

| Module/framework/package | Name and brief description of algorithm   | An example of a situation where using the provided GLM implementation provides superior performance compared to that of base R or its equivalent in Python (identify the equivalent in Python)  |
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| Base R                   | Iterative Weighted Least Squares with QR Decomposition - The Base R implementation of IWLS with QR Decomposition runs with $O(np^2)$ time complexity when processing $n$ observations and $p$ predictors. Each iteration of the algorithm performs matrix decomposition while the Matrix package ensures efficient processing of sparse design matrices.          | The system shows its best performance when dealing with problems containing thousands of observations alongside dozens of predictors while requiring precise numerical stability. When using heteroskedastic data for financial risk modeling the base R implementation achieves better convergence properties than the Python scikit-learn for analyzing non-linear loan default prediction relationships. The QR decomposition maintains better numerical stability when working with ill-conditioned data than gradient-based approaches do. |
| Big Data version of R    | Parallelized Block Coordinate Descent - Bigmemory and biglm packages use parallelized Block Coordinate Descent to process data with $O(nb)$ time complexity when $b$ represents the block size. These implementations manage data through disk-backed matrices while dividing information into chunks to perform block coordinate descent across available cores. | The system delivers better performance than standalone threaded operations when working with genomic data containing millions of observations. Bigmemory-based parallel coordinate descent provides 10-20 times speedup through core utilization without compromising memory usage when handling genome-wide association studies. Python framework Dask needs extensive setup to replicate  |

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|                    |  | the memory handling capabilities of its equivalent systems.  |
| Dask ML            | <p>Distributed Second-Order Methods -</p> <p>Dask ML enables distributed Hessian computation for its approximated Newton methods implementation. The algorithm operates at <math>O(np^2/k)</math> time complexity because its clever chunking strategies reduce matrix operation communication overhead.</p>   | <p>Most effective for predictive modeling with medium-sized clusters (5-20 nodes). The second-order optimization of Dask ML requires fewer iterations to build prediction models on distributed customer transaction data across multiple servers than first-order methods in PySpark even though it has higher per-iteration computation costs. The parallel approaches in R need users to implement distributed second-order methods manually.</p> |
| Spark R            | <p>Map-Reduce IRLS with Communication-Optimized Aggregation -</p> <p>The IRLS algorithm through Map-Reduce with Communication-Optimized Aggregation exists in SparkR with a running time complexity of <math>O(np^2/k + k \log k)</math> and <math>k</math> representing partition count. During coefficient updates the implementation uses broadcast variables and accumulators to reduce network traffic.</p> | <p>This method shows special efficiency when running across physically detached computing environments. The communication-optimized approach in SparkR reduces network overhead by 60-70% during telecommunications data analysis across multiple data centers which exceeds the network performance of both PySpark and parallel R implementations when network latency becomes a bottleneck.</p>   |
| Spark optimization | <p>Noise-Tolerant Stochastic Gradient Descent -</p> <p>The Spark MLlib implementation of SGD variants requires <math>O(npt)</math> computational complexity for <math>t</math> iterations. The system contains mechanisms for dynamic sampling speeds and robust updating protocols</p>  | <p>Superior for fault-tolerant computing on unreliable infrastructure. The noise-tolerant optimization of Spark enables model convergence in cloud environments where instance performance varies by maintaining stability while joblib with scikit-learn distributed through Python</p>   |

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|              | which preserve convergence behavior when stragglers interrupt distributed processes.   | would fail or operate slowly due to performance changes. The sampling mechanism adapts itself to different speeds of cluster nodes.  |
| Scikit-Learn | Specialized Solver Selection with Warm-Starting - Scikit-learn provides different solvers including LBFGS and SAGA and automatically selects the best one based on the problem type. Sequential problems benefit from the warm-starting feature which enables $O(\log(1/\epsilon))$ convergence when dealing with parameters that are similar to previous problems thus making hyperparameter tuning highly efficient. | The tool provides exceptional power for automated machine learning pipelines. The total computation time required for extensive logistic regression hyperparameter optimization becomes 70-80% shorter when scikit-learn utilizes its warm-starting approach compared to R's glmnet without this capability. The system shows superiority for AutoML systems that need to fit hundreds of slightly different models one after another. |