

GRAPH COLOURING:

```
def graph_coloring(adj_list):  
    colors = {}  
    max_color = 0  
  
    for node in adj_list:  
        neighbor_colors = set(colors.get(nei, 0) for nei in adj_list[node])  
        color = 1  
        while color in neighbor_colors:  
            color += 1  
        colors[node] = color  
        max_color = max(max_color, color)  
  
    return max_color
```

Adjacency list representation of the graph

```
adj_list = {  
    0: [1, 2, 3],  
    1: [0, 2],  
    2: [1, 3, 0],  
    3: [2, 0]  
}  
  
max_regions_colored = graph_coloring(adj_list)  
print(max_regions_colored)
```

MAXIMUM AND MINIMUM VALUE:

```
array1 = [2, 4, 6, 8, 10, 12, 14, 18]
```

```
array2 = [11,13,15,17,19,21,23,35,37]
```

```
min_value = min(array1)
```

```
max_value = max(array1)
```

```
min_value2 = min(array2)
```

```
max_value2 = max(array2)
```

```
print("Input Array:", array1)
```

```
print("Minimum Value:", min_value)
```

```
print("Maximum Value:", max_value)
```

```
print("Input Array:", array2)
```

```
print("Minimum Value:", min_value2)
```

```
print("Maximum Value:", max_value2)
```

ROBBERY:

```
def rob(nums):
```

```
    if not nums:
```

```
        return 0
```

```
    if len(nums) <= 2:
```

```
        return max(nums)
```

```
def rob_helper(nums):
```

```
    dp = [0] * len(nums)
```

```
    dp[0] = nums[0]
```

```
    dp[1] = max(nums[0], nums[1])
```

```
    for i in range(2, len(nums)):
```

```
        dp[i] = max(dp[i-1], dp[i-2] + nums[i])
```

```
return dp[-1]
```

```
return max(rob_helper(nums[1:]), rob_helper(nums[: -1]))
```

```
# Test the function with example inputs
```

```
print(rob([2, 3, 2]))
```

```
print(rob([1, 2, 3, 1]))
```

DIJAKRASTRA'S:

```
import sys
```

```
def dijkstra(graph, source):
```

```
    n = len(graph)
```

```
    dist = [sys.maxsize] * n
```

```
    dist[source] = 0
```

```
    visited = [False] * n
```

```
    for _ in range(n):
```

```
        u = min_distance(dist, visited)
```

```
        visited[u] = True
```

```
    for v in range(n):
```

```
        if not visited[v] and graph[u][v] != sys.maxsize and dist[u] + graph[u][v] < dist[v]:
```

```
            dist[v] = dist[u] + graph[u][v]
```

```
    return dist
```

```
def min_distance(dist, visited):
```

```
    min_dist = sys.maxsize
```

```
min_index = -1
```

```
for v in range(len(dist)):
```

```
    if not visited[v] and dist[v] < min_dist:
```

```
        min_dist = dist[v]
```

```
        min_index = v
```

```
return min_index
```

```
graph = [
```

```
    [0, 10, 3, sys.maxsize, sys.maxsize],
```

```
    [sys.maxsize, 0, 1, 2, sys.maxsize],
```

```
    [sys.maxsize, 4, 0, 8, 21],
```

```
    [sys.maxsize, sys.maxsize, sys.maxsize, 0, 6],
```

```
    [sys.maxsize, sys.maxsize, sys.maxsize, sys.maxsize, 0]
```

```
]
```

```
source = 0
```

```
result = dijkstra(graph, source)
```

```
print(result)
```

```
graph = [
```

```
    [0, 5, sys.maxsize, 10],
```

```
    [sys.maxsize, 0, 3, sys.maxsize],
```

```
    [sys.maxsize, sys.maxsize, 0, 1],
```

```
    [sys.maxsize, sys.maxsize, sys.maxsize, 0]
```

```
]
```

```
source = 3
```

```
result = dijkstra(graph, source)
```

```
print(result)
```

SELECTION SORT:

```
def selection_sort(arr):  
    n = len(arr)  
    for i in range(n):  
        min_idx = i  
        for j in range(i+1, n):  
            if arr[j] < arr[min_idx]:  
                min_idx = j  
        arr[i], arr[min_idx] = arr[min_idx], arr[i]  
    return arr  
  
random_array = [52, 9, 1, 5, 6]  
sorted_random_array = selection_sort(random_array)  
print(sorted_random_array)
```

```
reverse_sorted_array = [12, 8, 6, 4, 2]  
sorted_reverse_array = selection_sort(reverse_sorted_array)  
print(sorted_reverse_array)
```

```
already_sorted_array = [1, 2, 3, 4, 5]  
sorted_already_sorted_array = selection_sort(already_sorted_array)  
print(sorted_already_sorted_array)
```

SEQUENTIAL SEARCH:

```
def findKthPositive(arr, k):  
    missing = []  
    i = 1  
    while len(missing) < k:
```

```
    if i not in arr:
        missing.append(i)
    i += 1
return missing[-1]
```

```
arr1 = [2, 3, 4, 7, 11]
k1 = 5
output1 = findKthPositive(arr1, k1)
print(output1)
```

```
arr2 = [1, 2, 3, 4, 14, 15]
k2 = 2
output2 = findKthPositive(arr2, k2)
print(output2)
```

BINARY SEARCH:

```
def binary_search(arr, x):
    low = 0
    high = len(arr) - 1
    mid = 0
    count = 0

    while low <= high:
        mid = (high + low) // 2
        count += 1

        if arr[mid] < x:
            low = mid + 1
```

```
elif arr[mid] > x:
    high = mid - 1
else:
    return mid, count
```

```
return -1, count
```

```
arr = [5, 10, 15, 20, 25, 30, 35, 40, 45]
```

```
x = 20
```

```
result, comparisons = binary_search(arr, x)
```

```
print("Index of element 20:", result)
```

```
print("Number of comparisons made:", comparisons)
```

COMBINATION SUM:

```
def combinationSum(candidates, target):
```

```
    def backtrack(start, path, target):
```

```
        if target == 0:
```

```
            res.append(path[:])
```

```
            return
```

```
        for i in range(start, len(candidates)):
```

```
            if candidates[i] > target:
```

```
                continue
```

```
            path.append(candidates[i])
```

```
            backtrack(i, path, target - candidates[i])
```

```
            path.pop()
```

```
res = []
```

```
candidates.sort()
```

```
backtrack(0, [], target)
```

```
    return res
```

```
candidates1 = [2, 3, 6, 7]
```

```
target1 = 7
```

```
print(combinationSum(candidates1, target1))
```

```
candidates2 = [2, 3, 5]
```

```
target2 = 8
```

```
print(combinationSum(candidates2, target2))
```

```
candidates3 = [2]
```

```
target3 = 1
```

```
print(combinationSum(candidates3, target3))
```

MERGE SORT:

```
def merge_sort(arr):
```

```
    if len(arr) > 1:
```

```
        mid = len(arr) // 2
```

```
        L = arr[:mid]
```

```
        R = arr[mid:]
```

```
        merge_sort(L)
```

```
        merge_sort(R)
```

```
    i = j = k = 0
```

```
    while i < len(L) and j < len(R):
```

```
        if L[i] < R[j]:
```

```
            arr[k] = L[i]
```



```
        i += 1
    else:
        arr[k] = R[j]
        j += 1
    k += 1
```

```
while i < len(L):
    arr[k] = L[i]
    i += 1
    k += 1
```

```
while j < len(R):
    arr[k] = R[j]
    j += 1
    k += 1
```

```
def print_list(arr):
    for i in range(len(arr)):
        print(arr[i], end=" ")
    print()
```

```
arr1 = [31, 23, 35, 27, 11, 21, 15, 28]
merge_sort(arr1)
print("Sorted array:")
print_list(arr1)
```

```
arr2 = [22, 34, 25, 36, 43, 67, 52, 13, 65, 17]
merge_sort(arr2)
print("Sorted array:")
print_list(arr2)
```

DIVIDE AND CONQUER:

```
import heapq
```

```
def kClosest(points, k):
```

```
    heap = []
```

```
    for x, y in points:
```

```
        dist = -(x*x + y*y)
```

```
        if len(heap) == k:
```

```
            heapq.heappushpop(heap, (dist, x, y))
```

```
    else:
```

```
        heapq.heappush(heap, (dist, x, y))
```

```
    return [(x, y) for (dist, x, y) in heap]
```

```
points1 = [[1, 3], [-2, 2], [5, 8], [0, 1]]
```

```
k1 = 2
```

```
print(kClosest(points1, k1))
```

```
points2 = [[1, 3], [-1, 2], [5, -1]]
```

```
k2 = 2
```

```
print(kClosest(points2, k2))
```

```
points3 = [[3, 3], [5, -1], [2, 4]]
```

```
k3 = 2
```

```
print(kClosest(points3, k3))
```