

3.43) a) Continued; from previous attempt

$$4 \int_0^{1/2} x dx \int_{1/4}^{1/2} y dy = 4 \left(\frac{1}{8} \right) \left(\frac{1}{4} - \frac{1}{16} \right) = \frac{3}{64} = .046875$$

3.37) a) Correction of Prev attempt

$$\left. \begin{aligned} f(1,1) + f(1,2) + f(1,3) &= 1c + 2c + 3c = 6c \\ f(2,1) + f(2,2) + f(2,3) &= 2c + 4c + 6c = 12c \\ f(3,1) + f(3,2) + f(3,3) &= 3c + 6c + 9c = 18c \end{aligned} \right\} 36c$$

$$C = \frac{1}{36}$$

3.37 a) $f(x,y) = cxy \rightarrow 1 = \sum_{x=0}^3 \sum_{y=0}^3 cxy = f(0,0) + f(1,1) + f(2,2) + f(3,3)$

$f(0,0) + f(0,1) + f(0,2) = 0$

$f(1,0) + f(1,1) + f(1,2) = 0 + c + 2c = 3c$

$f(2,0) + f(2,1) + f(2,2) = 0 + 2c + 4c = 6c$

$f(3,0) + f(3,1) + f(3,2) = 0 + 3c + 6c = 9c$

$3c + 6c + 9c = 18c \rightarrow c = \frac{1}{18}$

3.43

a) $f(x,y) = 4xy$

$4 \int_0^{1/2} x dx \int_0^{1/4} y dy = 4 \cdot \frac{x^2}{2} \cdot \frac{y^2}{2} = 4 \left(\frac{(\frac{1}{2})^2}{2} \right) \left(\frac{(\frac{1}{4})^2}{2} \right) = \left(\frac{1}{4} \right) \left(\frac{1}{8} \right) = \frac{1}{32}$

$4 \left(\frac{1}{8} - 0 \right) \left(\frac{1}{32} - 0 \right) = \frac{4}{256} = \frac{1}{64}$

$\frac{1}{8} \cdot \frac{1}{32} = \frac{1}{256}$
 $\frac{1}{256} = \frac{1}{64}$

3.49

a, b)

		x			
f(x,y)		1	2	3	
y	1	.05	.05	.1	.2
	3	.05	.1	.35	.5
	5	.05	.2	.1	.3
		.1	.35	.55	1

c) $\frac{P(y|x)}{P(x)} = \frac{.1}{.35} = .286$

3.54

$f(2,3) = .1$

$x = .55$
 $y = .5$
 $xy = .19$

$f(2,3) \neq xy$

dependent

3.5] a) $x = C(x^2 + 4)$; $\sum_{x=0}^{x=3} C(x^2 + 4) = C[(4) + (5) + (8) + (13)] = C(30)$
 $1 = C(30) \quad C = \frac{1}{30}$

$$\boxed{C = \frac{1}{30}}$$

b) $C\binom{2}{x}\binom{3}{3-x}$; $1 = \sum C\binom{2}{x}\binom{3}{3-x} = C[(1)(1) + (2)(3) + (1)(3)]$
 $= C(1 + 6 + 3)$
 $= C(10)$

$$\boxed{C = \frac{1}{10}}$$

3.7] a) $100 \text{ hrs} = 1$; $120 \text{ hrs} = 1.2$
 $\int_0^1 x dx + \int_1^{1.2} (2-x) dx \rightarrow \frac{x^2}{2} + \frac{2x - x^2}{2}$

$$\left. \frac{x^2}{2} \right|_0^1 + \left. 2x - \frac{x^2}{2} \right|_1^{1.2} = \left[\frac{1^2}{2} - 0 \right] + \left[(2 \times 1.2) - \frac{1.2^2}{2} \right] - \left(2 - \frac{1}{2} \right)$$

$$\boxed{= .68}$$

b) $\int_{1/2}^1 x dx = \left. \frac{x^2}{2} \right|_{1/2}^1 = \frac{1}{2} - \left(\frac{1}{8} \right) = \boxed{.375}$

3.13]

$$f(x) = \begin{cases} f(0) & 0 \leq x < 1 \\ f(0) + f(1) & 1 \leq x < 2 \\ f(0) + f(1) + f(2) & 2 \leq x < 3 \\ \vdots & \vdots \\ 1 & x \geq 4 \end{cases}$$