

习题 3 (1), (2), (3). 4 (2)

3. (1) 解: 设 D 为 "A, B, C 至少有一个发生"

$$\text{则: } P(D) = P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(AB) - P(BC) - P(AC) + P(ABC)$$

$$\because P(AB) = P(BC) = 0. \text{ 故 } P(ABC) = \frac{5}{8} + P(ABC)$$

$$\text{则 } P(D) = \frac{5}{8}$$

$$(2) \text{ 解: } P(A \cup B) = P(A) + P(B) - P(AB) = \frac{1}{2} + \frac{1}{3} - \frac{1}{10} = \frac{11}{15}$$

$$\text{② } P(\bar{A} \bar{B}) = P(\overline{A \cup B}) = 1 - P(A \cup B) = \frac{4}{15}$$

$$\begin{aligned} \text{③ } P(A \cup B \cup C) &= P(A) + P(B) + P(C) - P(AB) - P(AC) - P(BC) + P(ABC) \\ &= \frac{1}{2} + \frac{1}{3} + \frac{1}{5} - \frac{1}{10} - \frac{1}{15} - \frac{1}{20} + \frac{1}{30} \\ &= \frac{17}{20} \end{aligned}$$

$$\text{④ } P(\bar{A} \bar{B} \bar{C}) = 1 - P(A \cup B \cup C) = 1 - \frac{17}{20} = \frac{3}{20}$$

$$\begin{aligned} \text{⑤ } P(\bar{A} \bar{B} C) &= P(\bar{A} \bar{B} - C) = P(\bar{A} \bar{B}) - P(\bar{A} \bar{B} \bar{C}) = \frac{4}{15} - \frac{3}{20} \\ &= \frac{7}{60} \end{aligned}$$

$$\begin{aligned} \text{⑥ } P(\bar{A} \bar{B} \cup C) &= P(\bar{A} \bar{B}) + P(C) - P(\bar{A} \bar{B} \bar{C}) \\ &= \frac{4}{15} + \frac{1}{5} - \frac{3}{20} \\ &= \frac{7}{20} \end{aligned}$$



(3) (i). 解: A, B 互不相容

$$\text{则 } A \cap B = \emptyset$$

$$A \cap (S - \bar{B}) = \emptyset$$

$$\text{且 } A \cap S - A \cap \bar{B} = \emptyset$$

$$\text{故 } A \cap \bar{B} = A \cap S = A$$

$$P(A\bar{B}) = P(A) = \frac{1}{2}$$

(ii) 解: $P(\bar{A}\bar{B}) = \frac{1}{8}$

$$A\bar{B} = A - B$$

$$P(A\bar{B}) = P(A - B) = P(A) - P(AB) = \frac{1}{2} - \frac{1}{8} = \frac{3}{8}$$

4. (2) ~~解~~ 解:

$$P(A\bar{B} \cup \bar{A}B) = P(A\bar{B}) + P(\bar{A}B) - P(A\bar{B} \bar{A}B)$$

$$= P(A\bar{B}) + P(\bar{A}B)$$

$$= P(A - B) + P(B - A)$$

$$= P(A) - P(AB) + P(B) - P(AB)$$

$$= P(A) + P(B) - 2P(AB)$$

