MA678 Homework 7

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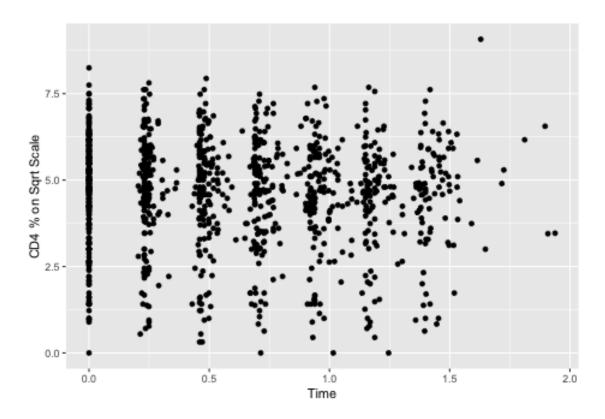
Data analysis

CD4 percentages for HIV infected kids

The folder cd4 has CD4 percentages for a set of young children with HIV who were measured several times over a period of two years. The dataset also includes the ages of the children at each measurement.

1. Graph the outcome (the CD4 percentage, on the square root scale) for each child as a function of time.

```
ggplot(hiv.data)+
  geom_point(aes(x=time,y=y))+
  labs(x ="Time", y = "CD4 % on Sqrt Scale")
```



2. Each child's data has a time course that can be summarized by a linear fit. Estimate these lines and plot them for all the children.

```
cd4_2 <- lm(y~time+factor(newpid)-1, data = hiv.data)
summary(cd4_2)</pre>
```

```
##
## Call:
  lm(formula = y ~ time + factor(newpid) - 1, data = hiv.data)
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
                                         Max
                    0.0000
##
   -3.6595 -0.3293
                             0.3347
                                     4.0036
##
##
  Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
## time
                      -0.38629
                                  0.05455
                                           -7.081 3.07e-12 ***
                                            13.078 < 2e-16 ***
## factor(newpid)1
                       4.56368
                                  0.34896
## factor(newpid)2
                       0.81507
                                  0.54578
                                             1.493 0.135716
                       5.95004
                                  0.29534
                                            20.146
                                                    < 2e-16 ***
## factor(newpid)3
## factor(newpid)4
                       5.61374
                                  0.31677
                                            17.722
                                                    < 2e-16 ***
## factor(newpid)5
                       4.00000
                                  0.77180
                                             5.183 2.76e-07 ***
## factor(newpid)6
                       5.36947
                                  0.31738
                                            16.918
                                                   < 2e-16 ***
                                                    < 2e-16 ***
                                  0.29436
                                            19.088
## factor(newpid)7
                       5.61896
## factor(newpid)8
                                            13.268
                                                    < 2e-16 ***
                       5.14703
                                  0.38791
## factor(newpid)9
                       6.21645
                                  0.34732
                                            17.898
                                                    < 2e-16 ***
## factor(newpid)10
                       5.71848
                                  0.31739
                                            18.017
                                                    < 2e-16 ***
## factor(newpid)11
                       2.44507
                                  0.29417
                                             8.312 3.89e-16 ***
## factor(newpid)12
                       4.36330
                                  0.31699
                                            13.765
                                                    < 2e-16 ***
## factor(newpid)13
                       5.33903
                                  0.44635
                                            11.962
                                                   < 2e-16 ***
## factor(newpid)14
                       3.00000
                                  0.77180
                                             3.887 0.000110 ***
## factor(newpid)15
                       5.24008
                                  0.31759
                                            16.499
                                                   < 2e-16 ***
## factor(newpid)16
                       2.39908
                                  0.38705
                                             6.198 9.03e-10 ***
## factor(newpid)17
                       6.10066
                                  0.31839
                                            19.161
                                                    < 2e-16 ***
                       6.02588
                                            17.412
## factor(newpid)18
                                  0.34608
                                                    < 2e-16 ***
## factor(newpid)19
                       4.10797
                                  0.38783
                                            10.592
                                                    < 2e-16 ***
## factor(newpid)20
                       5.00962
                                  0.44580
                                            11.237
                                                   < 2e-16 ***
## factor(newpid)21
                       5.00000
                                  0.77180
                                             6.478 1.60e-10 ***
## factor(newpid)22
                       6.16441
                                  0.77180
                                             7.987 4.66e-15 ***
## factor(newpid)23
                       1.59920
                                  0.34723
                                             4.606 4.76e-06 ***
## factor(newpid)24
                       4.81823
                                            10.772
                                                    < 2e-16 ***
                                  0.44728
## factor(newpid)25
                       4.76132
                                  0.31717
                                            15.012
                                                    < 2e-16 ***
                                            14.636
## factor(newpid)26
                       4.63303
                                  0.31656
                                                    < 2e-16 ***
## factor(newpid)27
                       4.38498
                                  0.31672
                                            13.845
                                                    < 2e-16 ***
                                                    < 2e-16 ***
## factor(newpid)28
                       5.65959
                                  0.54590
                                            10.367
                       4.52845
## factor(newpid)29
                                  0.38717
                                            11.696
                                                   < 2e-16 ***
                                             1.296 0.195454
## factor(newpid)30
                       1.00000
                                  0.77180
## factor(newpid)31
                       4.45824
                                  0.54608
                                             8.164 1.22e-15 ***
                       4.64821
                                            13.322
## factor(newpid)32
                                  0.34892
                                                   < 2e-16 ***
                       5.03494
                                  0.29431
                                            17.108
                                                    < 2e-16 ***
## factor(newpid)33
## factor(newpid)34
                       6.49167
                                  0.54579
                                            11.894
                                                    < 2e-16 ***
                       4.93661
                                  0.38757
                                            12.737
## factor(newpid)35
                                                    < 2e-16 ***
## factor(newpid)37
                       3.98526
                                  0.54579
                                             7.302 6.72e-13 ***
                       6.15939
                                            13.805
                                                    < 2e-16 ***
## factor(newpid)38
                                  0.44617
## factor(newpid)39
                       4.84721
                                  0.34613
                                            14.004 < 2e-16 ***
## factor(newpid)40
                       3.60555
                                  0.77180
                                             4.672 3.49e-06 ***
```

```
## factor(newpid)41
                       5.00000
                                   0.77180
                                             6.478 1.60e-10 ***
## factor(newpid)42
                       3.26132
                                   0.29446
                                            11.076
                                                    < 2e-16 ***
                                            16.759
## factor(newpid)43
                       4.93493
                                   0.29446
                                                     < 2e-16 ***
                       2.49104
                                             5.588 3.13e-08 ***
  factor(newpid)44
                                   0.44579
  factor(newpid)45
                       5.16288
                                   0.31782
                                            16.245
                                                     < 2e-16 ***
                                            11.010
                                                     < 2e-16 ***
## factor(newpid)46
                       3.50085
                                   0.31798
## factor(newpid)47
                       4.85968
                                   0.31796
                                            15.284
                                                     < 2e-16 ***
## factor(newpid)48
                       4.45407
                                   0.38739
                                            11.498
                                                     < 2e-16 ***
  factor(newpid)49
                       5.39827
                                   0.29437
                                            18.339
                                                     < 2e-16 ***
   factor(newpid)50
                       4.32745
                                   0.29426
                                            14.706
                                                     < 2e-16 ***
  factor(newpid)51
                       3.94551
                                   0.34618
                                            11.397
                                                     < 2e-16 ***
                                             6.109 1.54e-09 ***
  factor(newpid)52
                       1.79719
                                   0.29417
  factor(newpid)53
                       4.81554
                                   0.29411
                                            16.373
                                                    < 2e-16 ***
  factor(newpid)54
                       4.46903
                                   0.29419
                                            15.191
                                                     < 2e-16 ***
                       2.37752
                                             8.084 2.24e-15 ***
## factor(newpid)55
                                   0.29410
  factor(newpid)56
                       2.79201
                                   0.54578
                                             5.116 3.90e-07 ***
  factor(newpid)57
                       2.14991
                                   0.31692
                                             6.784 2.24e-11 ***
  factor(newpid)58
                       2.01600
                                   0.31692
                                             6.361 3.32e-10 ***
                                                    < 2e-16 ***
## factor(newpid)59
                       5.12724
                                   0.29440
                                            17.416
## factor(newpid)60
                       2.04462
                                   0.54578
                                             3.746 0.000192 ***
  factor(newpid)61
                       5.23903
                                   0.31671
                                            16.542
                                                     < 2e-16 ***
                       5.65826
                                   0.29448
                                            19.215
                                                     < 2e-16 ***
## factor(newpid)62
## factor(newpid)63
                       1.92512
                                   0.29426
                                             6.542 1.07e-10 ***
                       5.42219
## factor(newpid)64
                                   0.29418
                                            18.431
                                                     < 2e-16 ***
## factor(newpid)65
                       1.42126
                                   0.34611
                                             4.106 4.42e-05 ***
## factor(newpid)66
                       6.46556
                                   0.44592
                                            14.499
                                                    < 2e-16 ***
                       2.50677
                                   0.54579
                                             4.593 5.06e-06 ***
  factor(newpid)67
  factor(newpid)68
                       5.87367
                                   0.77180
                                             7.610 7.50e-14 ***
  factor(newpid)69
                       5.37708
                                   0.39062
                                            13.766
                                                    < 2e-16 ***
                       5.04789
                                   0.38676
                                            13.052
                                                    < 2e-16 ***
## factor(newpid)70
## factor(newpid)71
                       2.64575
                                   0.77180
                                             3.428 0.000638 ***
  factor(newpid)72
                       3.79504
                                   0.38672
                                             9.813
                                                     < 2e-16 ***
  factor(newpid)73
                       6.85565
                                   0.77180
                                             8.883
                                                     < 2e-16 ***
## factor(newpid)74
                       5.15287
                                   0.29412
                                            17.519
                                                     < 2e-16 ***
  factor(newpid)75
                       5.83766
                                   0.29416
                                            19.845
                                                     < 2e-16 ***
## factor(newpid)76
                       4.92242
                                   0.34748
                                            14.166
                                                     < 2e-16 ***
## factor(newpid)77
                       4.01660
                                   0.38672
                                            10.386
                                                     < 2e-16 ***
## factor(newpid)78
                       5.99278
                                   0.29415
                                            20.373
                                                     < 2e-16 ***
## factor(newpid)79
                       4.90326
                                   0.44575
                                            11.000
                                                     < 2e-16 ***
  factor(newpid)81
                       0.97153
                                   0.54589
                                             1.780 0.075492 .
## factor(newpid)82
                       3.25905
                                   0.34636
                                             9.409
                                                     < 2e-16 ***
  factor(newpid)83
                       0.94868
                                             1.229 0.219356
                                   0.77180
  factor(newpid)84
                       2.25870
                                   0.34701
                                             6.509 1.32e-10 ***
                       1.58969
                                             4.581 5.36e-06 ***
   factor(newpid)85
                                   0.34705
## factor(newpid)86
                       6.44121
                                   0.34644
                                            18.593
                                                     < 2e-16 ***
                                                     < 2e-16 ***
                       6.09731
                                            20.724
## factor(newpid)87
                                   0.29421
  factor(newpid)88
                       4.83296
                                   0.54579
                                             8.855
                                                     < 2e-16 ***
  factor(newpid)89
                       5.02052
                                   0.34621
                                            14.501
                                                     < 2e-16 ***
## factor(newpid)90
                       5.84808
                                   0.77180
                                             7.577 9.53e-14 ***
  factor(newpid)91
                       2.54897
                                   0.38706
                                             6.586 8.09e-11 ***
  factor(newpid)92
                       2.68623
                                   0.54579
                                             4.922 1.04e-06 ***
## factor(newpid)93
                       1.52443
                                   0.38637
                                             3.945 8.64e-05 ***
## factor(newpid)94
                       4.94328
                                   0.44775
                                            11.040 < 2e-16 ***
## factor(newpid)95
                       2.78151
                                   0.54578
                                             5.096 4.30e-07 ***
```

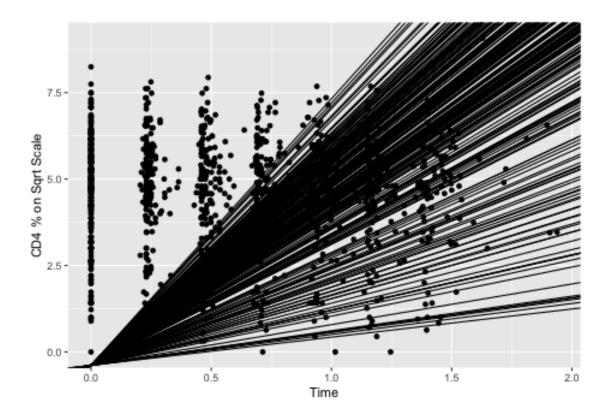
```
## factor(newpid)96
                       4.89898
                                   0.77180
                                             6.347 3.62e-10 ***
## factor(newpid)97
                       7.70878
                                   0.44671
                                            17.257
                                                    < 2e-16 ***
                                             6.214 8.22e-10 ***
## factor(newpid)98
                       4.79583
                                   0.77180
## factor(newpid)99
                       6.58753
                                   0.38674
                                            17.033
                                                    < 2e-16 ***
## factor(newpid)100
                       6.54584
                                   0.34609
                                            18.914
                                                    < 2e-16 ***
                                             7.329 5.54e-13 ***
## factor(newpid)101
                       5.65685
                                   0.77180
                                            20.708
                                                    < 2e-16 ***
## factor(newpid)103
                       6.11117
                                   0.29512
                                            11.230
                                                    < 2e-16 ***
## factor(newpid)104
                       3.55877
                                   0.31688
  factor(newpid)105
                       4.66845
                                   0.29461
                                            15.846
                                                    < 2e-16 ***
  factor(newpid)106
                       3.79964
                                   0.38686
                                             9.822
                                                    < 2e-16 ***
## factor(newpid)107
                       5.79041
                                   0.38686
                                            14.968
                                                    < 2e-16 ***
                       1.17737
                                             3.039 0.002447 **
## factor(newpid)108
                                   0.38739
## factor(newpid)109
                       4.04447
                                   0.54579
                                             7.410 3.13e-13 ***
## factor(newpid)110
                       5.32304
                                   0.29448
                                            18.076
                                                   < 2e-16 ***
                       2.13749
                                             3.916 9.74e-05 ***
## factor(newpid)111
                                   0.54580
## factor(newpid)112
                       4.04681
                                   0.29465
                                            13.734
                                                    < 2e-16 ***
## factor(newpid)113
                       6.34488
                                   0.31739
                                            19.991
                                                    < 2e-16 ***
## factor(newpid)114
                       4.95064
                                   0.29459
                                            16.805
                                                    < 2e-16 ***
                                            19.113
## factor(newpid)115
                       5.62952
                                   0.29454
                                                    < 2e-16 ***
## factor(newpid)116
                       4.25683
                                   0.54612
                                             7.795 1.95e-14 ***
## factor(newpid)117
                       4.41240
                                   0.34852
                                            12.660
                                                    < 2e-16 ***
## factor(newpid)118
                       5.31355
                                   0.34636
                                            15.341
                                                    < 2e-16 ***
                                             3.534 0.000432 ***
## factor(newpid)119
                       1.92914
                                   0.54582
## factor(newpid)120
                       6.83535
                                   0.31712
                                            21.555
                                                    < 2e-16 ***
## factor(newpid)121
                       6.12904
                                   0.44703
                                            13.711
                                                    < 2e-16 ***
## factor(newpid)122
                       5.43379
                                   0.44651
                                            12.169
                                                    < 2e-16 ***
## factor(newpid)123
                       2.96695
                                   0.54578
                                             5.436 7.18e-08 ***
## factor(newpid)124
                       3.16228
                                   0.77180
                                             4.097 4.60e-05 ***
                                            11.567
                                                    < 2e-16 ***
## factor(newpid)126
                       4.48243
                                   0.38753
## factor(newpid)127
                       5.25547
                                   0.34628
                                            15.177
                                                    < 2e-16 ***
## factor(newpid)128
                       4.75350
                                   0.54668
                                             8.695
                                                    < 2e-16 ***
## factor(newpid)129
                       0.97864
                                   0.34636
                                             2.825 0.004836 **
## factor(newpid)130
                       3.70472
                                   0.38672
                                             9.580
                                                     < 2e-16 ***
                       4.25708
                                            10.997
## factor(newpid)131
                                   0.38711
                                                     < 2e-16 ***
## factor(newpid)132
                       4.73853
                                   0.38778
                                            12.220
                                                    < 2e-16 ***
                                            11.918
                                                    < 2e-16 ***
## factor(newpid)133
                       3.77490
                                   0.31673
## factor(newpid)134
                       6.72519
                                   0.29422
                                            22.858
                                                     < 2e-16 ***
## factor(newpid)135
                       5.60776
                                   0.29440
                                            19.048
                                                     < 2e-16 ***
## factor(newpid)136
                       6.64977
                                   0.29433
                                            22.593
                                                     < 2e-16 ***
                                            19.261
## factor(newpid)137
                       5.67273
                                   0.29452
                                                     < 2e-16 ***
## factor(newpid)138
                       7.48331
                                   0.77180
                                             9.696
                                                     < 2e-16 ***
## factor(newpid)139
                       4.85189
                                   0.29479
                                            16.459
                                                    < 2e-16 ***
## factor(newpid)140
                       5.47249
                                   0.29452
                                            18.581
                                                    < 2e-16 ***
## factor(newpid)141
                       7.16773
                                   0.29440
                                            24.347
                                                     < 2e-16 ***
## factor(newpid)142
                       2.82420
                                   0.31707
                                             8.907
                                                     < 2e-16 ***
                                                    < 2e-16 ***
                       2.88106
                                   0.29437
                                             9.787
## factor(newpid)143
## factor(newpid)144
                       6.04833
                                   0.29423
                                            20.556
                                                    < 2e-16 ***
## factor(newpid)145
                       5.55106
                                   0.31688
                                            17.518
                                                    < 2e-16 ***
                                   0.31677
## factor(newpid)146
                       5.46320
                                            17.246
                                                    < 2e-16 ***
## factor(newpid)147
                       6.18166
                                   0.34655
                                            17.838
                                                    < 2e-16 ***
                                            11.988
                                                    < 2e-16 ***
  factor(newpid)148
                       5.34407
                                   0.44578
## factor(newpid)149
                       5.67007
                                   0.34615
                                            16.381
                                                    < 2e-16 ***
                       4.39422
## factor(newpid)150
                                   0.38642
                                            11.372
                                                    < 2e-16 ***
## factor(newpid)151
                       5.68779
                                   0.38640
                                            14.720
                                                    < 2e-16 ***
```

```
## factor(newpid)152
                       4.61519
                                   0.77180
                                             5.980 3.33e-09 ***
## factor(newpid)153
                       7.21403
                                   0.44577
                                            16.183
                                                    < 2e-16 ***
## factor(newpid)154
                       5.71394
                                   0.44580
                                            12.817
                                                     < 2e-16 ***
## factor(newpid)155
                       6.27073
                                   0.44579
                                            14.067
                                                     < 2e-16 ***
## factor(newpid)156
                       6.34439
                                   0.54578
                                            11.624
                                                    < 2e-16 ***
                                            14.371
## factor(newpid)157
                       6.41098
                                   0.44609
                                                    < 2e-16 ***
## factor(newpid)158
                       6.08632
                                   0.34692
                                            17.544
                                                    < 2e-16 ***
## factor(newpid)159
                       5.29916
                                   0.54594
                                             9.706
                                                    < 2e-16 ***
  factor(newpid)160
                       5.04712
                                   0.54579
                                             9.247
                                                     < 2e-16 ***
  factor(newpid)161
                       5.14072
                                   0.38657
                                            13.298
                                                    < 2e-16 ***
## factor(newpid)162
                       4.69277
                                   0.44588
                                            10.525
                                                     < 2e-16 ***
                       7.42011
                                            19.200
## factor(newpid)163
                                   0.38647
                                                    < 2e-16 ***
## factor(newpid)164
                       7.07418
                                   0.34873
                                            20.286
                                                    < 2e-16 ***
## factor(newpid)165
                       4.40042
                                   0.34744
                                            12.665
                                                    < 2e-16 ***
                       5.63845
                                            10.287
                                                     < 2e-16 ***
## factor(newpid)166
                                   0.54812
## factor(newpid)167
                       4.93276
                                   0.38713
                                            12.742
                                                    < 2e-16 ***
## factor(newpid)168
                       5.79989
                                   0.29425
                                            19.711
                                                    < 2e-16 ***
## factor(newpid)169
                       2.83271
                                   0.54605
                                             5.188 2.69e-07 ***
                       4.52041
                                            13.039
## factor(newpid)170
                                   0.34670
                                                    < 2e-16 ***
## factor(newpid)171
                       6.70820
                                   0.77180
                                             8.692
                                                    < 2e-16 ***
## factor(newpid)172
                       5.26891
                                   0.34643
                                            15.209
                                                    < 2e-16 ***
## factor(newpid)173
                                   0.54592
                                             2.924 0.003551 **
                       1.59625
                                            10.970
                                                    < 2e-16 ***
## factor(newpid)174
                       3.80765
                                   0.34709
                                            16.939
                                                    < 2e-16 ***
## factor(newpid)175
                       5.86770
                                   0.34640
## factor(newpid)176
                       5.71388
                                   0.44591
                                            12.814
                                                    < 2e-16 ***
## factor(newpid)177
                       4.65448
                                   0.38715
                                            12.022
                                                    < 2e-16 ***
## factor(newpid)178
                       6.64100
                                   0.34712
                                            19.132
                                                    < 2e-16 ***
## factor(newpid)179
                       5.42868
                                   0.44577
                                            12.178
                                                    < 2e-16 ***
                                   0.29417
                                            18.297
                                                    < 2e-16 ***
## factor(newpid)180
                       5.38254
## factor(newpid)181
                       7.58231
                                   0.31737
                                            23.891
                                                    < 2e-16 ***
## factor(newpid)182
                       6.87445
                                   0.44674
                                            15.388
                                                    < 2e-16 ***
## factor(newpid)183
                       4.73226
                                   0.54591
                                             8.669
                                                    < 2e-16 ***
## factor(newpid)184
                       4.69042
                                   0.77180
                                             6.077 1.87e-09 ***
                       5.32106
## factor(newpid)185
                                   0.31790
                                            16.738
                                                    < 2e-16 ***
## factor(newpid)186
                       2.26637
                                   0.34754
                                             6.521 1.22e-10 ***
                                            18.743
                                                    < 2e-16 ***
## factor(newpid)187
                       5.96108
                                   0.31804
## factor(newpid)188
                       5.64729
                                   0.34676
                                            16.286
                                                    < 2e-16 ***
## factor(newpid)189
                       0.89556
                                   0.54589
                                             1.641 0.101277
## factor(newpid)190
                       3.93221
                                   0.54593
                                             7.203 1.34e-12 ***
                                            10.611
## factor(newpid)191
                       4.73072
                                   0.44582
                                                    < 2e-16 ***
## factor(newpid)192
                       4.63493
                                   0.29415
                                            15.757
                                                    < 2e-16 ***
## factor(newpid)193
                       3.51569
                                   0.29414
                                            11.952
                                                    < 2e-16 ***
## factor(newpid)194
                       1.67399
                                   0.31665
                                             5.286 1.60e-07 ***
## factor(newpid)195
                       6.57259
                                            14.701
                                                    < 2e-16 ***
                                   0.44708
## factor(newpid)196
                       4.28686
                                   0.38778
                                            11.055
                                                    < 2e-16 ***
                                                    < 2e-16 ***
## factor(newpid)197
                       4.52015
                                            11.692
                                   0.38659
## factor(newpid)198
                       6.11686
                                   0.34677
                                            17.640
                                                    < 2e-16 ***
                                             9.247
## factor(newpid)199
                       3.58154
                                   0.38734
                                                     < 2e-16 ***
                                   0.31871
## factor(newpid)200
                       6.33062
                                            19.863
                                                    < 2e-16 ***
## factor(newpid)201
                       4.88817
                                   0.38837
                                            12.586
                                                    < 2e-16 ***
                                            11.144
                                                    < 2e-16 ***
  factor(newpid)202
                       6.08433
                                   0.54598
## factor(newpid)203
                       6.31594
                                   0.38792
                                            16.282
                                                    < 2e-16 ***
## factor(newpid)204
                       5.44066
                                   0.38672
                                            14.069
                                                    < 2e-16 ***
## factor(newpid)205
                       3.66210
                                   0.34771
                                            10.532
                                                    < 2e-16 ***
```

```
## factor(newpid)206
                      5.98915
                                  0.29415
                                           20.361
                                                    < 2e-16 ***
## factor(newpid)207
                      6.08204
                                  0.31761
                                           19.149
                                                   < 2e-16 ***
                                           12.010
## factor(newpid)208
                      4.17020
                                  0.34723
                                                    < 2e-16 ***
## factor(newpid)209
                      6.43027
                                  0.31684
                                           20.295
                                                    < 2e-16 ***
## factor(newpid)210
                      5.21148
                                  0.29412
                                           17.719
                                                    < 2e-16 ***
                                           18.167
## factor(newpid)211
                      5.34459
                                  0.29419
                                                    < 2e-16 ***
## factor(newpid)212
                      5.21535
                                  0.31670
                                           16.468
                                                    < 2e-16 ***
## factor(newpid)213
                      4.67607
                                  0.44578
                                           10.490
                                                    < 2e-16 ***
## factor(newpid)214
                      6.54179
                                  0.29428
                                           22.230
                                                   < 2e-16 ***
## factor(newpid)215
                      5.04463
                                  0.31666
                                           15.931
                                                   < 2e-16 ***
## factor(newpid)216
                      3.74901
                                  0.34628
                                           10.827
                                                    < 2e-16 ***
                      3.09943
                                            5.679 1.88e-08 ***
## factor(newpid)217
                                  0.54578
## factor(newpid)218
                      4.76821
                                  0.29420
                                           16,207
                                                   < 2e-16 ***
                                            7.097 2.76e-12 ***
## factor(newpid)219
                      5.47723
                                  0.77180
                      6.34478
                                           21.564
                                                   < 2e-16 ***
## factor(newpid)220
                                  0.29424
## factor(newpid)221
                      5.78464
                                  0.31662
                                           18.270
                                                    < 2e-16 ***
## factor(newpid)222
                      5.27235
                                  0.31785
                                           16.587
                                                    < 2e-16 ***
## factor(newpid)223
                      5.34864
                                  0.31661
                                           16.894
                                                   < 2e-16 ***
                                            6.978 6.19e-12 ***
## factor(newpid)224
                      3.80821
                                  0.54578
## factor(newpid)225
                      6.47400
                                  0.29413
                                           22.010
                                                   < 2e-16 ***
## factor(newpid)226
                      6.85178
                                  0.34695
                                           19.748
                                                   < 2e-16 ***
                                           19.631
                                                    < 2e-16 ***
## factor(newpid)227
                      6.21616
                                  0.31664
                                           14.758
                                                    < 2e-16 ***
## factor(newpid)228
                      4.67312
                                  0.31665
                      5.25787
## factor(newpid)229
                                  0.34628
                                           15.184
                                                   < 2e-16 ***
## factor(newpid)230
                      5.96217
                                  0.34628
                                           17.218
                                                   < 2e-16 ***
## factor(newpid)231
                      5.95432
                                  0.38653
                                           15.405
                                                    < 2e-16 ***
## factor(newpid)232
                      6.17519
                                  0.44620
                                           13.840
                                                   < 2e-16 ***
## factor(newpid)233
                      4.36377
                                  0.38636
                                           11.295
                                                   < 2e-16 ***
## factor(newpid)234
                      6.22240
                                  0.54578
                                           11.401
                                                   < 2e-16 ***
## factor(newpid)235
                      3.21066
                                  0.44635
                                            7.193 1.43e-12 ***
## factor(newpid)236
                      2.83698
                                  0.34674
                                            8.182 1.06e-15 ***
## factor(newpid)237
                      5.43365
                                  0.31707
                                           17.137
                                                    < 2e-16 ***
## factor(newpid)238
                      5.05647
                                  0.38660
                                           13.079
                                                    < 2e-16 ***
                      5.54035
                                           12.424
## factor(newpid)239
                                  0.44593
                                                   < 2e-16 ***
## factor(newpid)240
                      3.51138
                                  0.34603
                                           10.148
                                                   < 2e-16 ***
                                            7.924 7.49e-15 ***
## factor(newpid)241
                      6.11555
                                  0.77180
## factor(newpid)242
                      5.16910
                                  0.44592
                                           11.592
                                                   < 2e-16 ***
## factor(newpid)243
                      5.89800
                                           13.213
                                                    < 2e-16 ***
                                  0.44636
## factor(newpid)244
                      5.94175
                                           10.887
                                                    < 2e-16 ***
                                  0.54578
                                           12.745
## factor(newpid)245
                      4.92484
                                  0.38641
                                                   < 2e-16 ***
## factor(newpid)246
                      5.05558
                                  0.54579
                                            9.263
                                                   < 2e-16 ***
## factor(newpid)247
                      4.78539
                                  0.77180
                                            6.200 8.92e-10 ***
## factor(newpid)248
                      5.64132
                                  0.54579
                                           10.336
                                                   < 2e-16 ***
## factor(newpid)249
                      5.59464
                                            7.249 9.71e-13 ***
                                  0.77180
## factor(newpid)250
                      5.83524
                                  0.54579
                                           10.691 < 2e-16 ***
## factor(newpid)251
                      3.74166
                                            4.848 1.49e-06 ***
                                  0.77180
## factor(newpid)252
                      4.51291
                                  0.54582
                                            8.268 5.45e-16 ***
## factor(newpid)253
                      3.60555
                                  0.77180
                                            4.672 3.49e-06 ***
## factor(newpid)254
                      3.75520
                                  0.54598
                                            6.878 1.20e-11 ***
##
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.7718 on 821 degrees of freedom
## Multiple R-squared: 0.9809, Adjusted R-squared: 0.9751
```

```
## F-statistic: 168.1 on 251 and 821 DF, p-value: < 2.2e-16
```

```
ggplot(aes(x=time, y=y), data = hiv.data)+
geom_point()+
geom_abline(intercept = coef(cd4_2)[1], slope=coef(cd4_2)[2:length(coef(cd4_2))]) +
labs(x = "Time", y = "CD4 % on Sqrt Scale")
```



3. Set up a model for the children's slopes and intercepts as a function of the treatment and age at baseline. Estimate this model using the two-step procedure–first estimate the intercept and slope separately for each child, then fit the between-child models using the point estimates from the first step.

```
cd4_3 <- lm(y~time+factor(newpid)-1, data = hiv.data)
summary(cd4_3)</pre>
```

```
##
## Call:
## lm(formula = y ~ time + factor(newpid) - 1, data = hiv.data)
##
##
  Residuals:
##
                1Q
                    Median
                                 3Q
                                        Max
  -3.6595 -0.3293
                    0.0000 0.3347
                                     4.0036
##
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## time
                     -0.38629
                                  0.05455
                                           -7.081 3.07e-12 ***
## factor(newpid)1
                      4.56368
                                  0.34896
                                           13.078 < 2e-16 ***
## factor(newpid)2
                                            1.493 0.135716
                      0.81507
                                  0.54578
```

```
## factor(newpid)3
                       5.95004
                                   0.29534
                                            20.146
                                                    < 2e-16 ***
                                                    < 2e-16 ***
## factor(newpid)4
                       5.61374
                                   0.31677
                                            17.722
                                             5.183 2.76e-07 ***
## factor(newpid)5
                       4.00000
                                   0.77180
                                   0.31738
                                            16.918
                                                     < 2e-16 ***
## factor(newpid)6
                       5.36947
## factor(newpid)7
                       5.61896
                                   0.29436
                                            19.088
                                                     < 2e-16 ***
                                            13.268
## factor(newpid)8
                       5.14703
                                   0.38791
                                                     < 2e-16 ***
## factor(newpid)9
                       6.21645
                                   0.34732
                                            17.898
                                                     < 2e-16 ***
## factor(newpid)10
                       5.71848
                                   0.31739
                                            18.017
                                                     < 2e-16 ***
  factor(newpid)11
                       2.44507
                                   0.29417
                                             8.312 3.89e-16 ***
                                                     < 2e-16 ***
   factor(newpid)12
                       4.36330
                                   0.31699
                                            13.765
## factor(newpid)13
                       5.33903
                                   0.44635
                                            11.962
                                                     < 2e-16 ***
                                             3.887 0.000110 ***
  factor(newpid)14
                       3.00000
                                   0.77180
  factor(newpid)15
                       5.24008
                                   0.31759
                                            16.499
                                                     < 2e-16 ***
                                             6.198 9.03e-10 ***
## factor(newpid)16
                       2.39908
                                   0.38705
                                                     < 2e-16 ***
## factor(newpid)17
                       6.10066
                                   0.31839
                                            19.161
## factor(newpid)18
                       6.02588
                                   0.34608
                                            17.412
                                                     < 2e-16 ***
  factor(newpid)19
                       4.10797
                                            10.592
                                                     < 2e-16 ***
                                   0.38783
  factor(newpid)20
                       5.00962
                                   0.44580
                                            11.237
                                                     < 2e-16 ***
                       5.00000
## factor(newpid)21
                                   0.77180
                                             6.478 1.60e-10 ***
## factor(newpid)22
                       6.16441
                                   0.77180
                                             7.987 4.66e-15 ***
## factor(newpid)23
                       1.59920
                                   0.34723
                                             4.606 4.76e-06 ***
                                            10.772
                                                     < 2e-16 ***
## factor(newpid)24
                       4.81823
                                   0.44728
                                            15.012
                                                     < 2e-16 ***
## factor(newpid)25
                       4.76132
                                   0.31717
                                            14.636
## factor(newpid)26
                       4.63303
                                   0.31656
                                                     < 2e-16 ***
## factor(newpid)27
                       4.38498
                                   0.31672
                                            13.845
                                                     < 2e-16 ***
## factor(newpid)28
                       5.65959
                                   0.54590
                                            10.367
                                                     < 2e-16 ***
                       4.52845
                                            11.696
                                                     < 2e-16 ***
## factor(newpid)29
                                   0.38717
## factor(newpid)30
                       1.00000
                                   0.77180
                                             1.296 0.195454
                                             8.164 1.22e-15 ***
## factor(newpid)31
                       4.45824
                                   0.54608
## factor(newpid)32
                       4.64821
                                   0.34892
                                            13.322
                                                     < 2e-16 ***
## factor(newpid)33
                       5.03494
                                   0.29431
                                            17.108
                                                     < 2e-16 ***
  factor(newpid)34
                       6.49167
                                   0.54579
                                            11.894
                                                     < 2e-16 ***
  factor(newpid)35
                       4.93661
                                   0.38757
                                            12.737
                                                     < 2e-16 ***
                                             7.302 6.72e-13 ***
## factor(newpid)37
                       3.98526
                                   0.54579
## factor(newpid)38
                       6.15939
                                   0.44617
                                            13.805
                                                     < 2e-16 ***
                                                    < 2e-16 ***
## factor(newpid)39
                       4.84721
                                   0.34613
                                            14.004
## factor(newpid)40
                       3.60555
                                   0.77180
                                             4.672 3.49e-06 ***
## factor(newpid)41
                       5.00000
                                   0.77180
                                             6.478 1.60e-10 ***
## factor(newpid)42
                       3.26132
                                   0.29446
                                            11.076
                                                     < 2e-16 ***
                                            16.759
  factor(newpid)43
                       4.93493
                                   0.29446
                                                     < 2e-16 ***
## factor(newpid)44
                       2.49104
                                   0.44579
                                             5.588 3.13e-08 ***
  factor(newpid)45
                       5.16288
                                   0.31782
                                            16.245
                                                     < 2e-16 ***
  factor(newpid)46
                       3.50085
                                   0.31798
                                            11.010
                                                     < 2e-16 ***
                       4.85968
                                   0.31796
                                            15.284
                                                     < 2e-16 ***
   factor(newpid)47
## factor(newpid)48
                       4.45407
                                   0.38739
                                            11.498
                                                     < 2e-16 ***
                                            18.339
                                                     < 2e-16 ***
## factor(newpid)49
                       5.39827
                                   0.29437
## factor(newpid)50
                       4.32745
                                   0.29426
                                            14.706
                                                     < 2e-16 ***
  factor(newpid)51
                       3.94551
                                   0.34618
                                            11.397
                                                     < 2e-16 ***
## factor(newpid)52
                       1.79719
                                   0.29417
                                             6.109 1.54e-09 ***
## factor(newpid)53
                       4.81554
                                   0.29411
                                            16.373
                                                    < 2e-16 ***
                                                     < 2e-16 ***
  factor(newpid)54
                       4.46903
                                   0.29419
                                            15.191
## factor(newpid)55
                       2.37752
                                   0.29410
                                             8.084 2.24e-15 ***
## factor(newpid)56
                       2.79201
                                   0.54578
                                             5.116 3.90e-07 ***
## factor(newpid)57
                       2.14991
                                   0.31692
                                             6.784 2.24e-11 ***
```

```
## factor(newpid)58
                       2.01600
                                   0.31692
                                             6.361 3.32e-10 ***
## factor(newpid)59
                       5.12724
                                   0.29440
                                            17.416
                                                    < 2e-16 ***
                                             3.746 0.000192 ***
## factor(newpid)60
                       2.04462
                                   0.54578
                       5.23903
                                            16.542
                                                     < 2e-16 ***
  factor(newpid)61
                                   0.31671
## factor(newpid)62
                       5.65826
                                   0.29448
                                            19.215
                                                     < 2e-16 ***
                                             6.542 1.07e-10 ***
## factor(newpid)63
                       1.92512
                                   0.29426
## factor(newpid)64
                       5.42219
                                   0.29418
                                            18.431
                                                    < 2e-16 ***
## factor(newpid)65
                       1.42126
                                   0.34611
                                             4.106 4.42e-05 ***
  factor(newpid)66
                       6.46556
                                   0.44592
                                            14.499
                                                     < 2e-16 ***
   factor(newpid)67
                       2.50677
                                   0.54579
                                             4.593 5.06e-06 ***
## factor(newpid)68
                       5.87367
                                   0.77180
                                             7.610 7.50e-14 ***
  factor(newpid)69
                       5.37708
                                   0.39062
                                            13.766
                                                    < 2e-16 ***
  factor(newpid)70
                       5.04789
                                   0.38676
                                            13.052
                                                    < 2e-16 ***
## factor(newpid)71
                       2.64575
                                   0.77180
                                             3.428 0.000638 ***
                       3.79504
                                   0.38672
                                                     < 2e-16 ***
## factor(newpid)72
                                             9.813
## factor(newpid)73
                       6.85565
                                   0.77180
                                             8.883
                                                     < 2e-16 ***
  factor(newpid)74
                                            17.519
                                                     < 2e-16 ***
                       5.15287
                                   0.29412
## factor(newpid)75
                       5.83766
                                   0.29416
                                            19.845
                                                     < 2e-16 ***
## factor(newpid)76
                       4.92242
                                   0.34748
                                            14.166
                                                     < 2e-16 ***
## factor(newpid)77
                       4.01660
                                   0.38672
                                            10.386
                                                     < 2e-16 ***
## factor(newpid)78
                       5.99278
                                   0.29415
                                            20.373
                                                     < 2e-16 ***
                       4.90326
                                                     < 2e-16 ***
## factor(newpid)79
                                   0.44575
                                            11.000
                                             1.780 0.075492
## factor(newpid)81
                       0.97153
                                   0.54589
## factor(newpid)82
                       3.25905
                                   0.34636
                                             9.409
                                                     < 2e-16 ***
## factor(newpid)83
                       0.94868
                                   0.77180
                                             1.229 0.219356
## factor(newpid)84
                       2.25870
                                   0.34701
                                             6.509 1.32e-10 ***
## factor(newpid)85
                                   0.34705
                                             4.581 5.36e-06 ***
                       1.58969
## factor(newpid)86
                       6.44121
                                   0.34644
                                            18.593
                                                     < 2e-16 ***
                                            20.724
                                                     < 2e-16 ***
## factor(newpid)87
                       6.09731
                                   0.29421
## factor(newpid)88
                       4.83296
                                   0.54579
                                             8.855
                                                     < 2e-16 ***
## factor(newpid)89
                       5.02052
                                   0.34621
                                            14.501
                                                     < 2e-16 ***
  factor(newpid)90
                       5.84808
                                   0.77180
                                             7.577 9.53e-14 ***
  factor(newpid)91
                       2.54897
                                   0.38706
                                             6.586 8.09e-11 ***
                                             4.922 1.04e-06 ***
## factor(newpid)92
                       2.68623
                                   0.54579
## factor(newpid)93
                       1.52443
                                   0.38637
                                             3.945 8.64e-05 ***
## factor(newpid)94
                       4.94328
                                   0.44775
                                            11.040
                                                    < 2e-16 ***
## factor(newpid)95
                       2.78151
                                   0.54578
                                             5.096 4.30e-07 ***
## factor(newpid)96
                       4.89898
                                   0.77180
                                             6.347 3.62e-10 ***
## factor(newpid)97
                       7.70878
                                            17.257
                                                     < 2e-16 ***
                                   0.44671
                                             6.214 8.22e-10 ***
  factor(newpid)98
                       4.79583
                                   0.77180
## factor(newpid)99
                       6.58753
                                   0.38674
                                            17.033
                                                     < 2e-16 ***
  factor(newpid)100
                       6.54584
                                   0.34609
                                            18.914
                                                     < 2e-16 ***
  factor(newpid)101
                       5.65685
                                   0.77180
                                             7.329 5.54e-13 ***
                                   0.29512
                                            20.708
                                                    < 2e-16 ***
   factor(newpid)103
                       6.11117
## factor(newpid)104
                       3.55877
                                   0.31688
                                            11.230
                                                     < 2e-16 ***
                                            15.846
                                                     < 2e-16 ***
## factor(newpid)105
                       4.66845
                                   0.29461
  factor(newpid)106
                       3.79964
                                   0.38686
                                             9.822
                                                     < 2e-16 ***
  factor(newpid)107
                       5.79041
                                   0.38686
                                            14.968
                                                    < 2e-16 ***
## factor(newpid)108
                       1.17737
                                   0.38739
                                             3.039 0.002447 **
  factor(newpid)109
                       4.04447
                                   0.54579
                                             7.410 3.13e-13 ***
  factor(newpid)110
                       5.32304
                                   0.29448
                                            18.076
                                                     < 2e-16 ***
## factor(newpid)111
                       2.13749
                                   0.54580
                                             3.916 9.74e-05 ***
## factor(newpid)112
                       4.04681
                                   0.29465
                                            13.734
                                                    < 2e-16 ***
## factor(newpid)113
                       6.34488
                                   0.31739
                                            19.991
                                                    < 2e-16 ***
```

```
## factor(newpid)114
                       4.95064
                                   0.29459
                                            16.805
                                                    < 2e-16 ***
## factor(newpid)115
                                                    < 2e-16 ***
                       5.62952
                                   0.29454
                                            19.113
                                             7.795 1.95e-14 ***
## factor(newpid)116
                       4.25683
                                   0.54612
## factor(newpid)117
                       4.41240
                                   0.34852
                                            12.660
                                                    < 2e-16 ***
## factor(newpid)118
                       5.31355
                                   0.34636
                                            15.341
                                                     < 2e-16 ***
                       1.92914
                                             3.534 0.000432 ***
## factor(newpid)119
                                   0.54582
## factor(newpid)120
                       6.83535
                                   0.31712
                                            21.555
                                                    < 2e-16 ***
## factor(newpid)121
                       6.12904
                                   0.44703
                                            13.711
                                                    < 2e-16 ***
  factor(newpid)122
                       5.43379
                                   0.44651
                                            12.169
                                                    < 2e-16 ***
   factor(newpid)123
                       2.96695
                                   0.54578
                                             5.436 7.18e-08 ***
## factor(newpid)124
                       3.16228
                                   0.77180
                                             4.097 4.60e-05 ***
                                   0.38753
## factor(newpid)126
                       4.48243
                                            11.567
                                                    < 2e-16 ***
  factor(newpid)127
                       5.25547
                                   0.34628
                                            15,177
                                                    < 2e-16 ***
## factor(newpid)128
                       4.75350
                                   0.54668
                                             8.695
                                                    < 2e-16 ***
                       0.97864
                                             2.825 0.004836 **
## factor(newpid)129
                                   0.34636
  factor(newpid)130
                       3.70472
                                   0.38672
                                             9.580
                                                    < 2e-16 ***
                       4.25708
  factor(newpid)131
                                   0.38711
                                            10.997
                                                    < 2e-16 ***
  factor(newpid)132
                       4.73853
                                   0.38778
                                            12.220
                                                     < 2e-16 ***
                       3.77490
                                            11.918
## factor(newpid)133
                                   0.31673
                                                    < 2e-16 ***
## factor(newpid)134
                       6.72519
                                   0.29422
                                            22.858
                                                    < 2e-16 ***
## factor(newpid)135
                       5.60776
                                   0.29440
                                            19.048
                                                    < 2e-16 ***
                                   0.29433
                                            22.593
                                                     < 2e-16 ***
## factor(newpid)136
                       6.64977
                                            19.261
                                                     < 2e-16 ***
## factor(newpid)137
                       5.67273
                                   0.29452
                                             9.696
## factor(newpid)138
                       7.48331
                                   0.77180
                                                     < 2e-16 ***
## factor(newpid)139
                       4.85189
                                   0.29479
                                            16.459
                                                    < 2e-16 ***
## factor(newpid)140
                       5.47249
                                   0.29452
                                            18.581
                                                     < 2e-16 ***
## factor(newpid)141
                       7.16773
                                   0.29440
                                            24.347
                                                     < 2e-16 ***
## factor(newpid)142
                       2.82420
                                   0.31707
                                             8.907
                                                    < 2e-16 ***
                                             9.787
                                                    < 2e-16 ***
## factor(newpid)143
                       2.88106
                                   0.29437
                                            20.556
## factor(newpid)144
                       6.04833
                                   0.29423
                                                    < 2e-16 ***
## factor(newpid)145
                       5.55106
                                   0.31688
                                            17.518
                                                    < 2e-16 ***
  factor(newpid)146
                       5.46320
                                   0.31677
                                            17.246
                                                    < 2e-16 ***
  factor(newpid)147
                       6.18166
                                   0.34655
                                            17.838
                                                     < 2e-16 ***
                       5.34407
                                            11.988
## factor(newpid)148
                                   0.44578
                                                    < 2e-16 ***
## factor(newpid)149
                       5.67007
                                   0.34615
                                            16.381
                                                    < 2e-16 ***
                                            11.372
## factor(newpid)150
                       4.39422
                                   0.38642
                                                    < 2e-16 ***
## factor(newpid)151
                       5.68779
                                   0.38640
                                            14.720
                                                    < 2e-16 ***
## factor(newpid)152
                       4.61519
                                   0.77180
                                             5.980 3.33e-09 ***
## factor(newpid)153
                       7.21403
                                   0.44577
                                            16.183
                                                     < 2e-16 ***
                                            12.817
  factor(newpid)154
                       5.71394
                                   0.44580
                                                     < 2e-16 ***
## factor(newpid)155
                       6.27073
                                   0.44579
                                            14.067
                                                     < 2e-16 ***
  factor(newpid)156
                       6.34439
                                   0.54578
                                            11.624
                                                    < 2e-16 ***
  factor(newpid)157
                       6.41098
                                   0.44609
                                            14.371
                                                    < 2e-16 ***
  factor(newpid)158
                       6.08632
                                   0.34692
                                            17.544
                                                    < 2e-16 ***
## factor(newpid)159
                       5.29916
                                   0.54594
                                             9.706
                                                    < 2e-16 ***
## factor(newpid)160
                       5.04712
                                             9.247
                                                     < 2e-16 ***
                                   0.54579
## factor(newpid)161
                       5.14072
                                   0.38657
                                            13.298
                                                    < 2e-16 ***
  factor(newpid)162
                       4.69277
                                   0.44588
                                            10.525
                                                     < 2e-16 ***
## factor(newpid)163
                       7.42011
                                   0.38647
                                            19.200
                                                     < 2e-16 ***
  factor(newpid)164
                       7.07418
                                   0.34873
                                            20.286
                                                    < 2e-16 ***
                                            12.665
                                                    < 2e-16 ***
  factor(newpid)165
                       4.40042
                                   0.34744
## factor(newpid)166
                       5.63845
                                   0.54812
                                            10.287
                                                     < 2e-16 ***
## factor(newpid)167
                       4.93276
                                   0.38713
                                            12.742
                                                    < 2e-16 ***
## factor(newpid)168
                      5.79989
                                   0.29425
                                            19.711
                                                    < 2e-16 ***
```

```
## factor(newpid)169
                       2.83271
                                   0.54605
                                             5.188 2.69e-07 ***
## factor(newpid)170
                       4.52041
                                   0.34670
                                            13.039
                                                    < 2e-16 ***
## factor(newpid)171
                       6.70820
                                   0.77180
                                             8.692
                                                    < 2e-16 ***
## factor(newpid)172
                       5.26891
                                   0.34643
                                            15.209
                                                     < 2e-16 ***
## factor(newpid)173
                       1.59625
                                   0.54592
                                             2.924 0.003551 **
                                            10.970
## factor(newpid)174
                       3.80765
                                   0.34709
                                                    < 2e-16 ***
                                                    < 2e-16 ***
## factor(newpid)175
                       5.86770
                                   0.34640
                                            16.939
## factor(newpid)176
                       5.71388
                                   0.44591
                                            12.814
                                                    < 2e-16 ***
  factor(newpid)177
                       4.65448
                                   0.38715
                                            12.022
                                                    < 2e-16 ***
  factor(newpid)178
                       6.64100
                                   0.34712
                                            19.132
                                                    < 2e-16 ***
## factor(newpid)179
                       5.42868
                                   0.44577
                                            12.178
                                                    < 2e-16 ***
                       5.38254
                                            18.297
## factor(newpid)180
                                   0.29417
                                                    < 2e-16 ***
## factor(newpid)181
                       7.58231
                                   0.31737
                                            23.891
                                                    < 2e-16 ***
## factor(newpid)182
                                                    < 2e-16 ***
                       6.87445
                                   0.44674
                                            15.388
                       4.73226
                                  0.54591
                                                    < 2e-16 ***
## factor(newpid)183
                                             8.669
## factor(newpid)184
                       4.69042
                                   0.77180
                                             6.077 1.87e-09 ***
## factor(newpid)185
                       5.32106
                                   0.31790
                                            16.738
                                                    < 2e-16 ***
## factor(newpid)186
                       2.26637
                                   0.34754
                                             6.521 1.22e-10 ***
                                            18.743
## factor(newpid)187
                       5.96108
                                   0.31804
                                                    < 2e-16 ***
## factor(newpid)188
                       5.64729
                                   0.34676
                                            16.286
                                                    < 2e-16 ***
## factor(newpid)189
                       0.89556
                                   0.54589
                                             1.641 0.101277
## factor(newpid)190
                       3.93221
                                   0.54593
                                             7.203 1.34e-12 ***
                                            10.611
                                                    < 2e-16 ***
## factor(newpid)191
                       4.73072
                                   0.44582
                       4.63493
                                            15.757
## factor(newpid)192
                                   0.29415
                                                    < 2e-16 ***
                                            11.952
## factor(newpid)193
                       3.51569
                                   0.29414
                                                    < 2e-16 ***
## factor(newpid)194
                       1.67399
                                   0.31665
                                             5.286 1.60e-07 ***
## factor(newpid)195
                       6.57259
                                   0.44708
                                            14.701
                                                    < 2e-16 ***
## factor(newpid)196
                       4.28686
                                   0.38778
                                            11.055
                                                    < 2e-16 ***
                                            11.692
                                                    < 2e-16 ***
## factor(newpid)197
                       4.52015
                                   0.38659
## factor(newpid)198
                       6.11686
                                   0.34677
                                            17.640
                                                     < 2e-16 ***
## factor(newpid)199
                       3.58154
                                   0.38734
                                             9.247
                                                     < 2e-16 ***
## factor(newpid)200
                       6.33062
                                   0.31871
                                            19.863
                                                    < 2e-16 ***
  factor(newpid)201
                       4.88817
                                   0.38837
                                            12.586
                                                     < 2e-16 ***
                       6.08433
                                            11.144
## factor(newpid)202
                                   0.54598
                                                     < 2e-16 ***
## factor(newpid)203
                       6.31594
                                   0.38792
                                            16.282
                                                     < 2e-16 ***
                                            14.069
## factor(newpid)204
                       5.44066
                                   0.38672
                                                    < 2e-16 ***
## factor(newpid)205
                       3.66210
                                   0.34771
                                            10.532
                                                    < 2e-16 ***
## factor(newpid)206
                       5.98915
                                   0.29415
                                            20.361
                                                     < 2e-16 ***
## factor(newpid)207
                       6.08204
                                   0.31761
                                            19.149
                                                     < 2e-16 ***
                                            12.010
                                                    < 2e-16 ***
  factor(newpid)208
                       4.17020
                                   0.34723
## factor(newpid)209
                       6.43027
                                   0.31684
                                            20.295
                                                     < 2e-16 ***
## factor(newpid)210
                       5.21148
                                   0.29412
                                            17.719
                                                    < 2e-16 ***
## factor(newpid)211
                       5.34459
                                   0.29419
                                            18.167
                                                    < 2e-16 ***
  factor(newpid)212
                       5.21535
                                   0.31670
                                            16.468
                                                    < 2e-16 ***
## factor(newpid)213
                       4.67607
                                   0.44578
                                            10.490
                                                    < 2e-16 ***
## factor(newpid)214
                       6.54179
                                   0.29428
                                            22.230
                                                    < 2e-16 ***
## factor(newpid)215
                       5.04463
                                   0.31666
                                            15.931
                                                    < 2e-16 ***
## factor(newpid)216
                       3.74901
                                   0.34628
                                            10.827
                                                    < 2e-16 ***
## factor(newpid)217
                       3.09943
                                   0.54578
                                             5.679 1.88e-08 ***
## factor(newpid)218
                       4.76821
                                   0.29420
                                            16.207
                                                    < 2e-16 ***
  factor(newpid)219
                                             7.097 2.76e-12 ***
                       5.47723
                                   0.77180
## factor(newpid)220
                       6.34478
                                   0.29424
                                            21.564
                                                    < 2e-16 ***
## factor(newpid)221
                       5.78464
                                   0.31662
                                            18.270
                                                    < 2e-16 ***
## factor(newpid)222
                      5.27235
                                   0.31785
                                            16.587
                                                    < 2e-16 ***
```

```
## factor(newpid)223 5.34864
                                0.31661 16.894 < 2e-16 ***
## factor(newpid)224 3.80821
                                0.54578
                                          6.978 6.19e-12 ***
## factor(newpid)225 6.47400
                                0.29413 22.010 < 2e-16 ***
## factor(newpid)226 6.85178
                                0.34695 19.748 < 2e-16 ***
## factor(newpid)227
                     6.21616
                                0.31664
                                         19.631 < 2e-16 ***
## factor(newpid)228 4.67312
                                0.31665 14.758 < 2e-16 ***
## factor(newpid)229 5.25787
                                0.34628 15.184 < 2e-16 ***
                                0.34628 17.218 < 2e-16 ***
## factor(newpid)230 5.96217
## factor(newpid)231 5.95432
                                0.38653 15.405 < 2e-16 ***
## factor(newpid)232 6.17519
                                0.44620 13.840 < 2e-16 ***
## factor(newpid)233 4.36377
                                0.38636 11.295 < 2e-16 ***
                                0.54578 11.401 < 2e-16 ***
## factor(newpid)234
                     6.22240
## factor(newpid)235 3.21066
                                0.44635
                                          7.193 1.43e-12 ***
                                          8.182 1.06e-15 ***
## factor(newpid)236 2.83698
                                0.34674
## factor(newpid)237 5.43365
                                0.31707 17.137 < 2e-16 ***
## factor(newpid)238 5.05647
                                0.38660
                                         13.079 < 2e-16 ***
## factor(newpid)239 5.54035
                                0.44593 12.424 < 2e-16 ***
## factor(newpid)240 3.51138
                                0.34603 10.148 < 2e-16 ***
                                          7.924 7.49e-15 ***
## factor(newpid)241 6.11555
                                0.77180
## factor(newpid)242 5.16910
                                0.44592 11.592 < 2e-16 ***
## factor(newpid)243 5.89800
                                0.44636 13.213 < 2e-16 ***
## factor(newpid)244 5.94175
                                0.54578 10.887 < 2e-16 ***
                                0.38641 12.745 < 2e-16 ***
## factor(newpid)245 4.92484
                                          9.263 < 2e-16 ***
## factor(newpid)246 5.05558
                                0.54579
## factor(newpid)247 4.78539
                                0.77180
                                          6.200 8.92e-10 ***
## factor(newpid)248 5.64132
                                0.54579 10.336 < 2e-16 ***
## factor(newpid)249 5.59464
                                          7.249 9.71e-13 ***
                                0.77180
## factor(newpid)250 5.83524
                                0.54579 10.691 < 2e-16 ***
## factor(newpid)251 3.74166
                                0.77180
                                          4.848 1.49e-06 ***
## factor(newpid)252 4.51291
                                0.54582
                                          8.268 5.45e-16 ***
## factor(newpid)253
                     3.60555
                                0.77180
                                          4.672 3.49e-06 ***
## factor(newpid)254 3.75520
                                0.54598
                                          6.878 1.20e-11 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.7718 on 821 degrees of freedom
## Multiple R-squared: 0.9809, Adjusted R-squared: 0.9751
## F-statistic: 168.1 on 251 and 821 DF, p-value: < 2.2e-16
child <- hiv.data %>%
 dplyr::select(newpid, age.baseline, treatment)
child <- unique(child)</pre>
cd4_3_coef <- data.frame(child, cd4_3$coefficients[2:length(cd4_3$coefficients)])</pre>
colnames(cd4_3_coef) <- c("newpid", "age.baseline", "treatment", "coef.id")</pre>
rownames(cd4_3_coef) <- 1:250</pre>
cd4_3.id <- lm(coef.id ~ age.baseline + factor(treatment),data = cd4_3_coef)
summary(cd4 3.id)
##
## Call:
## lm(formula = coef.id ~ age.baseline + factor(treatment), data = cd4_3_coef)
## Residuals:
```

```
##
                   Median
                1Q
                               3Q
                   0.2265 1.1215
## -4.1594 -0.7039
                                  2.7256
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
                                          27.265
## (Intercept)
                      5.10627
                                 0.18728
                                                  < 2e-16 ***
## age.baseline
                      -0.12088
                                 0.04023
                                          -3.005 0.00293 **
## factor(treatment)2 0.14558
                                 0.18421
                                           0.790 0.43012
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 1.455 on 247 degrees of freedom
## Multiple R-squared: 0.03753,
                                   Adjusted R-squared:
## F-statistic: 4.816 on 2 and 247 DF, p-value: 0.008875
```

4. Write a model predicting CD4 percentage as a function of time with varying intercepts across children. Fit using lmer() and interpret the coefficient for time.

The coefficient for time is -0.366. It means if the time increases by 1 unit, then the CD4 percentage will decrease by 0.366 units on the square root scale.

```
cd4_4 <- lmer (y ~ time + (1 | newpid), data = hiv.data)
display(cd4_4)</pre>
```

```
## lmer(formula = y ~ time + (1 | newpid), data = hiv.data)
##
               coef.est coef.se
## (Intercept) 4.76
                         0.10
## time
               -0.37
                         0.05
##
## Error terms:
                         Std.Dev.
  Groups
             Name
## newpid
             (Intercept) 1.40
   Residual
                         0.77
##
## ---
## number of obs: 1072, groups: newpid, 250
## AIC = 3148.8, DIC = 3126.9
## deviance = 3133.9
```

```
cd4_4_coef <- data.frame(unique(hiv.data$newpid),coef(cd4_4)$newpid)
colnames(cd4_4_coef) <- c("newpid","intercept","time")</pre>
```

5. Extend the model in (4) to include child-level predictors (that is, group-level predictors) for treatment and age at baseline. Fit using lmer() and interpret the coefficients on time, treatment, and age at baseline.

The coefficient for time is -0.362. It means if the time increases by 1 unit, then the CD4 percentage will decrease by 0.362 units on the square root scale.

The coefficient for treatment is 0.18. This means that if the children are in treatment 2 their CD4 percentage will increase by 0.18 units on the square root scale.

The coefficient for age baseline is -0.119, so if the age baseline increases by 1 unit, then the CD4 percentage will decrease by 0.119 units on the square root scale.

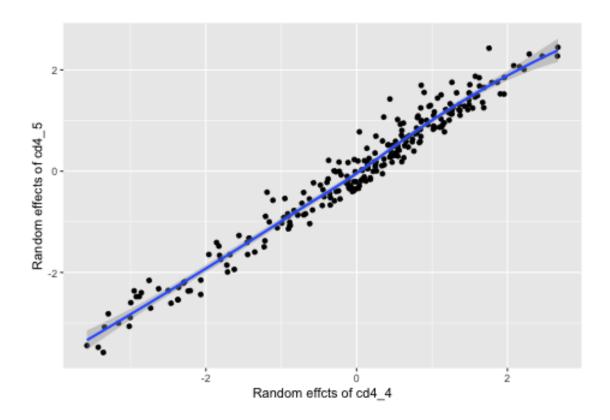
```
## lmer(formula = y ~ time + factor(treatment) + age.baseline +
       (1 | newpid), data = hiv.data)
##
##
                      coef.est coef.se
                                0.19
## (Intercept)
                      5.09
## time
                      -0.36
                                0.05
## factor(treatment)2 0.18
                                0.18
## age.baseline
                     -0.12
                                0.04
##
## Error terms:
## Groups
                         Std.Dev.
           Name
## newpid (Intercept) 1.37
## Residual
                         0.77
## ---
## number of obs: 1072, groups: newpid, 250
## AIC = 3149.2, DIC = 3110.9
## deviance = 3124.1
```

6. Investigate the change in partial pooling from (4) to (5) both graphically and numerically.

```
data_plot <- as.data.frame(cbind(unlist(ranef(cd4_4)),unlist(ranef(cd4_5))))
colnames(data_plot) <- c("cd4_4","cd4_5")

ggplot(data=data_plot,aes(x=cd4_4,y=cd4_5))+
    geom_point()+
    geom_smooth()+
    labs(x = "Random effcts of cd4_4", y = "Random effects of cd4_5")</pre>
```

```
## 'geom_smooth()' using method = 'loess' and formula = 'y ~ x'
```



display(cd4_4)

```
## lmer(formula = y ~ time + (1 | newpid), data = hiv.data)
              coef.est coef.se
## (Intercept) 4.76
                        0.10
                        0.05
              -0.37
## time
##
## Error terms:
## Groups Name
                        Std.Dev.
## newpid
           (Intercept) 1.40
## Residual
## ---
## number of obs: 1072, groups: newpid, 250
## AIC = 3148.8, DIC = 3126.9
## deviance = 3133.9
```

display(cd4_5)

```
## lmer(formula = y ~ time + factor(treatment) + age.baseline +
      (1 | newpid), data = hiv.data)
##
##
                    coef.est coef.se
## (Intercept)
                    5.09
                          0.19
                    -0.36
                              0.05
## time
## factor(treatment)2 0.18
                            0.18
## age.baseline
                -0.12
                            0.04
##
## Error terms:
```

```
## Groups Name Std.Dev.
## newpid (Intercept) 1.37
## Residual 0.77
## ---
## number of obs: 1072, groups: newpid, 250
## AIC = 3149.2, DIC = 3110.9
## deviance = 3124.1
```

7. Use the model fit from (5) to generate simulation of predicted CD4 percentages for each child in the dataset at a hypothetical next time point.

```
hiv_data_df <- as.data.frame(hiv.data)
predict_data <- hiv_data_df %>%
    dplyr::filter(!is.na(treatment)) %>%
    dplyr::filter(!is.na(age.baseline)) %>%
    dplyr::select(time, treatment, age.baseline, newpid, y)

predict <- predict(cd4_5, newdata = predict_data)
predict_cm <- cbind(predict_data, prediction = predict)
colnames(predict_cm)[1] <- c("prediction")</pre>
```

8. Use the same model fit to generate simulations of CD4 percentages at each of the time periods for a new child who was 4 years old at baseline.

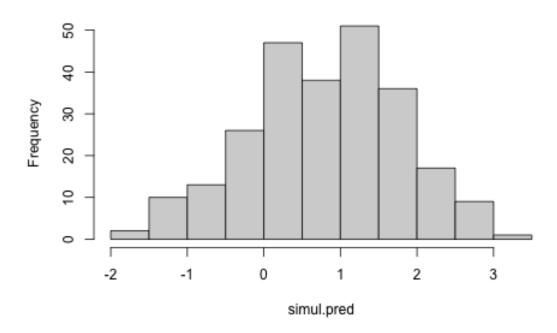
```
predict_data_2 <- hiv_data_df %>%
    dplyr::filter(is.na(hiv.data$treatment)==FALSE) %>%
    dplyr::filter(is.na(hiv.data$age.baseline)==FALSE) %>%
    dplyr::select(time,treatment,age.baseline,newpid,y) %>%
    dplyr::filter(round(age.baseline)==4)

predict_2 <- predict(cd4_5,newdata=predict_data_2)
predict_cm_2 <- cbind(predict_data_2, predict_2)
colnames(predict_cm_2)[1] <- c("prediction")</pre>
```

9. Posterior predictive checking: continuing the previous exercise, use the fitted model from (5) to simulate a new dataset of CD4 percentages (with the same sample size and ages of the original dataset) for the final time point of the study, and record the average CD4 percentage in this sample. Repeat this process 1000 times and compare the simulated distribution to the observed CD4 percentage at the final time point for the actual data.

```
}
hist(simul.pred)
```

Histogram of simul.pred



10. Extend the modelto allow for varying slopes for the time predictor.

```
cd4_10<-lmer(y~time+(1+time|newpid), data = hiv.data)</pre>
```

11. Next fit a model that does not allow for varying slopes but does allow for different coefficients for each time point (rather than fitting the linear trend).

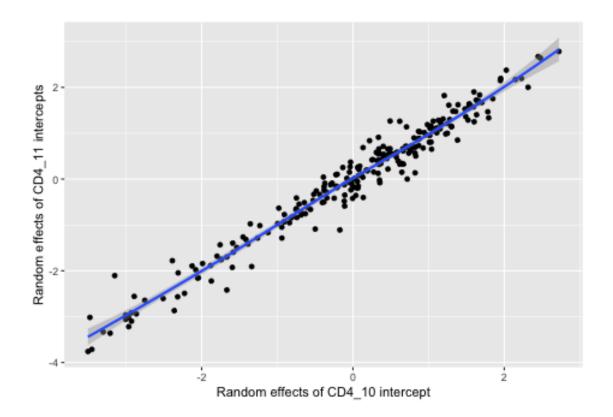
```
cd4_11<-lmer(y ~ factor(time) + (1 | newpid), data = hiv.data)</pre>
```

12. Compare the results of these models both numerically and graphically.

```
plot4_12 <- as.data.frame(cbind(unlist(ranef(cd4_10))[1:250],unlist(ranef(cd4_11))[1:250]))
colnames(plot4_12) <- c("cd4_10","cd4_11")

ggplot(data=plot4_12,aes(x=cd4_10,y=cd4_11))+
    geom_point()+
    geom_smooth()+
    labs(x = "Random effects of CD4_10 intercept", y = "Random effects of CD4_11 intercepts")</pre>
```

'geom_smooth()' using method = 'loess' and formula = 'y ~ x'



display(cd4_10)

```
## lmer(formula = y ~ time + (1 + time | newpid), data = hiv.data)
               coef.est coef.se
                         0.09
## (Intercept) 4.76
## time
               -0.36
                         0.07
##
## Error terms:
                         Std.Dev. Corr
  Groups
             Name
##
    newpid
             (Intercept) 1.39
##
             time
                         0.58
                                  -0.05
##
                         0.72
   Residual
## number of obs: 1072, groups: newpid, 250
## AIC = 3123.2, DIC = 3098.2
## deviance = 3104.7
```

display(cd4_11)

```
## lmer(formula = y ~ factor(time) + (1 | newpid), data = hiv.data)
##
                                coef.est coef.se
## (Intercept)
                                 4.77
                                          0.10
                                -1.23
## factor(time)0.205
                                          0.67
## factor(time)0.209999999999 0.21
                                          0.89
## factor(time)0.2133333333333 0.16
                                          0.94
## factor(time)0.21333333333333 -1.20
                                          0.94
## factor(time)0.2158333333333 1.47
                                          0.90
```

```
## factor(time)0.21583333333333 -0.25
                                       0.84
0.80
## factor(time)0.21833333333333 0.07
                                       0.90
## factor(time)0.21916666666667 -0.48
                                       0.85
## factor(time)0.22166666666667
                                       0.94
## factor(time)0.22416666666666
                              1.65
                                       0.86
## factor(time)0.224166666666667 -1.53
                                       0.63
## factor(time)0.22666666666667
                               1.42
                                       0.59
## factor(time)0.227499999999999999 -1.56
                                       0.89
## factor(time)0.2275
                               0.07
                                       0.46
## factor(time)0.2299999999999 -0.36
                                       0.59
## factor(time)0.23
                              -0.11
                                       0.12
## factor(time)0.2325
                              -0.59
                                       0.40
0.02
                                       0.84
## factor(time)0.23500000000001 -1.96
                                       0.80
## factor(time)0.2358333333333333
                               0.04
                                       0.29
## factor(time)0.2358333333333334
                                       0.62
                               0.18
## factor(time)0.2375
                               1.44
                                       0.89
## factor(time)0.23833333333333 -0.27
                                       0.49
## factor(time)0.238333333333333
                              0.85
                                       0.82
## factor(time)0.2408333333333 -0.21
                                       0.78
## factor(time)0.240833333333333
                                       0.59
## factor(time)0.2433333333333 -0.51
                                       0.89
## factor(time)0.24416666666667
                               0.09
                                       0.48
## factor(time)0.2458333333333333
                               0.09
                                       0.43
## factor(time)0.24583333333333 -0.25
                                       0.60
0.65
## factor(time)0.24666666666667
                               0.38
                                       0.85
## factor(time)0.24916666666666
                              0.15
                                       0.39
## factor(time)0.24916666666667 -0.48
                                       0.19
## factor(time)0.25166666666667
                               0.25
                                       0.43
## factor(time)0.2516666666668
                              0.31
                                       0.80
## factor(time)0.2525
                              -0.05
                                       0.94
## factor(time)0.25416666666667 -0.63
                                       0.84
## factor(time)0.255
                               0.33
                                       0.80
## factor(time)0.25666666666667
                               0.29
                                       0.63
## factor(time)0.25749999999999
                               0.09
                                       0.84
## factor(time)0.2575
                                       0.63
                               0.45
## factor(time)0.2625
                              -0.04
                                       0.84
## factor(time)0.265
                              -0.16
                                       0.85
## factor(time)0.26583333333333 -0.36
                                       0.84
## factor(time)0.26833333333333 -0.34
                                       0.59
## factor(time)0.2683333333333334
                               0.07
                                       0.49
## factor(time)0.2875
                               0.50
                                       0.53
## factor(time)0.2899999999999 -0.77
                                       0.94
## factor(time)0.29333333333333 -0.28
                                       0.94
## factor(time)0.30416666666667
                               0.31
                                       0.89
0.89
## factor(time)0.30666666666667
                              0.22
                                       0.59
## factor(time)0.32583333333333 -0.16
                                       0.89
## factor(time)0.32833333333333 -0.87
                                       0.94
0.94
## factor(time)0.35833333333333 0.57
                                       0.86
## factor(time)0.36416666666667 -0.07
                                       0.61
```

```
0.94
## factor(time)0.429166666666667 -0.44
                                    0.90
## factor(time)0.43833333333333 -0.85
                                    0.90
## factor(time)0.4408333333333 -0.10
                                    0.77
## factor(time)0.4433333333333 0.15
                                    0.85
## factor(time)0.44916666666667 -0.08
                                    0.79
## factor(time)0.45416666666666
                                    0.90
## factor(time)0.45416666666666 0.09
                                    0.86
## factor(time)0.455
                            -1.45
                                    0.89
## factor(time)0.45666666666667
                            0.24
                                    0.94
## factor(time) 0.4575
                            -0.14
                                    0.49
## factor(time)0.45916666666666666667 0.27
                                    0.62
0.46
## factor(time)0.46
                            -0.27
                                    0.17
## factor(time)0.46000000000001 -0.27
                                    0.31
## factor(time)0.46249999999999 -0.77
                                    0.48
## factor(time)0.4625
                                    0.41
                             0.43
## factor(time)0.46333333333333 -0.70
                                    0.81
## factor(time)0.465
                            -0.88
                                    0.48
## factor(time)0.4658333333333333
                            0.32
                                    0.59
## factor(time)0.46583333333333 -0.60
                                    0.83
## factor(time) 0.4675
                                    0.61
## factor(time)0.4683333333333 -0.80
                                    0.85
## factor(time)0.47083333333333 -0.36
                                    0.46
## factor(time)0.47083333333333 -0.46
                                    0.61
## factor(time)0.47333333333333 -0.17
                                    0.62
## factor(time)0.4733333333333 0.45
                                    0.79
0.82
## factor(time)0.47416666666667 -0.81
                                    0.80
## factor(time)0.47583333333333 -0.46
                                    0.80
## factor(time)0.475833333333334 -1.41
                                    0.58
0.40
0.58
## factor(time)0.479166666666667 -0.03
                                    0.25
## factor(time)0.48166666666666
                                    0.59
                            0.11
## factor(time)0.48166666666667
                            0.22
                                    0.43
## factor(time)0.48416666666667 -2.71
                                    0.81
## factor(time)0.485
                                    0.62
                             0.90
## factor(time)0.4874999999999 -0.23
                                    0.77
## factor(time)0.4875
                             1.80
                                    0.82
## factor(time)0.48750000000001
                            1.76
                                    0.80
0.85
                            0.09
## factor(time)0.495
                            -0.14
                                    0.60
## factor(time)0.49583333333333 -0.47
                                    0.86
## factor(time)0.49583333333333 -0.12
                                    0.94
## factor(time)0.49833333333333 -0.59
                                    0.39
## factor(time)0.49833333333333 -0.58
                                    0.38
## factor(time)0.50083333333333 -0.26
                                    0.79
## factor(time)0.50083333333333 0.05
                                    0.81
0.61
## factor(time)0.50333333333333 0.59
                                    0.84
## factor(time)0.5041666666666 0.24
                                    0.52
0.82
0.90
```

```
## factor(time)0.51166666666667 -1.10
                                      0.87
## factor(time)0.5141666666666 0.12
                                      0.62
## factor(time)0.515
                              0.16
                                      0.94
## factor(time)0.5175
                             -0.42
                                      0.38
## factor(time)0.51750000000001 -1.13
                                      0.82
## factor(time)0.53333333333333 -0.27
                                      0.64
## factor(time)0.533333333333334 -1.07
                                      0.87
## factor(time)0.53416666666666 0.22
                                      0.62
## factor(time)0.53666666666667 -0.48
                                      0.44
## factor(time)0.55583333333333 -0.22
                                      0.62
0.94
## factor(time)0.56416666666667 -0.77
                                      0.89
## factor(time)0.575
                             -0.35
                                      0.63
## factor(time)0.58083333333333 -0.28
                                      0.94
## factor(time)0.5825
                                      0.94
                              0.64
## factor(time)0.59416666666667 -0.48
                                      0.89
## factor(time)0.61083333333333 -1.09
                                      0.94
## factor(time)0.6375
                              1.80
                                      0.90
## factor(time)0.64833333333333 -2.11
                                      0.89
0.87
## factor(time)0.6575
                             -1.01
                                      0.94
## factor(time)0.67
                             -0.43
                                      0.85
## factor(time)0.67083333333333 -0.99
                                      0.49
## factor(time)0.6733333333333333
                             0.05
                                      0.94
## factor(time)0.67583333333333 -0.15
                                      0.67
## factor(time)0.68416666666667
                             0.53
                                      0.63
## factor(time)0.685
                                      0.84
                              0.61
## factor(time)0.6875
                             -1.59
                                      0.61
0.89
## factor(time)0.68916666666666 0.16
                                      0.81
## factor(time)0.69
                             -0.18
                                      0.16
## factor(time)0.6925
                              0.52
                                      0.55
## factor(time)0.69250000000001
                              0.90
                                      0.84
## factor(time)0.69333333333334 -0.48
                                      0.85
## factor(time)0.695
                              0.37
                                      0.84
## factor(time)0.69583333333333 -0.32
                                      0.86
## factor(time)0.69583333333333 -1.68
                                      0.83
## factor(time)0.6958333333333 0.82
                                      0.59
## factor(time)0.69750000000001 -1.49
                                      0.79
## factor(time)0.6983333333333 0.05
                                      0.84
## factor(time)0.69833333333333 -0.61
                                      0.59
0.49
## factor(time)0.70333333333333 -0.89
                                      0.58
## factor(time)0.70333333333333 -1.07
                                      0.82
## factor(time)0.704166666666667 -4.77
                                      0.80
## factor(time)0.70583333333333 -0.48
                                      0.49
## factor(time)0.70583333333333 -0.45
                                      0.77
0.80
0.80
## factor(time)0.70916666666667
                             0.23
                                      0.28
## factor(time)0.7116666666666 0.10
                                      0.84
## factor(time)0.71166666666667 -0.47
                                      0.81
## factor(time)0.7116666666666 -0.88
                                      0.57
## factor(time)0.71416666666667 -1.43
                                      0.58
```

```
## factor(time)0.7149999999999 -0.72
                                       0.79
## factor(time)0.71500000000001 -0.62
                                       0.86
## factor(time)0.7175
                              -1.01
                                       0.81
## factor(time)0.72
                              -4.32
                                       0.78
## factor(time)0.725
                              -0.65
                                       0.60
## factor(time)0.725833333333333
                             0.35
                                       0.84
## factor(time)0.7258333333333333
                              0.72
                                       0.83
## factor(time)0.7258333333333333
                              0.33
                                      0.94
## factor(time)0.72833333333333 -0.26
                                       0.29
## factor(time)0.7308333333333333
                             0.08
                                       0.51
## factor(time)0.73333333333333 -0.74
                                       0.84
0.81
## factor(time)0.73583333333333 -0.93
                                       0.67
## factor(time)0.73666666666666
                             0.05
                                       0.85
0.84
## factor(time)0.7425
                              -0.48
                                       0.94
## factor(time)0.74416666666666 0.15
                                      0.57
## factor(time)0.745
                              -0.39
                                       0.82
                                      0.37
## factor(time)0.7475
                              -0.36
## factor(time)0.75250000000001 -1.65
                                       0.84
## factor(time)0.75833333333333 0.22
                                       0.86
## factor(time)0.761666666666667 -0.59
                                       0.81
## factor(time)0.7633333333333 -0.13
                                       0.81
## factor(time)0.76333333333333 -0.02
                                       0.87
0.86
## factor(time)0.765833333333333 -1.22
                                       0.87
## factor(time)0.7666666666666 -0.44
                                       0.39
## factor(time)0.775
                              -1.57
                                       0.81
                              0.89
## factor(time)0.78
                                       1.58
0.89
## factor(time)0.785
                              -0.23
                                      0.83
## factor(time)0.7858333333333333
                              0.44
                                      0.80
## factor(time)0.78833333333333 -0.74
                                       0.94
0.82
## factor(time)0.8025
                              -0.56
                                       0.58
## factor(time)0.805
                              -1.58
                                      0.82
## factor(time)0.80500000000000 0.08
                                      0.79
## factor(time)0.80750000000001 -0.32
                                      0.89
## factor(time)0.82416666666667 -0.01
                                       0.63
## factor(time)0.8625
                              -0.45
                                       0.61
## factor(time)0.8675
                              0.56
                                       0.90
## factor(time)0.87833333333333 -0.23
                                       0.89
## factor(time)0.8816666666666 0.94
                                       0.94
## factor(time)0.89583333333333 -0.73
                                       0.89
## factor(time)0.90083333333333 -0.49
                                       0.85
## factor(time)0.9008333333333 0.30
                                       0.58
## factor(time)0.90333333333333 -1.03
                                       0.76
## factor(time)0.9033333333333333
                             2.25
                                       0.94
## factor(time)0.90583333333333 1.26
                                      0.90
## factor(time)0.90833333333333 -0.44
                                       0.90
0.94
## factor(time)0.909166666666667 -0.30
                                       0.81
## factor(time)0.91166666666667 -0.26
                                       0.79
## factor(time)0.91416666666666 0.58
                                       0.59
```

```
## factor(time)0.9175
                              -0.49
                                      0.84
## factor(time)0.91916666666667
                              0.05
                                      0.48
## factor(time)0.9199999999999 -0.94
                                      0.79
## factor(time)0.92
                                      0.27
                              -0.95
## factor(time)0.9200000000001 -0.15
                                      0.46
## factor(time)0.9225
                              -0.53
                                      0.59
## factor(time)0.925833333333333 -1.74
                                      0.59
## factor(time)0.925833333333333
                              0.34
                                      0.84
## factor(time)0.9283333333333333
                              0.04
                                      0.79
## factor(time)0.92833333333333 -0.94
                                      0.83
## factor(time)0.93083333333333 -0.72
                                      0.56
## factor(time)0.930833333333334 -1.97
                                      0.81
## factor(time)0.93333333333333 0.43
                                      0.82
## factor(time)0.93333333333333 0.01
                                      0.59
## factor(time)0.93416666666664 -0.82
                                      0.84
## factor(time)0.93416666666667 -1.03
                                      0.80
## factor(time)0.93583333333333 -0.52
                                      0.59
## factor(time)0.93583333333333 -0.73
                                      0.83
## factor(time)0.93666666666667
                             0.14
                                      0.79
## factor(time)0.938333333333333
                             0.03
                                      0.80
0.33
## factor(time)0.93916666666666 0.04
                                      0.33
## factor(time)0.9391666666666 -1.72
                                      0.82
0.41
## factor(time)0.94166666666667 -0.49
                                      0.81
## factor(time)0.94416666666667
                             0.12
                                      0.59
## factor(time)0.9475
                                      0.59
                              0.66
## factor(time)0.95250000000001 -0.45
                                      0.79
## factor(time)0.955
                              1.56
                                      0.84
## factor(time)0.95500000000001 -0.47
                                      0.81
## factor(time)0.95583333333333 -1.06
                                      0.85
## factor(time)0.9575
                              0.39
                                      0.79
## factor(time)0.95833333333333333
                             0.11
                                      0.36
## factor(time)0.95833333333333 -0.14
                                      0.46
## factor(time)0.96083333333333 -1.47
                                      0.82
0.84
0.83
## factor(time)0.96583333333333 0.05
                                      0.85
0.84
## factor(time)0.9774999999999 -3.22
                                      0.81
## factor(time)0.9775
                                      0.36
## factor(time)0.97750000000000 0.58
                                      0.86
## factor(time)0.98249999999999 -0.31
                                      0.82
## factor(time)0.9825
                              -0.08
                                      0.84
## factor(time)0.98333333333333 -0.02
                                      0.88
## factor(time)0.98583333333333 -0.41
                                      0.94
0.57
## factor(time)0.996666666666667 -0.95
                                      0.42
## factor(time)0.99916666666667 -0.98
                                      0.78
## factor(time)1
                              -0.99
                                      0.84
## factor(time)1.0016666666667
                             -0.36
                                      0.84
## factor(time)1.0025
                              -1.30
                                      0.84
## factor(time)1.0108333333333
                             -0.32
                                      0.81
## factor(time)1.0125
                              -0.75
                                      0.81
```

```
## factor(time)1.01583333333333
                                  -0.96
                                            0.61
## factor(time)1.02083333333333
                                  -1.29
                                            0.85
## factor(time)1.023333333333333
                                  -0.57
                                            0.90
                                   0.79
                                            0.89
## factor(time)1.0325
## factor(time)1.035
                                  -0.37
                                            0.39
## factor(time)1.04833333333333
                                  -1.29
                                            0.87
## factor(time)1.053333333333333
                                  -0.13
                                            0.83
## factor(time)1.0541666666667
                                  -0.54
                                            0.58
## factor(time)1.07583333333333
                                  -1.00
                                            0.85
## factor(time)1.0866666666667
                                   0.13
                                             1.58
## factor(time)1.09
                                  -1.53
                                            0.94
## factor(time)1.0925
                                  -0.63
                                            0.50
## factor(time)1.11416666666667
                                   0.10
                                            0.85
## factor(time)1.11666666666667
                                   0.94
                                            0.94
## factor(time)1.1308333333333
                                   0.28
                                            0.85
## factor(time)1.13583333333333
                                  -2.80
                                            0.94
## factor(time)1.1391666666667
                                   0.11
                                            0.79
## factor(time)1.1416666666667
                                  -0.48
                                            0.57
## factor(time)1.14416666666667
                                   1.06
                                            0.86
## factor(time)1.145
                                  -0.42
                                            0.89
## factor(time)1.1475
                                  -1.35
                                            0.84
## factor(time)1.1491666666667
                                            0.57
                                  -0.67
                                            0.22
## factor(time)1.15
                                  -0.41
## factor(time)1.1525
                                  -0.92
                                            0.46
## factor(time)1.15583333333333
                                  -1.17
                                            0.49
## factor(time)1.1575
                                  -0.14
                                            0.46
## factor(time)1.15833333333333
                                  -1.63
                                            0.59
  factor(time)1.160833333333333
                                  -1.02
                                            0.41
## factor(time)1.163333333333333
                                   0.86
                                            0.59
## factor(time)1.1641666666667
                                   0.31
                                            0.84
## factor(time)1.1658333333333333
                                  -1.58
                                            0.83
## factor(time)1.16833333333333
                                  -0.32
                                            0.80
## factor(time)1.1691666666667
                                  -0.52
                                            0.31
## factor(time)1.1716666666667
                                  -1.39
                                            0.57
## factor(time)1.17666666666667
                                            0.83
                                  -1.31
## factor(time)1.1775
                                  -0.10
                                            0.80
## factor(time)1.18
                                  -0.45
                                            0.80
## factor(time)1.18833333333333
                                  -0.10
                                            0.22
## factor(time)1.1966666666667
                                   0.32
                                            0.63
## factor(time)1.2016666666667
                                   0.09
                                            0.48
## factor(time)1.20416666666667
                                  -0.62
                                            0.59
## factor(time)1.2066666666667
                                            0.79
                                   0.30
## factor(time)1.2075
                                  -1.07
                                            0.47
## factor(time)1.2125
                                            0.84
                                   0.10
## factor(time)1.2241666666667
                                  -0.31
                                            0.86
## factor(time)1.22583333333333
                                   0.02
                                            0.86
## factor(time)1.2266666666667
                                  -0.02
                                            0.59
## factor(time)1.22916666666667
                                  -0.12
                                            0.59
## factor(time)1.2316666666667
                                  -1.42
                                            0.80
## factor(time)1.2325
                                  -0.12
                                            0.80
## factor(time)1.24583333333333
                                  -1.10
                                            0.48
## factor(time)1.24833333333333
                                  -1.65
                                            0.84
## factor(time)1.253333333333333
                                  -0.99
                                            0.90
## factor(time)1.2616666666667
                                  -0.42
                                            0.81
```

```
## factor(time)1.265
                                 -0.19
                                            0.47
## factor(time)1.2675
                                 -0.26
                                            0.84
## factor(time)1.2841666666667
                                 -2.30
                                            0.86
                                           0.87
## factor(time)1.3025
                                 -0.69
## factor(time)1.30333333333333
                                 -0.34
                                            0.57
## factor(time)1.31166666666667
                                 -1.86
                                           0.81
## factor(time)1.3416666666667
                                 -1.11
                                           0.79
## factor(time)1.35
                                 -0.55
                                           0.87
## factor(time)1.35833333333333
                                 -1.66
                                           0.84
## factor(time)1.36
                                 -0.09
                                           0.89
## factor(time)1.3608333333333
                                 -0.05
                                            0.89
## factor(time)1.36583333333333
                                 -0.75
                                            0.79
## factor(time)1.37166666666667
                                 -0.35
                                           0.57
## factor(time)1.3741666666667
                                 -0.69
                                           0.79
## factor(time)1.375
                                           0.79
                                 -0.83
## factor(time)1.3766666666667
                                 -3.03
                                           0.76
## factor(time)1.37916666666667
                                  0.03
                                           0.78
## factor(time)1.38
                                 -0.42
                                            0.32
## factor(time)1.3825
                                 -1.52
                                           0.55
## factor(time)1.38583333333333
                                 -0.78
                                           0.59
## factor(time)1.38583333333334
                                  0.17
                                           0.83
## factor(time)1.3875
                                 -0.22
                                            0.57
## factor(time)1.38833333333333
                                 -1.47
                                           0.80
## factor(time)1.39083333333333
                                 -0.58
                                           0.57
## factor(time)1.39583333333333
                                 -0.57
                                           0.60
## factor(time)1.39666666666667
                                  0.32
                                           0.77
## factor(time)1.39833333333333
                                 -0.33
                                           0.82
## factor(time)1.39916666666667
                                 -0.47
                                            0.31
## factor(time)1.40166666666667
                                 -2.16
                                           0.60
## factor(time)1.41
                                 -1.28
                                           0.55
## factor(time)1.4125
                                 -0.69
                                           0.83
## factor(time)1.415
                                 -0.18
                                           0.57
## factor(time)1.41833333333333
                                 -0.14
                                            0.46
## factor(time)1.4208333333333
                                 -0.74
                                           0.94
## factor(time)1.42416666666667
                                  0.39
                                            0.79
## factor(time)1.42583333333333
                                 -0.19
                                           0.81
## factor(time)1.42916666666667
                                  0.67
                                           0.87
## factor(time)1.4316666666667
                                 -0.13
                                           0.58
## factor(time)1.4366666666667
                                  0.45
                                           0.81
## factor(time)1.4375
                                 -0.88
                                           0.79
## factor(time)1.44583333333333
                                 -3.39
                                           0.81
0.90
                                 -0.85
## factor(time)1.4541666666667
                                 -0.44
                                           0.86
## factor(time)1.45583333333333
                                 -0.56
                                           0.79
## factor(time)1.4566666666667
                                 -0.19
                                           0.41
                                  0.31
                                           0.80
## factor(time)1.4625
## factor(time)1.47
                                  0.18
                                           0.58
## factor(time)1.4725
                                  0.13
                                            0.82
## factor(time)1.475
                                  0.27
                                           0.84
## factor(time)1.4816666666667
                                 -1.52
                                            0.84
## factor(time)1.48333333333333
                                 -0.60
                                           0.90
## factor(time)1.4925
                                 -2.59
                                           0.80
## factor(time)1.495
                                  0.20
                                           0.48
## factor(time)1.4975
                                  0.43
                                            0.63
```

```
## factor(time)1.5
                                  -0.30
                                            0.81
## factor(time)1.50583333333333
                                 -0.83
                                            0.89
## factor(time)1.51416666666667
                                   0.25
                                            0.79
                                 -1.94
## factor(time)1.5166666666667
                                            0.84
## factor(time)1.5191666666667
                                  -3.13
                                            0.86
## factor(time)1.53
                                            0.85
                                   0.51
## factor(time)1.5308333333333
                                            0.89
                                   0.11
## factor(time)1.53333333333333
                                 -0.13
                                            0.58
## factor(time)1.5416666666667
                                  -0.91
                                            0.81
## factor(time)1.5908333333333
                                 -1.28
                                            0.87
## factor(time)1.615
                                  -0.73
                                            0.83
## factor(time)1.6291666666667
                                            0.80
                                   3.59
## factor(time)1.648333333333333
                                 -1.52
                                            0.85
## factor(time)1.7166666666667
                                   0.00
                                            0.84
## factor(time)1.725
                                  -0.38
                                            0.79
## factor(time)1.8116666666667
                                   0.35
                                            0.85
## factor(time)1.8966666666667
                                            0.82
                                  -0.41
## factor(time)1.90833333333333
                                  -0.73
                                            0.86
## factor(time)1.93833333333333
                                 -0.88
                                            0.94
##
## Error terms:
                         Std.Dev.
## Groups
## newpid
             (Intercept) 1.41
## Residual
                         0.70
## ---
## number of obs: 1072, groups: newpid, 250
## AIC = 2980.5, DIC = 2698.6
## deviance = 2434.5
```

Figure skate in the 1932 Winter Olympics

The folder olympics has seven judges' ratings of seven figure skaters (on two criteria: "technical merit" and "artistic impression") from the 1932 Winter Olympics. Take a look at http://www.stat.columbia.edu/~gelman/arm/examples/olympics/olympics1932.txt

1. Construct a $7 \times 7 \times 2$ array of the data (ordered by skater, judge, and judging criterion).

```
## , , 1
##
##
        [,1] [,2] [,3] [,4] [,5] [,6] [,7]
        5.6
                       5.8
                             6.0
                                  5.0
## [1,]
             5.3 5.5
## [2,]
         5.6
              5.7
                   5.5
                        5.5
                             6.0
                                   5.5
## [3,]
         5.5
             5.6
                  5.7
                        5.6
                             5.5
                                   5.4
## [4.]
         5.5
              5.3
                   5.2
                        5.3
                             5.3
## [5,]
         5.8
             5.2
                   5.6
                        5.1
                             5.7
                                   5.1
                                        5.8
## [6,]
         5.8 5.4
                   5.8
                        5.7
                             5.8
                                   5.7
                                        5.8
## [7,]
         4.7 5.7 5.4 5.8
                             4.9
                                   5.3
                                       4.8
##
##
   , ,
##
        [,1] [,2] [,3] [,4] [,5] [,6]
##
                  4.0
## [1,]
         4.4
             4.8
                        4.8
                             5.4
                                   4.3
## [2,]
         4.5
              5.4
                   4.6
                        5.2
                             4.0
                                   4.8
                                        3.6
## [3,]
         4.5
              4.8
                   5.5
                        5.6
                             4.5
                                   4.6
## [4,]
         5.0
              4.5
                   4.8
                        5.1
                             4.6
## [5,]
         5.0
              5.5
                   4.8
                        5.0
                             4.5
                                  4.5
                                        4.0
## [6,]
         5.5
              5.8
                   5.2
                        5.3
                             5.2
                                  4.7
## [7,]
         5.1
              4.4
                  5.5
                        4.7
                             5.0
                                  4.0
```

2. Reformulate the data as a 98×4 array (similar to the top table in Figure 11.7), where the first two columns are the technical merit and artistic impression scores, the third column is a skater ID, and the fourth column is a judge ID.

```
olymp_98 <- dplyr::rename(olymp_array, skater_ID = pair, judge_ID = variable)
olymp_98 <- olymp_98[order(olymp_98*judge_ID),]
olymp_98 <- olymp_98[c("criterion", "value", "skater_ID", "judge_ID")]</pre>
```

3. Add another column to this matrix representing an indicator variable that equals 1 if the skater and judge are from the same country, or 0 otherwise.

```
olymp_98$SameCountry <-ifelse(olymp_98[,3] == " 1"&olymp_98[,4] == "judge_5",1,
    ifelse(olymp_98[,3] == " 2"&olymp_98[,4] == "judge_7",1,
    ifelse(olymp_98[,3] == " 3"&olymp_98[,4] == "judge_1",1,
    ifelse(olymp_98[,3] == " 4"&olymp_98[,4] == "judge_1",1,
    ifelse(olymp_98[,3] == " 7"&olymp_98[,4] == "judge_7",1,0)))))</pre>
```

4. Write the notation for a non-nested multilevel model (varying across skaters and judges) for the technical merit ratings and fit using lmer().

```
prog<- olymp_98 %>%
  dplyr::filter(criterion=="Program")
perform <- olymp_98 %>%
  dplyr::filter(criterion=="Performance")

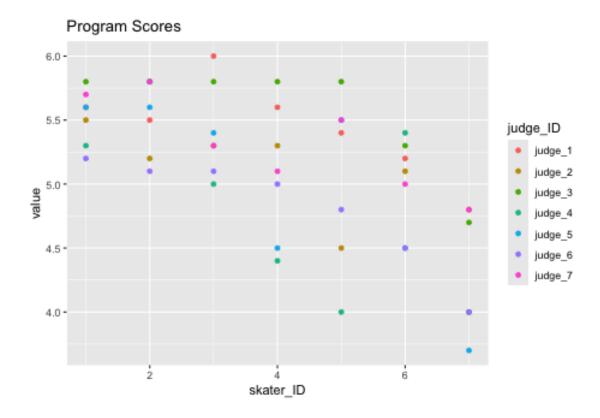
olympmod4 <- lmer(value ~ 1 + (1|skater_ID) + (1|judge_ID),data=prog)
summary(olympmod4)</pre>
```

Linear mixed model fit by REML ['lmerMod']

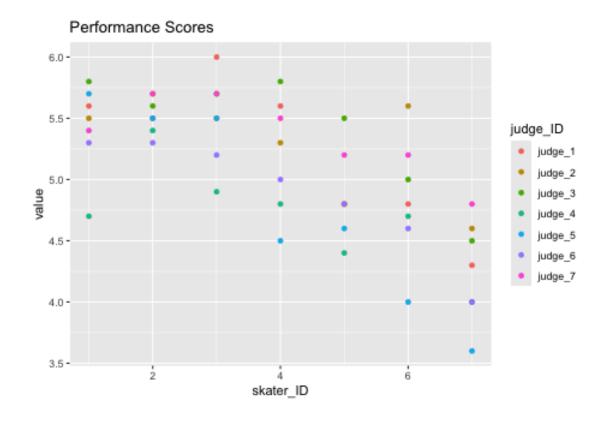
```
## Formula: value ~ 1 + (1 | skater_ID) + (1 | judge_ID)
##
      Data: prog
##
## REML criterion at convergence: 60
##
## Scaled residuals:
       Min
                  10
                      Median
                                    30
                                             Max
## -2.51025 -0.45646 -0.05459 0.63866 1.89709
##
## Random effects:
## Groups
              Name
                          Variance Std.Dev.
## skater_ID (Intercept) 0.17488 0.4182
## judge_ID (Intercept) 0.07664 0.2768
                          0.11057 0.3325
## Residual
## Number of obs: 49, groups: skater_ID, 7; judge_ID, 7
##
## Fixed effects:
##
               Estimate Std. Error t value
## (Intercept)
                 5.1347
                            0.1954
                                     26.28
  5. Fit the model in (4) using the artistic impression ratings.
olympmod5 <- lmer(value ~ 1 + (1|skater_ID) + (1|judge_ID),data=perform)
summary(olympmod5)
## Linear mixed model fit by REML ['lmerMod']
## Formula: value ~ 1 + (1 | skater_ID) + (1 | judge_ID)
##
      Data: perform
##
## REML criterion at convergence: 46.2
##
## Scaled residuals:
##
        Min
                  1Q
                       Median
                                    3Q
                                             Max
## -2.10128 -0.50469 -0.09884 0.40875 2.10489
##
## Random effects:
                          Variance Std.Dev.
## Groups
              Name
## skater_ID (Intercept) 0.20486 0.4526
## judge_ID (Intercept) 0.07759 0.2785
## Residual
                          0.07446 0.2729
## Number of obs: 49, groups: skater_ID, 7; judge_ID, 7
##
## Fixed effects:
##
               Estimate Std. Error t value
## (Intercept)
                 5.0918
                            0.2046
                                     24.88
  6. Display your results for both outcomes graphically.
```

ggplot(prog,aes(x=skater_ID,y=value,color=judge_ID))+geom_point()+

ggtitle("Program Scores")



ggplot(perform,aes(x=skater_ID,y=value,color=judge_ID))+geom_point()+
ggtitle("Performance Scores")



7. (Optional) Use posterior predictive checks to investigate model fit in (4) and (5).

Models for adjusting individual ratings:

A committee of 10 persons is evaluating 100 job applications. Each person on the committee reads 30 applications (structured so that each application is read by three people) and gives each a numerical rating between 1 and 10.

1. It would be natural to rate the applications based on their combined scores; however, there is a worry that different raters use different standards, and we would like to correct for this. Set up a model for the ratings (with parameters for the applicants and the raters).

```
model<-lmer(ratings~applicant ID+rater ID+(1+rater ID)rater ID))
```

2. It is possible that some persons on the committee show more variation than others in their ratings. Expand your model to allow for this.

```
model\_expanded <- lmer(ratings \sim applicant\_ID + (1 \mid rater\_ID) + (1 \mid applicant\_ID) + (0 + rater\_ID \mid rater\_ID))
```

Multilevel logistic regression

The folder speed.dating contains data from an experiment on a few hundred students that randomly assigned each participant to 10 short dates with participants of the opposite sex (Fisman et al., 2006). For each date, each person recorded several subjective numerical ratings of the other person (attractiveness, compatibility, and some other characteristics) and also wrote down whether he or she would like to meet the other person again. Label $y_{ij} = 1$ if person i is interested in seeing person j again 0 otherwise and r_{ij1}, \ldots, r_{ij6} as person i's numerical ratings of person j on the dimensions of attractiveness, compatibility, and so forth. Please look at http://www.stat.columbia.edu/~gelman/arm/examples/speed.dating/Speed% 20Dating%20Data%20Key.doc for details.

1. Fit a classical logistic regression predicting $Pr(y_{ij}=1)$ given person i's 6 ratings of person j. Discuss the importance of attractiveness, compatibility, and so forth in this predictive model. Attractiveness, fun, and sharing are all positive and statistically significant. Ambition is negative and significant.

```
dating_complete_pool <- glm(match~attr_o +sinc_o +intel_o +fun_o +amb_o +shar_o,data=dating,family=binor
summary(dating_complete_pool)</pre>
```

```
## sinc o
              -0.01996
                          0.03067 -0.651
                                            0.5152
## intel_o
               0.07176
                          0.03716
                                    1.931
                                            0.0535 .
## fun o
                          0.02922
                                    8.665 < 2e-16 ***
               0.25315
               -0.12099
                                   -4.264 2.01e-05 ***
## amb_o
                          0.02838
## shar o
               0.21225
                          0.02209
                                    9.608 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 6466.6 on 7030 degrees of freedom
## Residual deviance: 5611.0 on 7024 degrees of freedom
     (1347 observations deleted due to missingness)
## AIC: 5625
##
## Number of Fisher Scoring iterations: 5
```

2. Expand this model to allow varying intercepts for the persons making the evaluation; that is, some people are more likely than others to want to meet someone again. Discuss the fitted model.

```
dating_pooled_1 <- glmer(match~gender + attr_o +sinc_o +intel_o +fun_o +amb_o +shar_o+(1|iid),data=datis
summary(dating_pooled_1)</pre>
```

```
## Generalized linear mixed model fit by maximum likelihood (Laplace
     Approximation) [glmerMod]
##
  Family: binomial (logit)
## Formula: match ~ gender + attr_o + sinc_o + intel_o + fun_o + amb_o +
       shar_o + (1 | iid)
##
##
      Data: dating
  Control: glmerControl(optimizer = "bobyqa", optCtrl = list(maxfun = 1e+05))
##
                 BIC
                       logLik deviance df.resid
##
        AIC
##
     5543.3
              5605.0 -2762.6
                                5525.3
                                            7022
##
## Scaled residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
## -1.7414 -0.4457 -0.2882 -0.1459 10.3496
## Random effects:
## Groups Name
                       Variance Std.Dev.
           (Intercept) 0.4263
                                0.6529
## Number of obs: 7031, groups: iid, 551
##
## Fixed effects:
               Estimate Std. Error z value Pr(>|z|)
                           0.24367 -24.704 < 2e-16 ***
## (Intercept) -6.01967
## gender
                0.15358
                           0.09312
                                     1.649
                                             0.0991 .
## attr_o
                           0.02649
                                     8.896 < 2e-16 ***
                0.23562
## sinc_o
                           0.03261
                                    -0.432
                                             0.6655
               -0.01410
                                     1.767
## intel_o
               0.07009
                           0.03967
                                             0.0772 .
                                     8.348 < 2e-16 ***
## fun_o
                0.26212
                           0.03140
## amb_o
               -0.13132
                           0.03025 -4.341 1.42e-05 ***
## shar_o
               0.22461
                           0.02326
                                     9.658 < 2e-16 ***
```

3. Expand further to allow varying intercepts for the persons being rated. Discuss the fitted model.

```
# dating_pooled_2 <- stan_glmer(match ~ gender + attr_o+ sinc_o+ intel_o +

fun_o + amb + shar_o +

(1 | iid) + (1 | pid),

data = dating, family = binomial, refresh =0)

# summary(dating_pooled_2)</pre>
```

4. You will now fit some models that allow the coefficients for attractiveness, compatibility, and the other attributes to vary by person. Fit a no-pooling model: for each person i, fit a logistic regression to the data y_{ij} for the 10 persons j whom he or she rated, using as predictors the 6 ratings r_{ij1}, \ldots, r_{ij6} . (Hint: with 10 data points and 6 predictors, this model is difficult to fit. You will need to simplify it in some way to get reasonable fits.)

```
#uiid<-unique(dating$iid)
#dating_no_pool_list<-vector("list",length(uiid))
#for(i in 1:length(uiid)){
# attr_o +sinc_o +intel_o +fun_o +amb_o+shar_o,
# dating_no_pool_list[[i]] <- summary(glm(match~attr_o+shar_o,
# data=dating,
# subset = dating$iid==uiid[i],
# family=binomial))$coefficients
# }</pre>
```

5. Fit a multilevel model, allowing the intercept and the coefficients for the 6 ratings to vary by the rater i.

```
\#dating\_pooled\_3 \leftarrow stan\_glmer(match\sim gender + attr\_o + sinc\_o + intel\_o + fun\_o + amb\_o + shar\_o + (1 + attr\_o + attr\_
```

6. Compare the inferences from the multilevel model in (5) to the no-pooling model in (4) and the complete-pooling model from part (1) of the previous exercise.