

" Assignment. 02 "

- (i). All words in which "a" appears a trippled, if at all. clump of a's contain 3 or 6 or 9 ...

$$\rightarrow (aaa+b)^*$$

- (ii) All words that contain at least one of the string s_1, s_2, s_3 or s_4 .

$$\rightarrow (a+b)^*(s_1+s_2+s_3+s_4)(a+b)^*$$

- (iii) All words that contain exactly three bs in total.

$$\rightarrow a^*ba^*ba^*ba^*$$

- (iv). All words that contain exactly two bs or exactly three bs, not more.

$$\rightarrow a^*ba^*ba^* + a^*ba^*ba^*ba^*$$

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(iv). (i). All strings that end in double letter.

$$\rightarrow (a+b)^* \cdot (aa+bb)$$

(ii). All strings that have exactly one double letter in them.

$$\rightarrow (1+b)(ab)^*(ba)^*(b+1) + (a+1)(ba)^*(ab)^*(a+1)$$

(vi). All strings in which the letter b is never trippled.

$$\rightarrow (1+b+bb)(a+ab+abb)^*$$

(vii) All words in which "a" is trippled or "b" is trippled. but not both.

$$\rightarrow (a+b)^*a(a+b)^*a(a+b)^*a(a+b)^* + (a+b)^*b(a+b)^*b(a+b)^*b(a+b)^*$$

(viii). (i). All strings that do not have the substring ab.

$$\rightarrow b^*a^*$$

(ii). All strings that do not have both bba and abb.

$$\rightarrow a^*(baa^*)^*b^* + b^*(a^*ab)^*a^*$$

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Q. All strings in which the total no's of
a's is divisible by 3.

↳ $(b^*ab^*ab^*ab^*)^*$

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$$(b^*ab^*ab^*ab^*)^*$$

- (11) a) All strings in which any b's that occur are found in clumps of an odd number at a time, such as $abbaabbbab$.

$$a^*(b(bb)^*aa^*)^*(1 + b(bb)^*)$$

- b) All strings that have an even number of a's and an odd number of b's

$$(aa+bb+(ab+ba)(aa+bb)^*(ab+ba))^*$$

- c) All strings that have an odd number of a's and an odd number of b's

$$(ab+ba)(aa+bb+(ab+ba)(aa+bb)^*(ab+ba))^*$$

- (12) Let us reconsider the regular expression

$$(a+b)^*a(a+b)^*b(a+b)^*$$

- (1) Show that this is equivalent to

$$(a+b)^*ab(a+b)^*$$

$$babbaab + aababbaa$$

$$bbab$$

$$(i) \quad (ab)^*a \quad \text{or} \quad a(ba)^*$$

$(ab)^*a$, and $a(ba)^*$ represent same language no $bb's$ and starting and ending with a .

$$(ii) \quad (a^*+b)^* \quad \text{or} \quad (a+b)^*$$

$$(a^*)^* + b^* \quad a^* + b^*$$

$$a^* + b^* \quad a^* + b^*$$

Both are all strings Possible in $\Sigma = \{a, b\}$

$$(iii) \quad (a^* + b^*)^* \quad \text{or} \quad (a+b)^*$$

$$(a^*)^* + (b^*)^* \quad (a+b)^*$$

$$a^* + b^* \Rightarrow (a+b)^*$$