [289]: # Tabulating Actuals, Predictions and Differences for Hold-Out Data

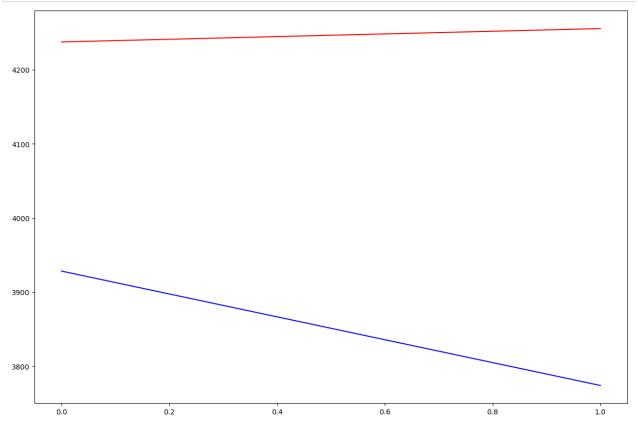
df_result_hold['Diff'] = 100 * (df_result_hold['Prediction'] - df_result_hold['Actual']) / df_result_hold['Actual'
```

Calculating the Correctness for Hold-Out Data

Plot of Actuals and Predictions for Hold-Out Data

Correctness: 89.73180378048244 %

```
In [291]: # Plot of Actuals and Predictions for Hold-Out Data
plt.figure(figsize=(15,10))
plt.plot(df_result_hold['Actual'], color='blue')
plt.plot(df_result_hold['Prediction'], color='red')
plt.show()
```



Observations

Optimized Model 2 Train Data Statistics:

• MAE: 395.44

MAE/Mean Ratio: 10.27%Correctness: 89.73%

Optimized Model 2 Overeall Observations

Mean Absolute Error (MAE):

Value: 395.44

Explanation: The MAE measures the average absolute difference between the actual and predicted values. In the context of Model 2 (GRU), an MAE of 395.44 indicates that, on average, the predictions made by the GRU model deviate from the actual values by approximately 395.44 units. Lower values of MAE indicate better predictive performance, as they signify smaller errors between predictions and actual observations.

MAE/Mean Ratio:

Value: 10.27%

Explanation: The MAE/Mean Ratio, or Mean Absolute Percentage Error (MAPE), expresses the MAE as a percentage of the mean of the actual values. In Model 2 (GRU), a ratio of 10.27% suggests that the average absolute error in predictions, relative to the mean of the actual values, is approximately 10.27%. Lower values indicate higher accuracy, as they represent smaller relative errors.

Correctness:

Value: 89.73%

Explanation: The Correctness metric represents the proportion of predictions that are considered correct, typically based on a predefined threshold or criterion. In Model 2, a correctness of 89.73% indicates that approximately 89.73% of the predictions made by the GRU model align with the actual observations. This metric provides a binary assessment of prediction accuracy, where higher values indicate a higher proportion of accurate predictions.

In summary, these evaluation metrics provide insights into the predictive performance of Model 2 based on its ability to minimize absolute errors, maintain low relative errors, and achieve correctness in its predictions. Compared to Model 1, Model 2 demonstrates significantly

Part X: Applications

Application to the Project:

Given the project's objective to develop predictive models for bike rental counts leveraging environmental and seasonal variables, the identification of Model 2 as the superior model holds significant implications for the project's success and outcomes:

Improved Predictive Accuracy: Incorporating Model 2 into the project's predictive modeling framework is expected to lead to higher accuracy in forecasting bike rental counts. This enhanced accuracy is crucial for meeting the project's objective of accurately predicting rental counts on an hourly or daily basis, considering factors such as weather conditions, seasonality, and temporal patterns.

Enhanced Decision Making: With Model 2 identified as the superior model, project stakeholders, including urban planners, transportation authorities, and bike sharing system operators, can confidently rely on its predictions for informed decision-making. Whether it's optimizing bike fleet management, allocating resources for maintenance and infrastructure, or planning promotional campaigns, the accurate predictions from Model 2 can provide valuable insights for strategic decision-making.

Event and Anomaly Detection: In the context of event detection and anomaly identification, Model 2's superior performance can significantly enhance the project's ability to detect and analyze significant urban events impacting bike rental behaviors. By leveraging Model 2's predictions alongside external data sources such as search engine queries or weather alerts, the project can develop robust algorithms for event detection and anomaly identification, contributing to a deeper understanding of urban dynamics and resilience.

Research and Insights: The identification of Model 2 as the superior model opens avenues for further research and analysis. By examining the underlying factors contributing to its superior performance, such as feature importance, model architecture, or data preprocessing techniques, the project can generate valuable insights into the dynamics of bike rental behaviors and the effectiveness of predictive analytics in urban transportation systems.

In summary, the recognition of Model 2 as the superior model in the context of the bike sharing predictive modeling project offers a pathway to enhanced predictive accuracy, informed decision-making, robust event detection capabilities, and valuable research insights, ultimately contributing to the advancement of predictive analytics in urban transportation systems.

In []: ▶	