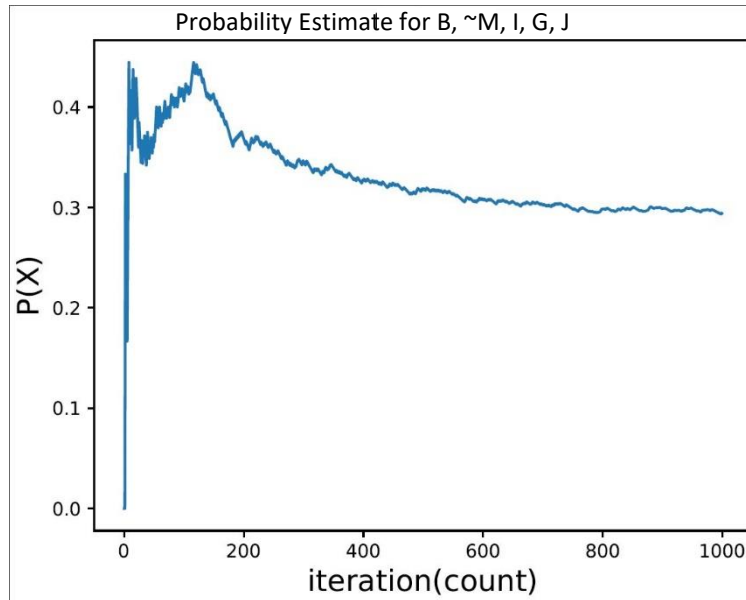


1. $P(b, \sim m, i, g, j)$:

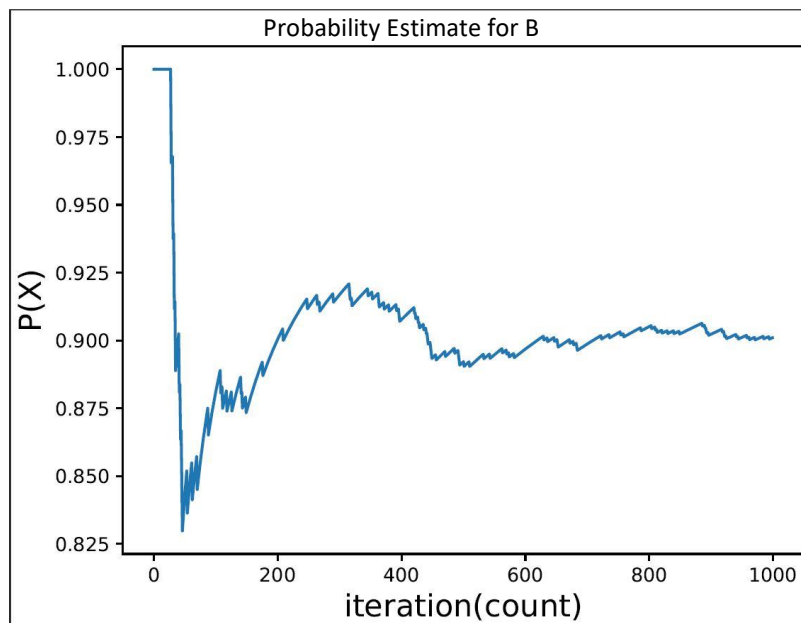
a. Exact probability computation: $P(b, \sim m, i, g, j) = 0.9 \times 0.9 \times 0.5 \times 0.8 \times 0.9 = \underline{0.2916}$

b. Running estimate plot (final estimate: 0.285):

**2. $P(b)$**

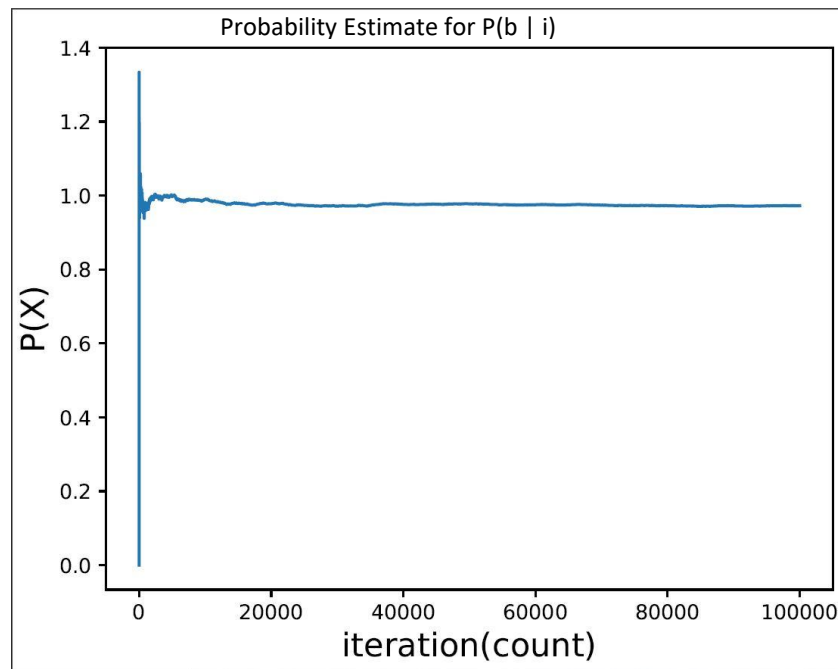
a. Exact probability computation: $P(b) = \underline{0.9}$

b. Running estimate plot (final estimate: 0.902):



3. $P(b | i)$

- Rejection percentage: 49.954%
- Exact probability calculation: given in project documentation 0.972
- Running estimate plot (final estimate: 0.9703):



4. $P(m | j, \sim b)$

- Rejection percentage: 99.81%
- Exact probability computation:

$$P(m | j, \sim b) = \alpha P(M, j, \sim b) = \alpha \sum_{\gamma} P(M, j, \sim b, \gamma)$$

$$\alpha \sum_{i, g} P(M, j, \sim b, i, g)$$

$$\alpha < P(m, j, \sim b, i, g) + P(m, j, \sim b, \sim i, \sim g), P(\sim m, j, \sim b, i, g) + P(\sim m, j, \sim b, \sim i, \sim g) >$$

$$P(m, j, \sim b, i, g) = P(m)P(\sim b)P(i | \sim b, m)P(g | \sim b, m, i)P(j | g)$$

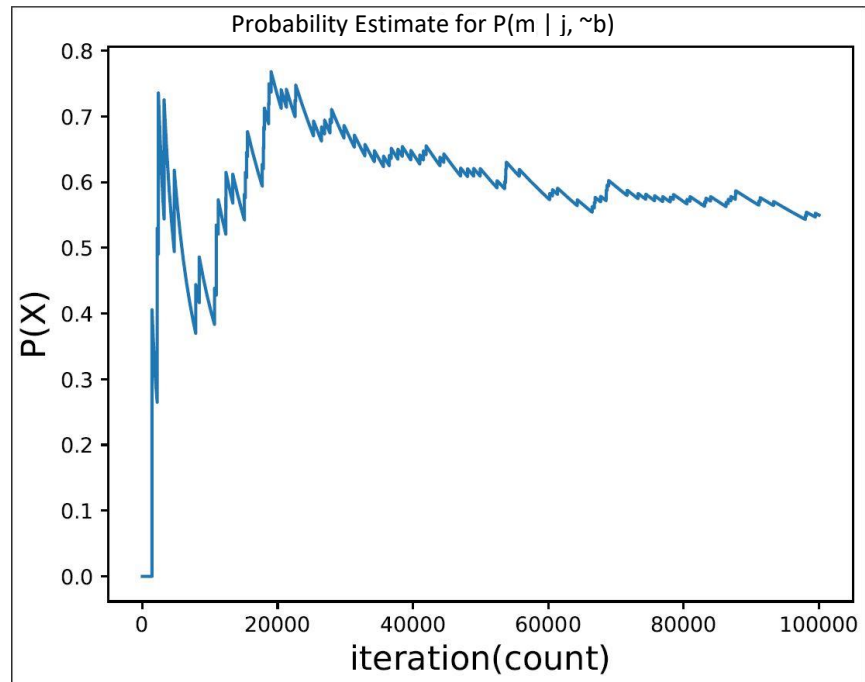
$$\alpha < P(m, \sim b, i, g, j) + P(m, \sim b, \sim i, \sim g, j), P(\sim m, \sim b, i, g, j) + P(\sim m, \sim b, \sim i, \sim g, j) >$$

$$\alpha < \underline{0.1 \times 0.1 \times 0.5 \times 0.2 \times 0.9} + \underline{0.1 \times 0.1 \times 0.5 \times 1 \times 0}, \underline{0.9 \times 0.1 \times 0.1 \times 0.1 \times 0.9} + \underline{0.9 \times 0.1 \times}$$

$$\underline{0.9 \times 1 \times 0} >$$

$\alpha < 0.0009, 0.00081 >$ $\alpha < 0.526, 0.474 >$

c. Running estimate plot (final estimate: 0.5497):



Note: All sample output generated by running the program once with no input or changes