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FIT3181 Deep Learning

Week 08: Learning Representation and DL for Language: Word Embedding

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Outline

- Text Analytics and Language Models
- Learning representation in machine learning and deep learning
- Word embedding
 - Skip-gram
 - Continuous bag of words (CBOW)
 - Negative sampling
- Something to vector
 - Doc2Vec
 - Node2Vec

Text analytics

Real-world Observed world **Text Data Express** Perceive Amazon Movie Reviews @AmznMovieRevws - Aug 25 **Symbolic** Madagascar: Escape 2 Africa. representation 36 **Text corpus** The product is My experience Your support team is **★★★★** Five Stars ok I guess so far has been useless By Taxx - August 21, 2015 fantastic! NEUTRAL **Amazon Verified Purchase** POSITIVE great story, but I felt the obese airbag NEGATIVE could have been more expressive Service reviews on FB Sentiment analysis Movie reviews **Numeric** representation ML algorithm

AR FASULTS

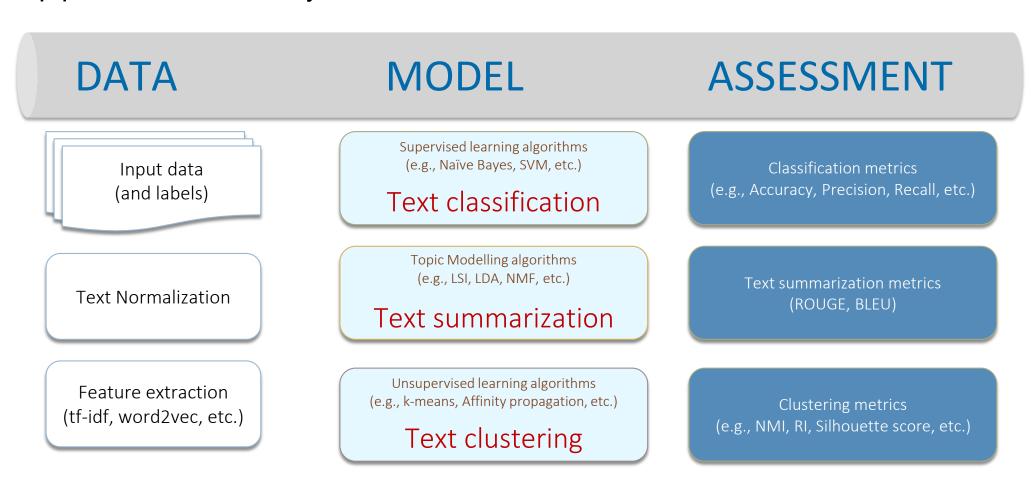
Text analytics' key tasks:

- Text classification
- Text clustering
- Text summarization

Some key applications

- Spam detection
- News articles categorization
- Marketing and CRM (customer relationship management)
- Recommendations

ML pipeline for Text analytics



Text normalization

- Expanding contractions
 - Contractions are shortened version of words or syllables
 - e.g., isn't → is not, you're → you are
 - Exist extensively and pose a problem to text analytics
- Lemmatization
 - removing word affixes to get to a base form of the root word.
 - e.g. cars \rightarrow car, running \rightarrow run, is \rightarrow be
- Removing special characters and symbols
 - e.g. !, .
- Removing stop words
 - e.g., a, and

One-hot vector encoding

Terms	Doc1	Doc2
goal		
data		
information		
insight		
you		

"The goal is to turn data into information, and information into insight" Carly Fiorina

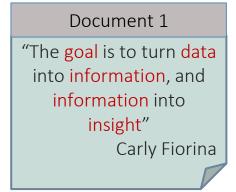
"You can have data without information, but you cannot have information without data."

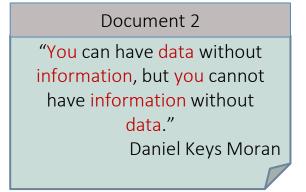
Daniel Keys Moran

$$\mathsf{one_hot}(\mathsf{goal}) = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} \qquad \qquad \mathsf{one_hot}(\mathsf{data}) = \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} \qquad \qquad \cdots$$

One-hot vector encoding

Terms	Doc1	Doc2
goal	1	
data	1	
information	2	
insight	1	
you	0	





$$= \begin{bmatrix} 1 \\ 1 \\ 2 \\ 1 \\ 0 \end{bmatrix}$$

Bag-of-word representation

Terms	Doc1	Doc2		
goal	1	0		
data	1	2		
information	2	2		
insight	1	0		
you	0	1		

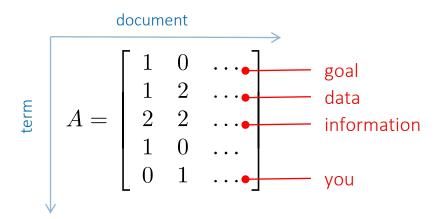
$$doc_1 = \begin{bmatrix} 1\\1\\2\\1\\0 \end{bmatrix} doc_2 = \begin{bmatrix} 0\\2\\2\\0\\1 \end{bmatrix}$$

"The goal is to turn data into information, and information into insight"

Carly Fiorina

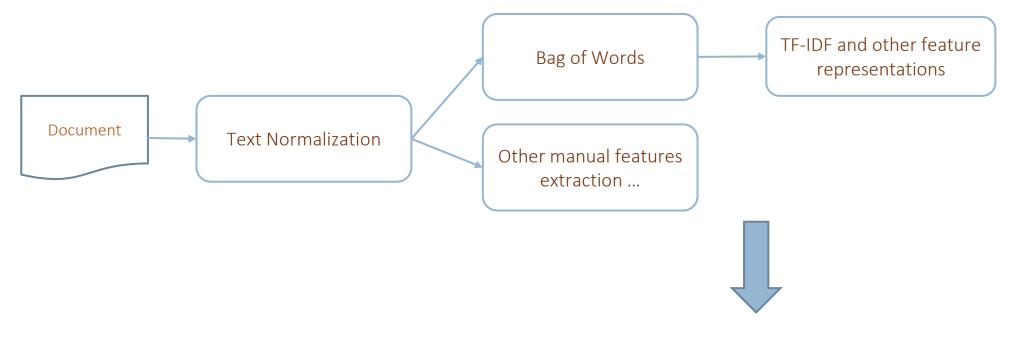
"You can have data without information, but you cannot have information without data."

Daniel Keys Moran



term-by-document matrix

Feature extraction



Each word and document become a point in a vector space!

Feature Extraction

Tf-Idf weighting

- More information beyond word counts
- tf: term frequency number of term occurrences in a document
- idf: inverse document-frequency how much information the term provides in corpus C.
 - $o idf(t,C) = \log \frac{|C|}{|C_t|}, \text{ where }$
 - |C|: the number of documents in the corpus
 - $|C_t| = |\{d \in C : t \in d\}|$: the number of documents containing term t
 - $_{\odot}$ More documents contain term t, less information it provides (idf →0)
- tf—idf:
 - $\circ tfidf(t,d,C) = tf(t,d) \times idf(t,C)$
- Question: what happens if term t is not in the corpus, i.e. $|C_t| = 0$?

Feature Extraction

Tf-Idf weighting

- Question: what happens if term t is not in the corpus?
 - o (One) solution smoothing

•
$$idf(t,C) = \log \frac{1+|C|}{1+|C_t|}$$

■ Normalizing v = tfidf

$$v_{norm} = \frac{v}{\sqrt{v_1^2 + \dots + v_n^2}}$$

TF-IDF example

term frequency (tf)

Terms	goal	data	information	insight	you
Doc1	1	1	2	1	0
Doc2	0	2	2	0	1

document frequency (df)

Terms	goal	data	information	insight	you
df	1	2	2	1	1

inverse document frequency (idf)

Terms	goal	data	information	insight	you
idf	0.69	0	0	0.69	0.69
	•		•		
	$log \frac{2}{1}$		$\log \frac{2}{2}$		

Document 1

"The goal is to turn data into information, and information into insight"

Carly Fiorina

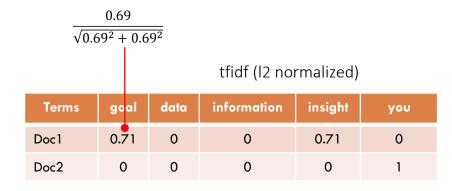
Document 2

"You can have data without information, but you cannot have information without data."

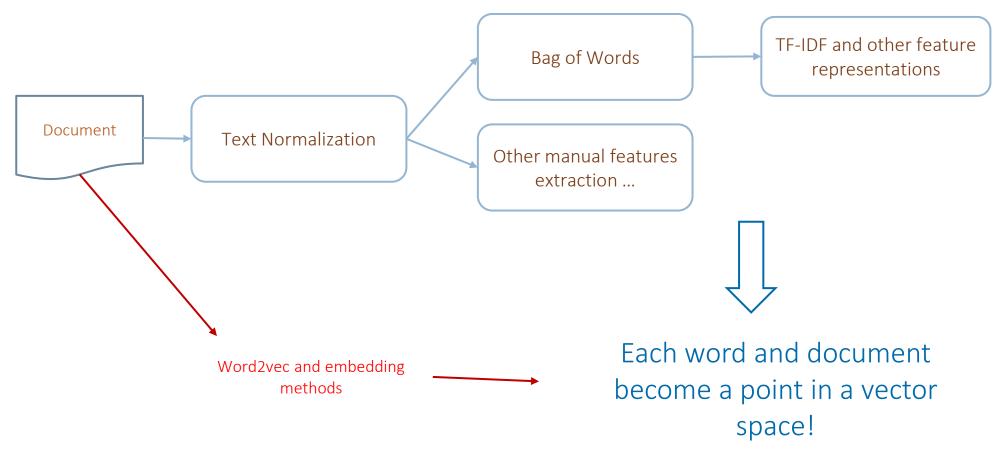
Daniel Keys Moran

Tf-idf

Terms	goal	data	information	insight	you
Doc1	0.69	0	0	0.69	0
Doc2	0	0	0	0	0.69



Feature extraction



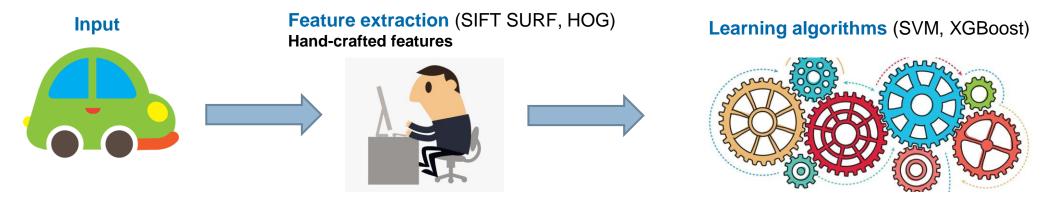


Machine Learning = Learning Representation++

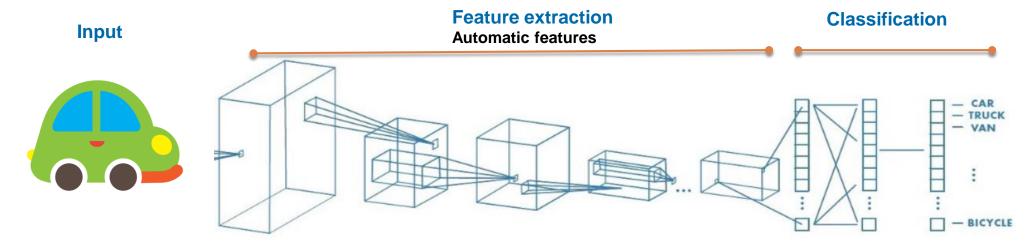
Hand-crafted and automatic feature extractor

Visual data

Traditional approach (hand-crafted feature learning)



Deep learning approach (automatic feature learning)



Hand-crafted and automatic feature extractor

Visual data

Traditional approach (hand-crafted feature learning)

Learning algorithm and feature extractor are disconnected

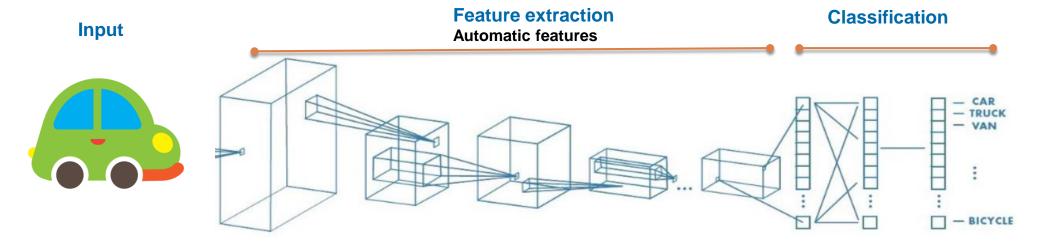


Learning algorithms (SVM, XGBoost)



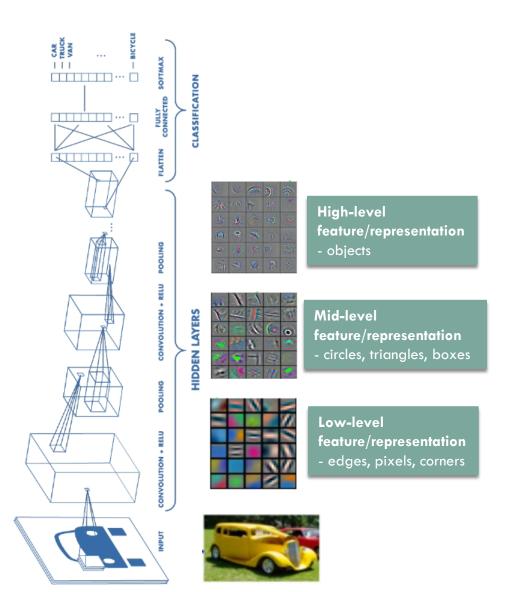
Deep learning approach (automatic feature learning)

Classification and feature extractor are connected

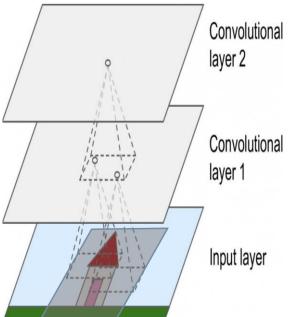


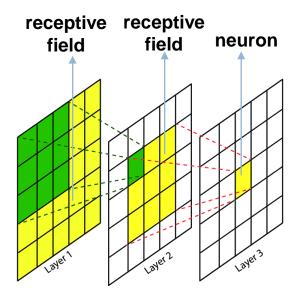
Automatic feature extractor

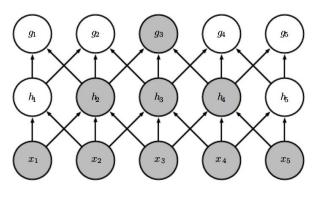
Deep learning for visual data



Neurons on higher layers have larger receptive fields (patches) on input images



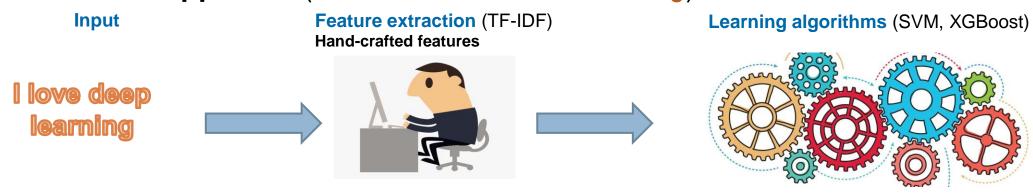




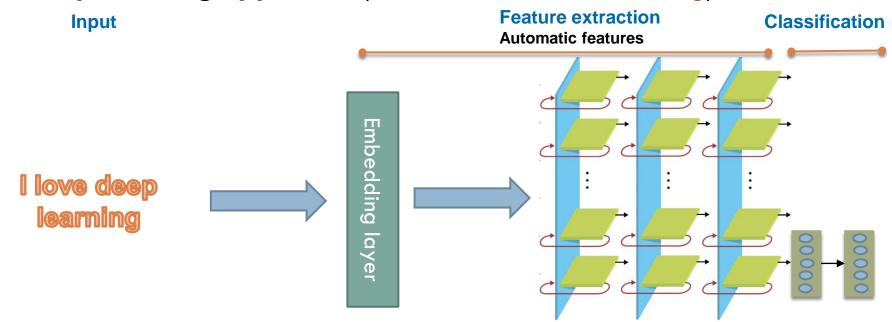
Hand-crafted and automatic feature extractor

Sequential data

Traditional approach (hand-crafted feature learning)



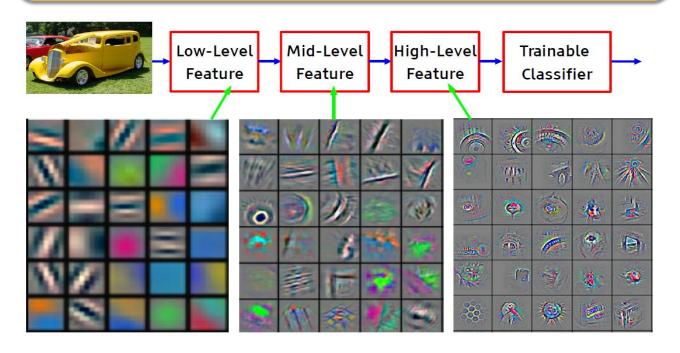
Deep learning approach (automatic feature learning)

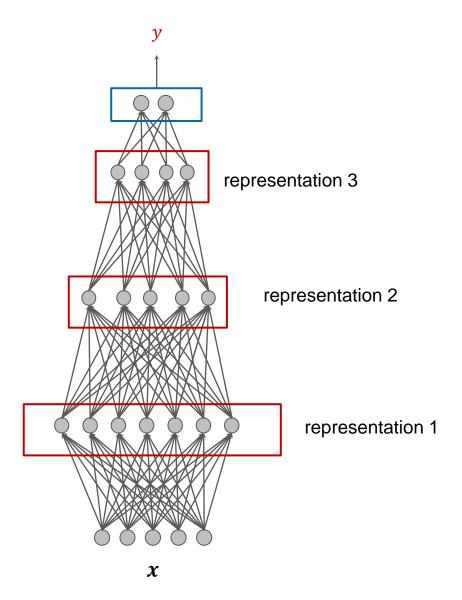


Learning representation in deep learning

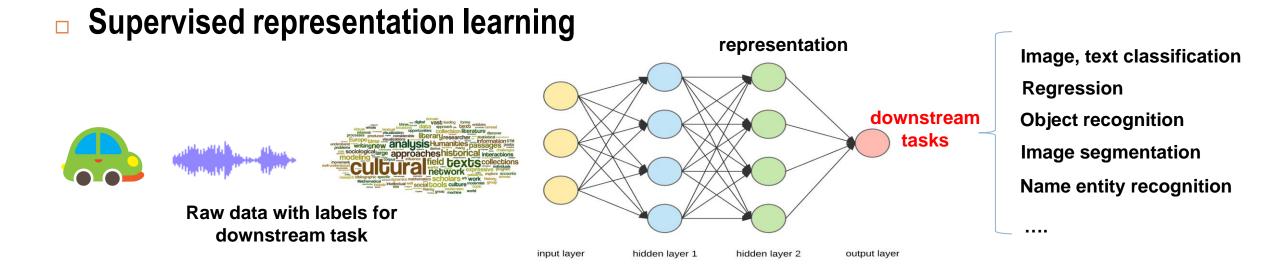
"Deep Learning: machine learning algorithms based on learning multiple levels of representation and abstraction"

Yoshua Bengio





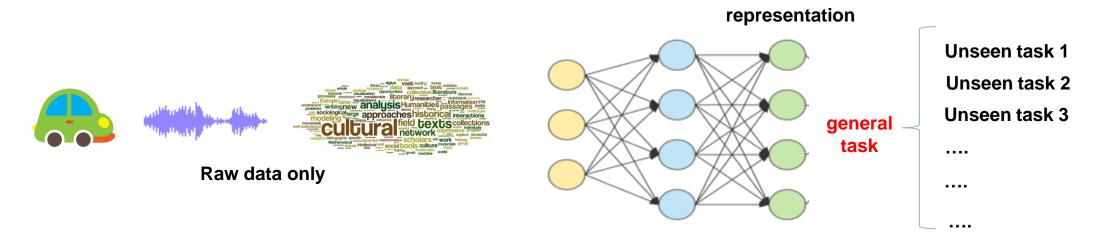
Learning representation in Deep Learning Supervised representation learning



Learning the representation that fits a specific downstream task.

Learning representation in Deep Learning Unsupervised representation learning

Unsupervised representation learning



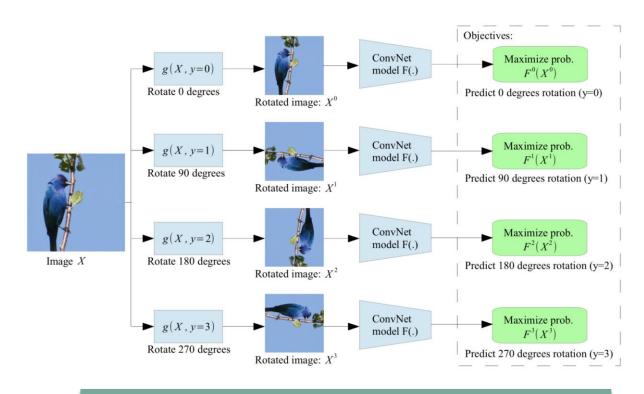
Learning the representation that fits many tasks.

Learning representation in Deep Learning

Self-supervised learning

- A possible and efficient workaround for unsupervised representation learning.
- Deep learning is only good at supervised learning that requires labels

- What if we have only raw data (images)?
 - Devise pretext task to require the model to predict something → supervised learning.
 - The art is to devise the good and meaningful pretext task.



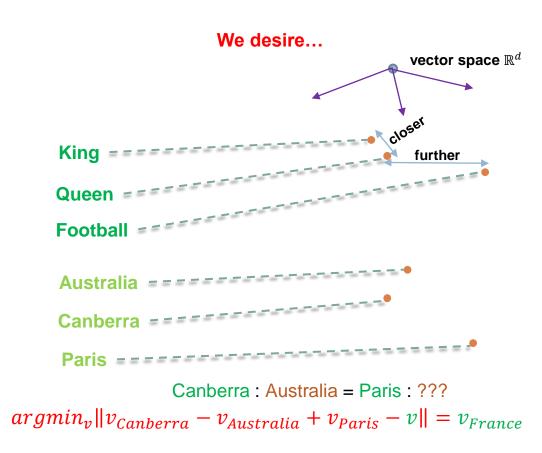
Pretext task:

- Rotate images 0° , 90° , 180° , 270° and try to predict the angle
- 4 labels for 0° , 90° , 180° , 270° .

Word embedding (Word2Vec)

Wikipedia text corpus





- We have: Many texts in Wikipedia
- We want: Learn vector representations for words that preserve semantic and linguistic relationship carried in the text corpus
- We need: Devise pretext task to cast the learning word representation to supervised learning.



Word embedding

Motivation of Word2Vec

"You shall know a word by the company it keeps"

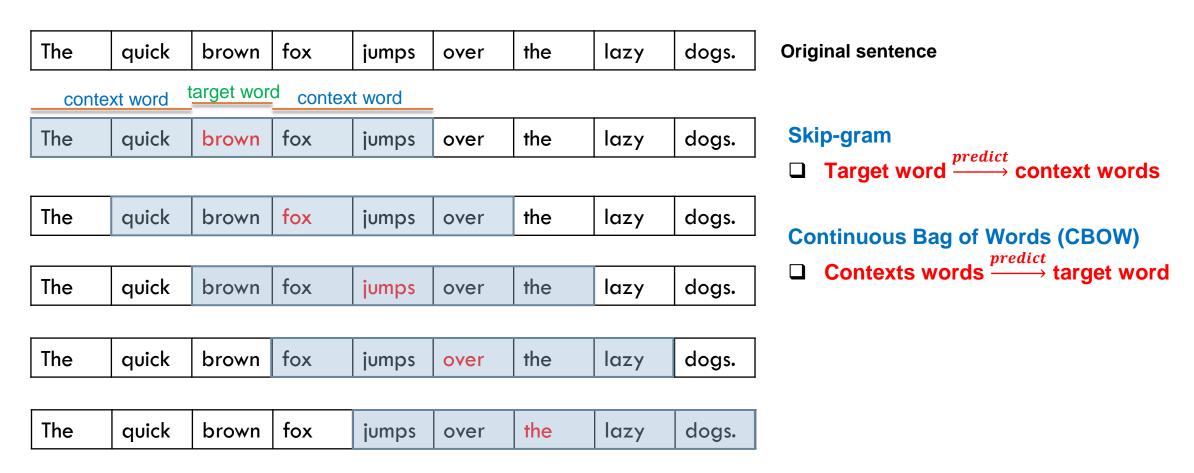


J.R. Firth 1957

Word2Vec: Pretext task

Pretext task

What is the pretext task of Word2Vec?



Skip-gram Pretext task

What is the **pretext task** of Skip-gram?

The	quick	brown	fox	jumps	over	the	lazy	dogs.	Skip-gram $\square \text{Target word} \xrightarrow{predict} \text{context words}$
conte	ext word	target wor	d contex	kt word					□ Target word ——— context words
The	quick	brown	fox	jumps	over	the	lazy	dogs.	(brown, the), (brown, quick), (brown, for), (brown, jumps)
							1		
The	quick	brown	fox	jumps	over	the	lazy	dogs.	(fox, quick), (fox, brown), (fox, jumps), (fox, overs)
The	quick	brown	fox	jumps	over	the	lazy	dogs.	(jumps, brown), (jumps, fox), (jumps, over), (jumps, the)
The	quick	brown	fox	jumps	over	the	lazy	dogs.	(over, fox), (over, jumps), (over, the), (over, lazy)
The	quick	brown	fox	jumps	over	the	lazy	dogs.	(the, jumps), (the, over), (the, lazy), (the, dogs)

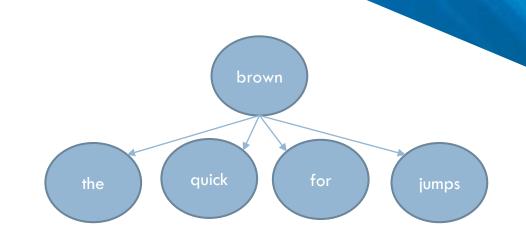
Skip-gram Modelling

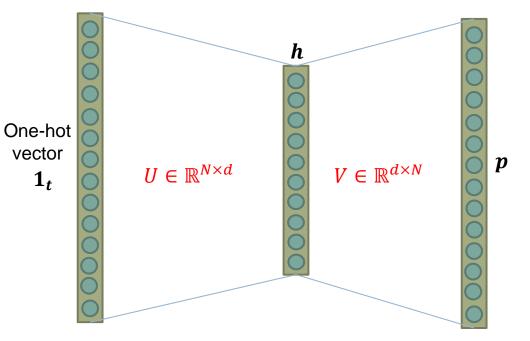
Current window

- The quick brown fox jumps
- $P(the,quick,for,jumps \mid brown) = P(the \mid brown) \times P(quick \mid brown) \times P(for \mid brown) \times P(jumps \mid brown)$
- $\log P(the, quick, for, jumps \mid brown) = \log P(the \mid brown) + \dots + \log P(jumps \mid brown)$
- brown, the), (brown, quick), (brown, for), (brown, jumps). Let consider tw = brown and cw = the.

Two matrices

- $_{\circ}$ $U \in \mathbb{R}^{N \times d}$ (N is vocabulary size, d is embedding size)
- $V \in \mathbb{R}^{d \times N}$
- Assume that indices of tw and cw are $1 \le t, c \le N$ respectively. The forward propagation is as follows:
 - $h = 1_t^T U = U_t^r \in \mathbb{R}^{1 \times d}, o = hV \in \mathbb{R}^{1 \times N}, p = softmax(o)$
 - \circ $P(cw = the \mid tw = brown) = p_c$
 - $\log P(cw = the \mid tw = brown) = \log p_c = U_t^r V_c^c \log(\sum_{k=1}^N \exp(U_t^r V_k^c))$
- Train the model by maximizing log likelihood.





Skip-gram

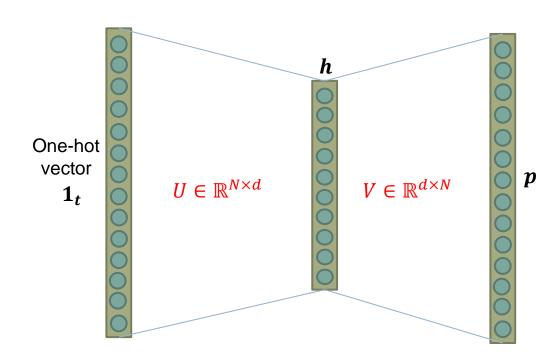
Drawback

Two matrices

- $U \in \mathbb{R}^{N \times d}$ (N is vocabulary size, d is embedding size)
- $V \in \mathbb{R}^{d \times N}$
- Assume that indices of tw and cw are $1 \le t, c \le N$ respectively. The forward propagation is as follows:
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 - $\log P(cw = the \mid tw = brown) = \log p_c = U_t^r V_c^c \log(\sum_{k=1}^N \exp(U_t^r V_k^c))$

Some drawbacks

- p = softmax(o) is computationally expensive
- $p \in \mathbb{R}^{1 \times N}$ is a distribution over the **vocabulary with size** N (usually very big) \rightarrow the values of p_i are **very tiny** \rightarrow **hard to train**
 - Hierarchical SoftMax
 - Negative sampling (more popular and efficient)



Skip-gram Negative sampling

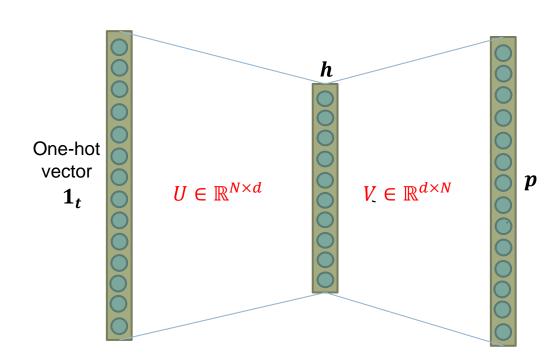
- Transform N-class prediction to binary prediction with negative examples
- Consider a positive (true) pair (tw=brown, cw = the)
 - o [(brown, the),1]
 - Sample randomly some (two) words
 - [(brown, ng_1 = hello), 0] and [(brown, ng_2 = awsome), 0]
 - Let denote the indices of ng_1 and ng_2 by $1 \le n_1$, $n_2 \le N$.

The forward propagation

- $h = 1_t^T U = U_t^r \in \mathbb{R}^{1 \times d}, o = hV \in \mathbb{R}^{1 \times N}, p = \underline{sigmoid}(o)$
- $P(y = 1 \mid \text{tw=brown}, \text{cw =} the) = p_c$
- $P(y = 1 \mid \text{tw=brown}, ng_1 = hello) = p_{n_1}$
- \circ $P(y = 1 \mid \text{tw=brown}, ng_2 = awsome) = p_{n_2}$

Optimization problem

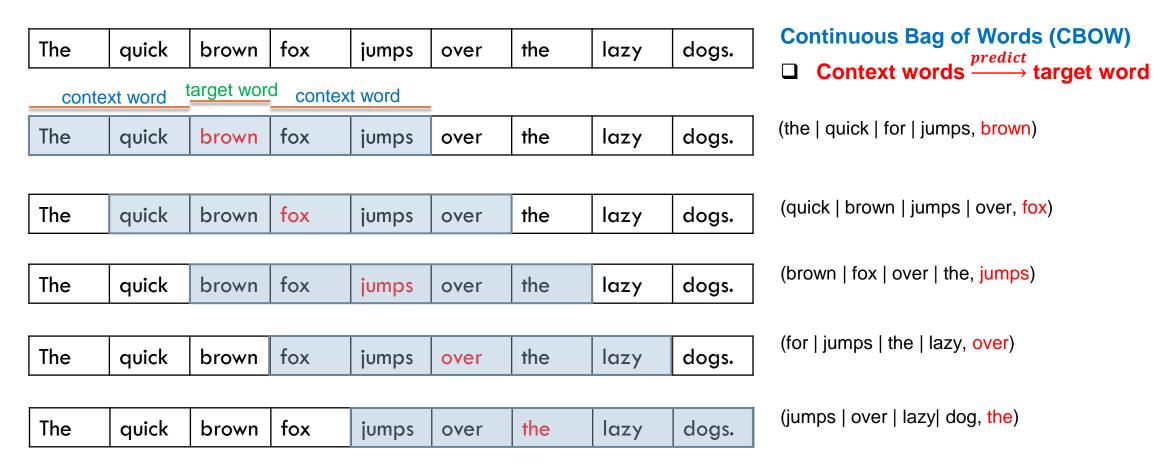
max $[\log p_c - \alpha \log p_{n_1} - \alpha \log p_{n_2}]$ where α >0 is a trade-off parameter.



Continuous Bag of Words (CBOW)

Pretext task

What is the pretext task of CBOW?



Continuous Bag of Words (CBOW)

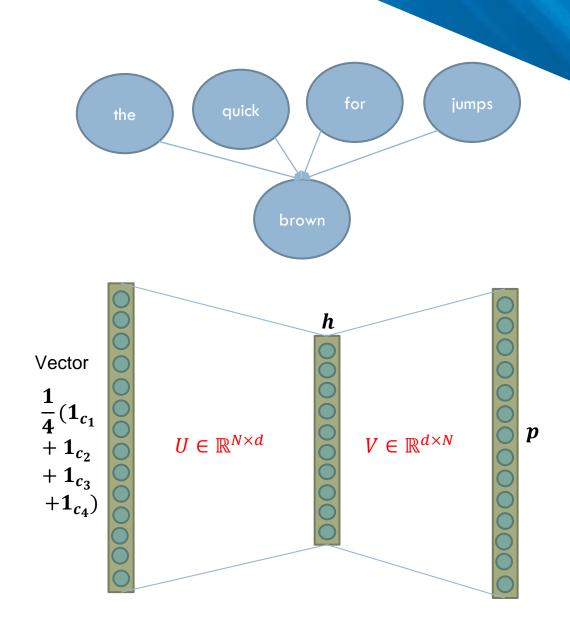
Modelling

Current window

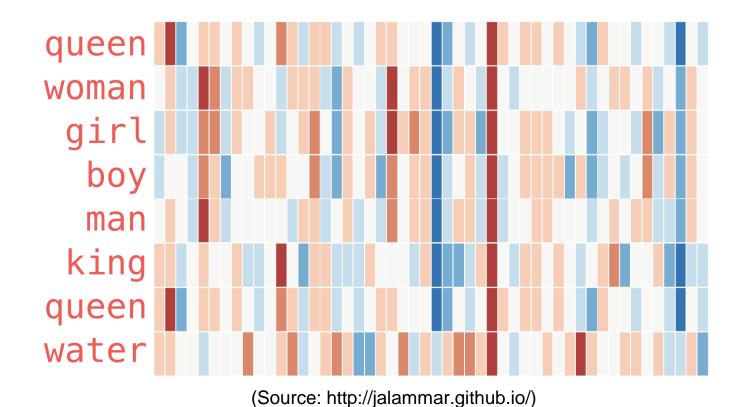
- The quick brown fox jumps
- □ Need to formulate: $P(brown \mid the, quick, for, jumps)$
- the | quick | for | jumps, brown). Let consider tw = brown and $cw_1 = the$, $cw_2 = quick$, $cw_3 = for$, $cw_4 = jumps$.

Two matrices

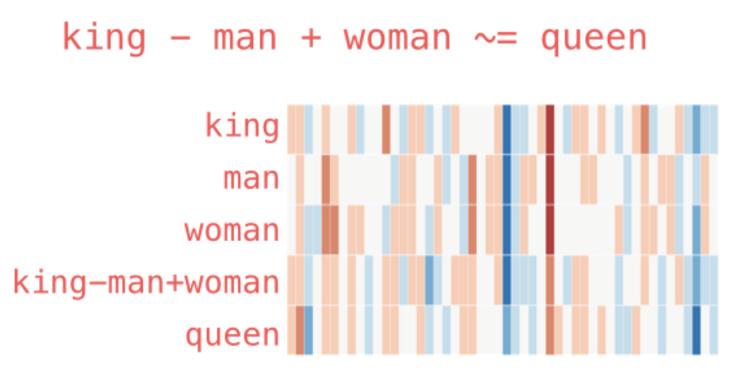
- $U \in \mathbb{R}^{N \times d}$ (N is vocabulary size, d is embedding size)
- $V \in \mathbb{R}^{d \times N}$
- Assume that indices of tw is $1 \le t \le N$ and $cw_{1:4}$ are $1 \le c_{1:4} \le N$ respectively. The forward propagation is as follows:
 - $h = \frac{\mathbf{1}_{c_1}^T + \dots + \mathbf{1}_{c_4}^T}{4} U = \frac{1}{4} \left(U_{c_1}^r + \dots + U_{c_4}^r \right) = \overline{U^r} \in \mathbb{R}^{1 \times d}, o = hV \in \mathbb{R}^{1 \times N}, p = softmax(o)$
 - $P(brown \mid the, quick, for, jumps) = p_t$
 - $\log P(\frac{brown}{the, quick, for, jumps}) = \log p_t = \overline{U^r}V_t^c \log(\sum_{k=1}^N \exp(\overline{U^r}V_t^c))$
- Train the model by maximizing log likelihood.



Visualization of Word2Vec representations

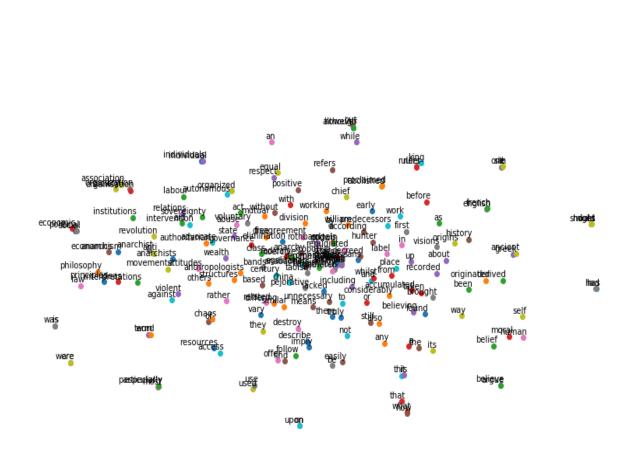


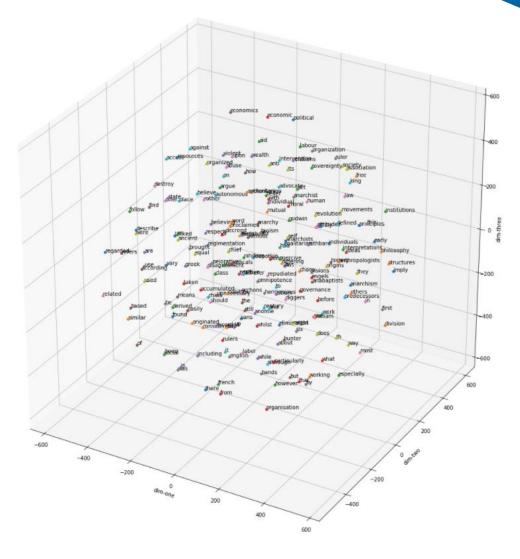
Visualization of Word2Vec representations



(Source: http://jalammar.github.io/)

Visualization of Word2Vec representations

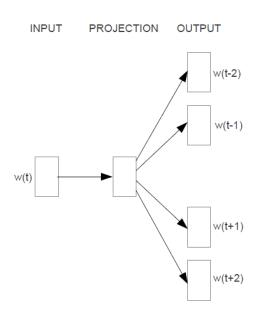




3D t-SNE plot

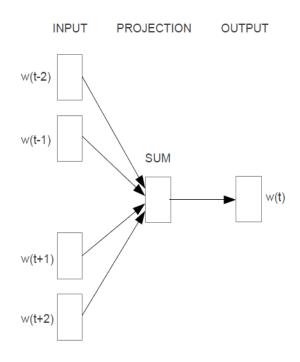
Word2Vec: Summary

- Skip-gram: predict the context words based on the target word.
- Continuous-bag-of-word (CBOW): predict the target word based on the context words.



Skip-gram

- Negative sampling: speed up training by subsampling (e.g., frequent words)
- Hierarchical softmax: deal with large vocabulary: O(V) to $O(\log V)$.





Word2Vec in use

Train Word2Vec on a dataset

```
import gensim.downloader as api
from gensim.models import Word2Vec

dataset = api.load("text8")
model = Word2Vec(dataset)
model.save("./text8-word2vec.bin")
```

Train Word2Vec on text8 dataset (skip-gram, window size =5)

```
from gensim.models import KeyedVectors
model = KeyedVectors.load("./text8-word2vec.bin")
word_vectors = model.wv
```

Load pretrained Word2Vec from a file

```
word vectors.get vector('king')
array([ 1.0615952 , 3.374791 , -2.4529877 , -0.89189297, 2.0385118 ,
      -1.0867552 , -1.2593621 , 0.20547654, -0.70700854, 0.29547456,
      -0.9151951 , 0.99069464, 1.7152157 , 0.64989454, 0.33458185,
       2.499265 , -1.0269971 , 4.957024 , -6.161608 , -0.10745641,
       0.10324214, 1.1219409, 0.98975873, -0.08191033, -0.7929074,
      -0.28150806, -1.0557121 , 0.27056807, 0.31582335, 2.9731138 ,
      -1.4136707 , 0.93965536, 1.1514933 , 0.38530475, -1.5722595 ,
      -0.08922919, -1.2710185 , -0.7054481 , 0.7354161 , 1.4659075 ,
       1.2870685 , -1.2874846 , -1.6638854 , 0.20794497, -0.1928033 ,
      -3.8513193 , -0.0873706 , 0.43098506 , 0.12324328 ,-1.6535882 ,
      -0.6248446 , -0.28294212 , 1.4047468 , -0.42495435 , 0.7049425 ,
      -0.26330888, -1.7225645 , -0.866658 , 1.3149631 , -0.5719914 ,
      -1.3960481 , 1.7349594 , 2.8976836 , 2.233186 , 0.905698 ,
       0.24419262, 1.7447696 , 2.4310687 , -0.6564301 , 2.1977458 ,
      -0.28740513, -0.0529648 , 1.8151288 , 1.2035793 , 0.51843506,
       2.2382748 , -1.7706063 , -1.7169152 , -3.8160467 , 0.2048373 ,
       1.1777579 , 2.9256532 , 0.7214914 , -3.804784 , -0.3797294 ,
      -1.3870562 , -1.8468527 , 0.96608454, -0.51972026, -1.4571909 ,
      -2.1815338 , -1.7526524 , -2.4643364 , -0.5413108 , -0.6252542 ,
       0.33478758, -0.27308032, -2.7191868, -2.4398658, -1.7016346],
     dtype=float32)
```

Get vector representation of a word

```
word_vectors.cosine_similarities(word_vectors.get_vector('king'), [word_vectors.get_vector('queen'), word_vectors.get_vector('australia')])
array([0.7218381 , 0.09479931], dtype=float32)
```

Compute cosine similarity

Advanced operations with Word2Vec

```
def print_most_similar(word_conf_pairs, k):
    for i, (word, conf) in enumerate(word_conf_pairs):
        print("{:.3f} {:s}".format(conf, word))
        if i >= k-1:
            break
    if k < len(word_conf_pairs):
        print("...")</pre>
```

Print returned results in better form

```
print_most_similar(word_vectors.most_similar("king"), 10)

0.759 prince
0.722 queen
0.712 vii
0.698 emperor
0.682 kings
0.669 elector
0.668 regent
0.666 constantine
0.663 throne
0.663 pope
```

Top 10 similar words of king

```
print_most_similar(word_vectors.most_similar("china"), 10)

0.795 japan
0.760 taiwan
0.746 india
0.667 thailand
0.661 indonesia
0.651 pakistan
0.647 tibet
0.645 afghanistan
0.643 burma
0.639 kazakhstan
```

Top 10 similar words of China

Word2Vec for initializing embedding matrix

```
class RNN Spam Detection:
    def init (self, run mode="scratch", embed model= "glove-wiki-gigaword-300", embed size = 128, data manager= None):
        self.embed model = embed model
        self.embed size = embed size
        if run mode != 'scratch':
            self.embed_size = int(self.embed_model.split("-")[-1])
        self.data_manager = data_manager
        self.vocab_size = self.data_manager.vocab_size +1
       self.word2idx = self.data manager.word2idx
        self.embed matrix = np.zeros((self.vocab size, self.embed size))
        self.run mode = run mode
        self.model = None
    def build embedding matrix(self):
       if os.path.exists("E.npy"): #file existed
            self.embed matrix = np.load("E.npy")
                                                           #Load the file for embedding matrix if existed
        else: #file not existed or first-time run
            self.word2vect = api.load(self.embed model)
                                                         #load embedding model
            for word, idx in self.word2idx.items():
                try:
                    self.embed_matrix[idx] = self.word2vect.word_vec(word)
                                                                             #assign weight for the corresponding word and index
                except KeyError: #word cannot be found
                    pass
            np.save("E.npy", self.embed_matrix)
    def build(self):
       inputs = tf.keras.layers.Input(shape=[None])
        if self.run_mode == "scratch":
            self.embedding layer = tf.keras.layers.Embedding(self.vocab size, self.embed size, mask zero= True, trainable= True)
        else: #fine-tuned
            self.build embedding matrix()
            self.embedding layer = tf.keras.layers.Embedding(self.vocab size, self.embed size,
                                                        weights= [self.embed_matrix], trainable= True)
       h = self.embedding_layer(inputs)
       h = tf.keras.layers.GRU(256, return_sequences=True)(h)
        h = tf.keras.layers.GRU(128)(h)
        h = tf.keras.layers.Dense(1, activation="sigmoid")(h)
        self.model = tf.keras.Model(inputs= inputs, outputs=h)
```

Word2Vec for initializing embedding matrix

Training embedding matrix from scratch

Using Word2Vec to initialize embedding matrix and fine tune

Something to Vector

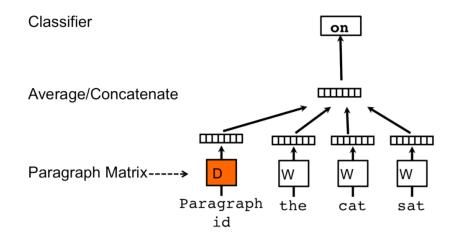
Recent methods on learning embedding Something to Vector

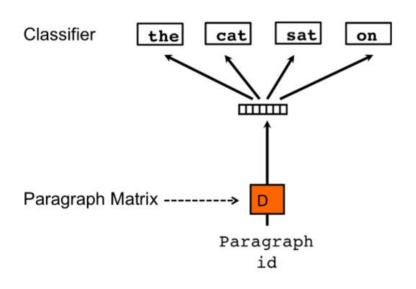
Recent Methods	
word2vec (Mikolov, et al. 2013)	distributed representation for words
doc2vec (Le an Mikolov, 2014)	distributed representation of sentences and documents
topic2vec (Niu and Dai, 2015)	distributed representation for topics
item2vec (Barkan and Koenigstein, 2016)	distributed representation of items in recommender systems
med2vec (Choi et al., 2016)	distributed representations of ICD codes
node2vec (Grover and Leskovec, 2016)	distributed representation for nodes in a network
paper2vec (Ganguly and Pudi, 2017)	distributed representations of textual and graph- based information
sub2vec (Adhikari et al., 2017)	distributed representation for subgraphs
cat2vec (Wen et al., 2017)	distributed representation for categorical values
fis2vec (2017)	distributed representation for frequent itemsets

Documents to Vectors

doc2vec (Le an Mikolov, 2014)

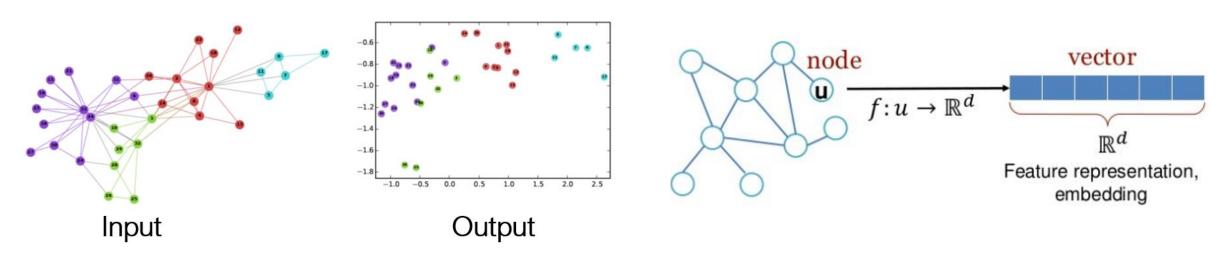
- N documents (paragraphs) and M words
 - Embedding matrix for documents (paragraphs): $D \in \mathbb{R}^{N \times p}$
 - Embedding matrix for words: $W \in \mathbb{R}^{M \times q}$
- Embedding paragraph id and word ids to paragraph vector $(\mathbb{R}^{1 \times p})$ and word vector $(\mathbb{R}^{1 \times q})$
 - Take average and concatenate
- Given a document (paragraph), the task is to predict the target word from the context words or vice versa.





Nodes to Vectors

node2vec (Grover and Leskovec, 2016)



(Source: snap.stanford.edu/proj/embeddings-www, WWW 2018)

Motivation:

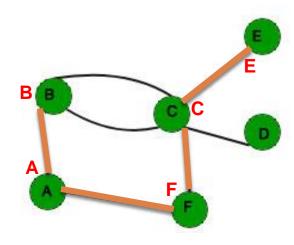
 Find embedding of nodes to d-dimensions so that "similar" nodes in the graph have embeddings that are close together.

Node2Vec

Do random walks on the graph

 $○ B, A, F, C, E \rightarrow each node is a word <math>\rightarrow F \xrightarrow{predict} B, A, C, E$

- How to find good random walks?
 - Cover all important paths in a graph
 - Balance between microscopic and macroscopic views



Node2Vec

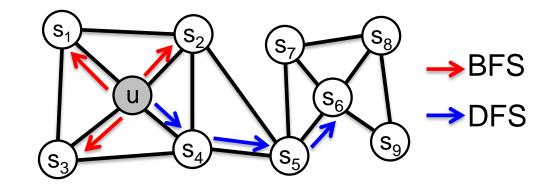
DFS vs BFS

$$N_{BFS}(u) = \{ s_1, s_2, s_3 \}$$

Local microscopic view

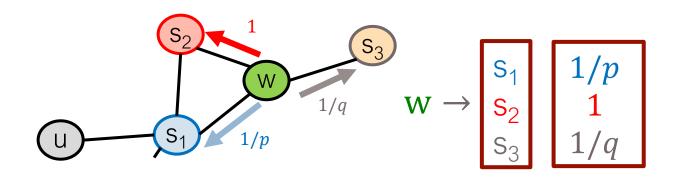
$$N_{DFS}(u) = \{s_4, s_5, s_6\}$$

Global macroscopic view



Node2Vec Random walks

- Walker is at w. Where to go next?
- p, q model transition probabilities
 - ∘ p ... return parameter
 - o q ... "walk away" parameter
- BFS-like walk: Low value of p
- DFS-like walk: Low value of q



(Source: snap.stanford.edu/proj/embeddings-www, WWW 2018)

Reading and references

- Word embedding paper: https://papers.nips.cc/paper/5021-distributed-representations-of-words-and-phrases-and-their-compositionality.pdf
- Good document to explain Word2Vec: https://arxiv.org/pdf/1411.2738.pdf
- Doc2Vec paper: https://cs.stanford.edu/~quocle/paragraph_vector.pdf
- Node2Vec paper: https://arxiv.org/pdf/1607.00653.pdf
- Good blog for self-supervised learning: https://lilianweng.github.io/lillog/2019/11/10/self-supervised-learning.html

Summary

- Text Analytics and Language Models
- Learning representation in machine learning and deep learning
- Word embedding
 - Skip-gram
 - Continuous bag of words (CBOW)
 - Negative sampling
- Something to vector
 - Doc2Vec
 - Node2Vec

Thanks for your attention! Question time



Appendix

Motivation

- All relevant text analytics/NLP tasks
 - e.g., text classification into: politics, medical, business, science, sports
- Understand the meaning of words in the document.
 - A lot of them you never seen. In fact the ones that you rarely see tend to be the most important ones.

```
model.most_similar('insomnia')

[(u'sleeplessness', 0.6954464316368103),
  (u'chronic_insomnia', 0.6937799453735352),
  (u'sleep_disorders', 0.6682900190353394),
  (u'excessive_sleepiness', 0.6534832119941711),
  (u'migraine', 0.6464337706565857),
  (u'anxiety_insomnia', 0.6439672112464905),
  (u'constipation', 0.6267993450164795),
  (u'nighttime_heartburn', 0.6188271045684814),
  (u'migraines', 0.6186375617980957),
  (u'migraine_headaches', 0.6150763034820557)]
```

What does 'insomnia' mean?

Motivation

- Estimate the similarity between two words
- Why symbolic/one-hot vector representation will fail?
 - can't capture 'context' around word is presented independently!

```
import numpy as np
from numpy import dot
from numpy.linalg import norm
# compute cosine similarity for two vector u & v
def cosine sim(u, v):
    return dot(u, v)/(norm(u)*norm(v))
vocabulary = ['king', 'man', 'queen', 'woman']
tokens = {w:i for i,w in enumerate(vocabulary)}
N = len(vocabulary)
W = np.zeros((N, N))
np.fill diagonal(W, 1)
print ("cosine similarity('king','woman'): {}".format(cosine sim(W[tokens['king']], W[tokens['woman']])))
print ("cosine_similarity('man','woman'): {}".format(cosine_sim(W[tokens['man']], W[tokens['woman']])))
print ("cosine similarity('queen','woman'): {}".format(cosine sim(W[tokens['queen']], W[tokens['woman']])))
cosine_similarity('king','woman'): 0.0
cosine similarity('man','woman')
cosine similarity('queen','woman'): 0.0
```

Motivation

- Estimate the similarity between two words
- Why symbolic/one-hot vector representation will fail?
 - can't capture 'context' around word is presented independently!

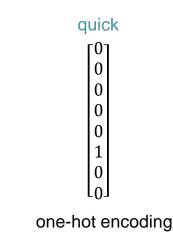
```
from gensim.models import
# load pre-trained GoogleNews model
model_file = 'model/GoogleNews_small'
W = Word2Vec.load(model_file)

print ("cosine_similarity('king','woman'): {}".format(cosine_sim(W['king'], W['woman'])))
print ("cosine_similarity('man','woman'): {}".format(cosine_sim(W['man'], W['woman'])))
print ("cosine_similarity('queen','woman'): {}".format(cosine_sim(W['queen'], W['woman'])))
cosine_similarity('king','woman'): 0.128479748964
cosine_similarity('man','woman'): 0.766401290894
cosine_similarity('queen','woman'): 0.316181391478
```

Toy example

Corpus: the quick brown fox jumps over the lazy dog

- Tokens: {'brown': 0, 'lazy': 1, 'over': 2, 'fox': 3, 'dog': 4, 'quick': 5, 'the': 6, 'jumps': 7}
- Number of tokens N = 8
- Context (window) size C = 1
- Size of embedded vectors d = 3
- U&V: collections of input & output vectors



 w_{t-1}

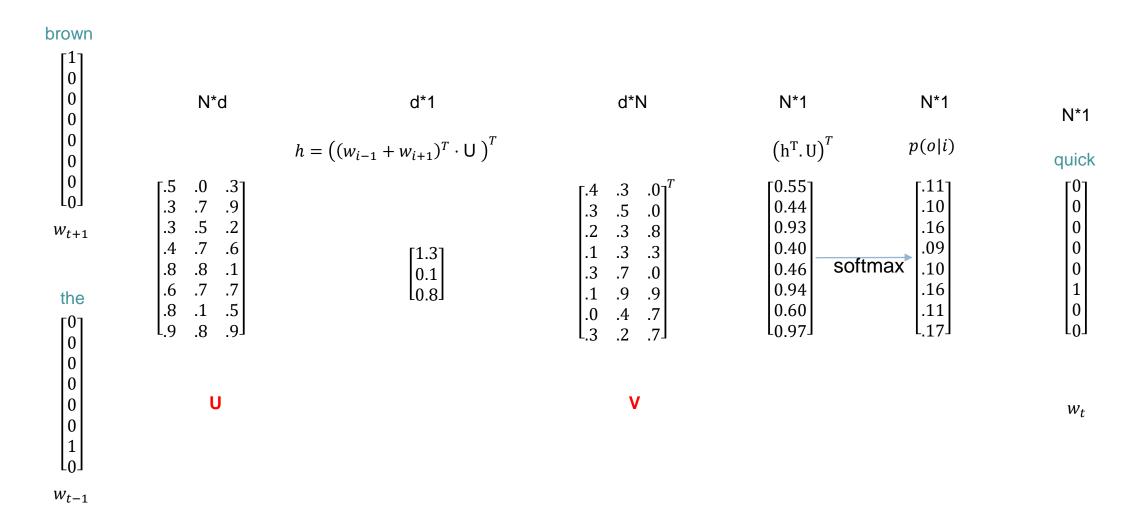
context

Skip-gram, forward propagation

center

N*1 N*d d*1 d*N N*1 N*1 $\begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$ $h = (1_{\mathsf{t}}^T \cdot \mathsf{U})^T$ $(h^T V)^T$ p(o|i)quick brown $\begin{bmatrix} 0.45 \\ 0.53 \end{bmatrix}^T$.10 .14 [.6] .7 .7] 0.89 0.48 0.67 softmax .1 .7 .21 .12 .13 1.32 .9 .8 .9 .5 .0 .3 0.77 w_{t+1} .9] [0.81]0 0 0 0 0 1 U V $w_t = 1_t$ the

CBOW, forward propagation



context center

Learning word2vec: skip-gram

- For each word t = 1 ... T, predict surrounding words in a window of "radius" C of every word.
- Objective function: Maximize the probability of any context word given the current centre word:

$$J(\theta) = \prod_{t=1}^{T} \prod_{-C \le j \le C, j \ne 0} p(w_{t+j}|w_t; \theta)$$

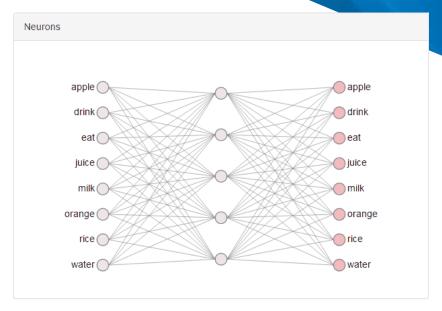
Or, equivalently minimize the negative log likelihood:

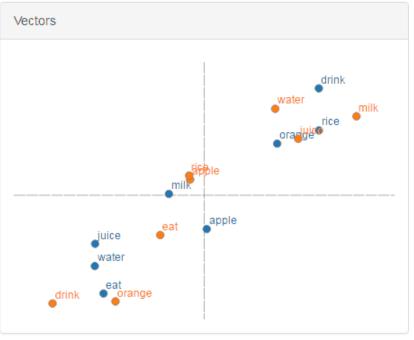
$$J(\theta) = -\frac{1}{T} \sum_{t=1}^{T} \sum_{-C \le j \le C, j \ne 0} \log \left(p(w_{t+j} | w_t; \theta) \right)$$

where $p(o|i) = \frac{e^{u_o^T v_i}}{\sum_{w=1}^W e^{u_w^T v_i}}$, the softmax function, converting scores all classes into a probability distribution

Word embedding

- Representing meaning of words
 - Important for all NLP tasks.
 - WordNet
 - Discrete/one-hot representation
 - Methods: LSA, MDS, LDA
- Word2vec (Mikolov et al. 2013)
 - Distributed representation for word
 - What does it mean? Learn a real-valued vector for each word.
 - Small distances induce similar words
 - Compositionality induces real-valued vector representation for phrases/sentences.
 - A simple application of NN with exactly 2 layers!





https://ronxin.github.io/wevi/