

# Marketing analysis

## I- General introduction

**Origin** The present dataframe has been created for marketing analysis purposes. It assembles various personal information about 2239 customers, such as their education level, income, age, marital status, number of children at home... It also shows their consuming habits (amount spent on wine, on sweets...) and the number of purchases made on discounted products.

There is very few context concerning this dataframe, since the source is unknown. It is not clear when these informations were registered, but probably by 2014 since the date of customers' enrollment within the company doesn't go further than 2014.

**Aims** *To predict the customer's behavior (Number of purchases made with a discount) depending on the most significant personal attributes* To categorize participants in a few typical profiles (probably with PCA)

### Attributes

- *People*

ID: Customer's unique identifier Year\_Birth: Customer's birth year Education: Customer's education level Marital\_Status: Customer's marital status Income: Customer's yearly household income Kidhome: Number of children in customer's household Teenhome: Number of teenagers in customer's household Dt\_Customer: Date of customer's enrollment with the company Recency: Number of days since customer's last purchase Complain: 1 if customer complained in the last 2 years, 0 otherwise

- *Products*

MntWines: Amount spent on wine in last 2 years MntFruits: Amount spent on fruits in last 2 years MntMeatProducts: Amount spent on meat in last 2 years MntFishProducts: Amount spent on fish in last 2 years MntSweetProducts: Amount spent on sweets in last 2 years MntGoldProds: Amount spent on gold in last 2 years

- *Promotions*

NumDealsPurchases: Number of purchases made with a discount AcceptedCmp1: 1 if customer accepted the offer in the 1st campaign, 0 otherwise AcceptedCmp2: 1 if customer accepted the offer in the 2nd campaign, 0 otherwise AcceptedCmp3: 1 if customer accepted the offer in the 3rd campaign, 0 otherwise AcceptedCmp4: 1 if customer accepted the offer in the 4th campaign, 0 otherwise AcceptedCmp5: 1 if customer accepted the offer in the 5th campaign, 0 otherwise Response: 1 if customer accepted the offer in the last campaign, 0 otherwise NumStorePurchases: Number of purchases made directly in stores

Before loading the dataset, we want to make sure we have all the necessary packages installed and loaded, and that the code can be run by anybody.

```
if(!require(pacman)) {  
  install.packages("pacman")  
  library(pacman)  
}
```

```
## Loading required package: pacman
```

```
pacman::p_load(tidyverse, gtsummary, ggpubr, moments, here, sjPlot, parameters, effectsize)

path = here("JULIETTE")
setwd(path)
data <- read.table("marketing_campaign.csv", header=T, sep="\t")
```

## II - Data overview and clearing

```
summary(data)
```

```
##           ID           Year_Birth      Education      Marital_Status
##  Min.      :    0      Min.      :1893      Length:2240      Length:2240
##  1st Qu.: 2828      1st Qu.:1959      Class :character      Class :character
##  Median : 5458      Median :1970      Mode  :character      Mode  :character
##  Mean    : 5592      Mean    :1969
##  3rd Qu.: 8428      3rd Qu.:1977
##  Max.    :11191      Max.    :1996
##
##           Income           Kidhome           Teenhome           Dt_Customer
##  Min.      : 1730      Min.      :0.0000      Min.      :0.0000      Length:2240
##  1st Qu.: 35303      1st Qu.:0.0000      1st Qu.:0.0000      Class :character
##  Median : 51382      Median :0.0000      Median :0.0000      Mode  :character
##  Mean    : 52247      Mean    :0.4442      Mean    :0.5062
##  3rd Qu.: 68522      3rd Qu.:1.0000      3rd Qu.:1.0000
##  Max.    :666666      Max.      :2.0000      Max.      :2.0000
##  NA's      :24
##           Recency           MntWines           MntFruits           MntMeatProducts
##  Min.      : 0.00      Min.      : 0.00      Min.      : 0.0      Min.      : 0.0
##  1st Qu.:24.00      1st Qu.: 23.75      1st Qu.: 1.0      1st Qu.: 16.0
##  Median :49.00      Median : 173.50      Median : 8.0      Median : 67.0
##  Mean    :49.11      Mean    : 303.94      Mean    : 26.3      Mean    : 166.9
##  3rd Qu.:74.00      3rd Qu.: 504.25      3rd Qu.: 33.0      3rd Qu.: 232.0
##  Max.    :99.00      Max.    :1493.00      Max.    :199.0      Max.    :1725.0
##
##  MntFishProducts MntSweetProducts MntGoldProds NumDealsPurchases
##  Min.      : 0.00      Min.      : 0.00      Min.      : 0.00      Min.      : 0.000
##  1st Qu.: 3.00      1st Qu.: 1.00      1st Qu.: 9.00      1st Qu.: 1.000
##  Median :12.00      Median : 8.00      Median :24.00      Median : 2.000
##  Mean    :37.53      Mean    :27.06      Mean    :44.02      Mean    : 2.325
##  3rd Qu.:50.00      3rd Qu.:33.00      3rd Qu.:56.00      3rd Qu.: 3.000
##  Max.    :259.00      Max.    :263.00      Max.    :362.00      Max.    :15.000
##
##  NumWebPurchases NumCatalogPurchases NumStorePurchases NumWebVisitsMonth
##  Min.      : 0.000      Min.      : 0.000      Min.      : 0.00      Min.      : 0.000
##  1st Qu.: 2.000      1st Qu.: 0.000      1st Qu.: 3.00      1st Qu.: 3.000
##  Median : 4.000      Median : 2.000      Median : 5.00      Median : 6.000
##  Mean    : 4.085      Mean    : 2.662      Mean    : 5.79      Mean    : 5.317
##  3rd Qu.: 6.000      3rd Qu.: 4.000      3rd Qu.: 8.00      3rd Qu.: 7.000
##  Max.    :27.000      Max.    :28.000      Max.    :13.00      Max.    :20.000
##
##  AcceptedCmp3      AcceptedCmp4      AcceptedCmp5      AcceptedCmp1
```

```
## Min. :0.00000 Min. :0.00000 Min. :0.00000 Min. :0.00000
## 1st Qu.:0.00000 1st Qu.:0.00000 1st Qu.:0.00000 1st Qu.:0.00000
## Median :0.00000 Median :0.00000 Median :0.00000 Median :0.00000
## Mean :0.07277 Mean :0.07455 Mean :0.07277 Mean :0.06429
## 3rd Qu.:0.00000 3rd Qu.:0.00000 3rd Qu.:0.00000 3rd Qu.:0.00000
## Max. :1.00000 Max. :1.00000 Max. :1.00000 Max. :1.00000
##
## AcceptedCmp2 Complain Z_CostContact Z_Revenue
## Min. :0.00000 Min. :0.000000 Min. :3 Min. :11
## 1st Qu.:0.00000 1st Qu.:0.000000 1st Qu.:3 1st Qu.:11
## Median :0.00000 Median :0.000000 Median :3 Median :11
## Mean :0.01339 Mean :0.009375 Mean :3 Mean :11
## 3rd Qu.:0.00000 3rd Qu.:0.000000 3rd Qu.:3 3rd Qu.:11
## Max. :1.00000 Max. :1.000000 Max. :3 Max. :11
##
## Response
## Min. :0.0000
## 1st Qu.:0.0000
## Median :0.0000
## Mean :0.1491
## 3rd Qu.:0.0000
## Max. :1.0000
##
```

```
str(data)
```

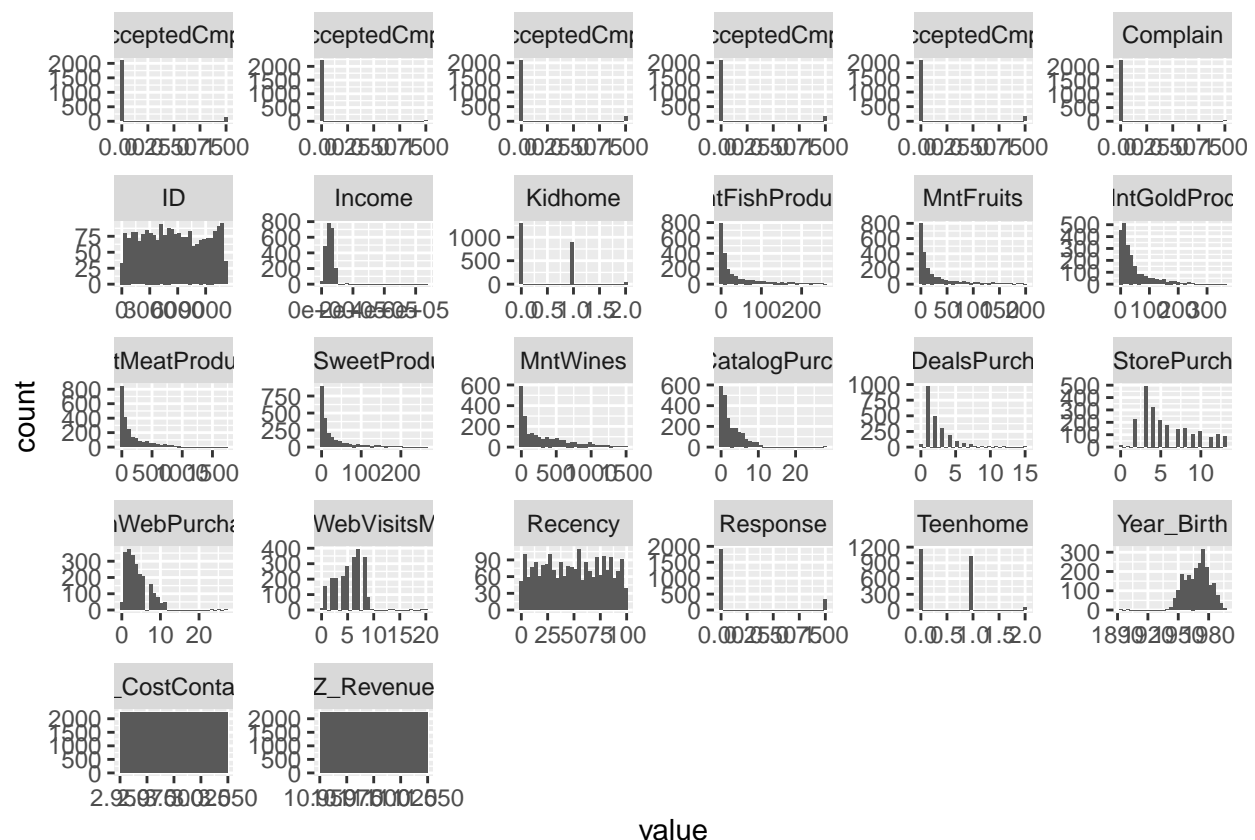
```
## 'data.frame': 2240 obs. of 29 variables:
## $ ID : int 5524 2174 4141 6182 5324 7446 965 6177 4855 5899 ...
## $ Year_Birth : int 1957 1954 1965 1984 1981 1967 1971 1985 1974 1950 ...
## $ Education : chr "Graduation" "Graduation" "Graduation" "Graduation" ...
## $ Marital_Status : chr "Single" "Single" "Together" "Together" ...
## $ Income : int 58138 46344 71613 26646 58293 62513 55635 33454 30351 5648 ...
## $ Kidhome : int 0 1 0 1 1 0 0 1 1 1 ...
## $ Teenhome : int 0 1 0 0 0 1 1 0 0 1 ...
## $ Dt_Customer : chr "04-09-2012" "08-03-2014" "21-08-2013" "10-02-2014" ...
## $ Recency : int 58 38 26 26 94 16 34 32 19 68 ...
## $ MntWines : int 635 11 426 11 173 520 235 76 14 28 ...
## $ MntFruits : int 88 1 49 4 43 42 65 10 0 0 ...
## $ MntMeatProducts : int 546 6 127 20 118 98 164 56 24 6 ...
## $ MntFishProducts : int 172 2 111 10 46 0 50 3 3 1 ...
## $ MntSweetProducts : int 88 1 21 3 27 42 49 1 3 1 ...
## $ MntGoldProds : int 88 6 42 5 15 14 27 23 2 13 ...
## $ NumDealsPurchases : int 3 2 1 2 5 2 4 2 1 1 ...
## $ NumWebPurchases : int 8 1 8 2 5 6 7 4 3 1 ...
## $ NumCatalogPurchases : int 10 1 2 0 3 4 3 0 0 0 ...
## $ NumStorePurchases : int 4 2 10 4 6 10 7 4 2 0 ...
## $ NumWebVisitsMonth : int 7 5 4 6 5 6 6 8 9 20 ...
## $ AcceptedCmp3 : int 0 0 0 0 0 0 0 0 0 1 ...
## $ AcceptedCmp4 : int 0 0 0 0 0 0 0 0 0 0 ...
## $ AcceptedCmp5 : int 0 0 0 0 0 0 0 0 0 0 ...
## $ AcceptedCmp1 : int 0 0 0 0 0 0 0 0 0 0 ...
## $ AcceptedCmp2 : int 0 0 0 0 0 0 0 0 0 0 ...
## $ Complain : int 0 0 0 0 0 0 0 0 0 0 ...
## $ Z_CostContact : int 3 3 3 3 3 3 3 3 3 3 ...
```

```
## $ Z_Revenue      : int  11 11 11 11 11 11 11 11 11 11 ...
## $ Response       : int   1 0 0 0 0 0 0 0 1 0 ...
```

```
data %>%
  keep(is.numeric) %>%
  gather() %>%
  ggplot(aes(value)) +
  facet_wrap(~key, scales = "free") +
  geom_histogram()
```

```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

```
## Warning: Removed 24 rows containing non-finite values (stat_bin).
```



We are only interested in the total number of promotions accepted by the customers, since we don't have details about the nature of each promotion.

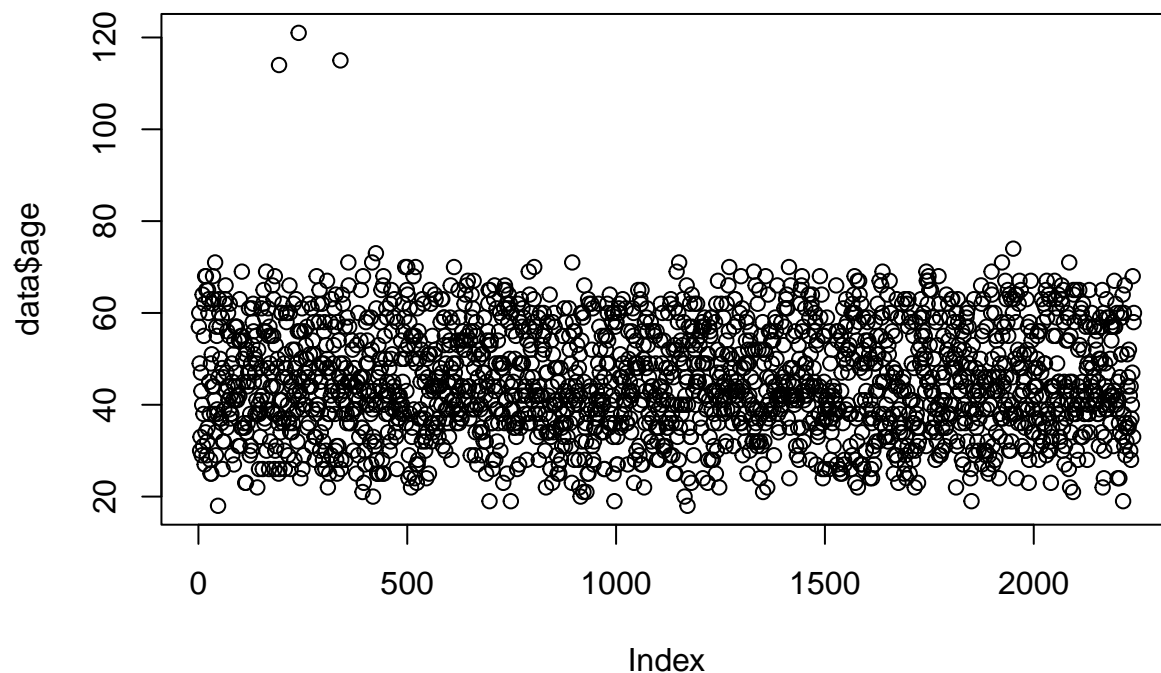
```
data$AcceptedCmpTotal <- data$AcceptedCmp1 + data$AcceptedCmp2 + data$AcceptedCmp3 + data$AcceptedCmp4 +
```

The dataframe contains many variables, some are superfluous for our analysis (web visits and purchases, complains, catalog purchases, Z\_Revenue and Z\_CostContact which we don't have information about)

```
data$Complain <- data$NumWebVisitsMonth <- data$NumWebPurchases <- data$NumCatalogPurchases <- data$Z_Revenue <-
```

We want to calculate the age of the customers. If we proceed with “2021 - data\$Year\_Birth” we would get their current age. It makes sense to use “data\$Year\_Birth”, although here we are only assuming that it was indeed registered in 2014.

```
data$age <- 2014 - data$Year_Birth
plot(data$age)
```



We see 3 outliers who seems to be older than 110 years old. The corresponding birth years are 1893, 1900 and 1899. The first one could be corrected by 1993, the second one would be due to 2 typing errors which is improbable, and the third could be replaced by 1999 but it corresponds to someone who has a PhD education level, which is unlikely at age 15. Since the dataset is very big, we can choose to delete these lines.

```
which(data$age>110)
```

```
## [1] 193 240 340
```

```
data <- data[-c(193, 240, 340),]
```

Marital\_Status can be simplified in only a few levels, and transformed into a factor. Since the “other” section represents less than 1% of the participants, it is not enough to model it as a factor. We then transform some relevant variables into factors.

```
data$Marital_Status <- factor(data$Marital_Status, labels = c("Other", "Single", "Single", "Married", "Married", "Married"))
data$Marital_Status[data$Marital_Status=="Other"] <- NA; data$Marital_Status = droplevels(data$Marital_Status)

data$Education <- factor(data$Education)
data$Teenhome <- factor(data$Teenhome)
data$AcceptedCmpTotal <- factor(data$AcceptedCmpTotal)
data$Kidhome <- factor(data$Kidhome, labels = c("no", "yes", "yes"))
```

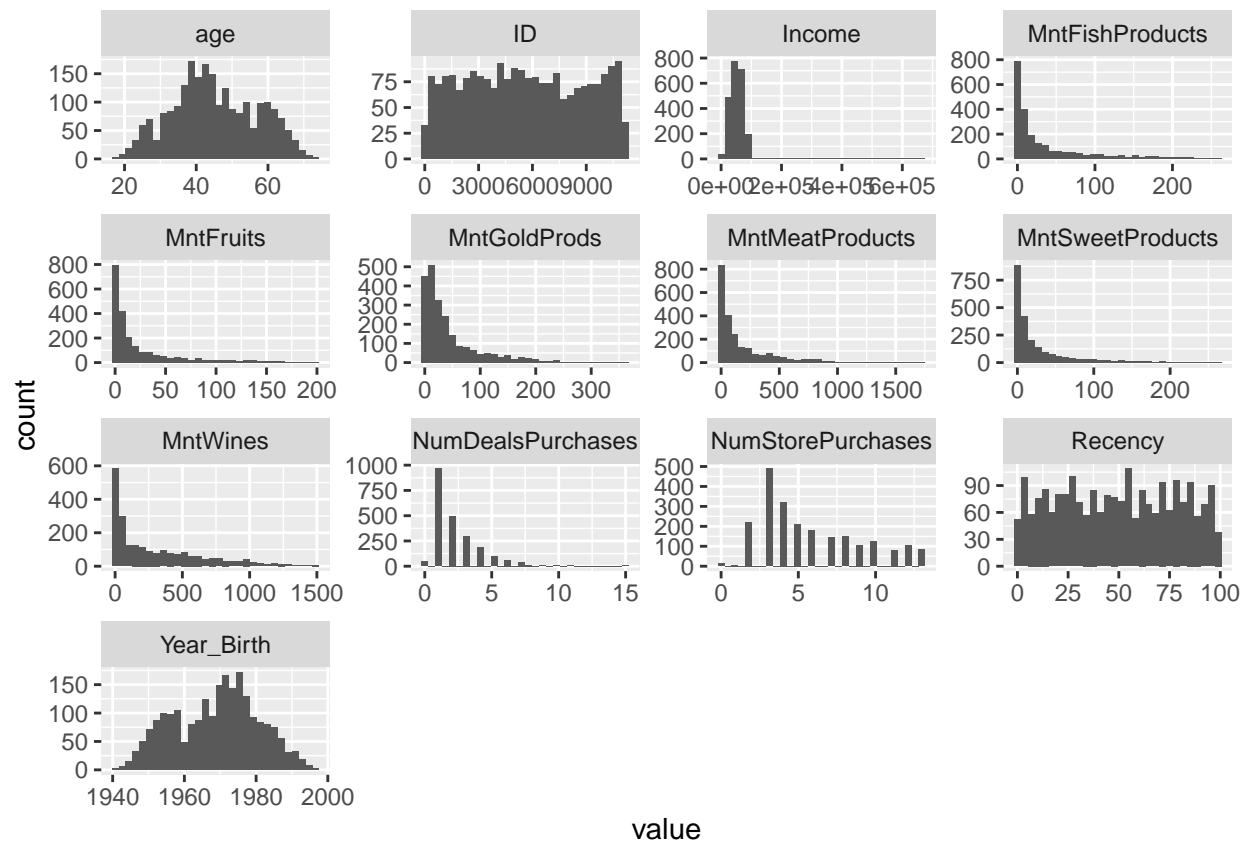
For Kidhome, we fused the answers “1” and “2” because there are only 2% of “2” which is not enough information to model it as a one separate factor.

We now want to plot all the variables again, and check again whether anything is abnormal.

```
data %>%
  keep(is.numeric) %>%
  gather() %>%
  ggplot(aes(value)) +
  facet_wrap(~key, scales = "free") +
  geom_histogram()
```

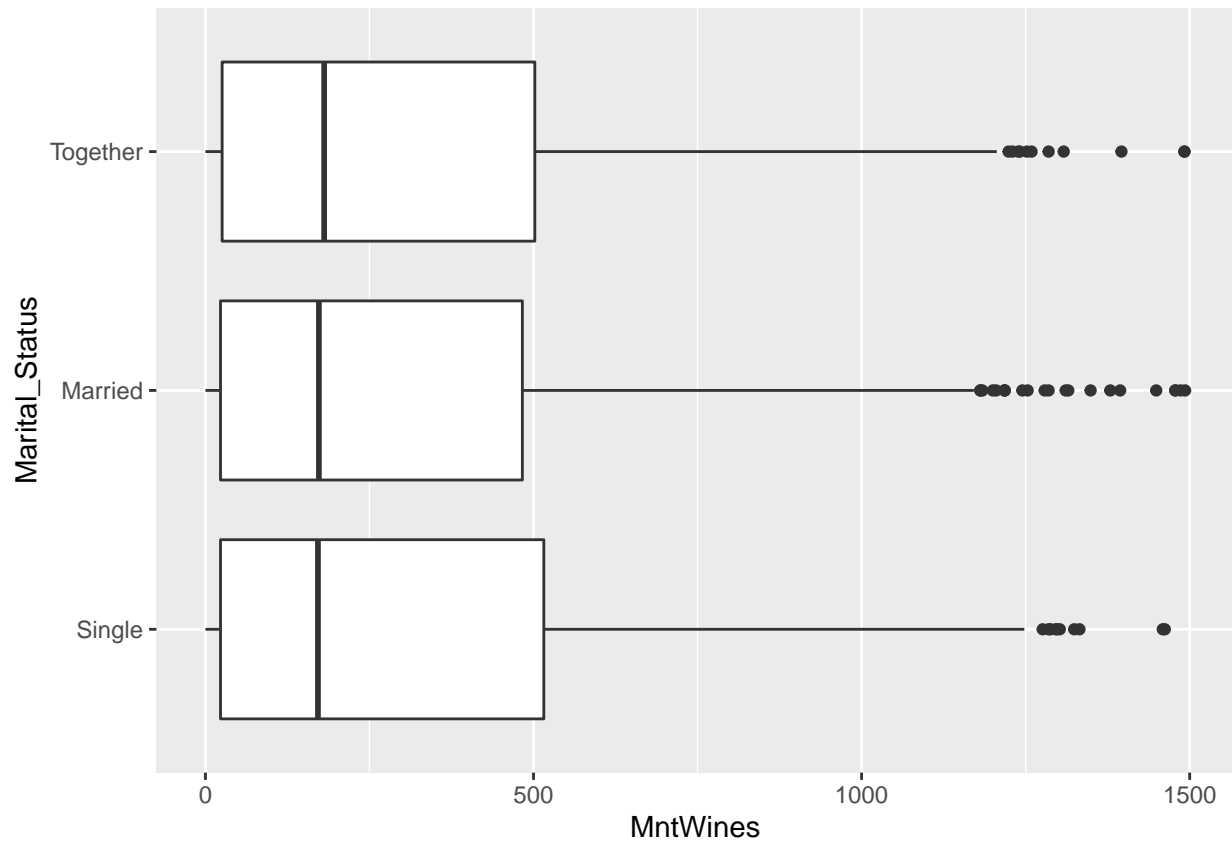
```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

```
## Warning: Removed 24 rows containing non-finite values (stat_bin).
```

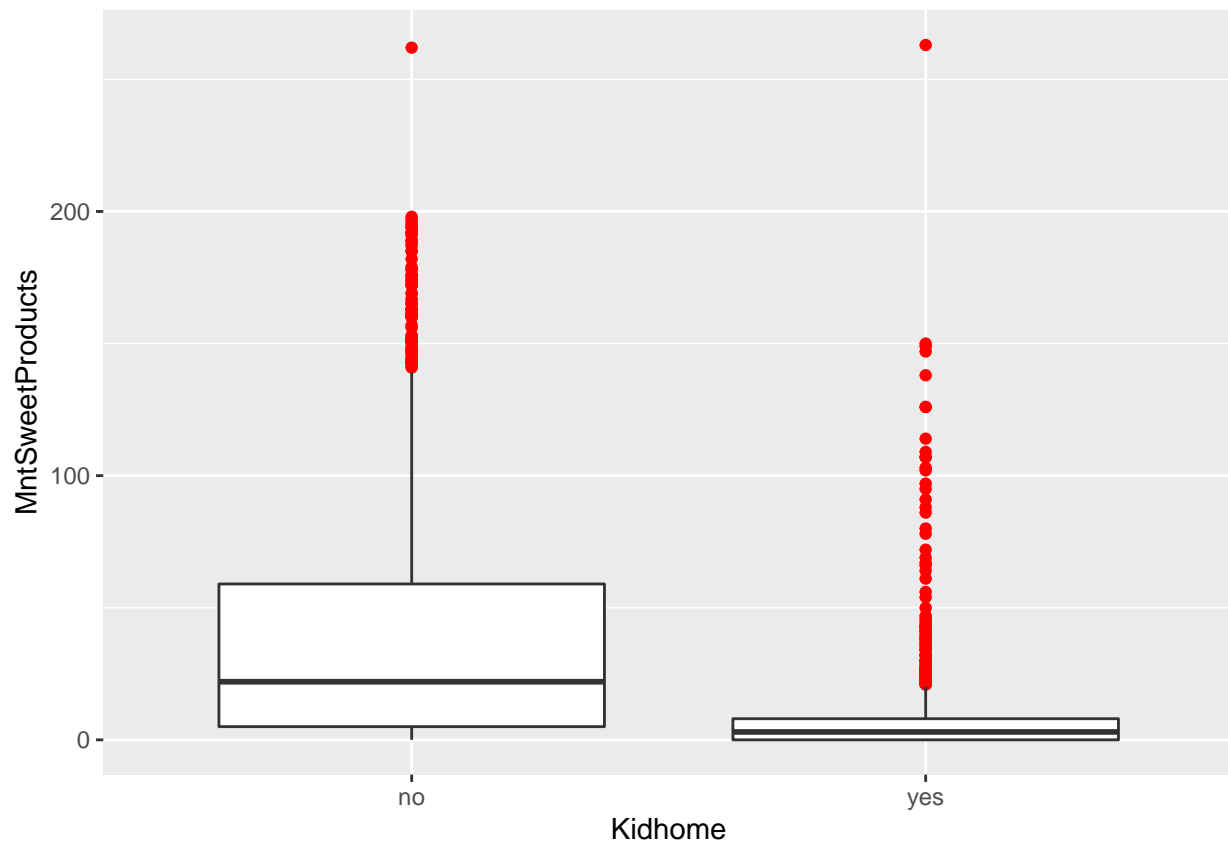


### III - Hypotheses

```
#####
data %>%
  filter(!is.na(Marital_Status)) %>%
  # filter on non-missing values
  ggplot(aes(MntWines, Marital_Status)) + geom_boxplot(na.rm = TRUE)
```

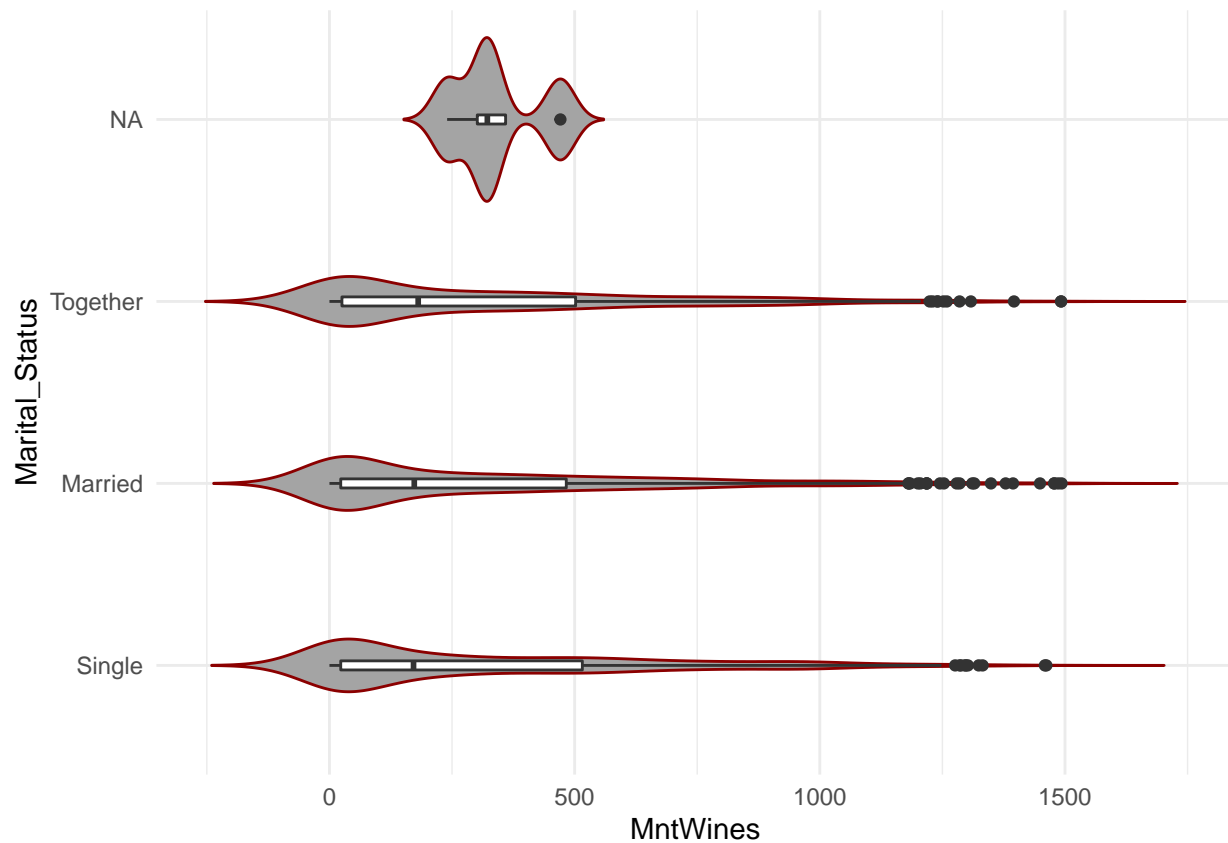


```
ggplot(data, aes(Kidhome, MntSweetProducts))+ geom_boxplot(outlier.colour = "red") #+ geom_point(position = "jitter", colour = "red")
```



```
ggplot(data, aes(x=MntWines, y=Marital_Status)) +  
  geom_violin(trim=FALSE, fill='#A4A4A4', color="darkred")+  
  geom_boxplot(width=0.05) + theme_minimal()
```

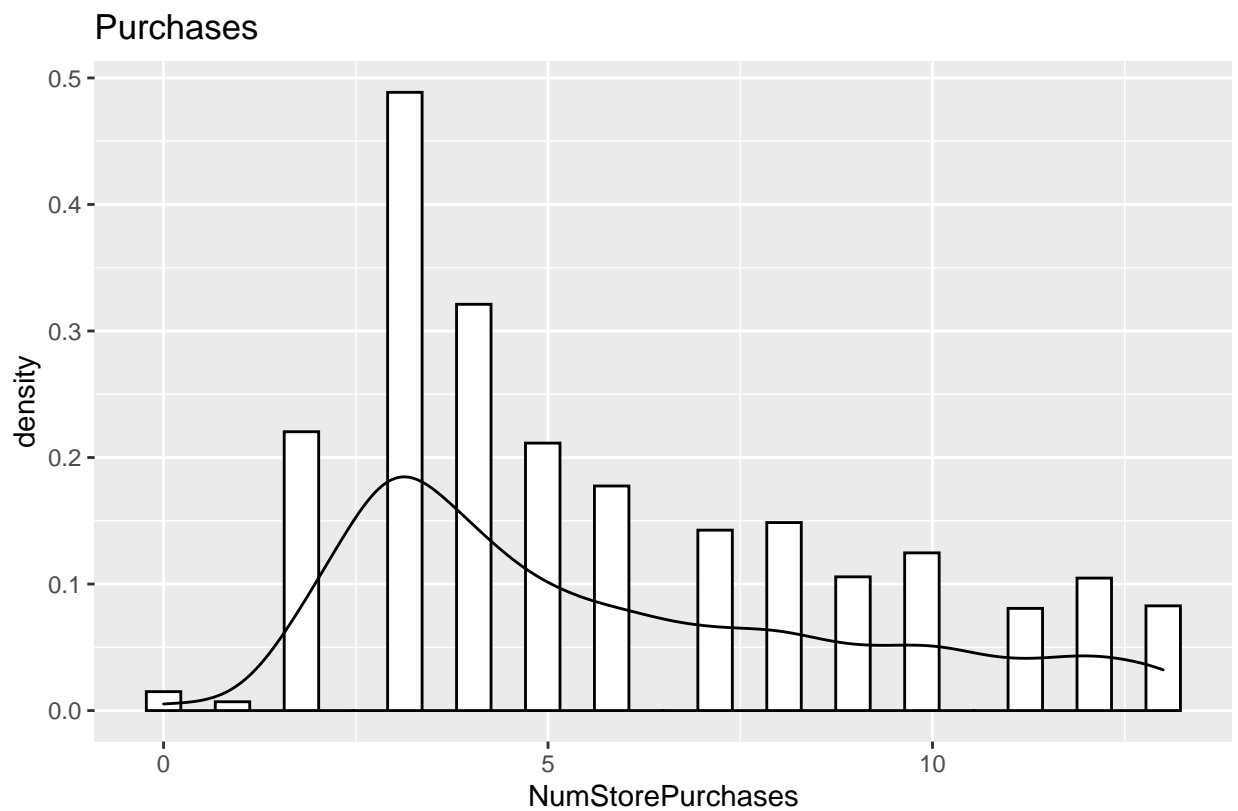




In order to consider NumStorePurchases and NumDealsPurchases as response variables for linear variables, we first have to check normality.

```
ggplot(data, aes(x = NumStorePurchases)) +
  geom_histogram(aes(y = ..density..),
                 colour = 1, fill = "white") +
  geom_density(adjust = 1) + labs(title = "Purchases",
  caption = paste("skewness =", round(moments::skewness(data$NumStorePurchases, na.rm = TRUE), 2)))
```

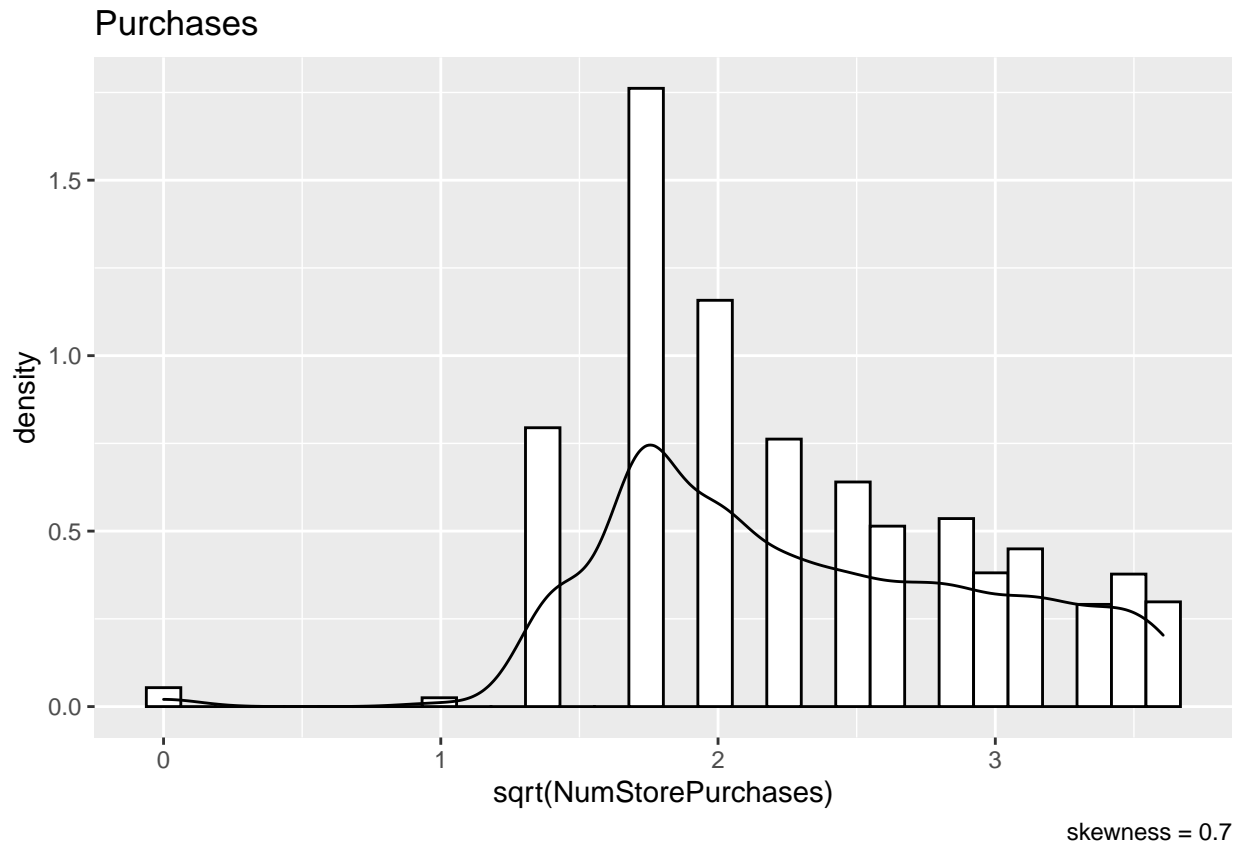
```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



skewness = 0.7

```
ggplot(data, aes(x = sqrt(NumStorePurchases))) +  
  geom_histogram(aes(y = ..density..),  
                 colour = 1, fill = "white") +  
  geom_density(adjust = 1) + labs(title = "Purchases",  
    caption = paste("skewness =", round(moments::skewness(data$NumStorePurchases, na.rm = TRUE), 2)))
```

```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

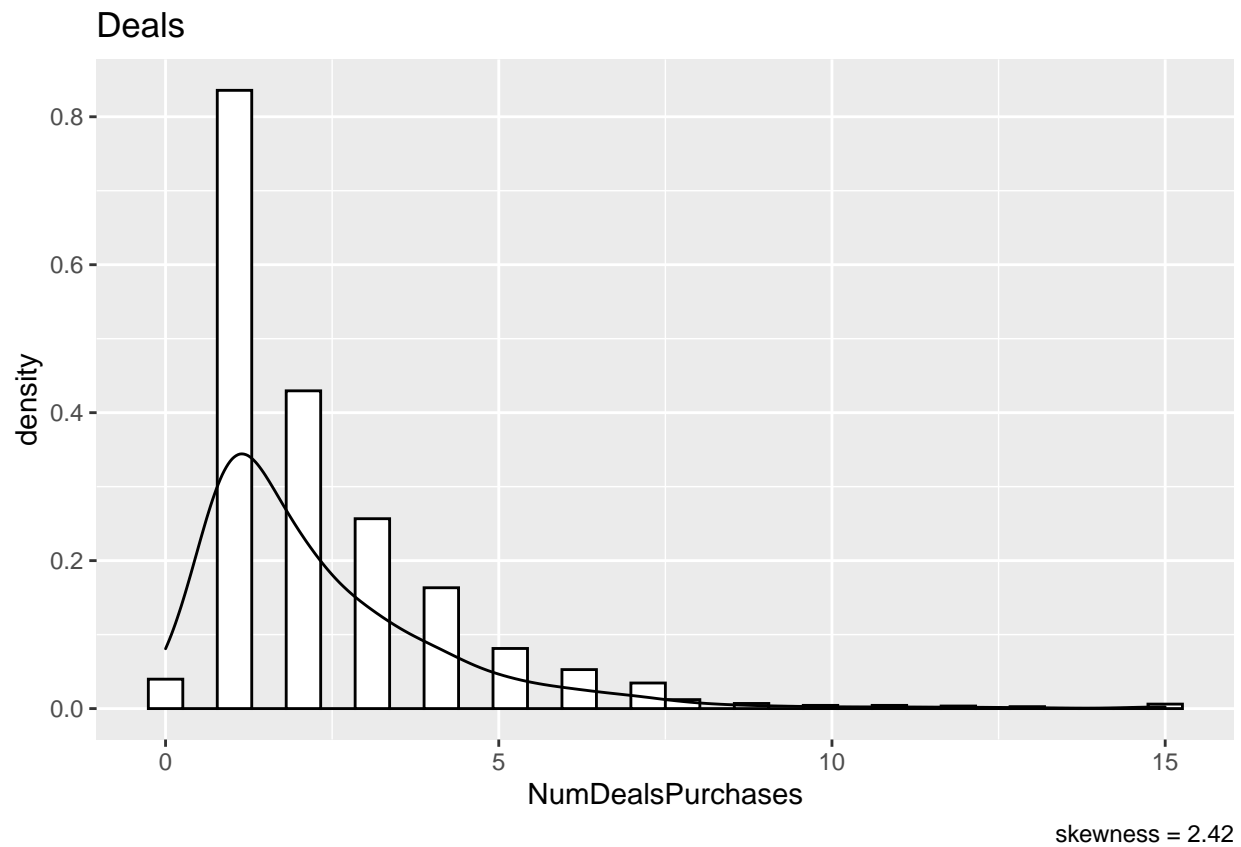


*#what should we do with NumStorePurchases ? even while using sqrt, there is no normality*

Here we will check the normality for NumDealsPurchases. It seems like skewness is better if we use the square root formula instead, although it is still not ideal.

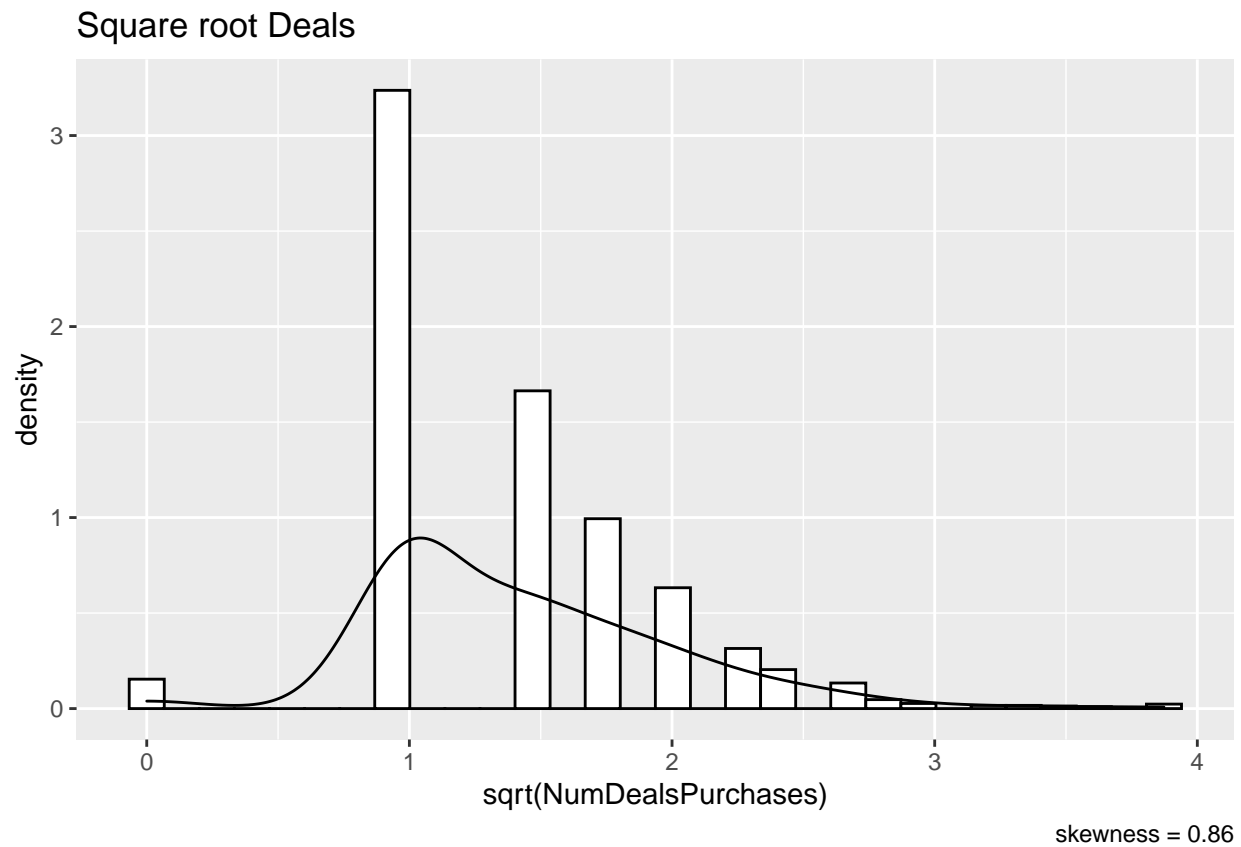
```
ggplot(data, aes(x = NumDealsPurchases)) +
  geom_histogram(aes(y = ..density..),
    colour = 1, fill = "white") +
  geom_density(adjust = 2) + labs(title = "Deals",
    caption = paste("skewness =", round(moments::skewness(data$NumDealsPurchases, na.rm = TRUE), 2)))
```

## 'stat\_bin()' using 'bins = 30'. Pick better value with 'binwidth'.



```
ggplot(data, aes(x = sqrt(NumDealsPurchases))) +
  geom_histogram(aes(y = ..density..),
    colour = 1, fill = "white") +
  geom_density(adjust = 2) + labs(title = "Square root Deals",
    caption = paste("skewness =", round(moments::skewness(sqrt(data$NumDealsPurchases), na.rm = TRUE), 2))
```

```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

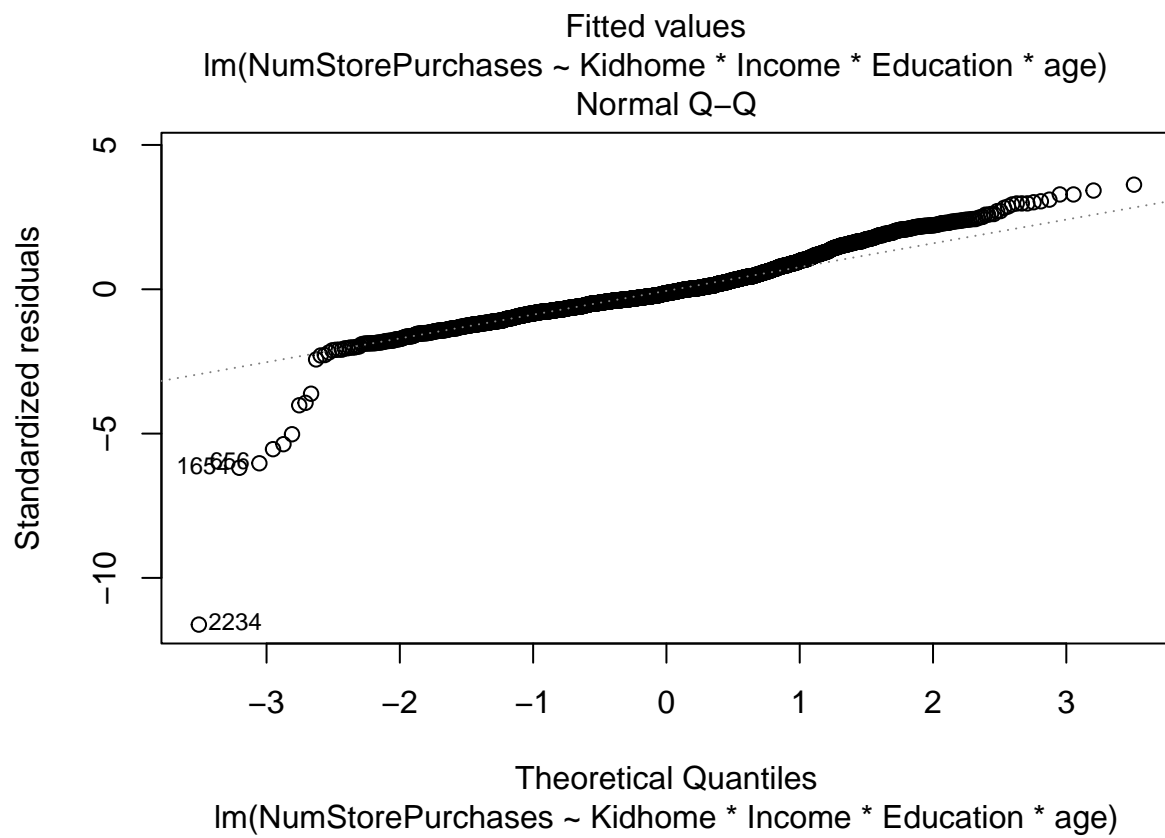
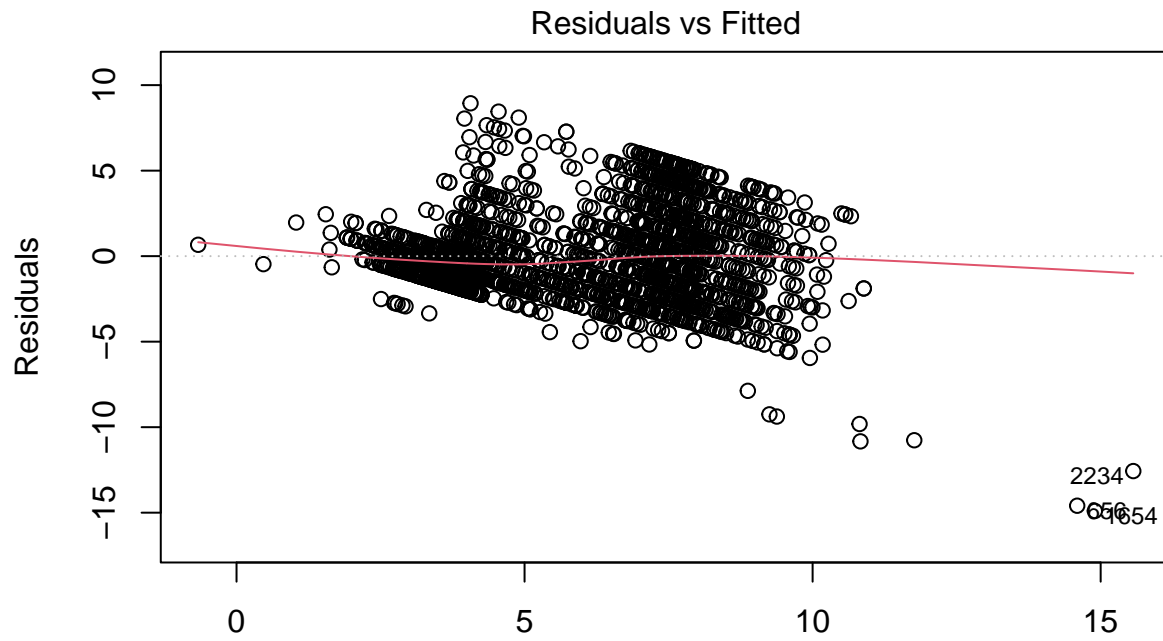


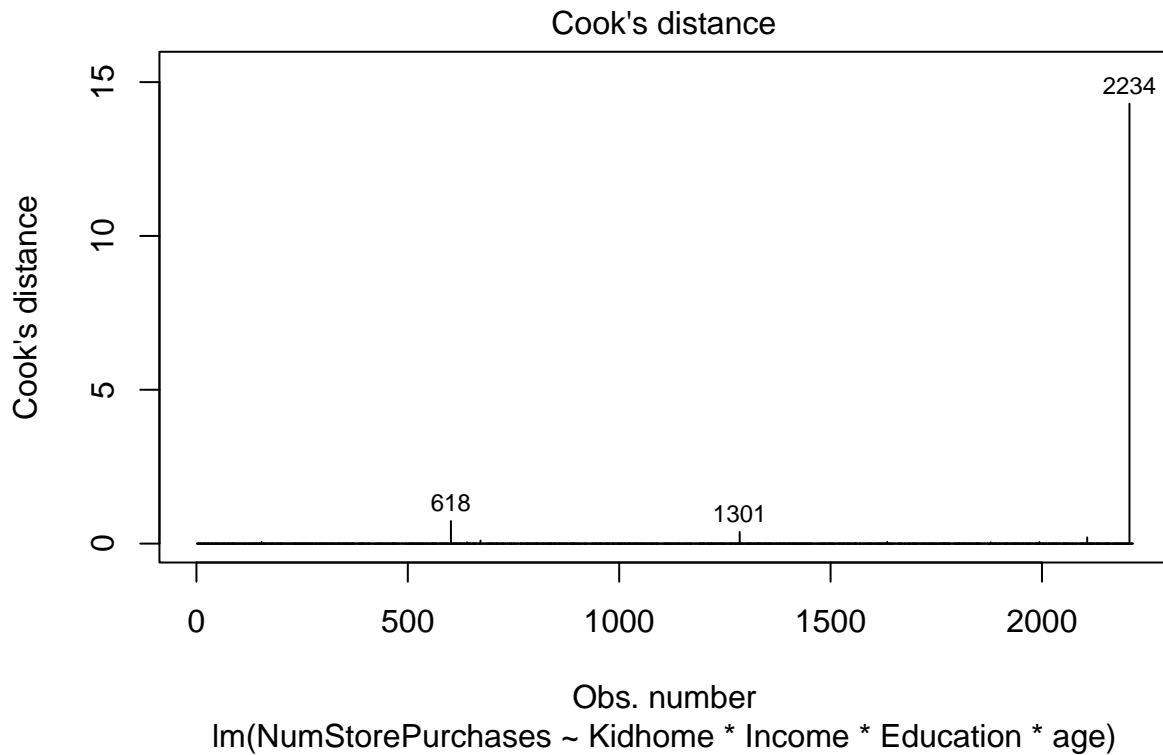
## IV - Modelling

## A. Linear model

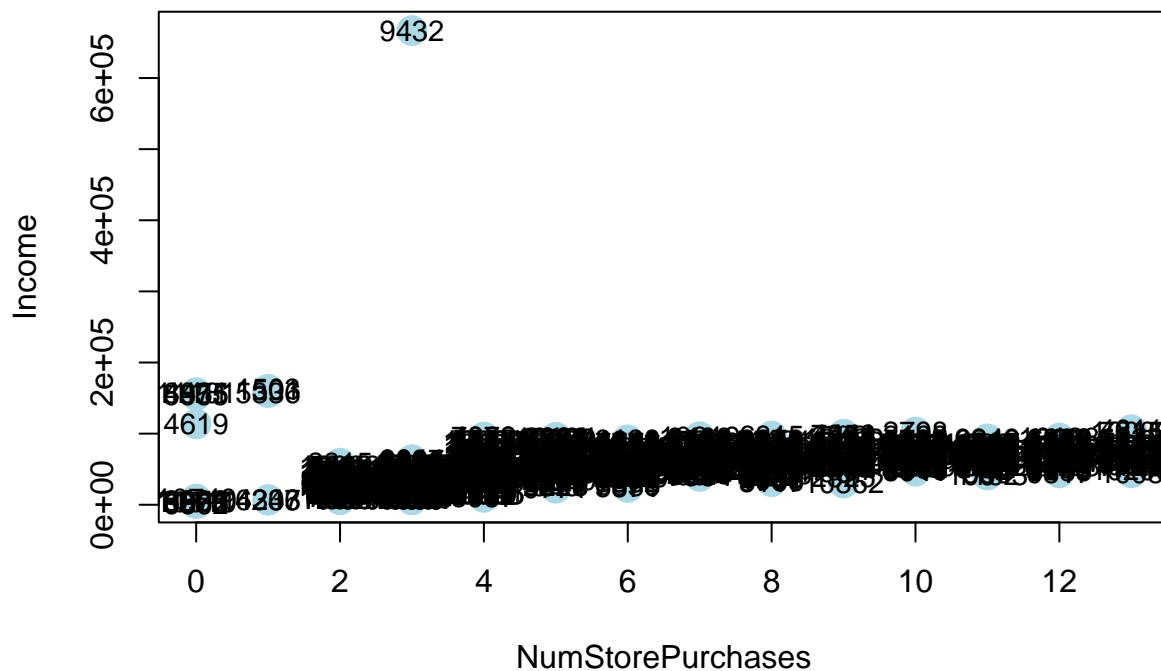
### A.1. Creating the model

```
m1 <- lm(data=data, NumStorePurchases ~ Kidhome*Income*Education*age)
plot(m1, c(1:2,4), ask=F)
```





```
plot(Income ~ NumStorePurchases, col="lightblue", pch=19, cex=2, data)
text(Income ~ NumStorePurchases, labels=ID, data, cex=0.9, font=1)
```

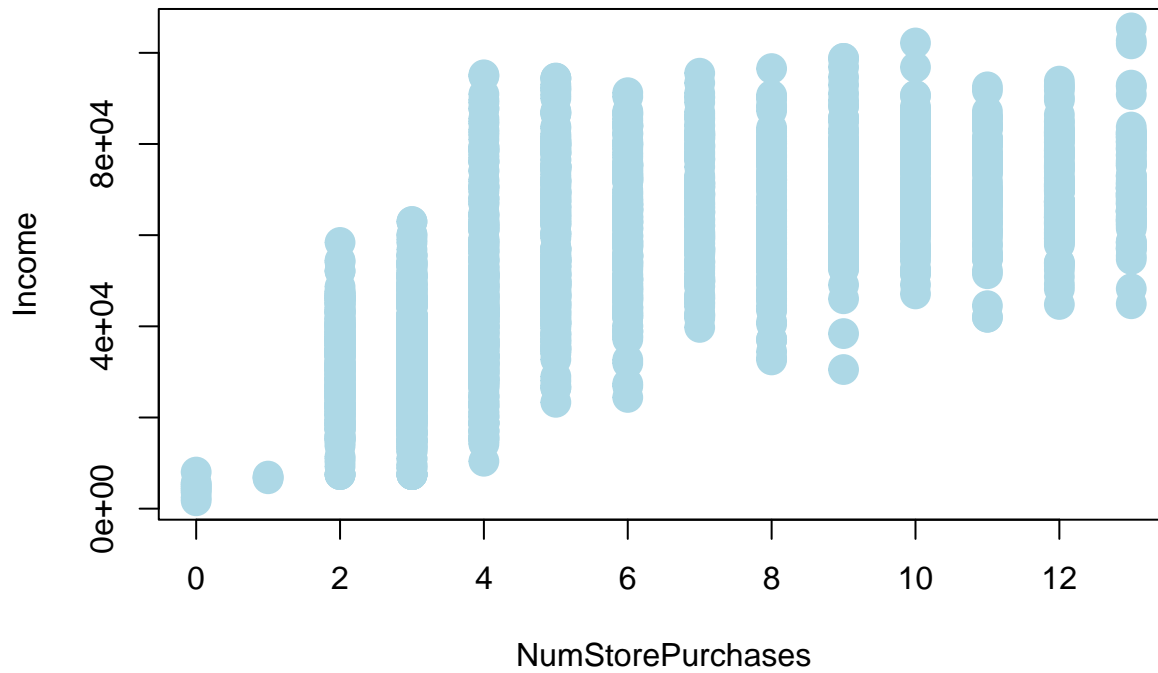


A.2.

**Assessing outliers :** here we observe peculiar outliers for “Income”. One income is equal to 666 666, and when income is higher than 150 000, people probably don’t respond. We can safely remove these outliers.

```
newdf = data %>%
  filter(!ID %in% c(9432, 5555, 4619, 5336, 1501, 1503, 8475, 4931, 11181) )
```

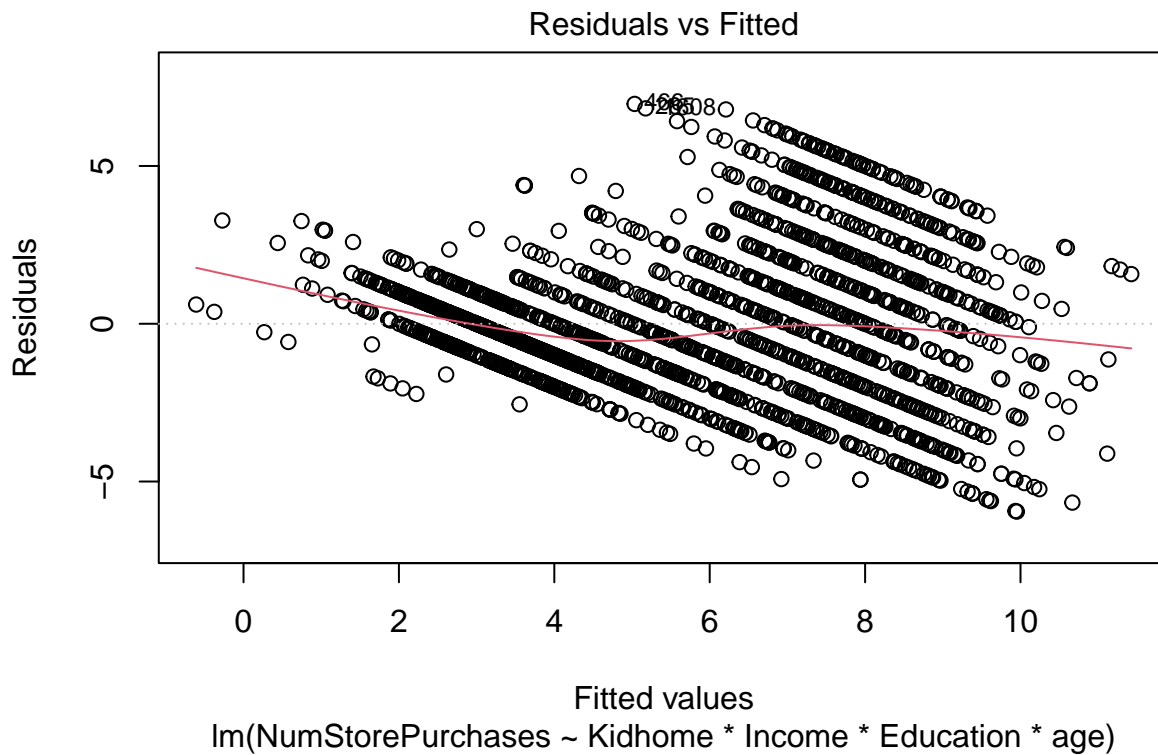
```
plot(Income ~ NumStorePurchases, col="lightblue", pch=19, cex=2, data=newdf)
```



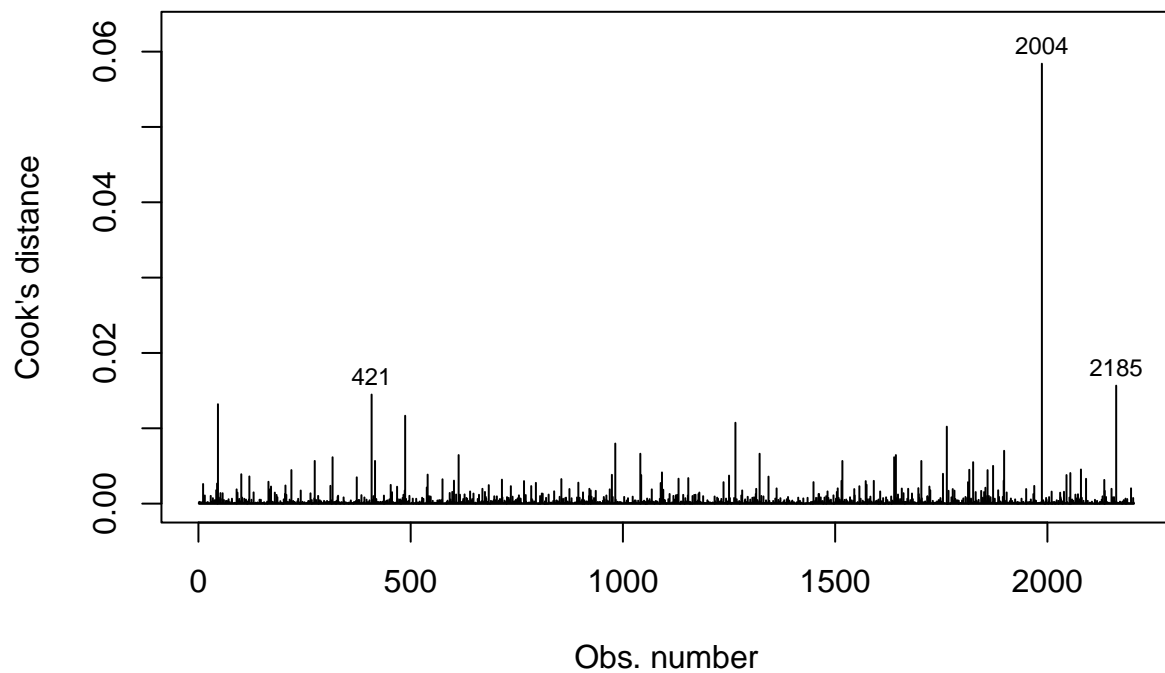
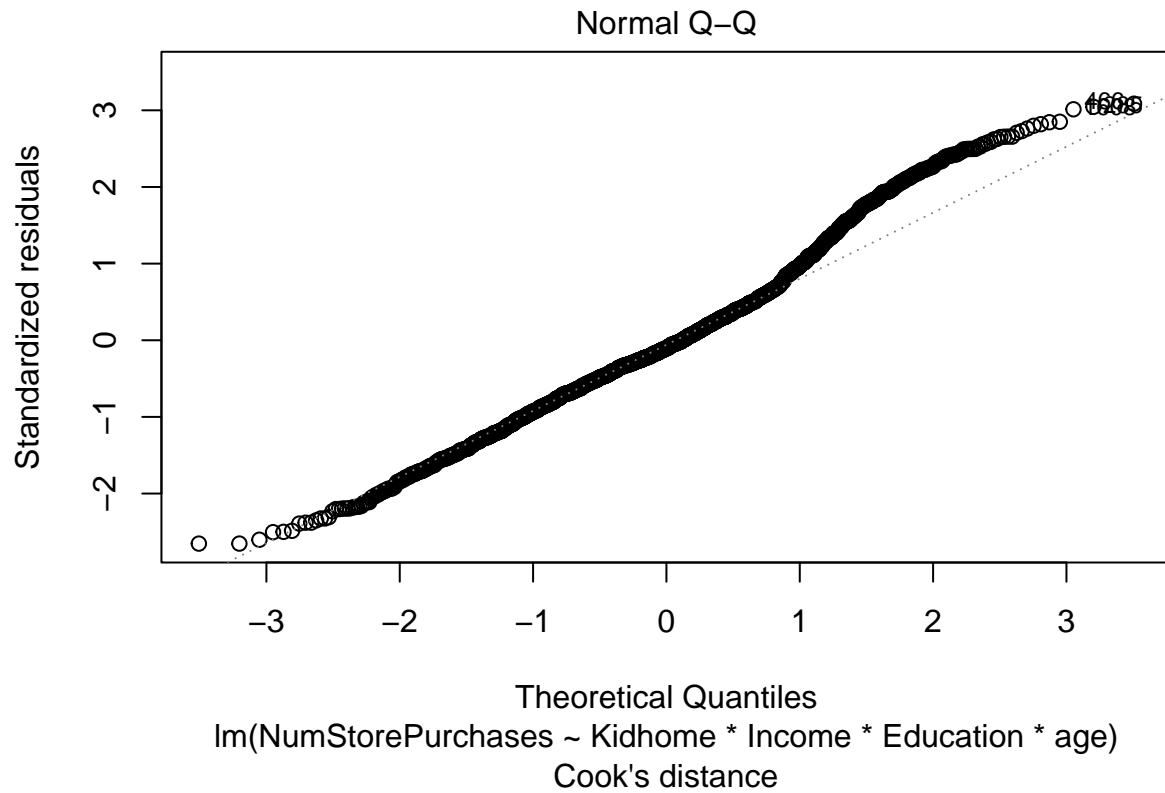
A.3.

Reassessing without the outliers

```
m1 <- lm(data=newdf, NumStorePurchases ~ Kidhome*Income*Education*age)
plot(m1, c(1:2,4), ask=F)
```







A.4.

**Filtering the variables to keep : AIC** Here we use the stepAIC function to select the model that has the best AIC.

```
ms <- MASS::stepAIC(m1, direction = "both", trace = FALSE) #il choisit le meilleur AIC
ms$anova
```

```
## Stepwise Model Path
```

```
## Analysis of Deviance Table
##
## Initial Model:
## NumStorePurchases ~ Kidhome * Income * Education * age
##
## Final Model:
## NumStorePurchases ~ Kidhome + Income + Education + age + Kidhome:Income +
##   Kidhome:Education + Income:Education + Kidhome:age + Income:age +
##   Education:age + Kidhome:Income:Education + Income:Education:age
##
##
##              Step Df  Deviance Resid. Df Resid. Dev      AIC
## 1
## 2 - Kidhome:Income:Education:age  4 26.205697      2168   11164.28 3647.870
## 3   - Kidhome:Education:age      4 14.097325      2172   11178.38 3642.652
## 4     - Kidhome:Income:age       1  8.240739      2173   11186.62 3642.276
```

### A.5. Computing the final model

```
finalm1 <- lm(data=newdf, NumStorePurchases ~ Kidhome + Income + Education + age + Kidhome:Income + Kidhome:Education + Income:Education + Kidhome:age + Income:age + Education:age + Kidhome:Income:Education + Income:Education:age)
```

**A.6. Checking for interferences** We first use the effectsize function : everything that has 0.00 on the left of the 90% CI column has a “meaningless” effect size, but we still keep them on the model. We also call the sjPlot function to plot all the estimates or to plot only one term at a time.

```
parameters::model_parameters(anova(finalm1))
```

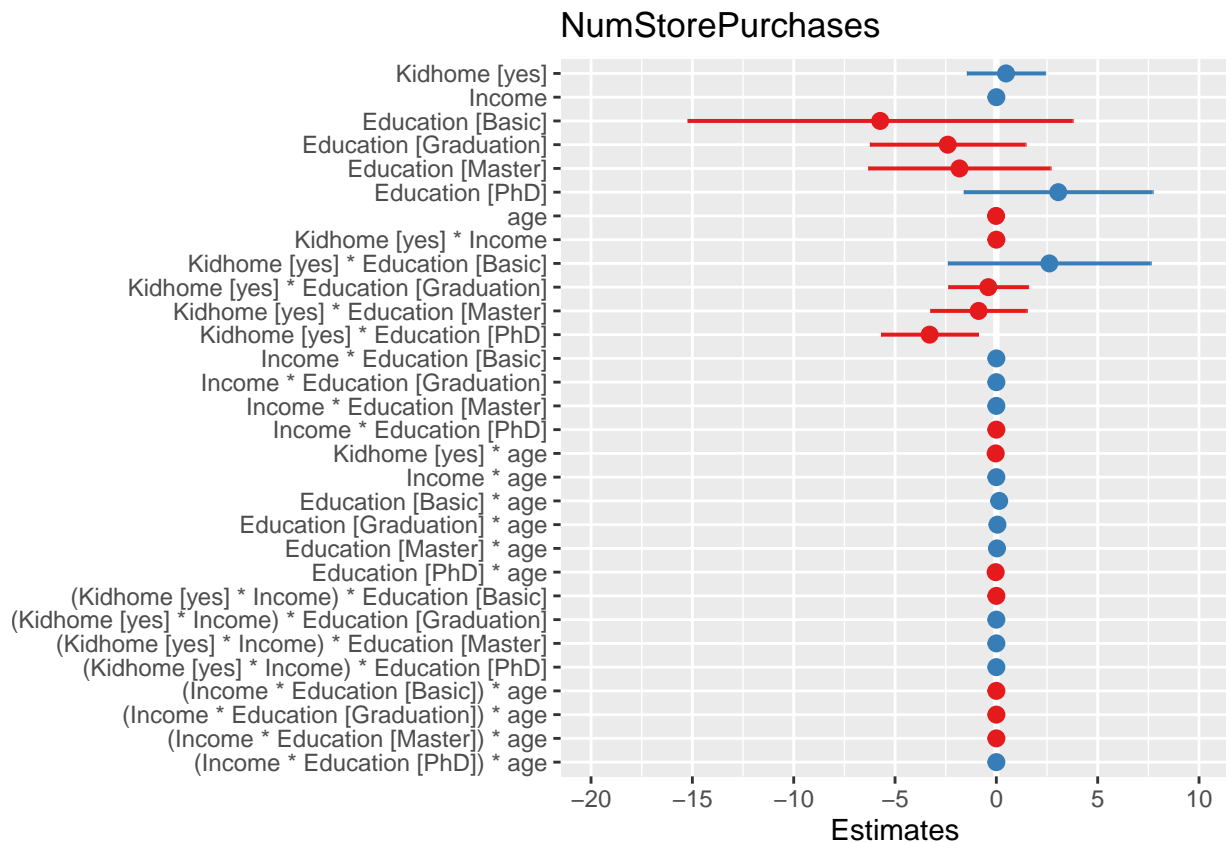
```
## Parameter | Sum_Squares | df | Mean_Square | F | p
## -----
## Kidhome | 6242.08 | 1 | 6242.08 | 1212.52 | < .001
## Income | 5446.16 | 1 | 5446.16 | 1057.92 | < .001
## Education | 10.29 | 4 | 2.57 | 0.50 | 0.736
## age | 24.65 | 1 | 24.65 | 4.79 | 0.029
## Kidhome:Income | 4.87 | 1 | 4.87 | 0.95 | 0.331
## Kidhome:Education | 31.63 | 4 | 7.91 | 1.54 | 0.189
## Income:Education | 26.11 | 4 | 6.53 | 1.27 | 0.280
## Kidhome:age | 36.69 | 1 | 36.69 | 7.13 | 0.008
## Income:age | 5.97 | 1 | 5.97 | 1.16 | 0.282
## Education:age | 11.41 | 4 | 2.85 | 0.55 | 0.696
## Kidhome:Income:Education | 52.82 | 4 | 13.20 | 2.56 | 0.037
## Income:Education:age | 49.16 | 4 | 12.29 | 2.39 | 0.049
## Residuals | 11186.62 | 2173 | 5.15 | |
##
## Anova Table (Type 1 tests)
```

```
effectsize::eta_squared(finalm1, ci = 0.9)
```

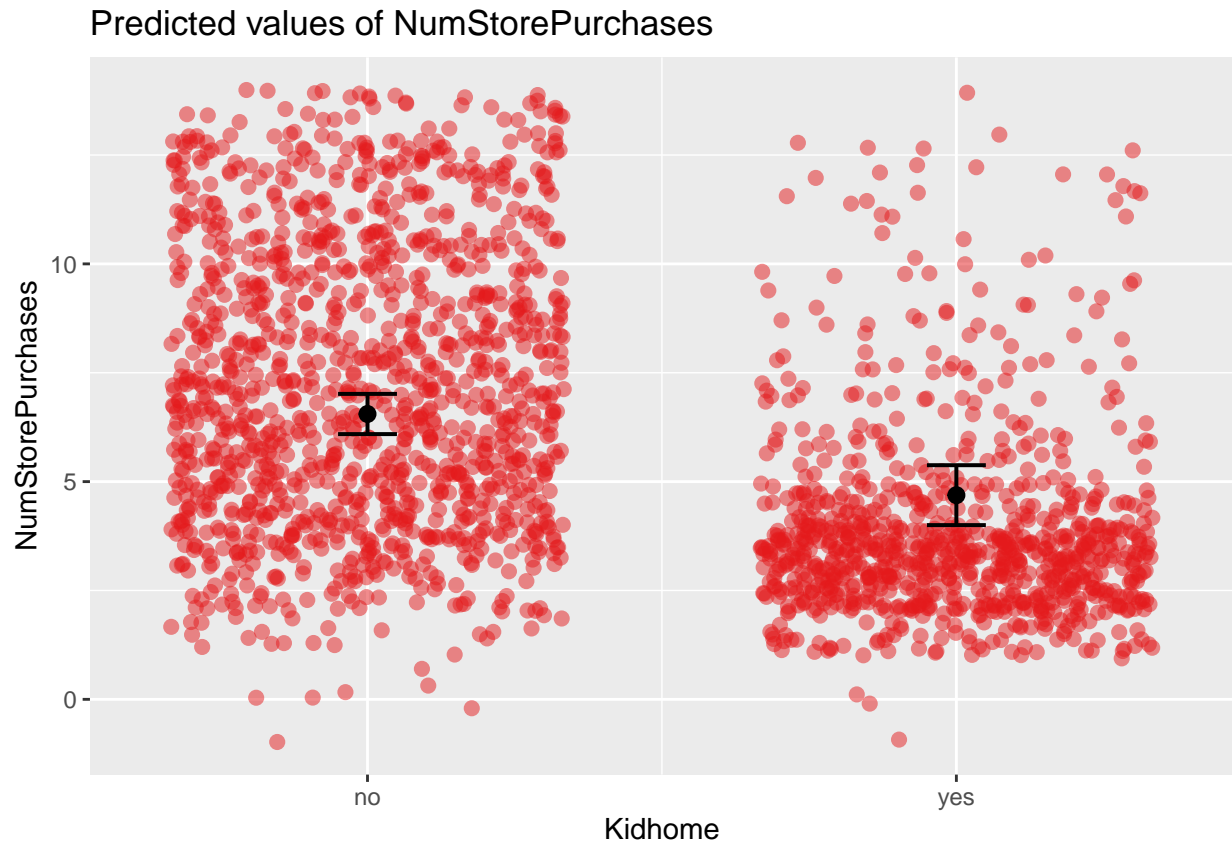
```
## # Effect Size for ANOVA (Type I)
##
## Parameter | Eta2 (partial) | 90% CI
## -----
## Kidhome | 0.36 | [0.34, 1.00]
```

```
## Income | 0.33 | [0.31, 1.00]
## Education | 9.19e-04 | [0.00, 1.00]
## age | 2.20e-03 | [0.00, 1.00]
## Kidhome:Income | 4.35e-04 | [0.00, 1.00]
## Kidhome:Education | 2.82e-03 | [0.00, 1.00]
## Income:Education | 2.33e-03 | [0.00, 1.00]
## Kidhome:age | 3.27e-03 | [0.00, 1.00]
## Income:age | 5.33e-04 | [0.00, 1.00]
## Education:age | 1.02e-03 | [0.00, 1.00]
## Kidhome:Income:Education | 4.70e-03 | [0.00, 1.00]
## Income:Education:age | 4.38e-03 | [0.00, 1.00]
##
## - One-sided CIs: upper bound fixed at (1).
```

```
sjPlot::plot_model(finalm1)
```

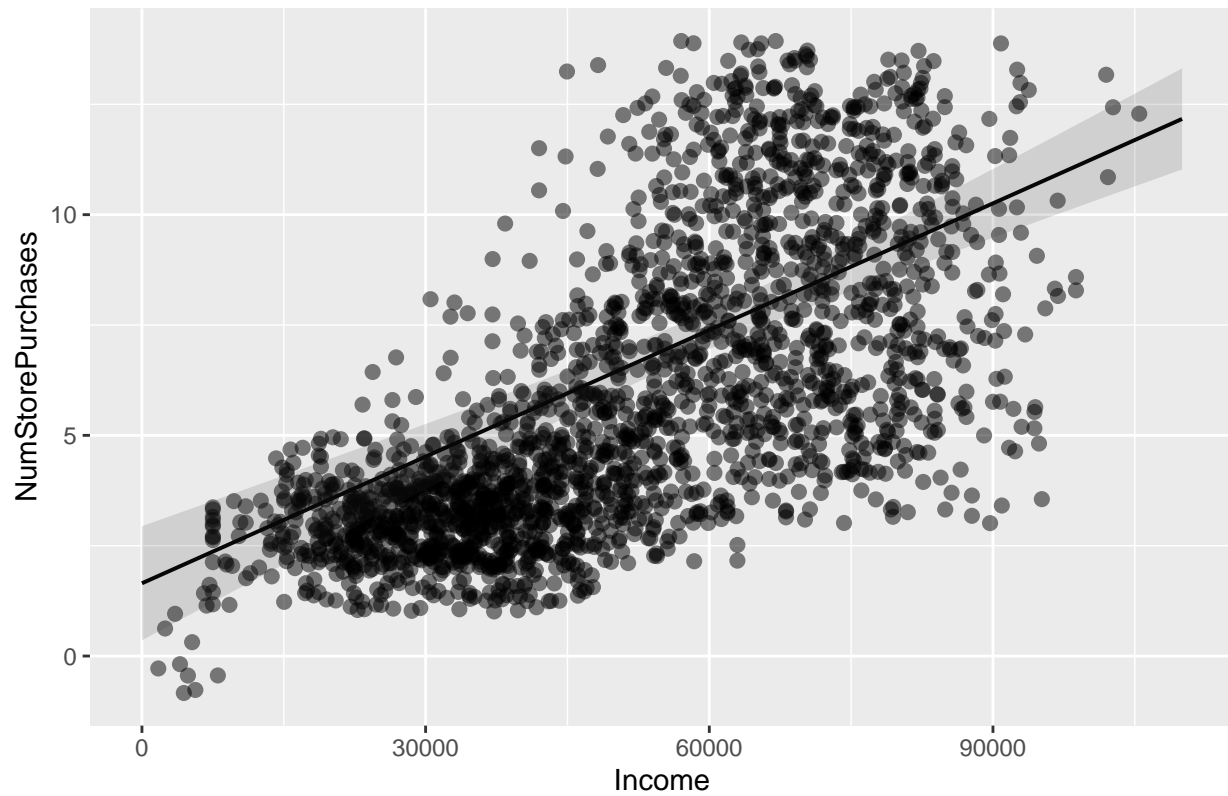


```
sjPlot::plot_model(finalm1, type = "pred", terms = "Kidhome", show.data = T, jitter = 1)
```

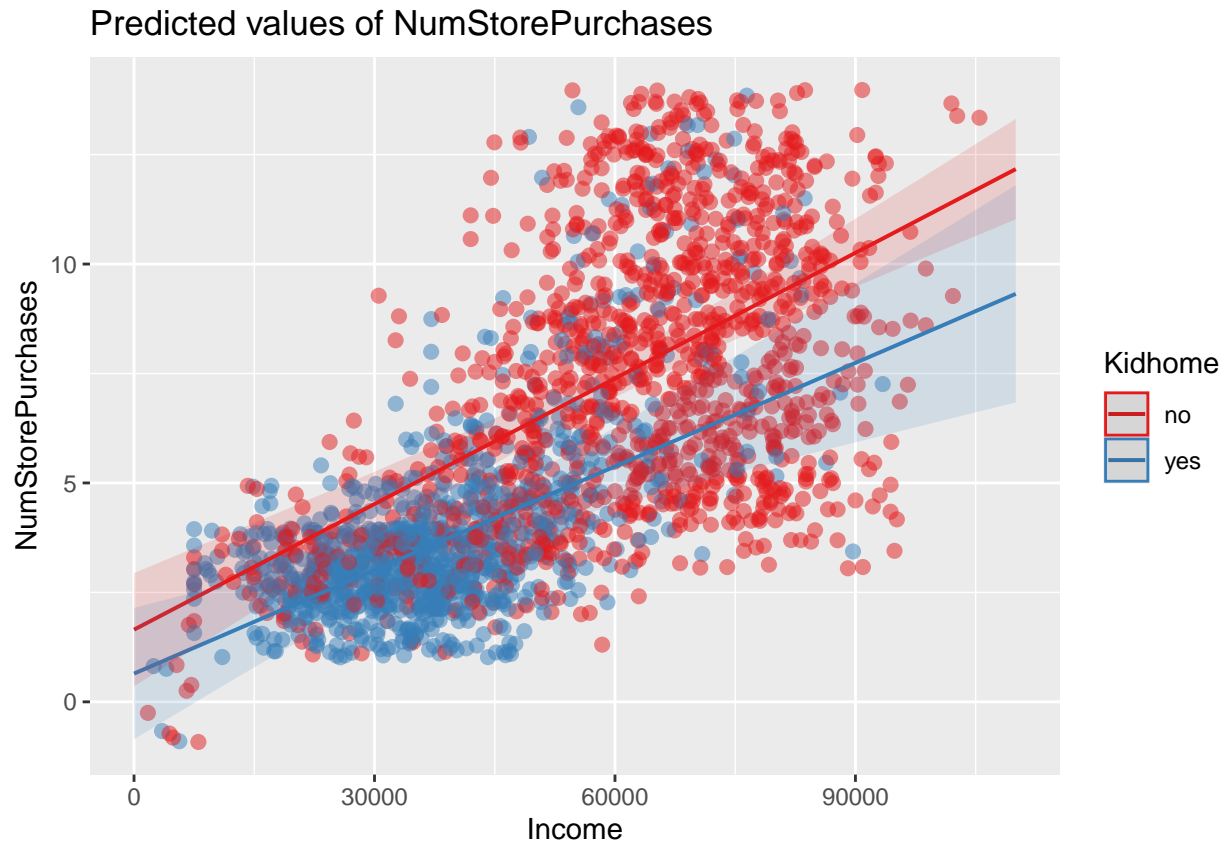


```
sjPlot::plot_model(finalm1, type = "pred", terms = "Income", show.data = T, jitter = 1)
```

Predicted values of NumStorePurchases



```
sjPlot::plot_model(finalm1, type = "pred", terms = c("Income", "Kidhome"), show.data = T, jitter = 1)
```



```
sjPlot::plot_model(finalm1, type = "pred", terms = c("Income", "Education"), show.data = T, jitter = F)
```

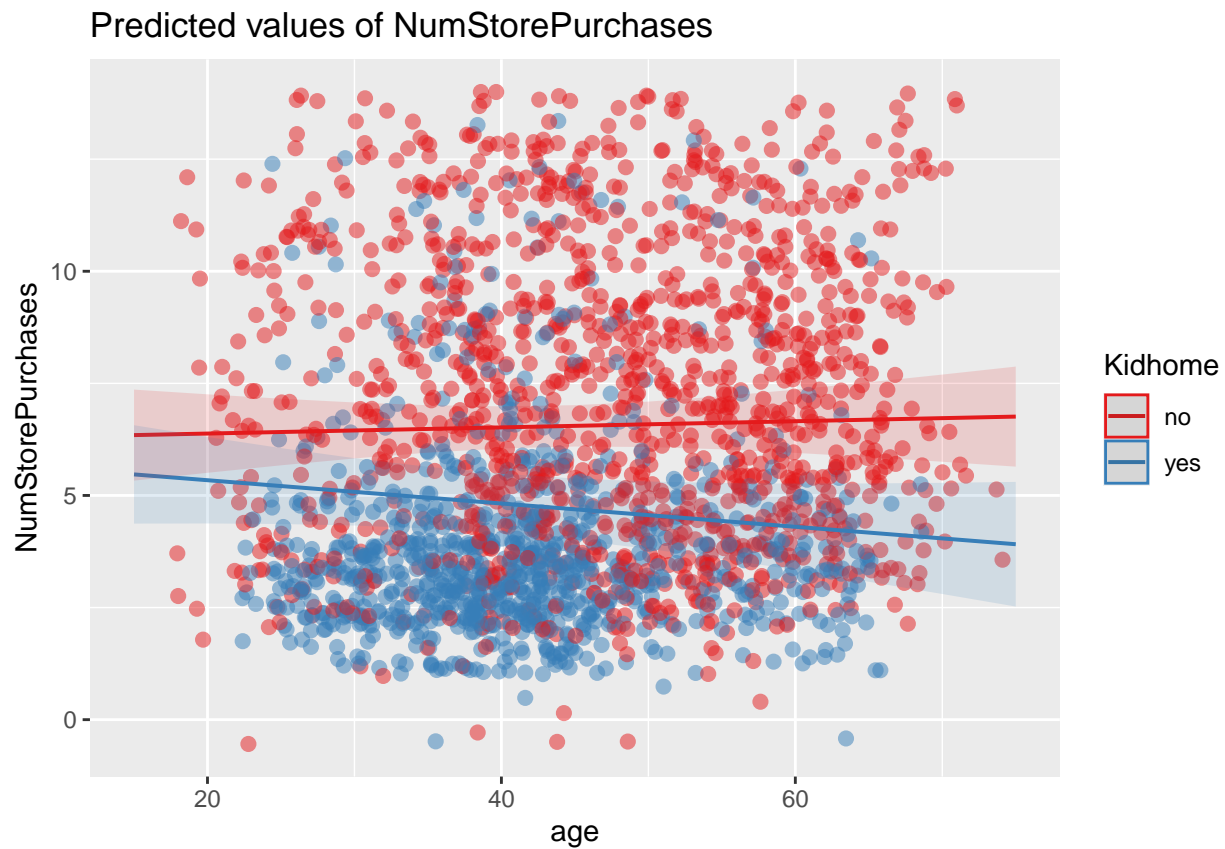


```
sjPlot::plot_model(finalm1, type = "pred", terms = c("Income", "age"), show.data = T, jitter = 1)
```



```
sjPlot::plot_model(finalm1, type = "pred", terms = c("age", "Kidhome"), show.data = T, jitter = 1)
```





*#what is this for?*

```
sjPlot::tab_model(finalm1, rm.terms = c("*Education.Q", "Education^4", "Income:Education.C", "Education
```

NumStorePurchases

Predictors

Estimates

CI

p

(Intercept)

2.25

-1.26 – 5.76

0.208

Kidhome [yes]

0.48

-1.45 – 2.41

0.628

Income

0.00

0.00 – 0.00  
 0.010  
 Education [Basic]  
 -5.73  
 -15.23 – 3.77  
 0.237  
 Education [Graduation]  
 -2.40  
 -6.24 – 1.44  
 0.221  
 Education [Master]  
 -1.82  
 -6.32 – 2.68  
 0.427  
 Education [PhD]  
 3.05  
 -1.61 – 7.71  
 0.199  
 age  
 -0.01  
 -0.10 – 0.07  
 0.750  
 Kidhome [yes] \* Income  
 -0.00  
 -0.00 – 0.00  
 0.383  
 Kidhome [yes] \* Education[Basic]  
 2.61  
 -2.39 – 7.62  
 0.306  
 Kidhome [yes] \* Education[Graduation]  
 -0.40  
 -2.37 – 1.57  
 0.692  
 Kidhome [yes] \* Education[Master]  
 -0.88

-3.25 – 1.50  
 0.470  
 Kidhome [yes] \* Education[PhD]  
 -3.29  
 -5.68 – -0.91  
 0.007  
 Income \* Education[Basic]  
 0.00  
 -0.00 – 0.00  
 0.298  
 Income \* Education[Graduation]  
 0.00  
 -0.00 – 0.00  
 0.143  
 Income \* Education[Master]  
 0.00  
 -0.00 – 0.00  
 0.542  
 Income \* Education [PhD]  
 -0.00  
 -0.00 – 0.00  
 0.298  
 Kidhome [yes] \* age  
 -0.03  
 -0.05 – -0.01  
 0.003  
 Income \* age  
 0.00  
 -0.00 – 0.00  
 0.570  
 Education [Basic] \* age  
 0.14  
 -0.08 – 0.36  
 0.210  
 Education [Graduation] \*age  
 0.05

-0.03 – 0.14  
 0.234  
 Education [Master] \* age  
 0.03  
 -0.07 – 0.13  
 0.549  
 Education [PhD] \* age  
 -0.03  
 -0.14 – 0.07  
 0.512  
 (Kidhome [yes] \* Income)\* Education [Basic]  
 -0.00  
 -0.00 – 0.00  
 0.392  
 (Kidhome [yes] \* Income)\* Education [Graduation]  
 0.00  
 -0.00 – 0.00  
 0.374  
 (Kidhome [yes] \* Income)\* Education [Master]  
 0.00  
 -0.00 – 0.00  
 0.153  
 (Kidhome [yes] \* Income)\* Education [PhD]  
 0.00  
 0.00 – 0.00  
 0.005  
 (Income \* Education[Basic]) \* age  
 -0.00  
 -0.00 – 0.00  
 0.209  
 (Income \* Education[Graduation]) \* age  
 -0.00  
 -0.00 – 0.00  
 0.113  
 (Income \* Education[Master]) \* age  
 -0.00

```

-0.00 - 0.00
0.574
(Income * Education[PhD]) * age
0.00
-0.00 - 0.00
0.716
Observations
2204
R2 / R2 adjusted
0.516 / 0.510

```

## B. Principal component analysis

```

# pm1 <- prcomp(data, ~ + "Year_Birth" + "Education" + "Marital_Status" + "Income" + "#Kidhome"
clean_data <- data[rowSums(is.na(data)) == 0, ]
pm1 <- prcomp(clean_data[, -c(1, 3, 4, 6, 7, 8, 18)], scale = TRUE)
summary(pm1)

```

```

## Importance of components:
##              PC1      PC2      PC3      PC4      PC5      PC6      PC7
## Standard deviation    2.0965 1.4242 1.04714 1.00079 0.90502 0.80789 0.70029
## Proportion of Variance 0.3663 0.1690 0.09138 0.08346 0.06826 0.05439 0.04087
## Cumulative Proportion 0.3663 0.5353 0.62667 0.71013 0.77839 0.83278 0.87364
##              PC8      PC9      PC10     PC11      PC12
## Standard deviation    0.65473 0.64171 0.61837 0.54168 6.551e-15
## Proportion of Variance 0.03572 0.03432 0.03187 0.02445 0.000e+00
## Cumulative Proportion 0.90937 0.94368 0.97555 1.00000 1.000e+00

```

```
names(data)
```

```

## [1] "ID"          "Year_Birth"  "Education"
## [4] "Marital_Status" "Income"      "Kidhome"
## [7] "Teenhome"     "Dt_Customer" "Recency"
## [10] "MntWines"     "MntFruits"   "MntMeatProducts"
## [13] "MntFishProducts" "MntSweetProducts" "MntGoldProds"
## [16] "NumDealsPurchases" "NumStorePurchases" "AcceptedCmpTotal"
## [19] "age"

```

#scale= standardise tout, car certains var. ont des échelles très différentes