

Infix to postfix - Application of stacks (1)

Find the result of the following infix expression:

1. $3 + 5 * 7 - 4^2$

$$3 + 5 * 7 - 16$$

$$3 + 35 - 16$$

$$38 - 16$$

$$\underline{\underline{22}}$$

2. $500 + 5^3 - (10 + 56) * 9$

$$500 + 5^3 - 66 * 9$$

$$500 + 125 - 66 * 9$$

$$625 - 594$$

$$\underline{\underline{31}}$$

3. $3 + 5^6 - 7$

4. $254 + 10 - 9$

5. $365 * 5.2 * 7 + 10/10$

6. $3 + 5 * (7 - 4)^2$

7. $8 * (5^4 + 2) - 6^2 / (9 * 3)$

Infix to postfix Expression Conversion

1. $A + B / C * D - E / (F + G)$

$$A + \underline{B / C} * D - E / (F + G)$$

$$A + \underline{BC /} * D - E / (F + G)$$

$$A + BC / D * - E / (F + G)$$

$$A + BC / D * - E FG + /$$

$$\underline{ABC / D * + - EFG + /}$$

$$ABC / D * + EFG + / -$$

How to Evaluate a postfix Expression

Consider Infix expression

$$3 + 5 * (\underbrace{5 / 5}_1) - \underbrace{2^2}_2 = 4$$

Postfix expression

$$3 + 5 * 55 / - 2^2$$

$$3 + 5 * 55 / - 22^{\wedge}$$

$$3 + 555 / * - 22^{\wedge}$$

$$3555 / * + - 22^{\wedge}$$

$$35555 / * + 22^{\wedge} -$$

Evaluation of postfix expression

(2)

$$3555/*+22^1-$$

1. $5 \times 5 = 1$

$$351*+22^1-$$

2. $5 \times 1 = 5$

$$35+22^1-$$

3. $3+5=8$

$$822^1-$$

4. $2^1 2 = 4$

$$84-$$

5. $8-4=4$

Postfix Expression Conversion using stack

Consider the Infix Expression

$$7 + 5 * 3 / 5 \wedge 1 + (3 - 2)$$

1. Consider 7.

7 is operand so print 7

2. Consider +

+ is operator, so push +

3. Consider 5

5 is operand so print 5

4. Consider *

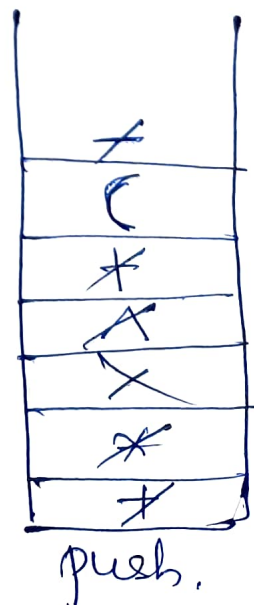
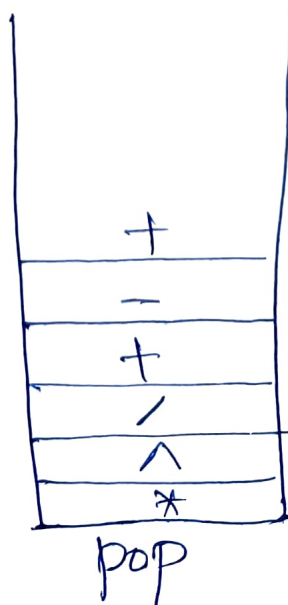
~~+~~ *, so we can push *

5. Consider 3

3 is operand so print 3.

print

$$7 5 3 * 5 \wedge 1 / + 3 2 - +$$



Consider /

= /

o pop * and print *

o push / check

+ * /

7. push /
print 5

8. Consider ^

/ * ^

push ^

9. print 1

10. Consider +

1 > +

So pop 1 and print 1

/ > +

So pop / and print /

+ = +

So pop + and print +

Now push +

11. Consider (

When '(' operator simply push (

12. print 3

13. Consider —

(\neq —

So push —

14. print 2

15. when consider ')' right operator
when ')' operator, pop all operator in the
stack

16. pop — & print —

17. 'C' operator, pop it simply.

18. pop + & print +

create the postfix expression

7 5 3 * 5 1 ^ / + 3 2 - +

1. push 7
2. push 5
3. push 3
4. we got * operator
so pop last 2 symbols
and perform evaluation
pop 5 & 3 and
perform *

$$5 * 3 = 15$$

And store back 15 on to the stack
push 15

5. push 5

6. push 1

7. we encountered ^ operator.

so pop 5 & 1 apply ^

$$5 \wedge 1 = 5$$

push 5

8. we encountered / operator

so pop 15 & 5 apply /

$$15 / 5 = 3$$

1
2
3
10
3
8
1
8
15
3
5
7

$B * A$ or
 $B + A$ or
 $B \wedge A$

9. we encountered +
pop 7 & 3.

$$7 + 3 = 10$$

10. push 3.

11. push 2

12. we encountered -

pop 3 & 2

$$3 - 2 = 1$$

push 1

13. we encountered +

pop 10 & 1

$$10 + 1 = 11$$

push 11.

14. print 11

pl 2

5

in expression to postfix expression
using stack.

$(a+b*c-d)/(e*f)$

~~print~~

1. '('
push '('
2. 'a'
print 'a'
3. '+'

~~+~~ +
push '+'

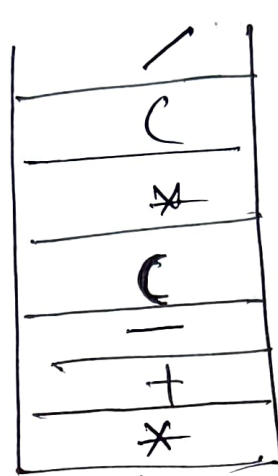
4. 'b'
print b
5. '*'

~~+~~ *
push '*'

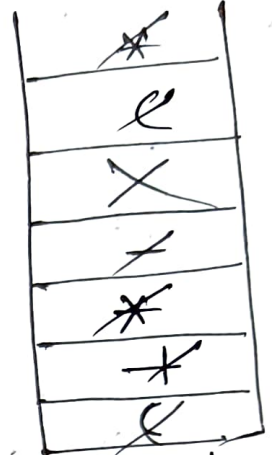
6. 'c'
print 'c'

7. '-'
* > -

pop * to postfix
& print *



postfix



stack.

print

$abc*+d-e*f/$

7. + = -
pop + to postfix & print +

(~~+~~ -
So push '(' on to
stack

8. 'd'
print d

9.)
pop - to postfix & print -

(= pop

10) '/'

Stack is empty, no need to compare, just push it on to stack.

11) '('

push to stack

12) 'e'

print e

13) '*'

~~C~~ * *

push '*' on to stack

14) 'f'

print f

15) ')'.

pop * and print *

16) '('

pop '('

17) '/'

pop / and print /

Example 3

$$a + b * (c \wedge d - e) \wedge (f + g * h) - i$$

a array of Infix to postfix conversion

7	+	(9	-	5)	*	2	10
0	1	2	3	4	5	6	7	8	

(6)

fix

7	9	5	-	2	*	+	'10'		
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$\Rightarrow i=0, j=0$

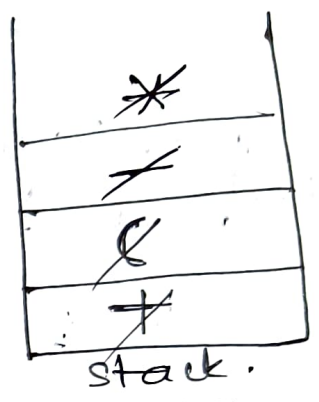
Symbol = infix[0]

Symbol = 7

$\Rightarrow i=1, j=1$

Symbol = infix[1].

Symbol = + push(symbol) on to stack.



$\Rightarrow i=2, j=1$

Symbol = infix[2].

Symbol = (

push(symbol) on to stack

$\Rightarrow i=3, j=1$

Symbol = infix[3].

Symbol = 9

push(symbol) on to postfix array, $j++$

$\Rightarrow i=4, j=2$

Symbol = infix[4].

Symbol = -

while (! is Empty () = True .

$\{ \}$
 $\text{precedence}(\text{stack}[\text{top}]) \geq \text{precedence}(\text{symbol})$

$\text{precedence}('(') \geq \text{precedence}('-')$

$0 \neq 1$

push(symbol)
i.e., push '-' on to the stack.

$\Rightarrow i = 5, j = 2$

symbol = infix[5]

symbol = 5

push(symbol = 5) onto the ~~stack~~ postfix array. $j++$.

$\Rightarrow i = 6, j = 3$

symbol = infix[6].

symbol = ')'

while (next = pop() != '(')

next = - != '(' true.

pop '-' on ~~push~~ ^{insert} it onto postfix

postfix[3++] = - & pop ')' from stack.

$j = 4$

360026
7, j=4
symbol = infix[7]
pop '7' that it.

⇒ i=8, j=4
symbol = infix[8]

⇒ i=7, j=4
symbol = infix[7].
symbol = *

while (!isEmpty()) → True.

p(stack[top]) >= p(symbol)

+ >= * False.

push '+' onto the stack.

⇒ i=8, j=4
symbol = infix[8].

symbol = 2

push '2' onto the postfix array.

j=5

⇒ i=9, j=5
9 < 9.

⇒ while (!isEmpty()) = True.

postfix[5] = pop() = *

j=6

\Rightarrow while (!is Empty ()) \rightarrow True ,
postfix [6] = pop() = +

\Rightarrow postfix [7] = '\0' .