

# **Real Time Fluid Simulation using Smoothed-Particle Hydrodynamics and OpenGL**

**Computer Graphics CS 488**

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This paper talks about the implementation of a real time Fluid simulation  
displayed in OpenGL ... blaaaaaaaaaaaaa

## 1 Introduction

Hello World! This is how you can cite a paper Akenine-Möller, Haines, and Hoffman 2008 Let's go to a new line

Let's go to a new paragraph

Let's write a formula

$$\sum_{i=0}^N \int_{-\infty}^{\infty} e^{-\frac{1}{2}x^2} dx$$

It's not that hard ;)

## 2 Mathematical Background

$$a_i^n = \frac{F_i^n}{m_i} = \dots \quad (1)$$

## 3 The Algorithm

In the following, we denote the position for the particle  $i$  at time  $t$  as  $x_i^t$ , its velocity as  $v_i^t$  and its acceleration as  $a_i^t$ . We omit the vector notation  $(\mathbf{x}, \mathbf{v}, \mathbf{a})$  for these quantities, since the following equations are valid for the vectors as well as for each component individually.

As suggested in S. Adami 2012, we use the *Velocity-Verlet* time stepping scheme as follows:

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### Algorithm 1: Single Timestep with Velocity Verlet Algorithm

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**Data:**  $x_i^t, v_i^{t-\frac{\Delta t}{2}}, a_i^t, \Delta t$

**Result:**  $x_i^{t+\Delta t}, v_i^{t+\frac{\Delta t}{2}}, a_i^{t+\Delta t}$

$$v_i^{t+\frac{\Delta t}{2}} = v_i^{t-\frac{\Delta t}{2}} + \Delta t a_i^t ;$$

$$x_i^{t+\Delta t} = x_i^t + \Delta t v_i^{t+\frac{\Delta t}{2}} ;$$

$$a_i^{t+\Delta t} = a_i^{t+\Delta t}(x_i^{t+\Delta t}, m_i) \text{ from equation 1 ;}$$


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## Appendix: Code

## References

- Akenine-Möller, Tomas, Eric Haines, and Natty Hoffman (2008). *Real-Time Rendering 3rd Edition*. Natick, MA, USA: A. K. Peters, Ltd., p. 1045. ISBN: 987-1-56881-424-7.
- S. Adami X.Y. Hu, N.A. Adams (2012). “A generalized wall boundary condition for smoothed particle hydrodynamics”. In: *Journal of Computational Physics* 231.