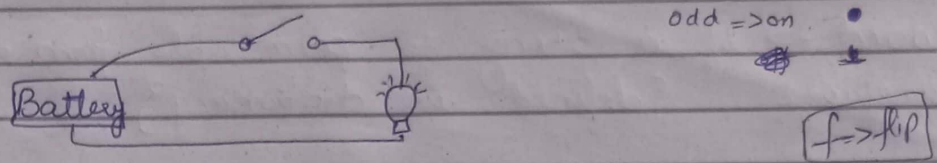
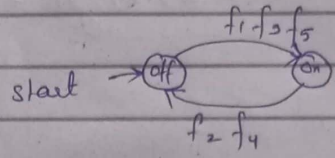


# TOA

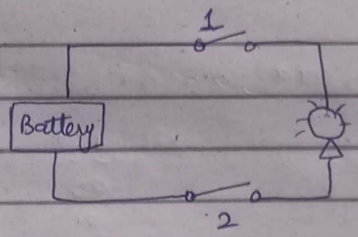
Decoder  $\rightarrow$  select  
Automata  $\Rightarrow$  automatic



jitna zadha data utni zadha accuracy



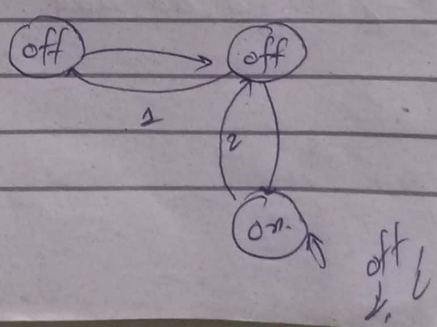
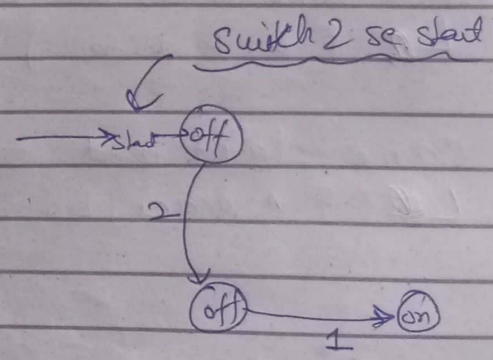
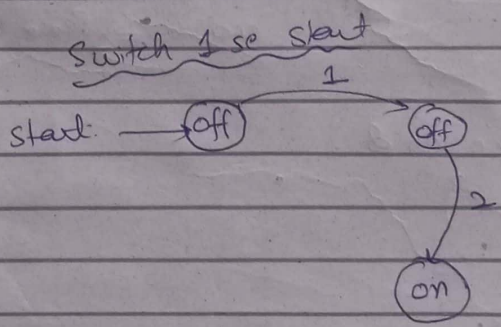
shru mai bulb off he hote  
odd mai on hote hai



	①	2	③	
	↓	↓	↓	$\rightarrow$ on (odd)
$S_1$	1	on	off	1
$S_2$	1	0	1	

circuit break  
off

both bulb will ~~use~~ on only  
when both were switched  
on at odd



alphabet  $\rightarrow$  finite <sup>non-empty</sup> sets of symbols  
 language  $\rightarrow$  sets of words

$$\Sigma = \{a, b\}$$

string  $\rightarrow$  any combination of alphabets

word,  
 $\rightarrow$  apple  $\rightarrow$  string  
 $\rightarrow$  pple  $\rightarrow$  string

tokenization

word  $\Rightarrow$  if a string is permissible from a language {defined in dictionary}

Null String  $\Rightarrow \epsilon$  or  $\wedge \Rightarrow$  length = 0

$$\Sigma = \{a, b\}$$

$$\Rightarrow 2^2 = 4$$

aa

ab

ba

bb

$$L = \{\wedge, a, b, aa, ab, ba, bb\}$$

00  
 01  
 10  
 11

English language

Description  $\rightarrow$  All words of a's and b's which starts and ends at different alphabets.

$$L = \{a, b, ab, ba, \dots\}$$

aa  $\times \Rightarrow$  Reaso.

Same start and same end.

$$L = \{\wedge, aa, bb, \dots\}$$

$$\{a^n : n = 1, 2, 3, \dots\} \Rightarrow L = \{a, aa, aaa, \dots\}$$

$$a^0 \Rightarrow \{\wedge\}$$





odd length  $\Rightarrow$  odd string's length

$\Sigma\{a\} \Rightarrow$  odd

$L = \{a, aaa, aa \dots\}$

$\Sigma\{a\} \Rightarrow$  even

$L = \{aa, aaaa, \dots\}$

$\hookrightarrow$

$L = \{a^0, a^2, a^4, \dots\}$

$\Sigma = \{0, 1, 2\}$

$\rightarrow 3^1 = 3$

$\Rightarrow 3^2 = 9$

$\uparrow$   
base

combinations  
 $\rightarrow$  length 2 ko nikalen

$E^L$  - no of string combinations  
alphabet's length =

$$3^2 = 9$$

00
01
02
10
11
12
20
21
22

$$3^3 = 27$$

$\rightarrow$  3 dafa  
copy karna hai

① Equal

$\Sigma = \{a, b\} \Rightarrow$  alphabet

$L = \{a, ab, aabb, abab, \dots\}$

② Even length

{ even no of a and b }

$\Sigma = \{a, b\}$

$= \{a, aa, bb, aabb, aaaa, \dots\}$

③ Integer

$\Sigma = \{0, \pm 1, \dots\}$



$$\Sigma\{a,b\} \quad \{a^n b^n a^n\} \quad n=2$$

$$\hookrightarrow aa\ bb\ aa$$

## Palindrome

bab

ایسی language string لیتی ہے جس کے reverse کرنے پر original string اور reverse string equal آتا ہے۔ اس میں set of alphabets کا استعمال ہوتا ہے۔

## ◉ KLEEN'S STAR / KLEEN'S CLOSURE (\*)

→ this is operator  
{they perform actions}

operation(+,-)

$\Sigma^*$  (collection of all strings  $\Sigma$ , including null  $\epsilon$ )

$\Sigma$  سے ملتی جلتی strings لیتی ہیں وہ سب  $\Sigma^*$  میں آجاتی ہیں۔

① It accepts null.

② It generates all possible combinations.

③ It always generate infinite language.

جس کا \* لیتے اس سے infinite language / infinite length (set of)

→ yeh operator language ko explain krne k liye

$$\Sigma = \{x\}$$

$$\Rightarrow \Sigma^* = \{\epsilon, x, xx, xxx, \dots\}$$

$$\Sigma = \{aab, c\}$$

$$\Rightarrow \Sigma^* = \{\epsilon, aab, c, aab aab, aab c, c aab, c c \dots\}$$

$$\Sigma = \{a, b\}$$

$$L = \{a, ab\}$$

$$L^* = \{\epsilon, a, ab, aab, aba, abab, \dots\}$$

a se start hoga.  
magre bikhre rahi  
aye gae

(Describe this language (logical definition))  
Language start with a, b will never be placed consecutively

$$S = \{a, b, ab\}$$

$$T = \{a, b, bb\}$$

$$S^* = \{ \lambda, a, b, \overline{ab}, ab, ba, bb, \dots \}$$

$\Rightarrow$  They are equal bcz of \*

$$T^* = \{ \lambda, a, b, \overline{bb}, ab, ba, bb, \dots \}$$

KLEEN (Plus)(+) Operator

④ It does not accept Null

②, ③  $\rightarrow$  same { infinite + all possible combinations }

$$\Sigma = \{0, 1\}$$

$$\Sigma^+ = \{0, 1, 00, 01, 10, 11, \dots\}$$

Theorem  $S \Rightarrow \text{language}$   
 $S^* = S^{**}$

$S^*$  jab kr diya toh sarehi combinations agaye toh  $S^{**}$  mai bhi ushi hon gaye kyu ki is k andar all combinations hon.

$S^* \subset S^{**} \rightarrow S^*$  subset hai  $S^{**}$  ka toh is ko andar sah hi agaye

$S^* \subset S^{**}$ ,  $S^{**} \in S^*$ , Hence  $S^* = S^{**}$ .

Assignment 1

max - solve



## TOA

### Quiz

$$L = \{aa, b\}$$

$$L^* = ?$$

Define language logically

logically  
(short + fm)

Null + all combination of a's and b's  
where a comes twice always.

(→ Null + even pairs of a's  
~~and b's~~)

### Recursive definition of language

3 steps for recursive definition

① Initialization (Universal truth)

② Formula, Condition (Criteria)

③ Else (No string except those 2 steps, are allowed to be in language)

#### Step 1

1 is an integer

#### Step 2

if (n) is an integer then

$n+1$ ,  $n-1$  is also an integer

} yeh recursive  
yeh iterate  
for 'for'

#### Step 3

Nothing else is an integer

#### Even

① 2 is an <sup>even</sup> integer

② if x is an even integer then  $x+2$ ,  $x-2$  is also an even integer

①  $\Sigma = \{a, b\}$

ending in a

Step 1

a is in language

Step 2

$S(x)$  is also in language where  $S \in \Sigma^*$   
(string)

$S(x) \Rightarrow$  matlab  $\Rightarrow$  S jis k andu a, b k combination agaye, x means a

② starts with b

Step 1 b is on laguan

Step 2 b(s) - - - - -

containing at least 1 b

~~③~~ ③ Beech mai b aye  
 $S b S$   $S \in \Sigma^*$

④ an 'a' followed by some b's  
(may be no b's)

Step 1

a is in language

Step 2

a(s) is in language where  $S \in b^*$

$\{ \rightarrow \text{Beech mai b aye}$   
 $\leftarrow \text{Beech mai b aye}$

follow  $\Rightarrow$

اگر 1 b